GATE 2022 EE

EE23BTECH11023-ABHIGNYA GOGULA

Question27:

An inductor having a Q-factor of 60 is connected in series with a capacitor having a Q-factor of 240. The overall Q-factor of the circuit is . (Round off to the nearest integer)

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Solution

$$Q_{1} = \frac{\omega_{0}L}{R_{1}}$$

$$(1)$$

$$Q_2 = \frac{1}{\omega_0 C R_2}$$
 (2)

at resonance as $\omega_0 L = \frac{1}{\omega_0 C}$ hence

$$Q_2 = \frac{\omega_0 L}{R_2} \tag{3}$$

$$Q = \frac{\omega_0 L}{R_1 + R_2} \tag{4}$$

$$Q = \frac{\omega_0 L}{R_1 + R_2}$$

$$Q = \frac{1}{\frac{R_1}{\omega_0 L} + \frac{R_2}{\omega_0 L}}$$

$$(5)$$

$$Q = \frac{Q_1 Q_2}{Q_1 + Q_2} \tag{6}$$

then from (??)

$$Q = \frac{60 \times 240}{60 + 240} \tag{7}$$

$$Q = 48 \tag{8}$$