

## Problem Set 5

### Submission Instruction and Requirement:

**Due date: 2.30pm 7<sup>th</sup> June 2019**

- 1) Name the file in the pattern of "studentid.yourname.ps5", submit a doc/docx/pdf file.
- 2) Write a report on the tasks you have attempted, label each figure/table properly. You may add figures/tables from this document into your report.
- 3) Submit the zip/rar file to Blackboard on time.

### Task 1 (8 marks)

Draw a graph for each of the following expressions.

- 1)  $f(n) = n + 100$
- 2)  $f(n) = 4n^2$
- 3)  $f(n) = \log_{10} n$
- 4)  $f(n) = 3n$
- 5)  $f(n) = n!$
- 6)  $f(n) = 20n$
- 7)  $f(n) = 3$
- 8)  $f(n) = n^{2/3}$

Arrange the graphs you have generated from the slowest to fastest. Write down the expressions by the growth rates with respect to  $n$ . (Hint: MS-Excel, MATLAB or similar tools can help in drawing the graph).

### Task 2 (4 marks)

Compare Algorithm A and Algorithm B for calculating factorial of  $n$ . State the Big O notation for each algorithm. Are their Big O notations different or the same? Explain why.

Algorithm A	Algorithm B
<pre>int factorial(int n) {     int i, factorial = 1;     for (i = 1; i &lt;= n; ++i)     {         factorial *= i;         // factorial = factorial * i;     }     return factorial; }</pre>	<pre>int factorial(int n) {     if(n!=1)         return n*factorial(n-1); }</pre>

**Task 3 (4 marks)**

Analyse the algorithm given in pseudocode below:

```
While direction = NULL AND  $j \leq \text{numberOfPoints}$ 
    if  $d_j \geq (p_i + \text{stepSize})$ , then
        Set Direction = UP.
        Plot 'X' at  $p_i$  at the current columnNumber
        While  $p_i + \text{stepSize} \leq d_j$ 
            set  $p_i = p_{i-1} + \text{stepSize}$ ,
            Plot 'X' at  $p_i$  at the current columnNumber
            Increment i
        Endwhile
    Else if  $d_j \leq (p_i - \text{stepSize})$ , then
        Set Direction = DOWN.
        Plot 'O' at  $p_i$  at the current columnNumber
        While  $p_i - \text{stepSize} \geq d_j$ 
            set  $p_i = p_{i-1} - \text{stepSize}$ ,
            Plot 'O' at  $p_i$  at the current columnNumber
            Increment i
        Endwhile
    Endif
    Increment j.
Endwhile
```

State the Big O notation for the above algorithm. Explain your answer.

**Task 4 (4 marks)**

```
int Fibonacci(int n) {
    if (n <= 1) return n;
    return Fibonacci(n - 2) + Fibonacci(n - 1);
}
```

Analyse the algorithm to calculate Fibonacci number given above.

State the Big O notation for the above algorithm. Explain your answer.

(Hint: try a few values for n to see how fast the recursive call grows)