

GATE 2021 BM

EE:1205 Signals and System
Indian Institute of Technology, Hyderabad

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Question 5: Let $X(j\omega)$ denotes the Fourier transform of $x(t)$. If

$$X(j\omega) = 10e^{-j\pi f} \left(\frac{\sin(\pi f)}{\pi f} \right) \quad (1)$$

On comparing, we get $A = 10$ and $\tau = 1$,

$$x(0) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) d\omega \quad (6)$$

$$10\text{rect}(t) \longleftrightarrow 10\text{sinc}(f) \quad (7)$$

then $\frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) d\omega = \text{_____}$. (where $\omega = 2\pi f$)

- (A) 10π
- (B) 100
- (C) 10
- (D) 20π

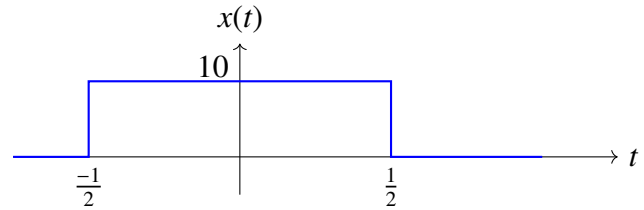


Fig. 2

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Solution

$$A\text{rect}\left(\frac{t}{\tau}\right) \longleftrightarrow A\tau\text{sinc}(f\tau) \quad (2)$$

$$x(t) \longleftrightarrow X(j\omega) \quad (3)$$

$$x(t-a) \longleftrightarrow e^{-j\omega a} X(j\omega) \quad (4)$$

$$10\text{rect}\left(t - \frac{1}{2}\right) \longleftrightarrow 10e^{-j2\pi f \times \frac{1}{2}} \text{sinc}(f) \quad (8)$$

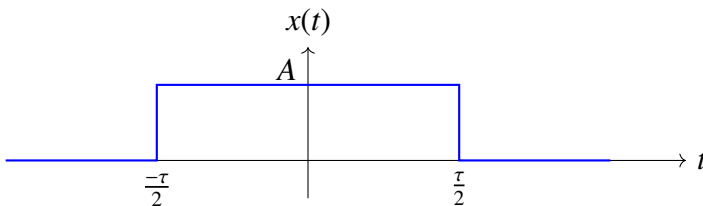


Fig. 1

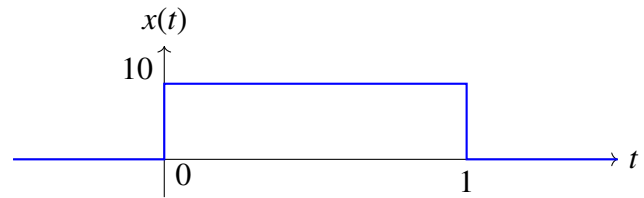


Fig. 3

From the above figure, $x(0)$ is 10.
Hence, the correct option is (C).

From $X(j\omega)$, we can have $x(t)$ as

$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega \quad (5)$$