

# Statistical Learning for Halide Perovskite Discovery

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# Outline

- 1 AI Background
- 2 Chemistry Background
- 3 Pipeline
- 4 Feature Engineering
- 5 Supervised Architectures
- 6 References

# Artificial Intelligence I

## The Four Approaches to AI

### Thinking Humanly

- Turing test approach  
(The Six Fields of AI)
- NLP
- Knowledge Representation
- automated reasoning
- Machine Learning
- computer vision
- robotics

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### Acting Humanly

- cognitive modeling approach
- neuromorphic algorithms

### Thinking Rationally

- Laws of Thought
- logical positing
- proven algorithms
- correct inference
- syllogistic reason

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### Acting Rationally

- The rational agent
- inference + reflex
- inference vs deduction

Russell and Norvig [2010]

# Machine Learning I

## ML Contributes to AI

- Adaptable **agent**
  - Contextual judgment of **percept** relevance
  - Autonomous utilization of **percept sequence**
- Learning
  - **function** performance improves with exposure to more percepts

## Definition (Artificial Agency)

**agent** self-contained sensor->function->action pipeline

**function** Set of all possible responses for all possible percepts

**percept** sensory input

**percept sequence** history of sensory input

# Machine Learning II

## Supervised Training

Encourage the agent to behave "correctly"

- 1 Minimize Loss
- 2 Maximize Score

## Unsupervised Training

The agent determines something principally true about its environment using mathematical/logical characterization methods.

- find eigenvectors and eigenvalues
- differentially calculate optima

# Inverse Design

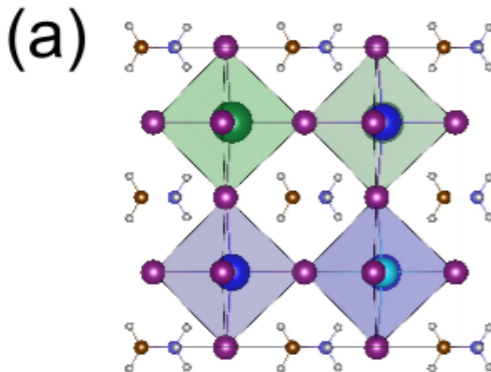
## A Type of AI Implementation

**senses** maps points in many dimensions

**function** reliably navigates it's environment searching for optima

**action** returns its findings to human interpreters

# Perovskite Structure and Chemistry



**Figure:** Example of hybrid organic-inorganic  $\text{MAPbI}_3$  Mannodi-Kanakkithodi and Chan [2022]

# Our Dataset

## DFT Simulations

- 1 geometry optimization
- 2 Static band structure and optical absorption

## Levels of Theory

- PBE
- HSE06
- PBE+HSE06(SOC)
- Experimental

Formula	$bg_{ev}$	$\eta$	LoT
MAPbCl <sub>3</sub>	3.0300	0.0020	EXP
CsPbI <sub>0.375</sub> Br <sub>2.625</sub>	1.6880	0.1532	PBE
RbSnBr <sub>2.625</sub> Cl <sub>0.375</sub>	1.4467	NaN	HSE
CsGeCl <sub>3</sub>	1.0510	0.1767	PBE
MASr <sub>0.5</sub> Pb <sub>0.5</sub> Cl <sub>3</sub>	5.3125	NaN	HSE
MABa <sub>0.25</sub> Pb <sub>0.75</sub> I <sub>3</sub>	1.9980	0.0155	PBE
MASnI <sub>3</sub>	2.5741	NaN	HSE
MACa <sub>0.5</sub> Pb <sub>0.5</sub> Cl <sub>3</sub>	5.3219	NaN	HSE
...	...	...	...



# Band Gap Fidelity I

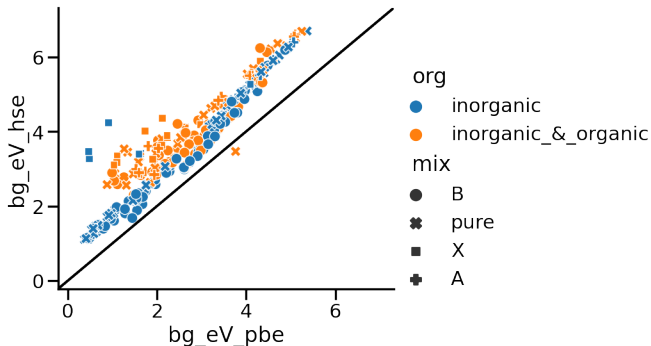


Figure: PBE vs HSE Band Gaps

# Band Gap Fidelity II

Almora et al. [2020]

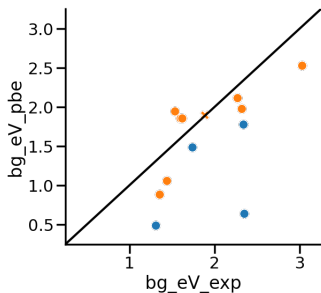


Figure: PBE vs Almora BG

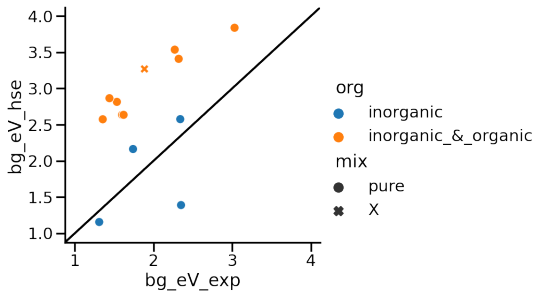


Figure: HSE vs Almora BG

# Data Pre-Processing

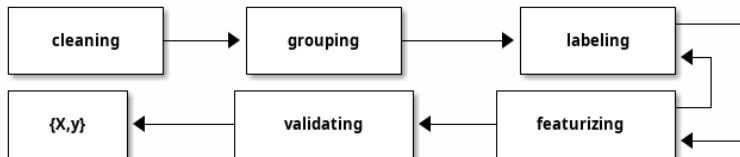
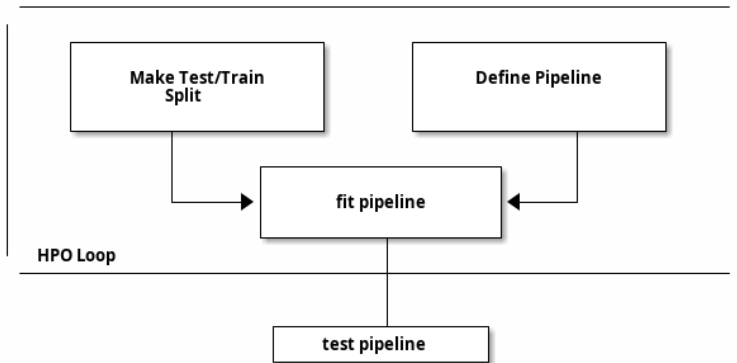


Figure: Data Preprocessing Workflow to Implement with Python Pandas

# Machine Learning Pipeline



**Figure:** Machine Learning Pipeline to Implement with Python SciKit-Learn

# Implementation in Jupyter Python I

```
import sys, os
sys.path.append(os.path.expanduser("~/src/cmcl"))
sys.path.append(os.path.expanduser("~/src/spyglass"))
import pandas as pd
import numpy as np
import cmcl
from spyglass.model_imaging import parityplot
from sklearn.pipeline import make_pipeline
from sklearn.<module> import NumPreProcessor1
from sklearn.<module> import CatPreProcessor1
from sklearn.<module> import NumPreProcessor2
from sklearn.<module> import CatPreProcessor2
from sklearn.<module> import Estimator

df = pd.read_<data>('./file.<data>')
df = df.groupby('Formula', as_index=False).agg(
    {'bg_eV': 'median',
     'efficiency': 'median'})
```

# Implementation in Jupyter Python II

```
dc = df.ft.comp()
dc = dc.assign(label='label')

numeric_features = dc
    .select_dtypes(np.number)
    .columns
    .to_list()
numeric_pipeline = make_pipeline(NumPreProcessor1(),
                                  NumPreProcessor2())

categorical_features = mc
    .select_dtypes('object')
    .columns
    .to_list()
catagorical_pipeline = make_pipeline(CatPreProcessor1(),
                                     CatPreProcessor2())
```

# Implementation in Jupyter Python III

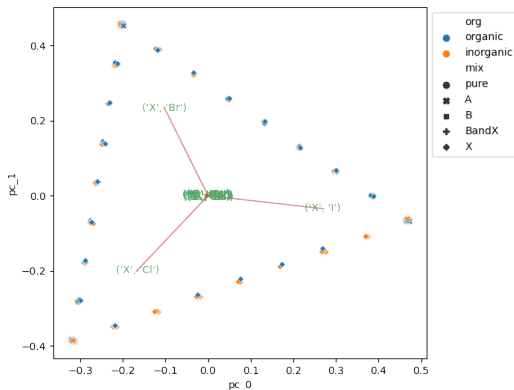
```
preprocessor = colt(  
    transformers=[  
        ("num", numeric_pipeline, numeric_features),  
        ("cat", categorical_pipeline, categorical_features),  
    ]  
)  
  
ss = ShuffleSplit(n_splits=1, train_size=0.8,  
                 random_state=None)  
train_idx, test_idx = next(ss.split(dc))  
dc_tr, dc_ts = dc.iloc[train_idx], dc.iloc[test_idx]  
df_tr, df_ts = df.iloc[train_idx], df.iloc[test_idx]  
  
pipe = make_pipeline(preprocessor, Estimator())  
  
pipe.fit(dc_r, df_tr.<target>)
```

# Implementation in Jupyter Python IV

```
p, data = parityplot(pipe,
                      dc_ts, df_ts.<target>.to_frame(),
                      aspect=1.0)
p.figure.show()
```



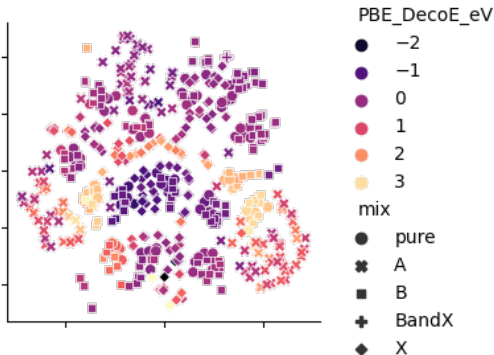
# PCA



$$UAU^\dagger = Q^{-1}SQ$$

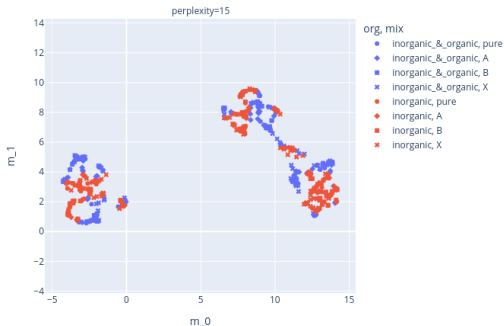
**Figure:** Learn transformation matrix  $U$  to diagonalizes the matrix  $A$ . The Principal Components in  $Q$  corresponding to the largest two Singular Values in  $S$  contain the majority of the variance in the data.

# tSNE



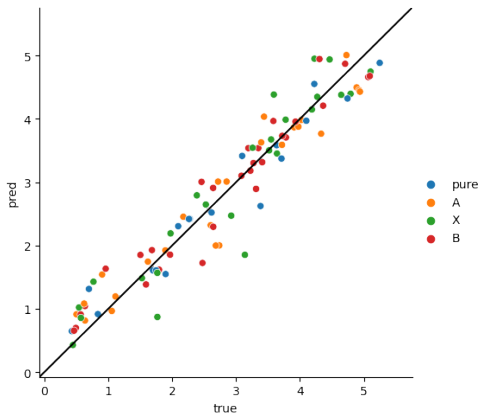
**Figure:** Learn a low-dimensional (2 or 3D) embedding space in which statistical similarity governs the proximity of high-dimensional data points

# UMAP



**Figure:** Learn a manifold embedding space in which nearest neighbors form clusters

# Linear regression on BG I



**Figure:** OLS determines  $\vec{w}$  so that  $f(x) = \vec{x}^T \vec{w}$ ,  $y_i = f(x_i) + \epsilon_i$  and all  $\epsilon_i$  are as small as possible

# Linear regression on BG II

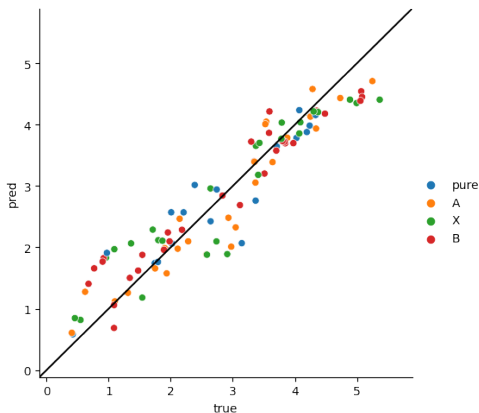


Figure: elasticnet determines  $\vec{w}$  as before, but also works to sparsify the model

# OLS weights

site	element	
A	Cs	23.771206
A	FA	25.794831
A	K	22.774475
A	MA	25.452629
A	Rb	23.282988
B	Ba	-32.603053
B	Ca	-31.378385
B	Ge	-45.001044
B	Pb	-42.526511
B	Sn	-46.868114
B	Sr	-32.068490
X	Br	0.939374
X	Cl	1.769032
X	I	0.140658

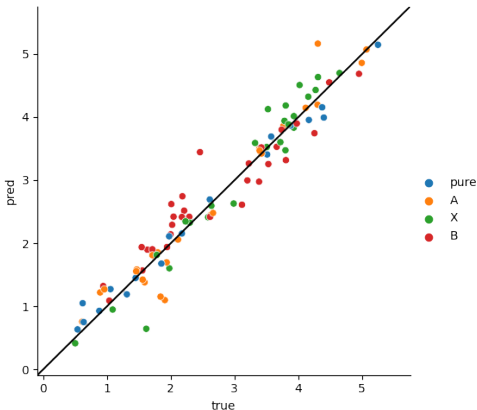
	RSS
A	54.213044
B	95.426246
X	2.007905

# elasticnet weights

site	element	
A	Cs	-0.191057
A	FA	1.589015
A	K	-1.081903
A	MA	1.214167
A	Rb	-0.530437
B	Ba	5.139688
B	Ca	6.424156
B	Ge	-5.879154
B	Pb	-3.673012
B	Sn	-7.689152
B	Sr	5.678253
X	Br	0.000000
X	Cl	0.819669
X	I	-0.786942

	RSS
A	2.342552
B	14.391222
X	1.136281

# Gaussian Process or BG I



**Figure:** GPR picks functions from a distribution derived from the data covariance. The functions that satisfy the data form the fit.



# Gaussian Process or BG II

## Regularization with Priors

Conditional Probability  $P(x|y) = \frac{P(x)P(y|x)}{P(x)}$

Conditional Odds  $O(x|y) = O(x) \frac{P(x|y)}{P(x|\neg y)}$

Isolated Bayesian Prior  $B = \frac{P(x|y)}{P(x|\neg y)}$

- Osbel Almora, Derya Baran, Guillermo C. Bazan, Christian Berger, Carlos I. Cabrera, Kylie R. Catchpole, Sule ErtenEla, Fei Guo, Jens Hauch, Anita W. Y. HoBaillie, T. Jesper Jacobsson, Rene A. J. Janssen, Thomas Kirchartz, Nikos Kopidakis, Yongfang Li, Maria A. Loi, Richard R. Lunt, Xavier Mathew, Michael D. McGehee, Jie Min, David B. Mitzi, Mohammad K. Nazeeruddin, Jenny Nelson, Ana F. Nogueira, Ulrich W. Paetzold, NamGyu Park, Barry P. Rand, Uwe Rau, Henry J. Snaith, Eva Unger, Lídice VaillantRoca, HinLap Yip, and Christoph J. Brabec. Device performance of emerging photovoltaic materials (version 1). *Advanced Energy Materials*, 11(11):2002774, 2020. doi: 10.1002/aenm.202002774. URL <http://dx.doi.org/10.1002/aenm.202002774>.
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