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# **GATE 2021**

### EE22BTECH11060 - TEJAVATH KUSHAL\*

**Q.40**: For a unit step input u[n], a discrete-time LTI system produces an output signal  $(2\delta[n+1] + \delta[n] + \delta[n-1])$ . Let y[n] be the output of the system for an input  $((\frac{1}{2}^n)u[n])$ . The value of y[0] is:

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#### Ans.

Input	Output
u[n]	$s(n) = 2\delta[n+1] + \delta[n] + \delta[n-1]$
$\left(\frac{1}{2}\right)^n u[n]$	y[n]
TABLE 0	

INPUT-OUTPUT PARAMETER TABLE

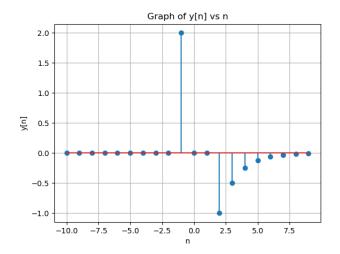


Fig. 0. Plot of y(n) v/s n

## For impulse response

$$h(n) = s(n) - s(n-1)$$
(1)

$$h(n) = 2\delta(n+1) + \delta(n) + \delta(n-1) - 2\delta(n) - \delta(n-1) - \delta(n-1-1)$$

$$\implies h(n) = 2\delta(n+1) - \delta(n) - \delta(n-2) \tag{3}$$

For input  $x(n) = \left(\frac{1}{2}\right)^n u(n)$ 

$$y(n) = x(n) * h(n)$$
(4)

$$= x(n) * [2\delta(n+1) - \delta(n) - \delta(n-2)]$$
(5)

$$= 2x(n+1) - x(n) - x(n-2)$$
 (6)

$$= 2\left(\frac{1}{2}\right)^{n+1} u(n+1) - \left(\frac{1}{2}\right)^{n} u(n)$$

$$-\left(\frac{1}{2}\right)^{n-2}u(n-2) \qquad (7)$$

$$\implies y(0) = 0 \tag{8}$$