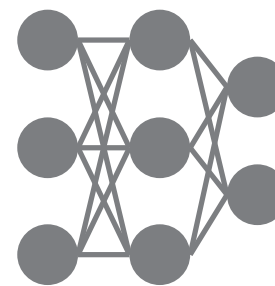


$$\begin{aligned} \min_{x \in \mathbb{R}, y \in \mathbb{Z}} \quad & (a - x)^2 + 50(y - x^2)^2 \\ \text{s.t.} \quad & y \geq \frac{1}{2}b, x^2 \leq b, x \leq 0, y \geq 0 \end{aligned}$$



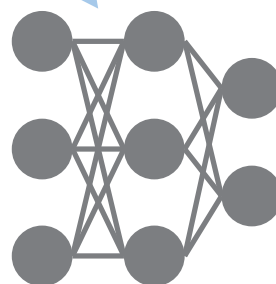
**Relaxed Solution Mapping**  
 $\pi_{\Theta_1}(a, b)$

**Input:**  $a = 3.83, b = 6.04$

**Learnable Threshold**  
 $\varphi_{\Theta_1}(a, b, \bar{x}, \bar{y})$

**Hidden State:**

$h_x = -0.69, h_y = -1.84$



Neural Network  $\delta_{\Theta_2}(a, b, \bar{x}, \bar{y})$

**Relaxed Solution:**

$\bar{x} = -1.14, \bar{y} = 3.09$

**Update Continuous Var:**

$\hat{x} = \bar{x} + h_x = -1.83$

**Round Integer Var:**

$v = \text{Sigmoid}(h_y) = 0.14$

$\bar{y} - \lfloor \bar{y} \rfloor < v \rightarrow \hat{y} = \lfloor \bar{y} \rfloor = 3$

**Mixed-Integer Solution:**  $\hat{x} = -1.83, \hat{y} = 3$

**Loss Function:**  $\mathcal{L}_{Obj} + \lambda \cdot \mathcal{L}_{Viol}$