

1. $\Theta(n^2)$ $c_1 = 2, c_2 = 3, n_0 = 1$

2. $O(n^2 2^n)$ $c = 101, n_0 = 10$

3.

(1) $O(n^3)$

i will iterate from $0 \sim n-1$, it take n times

j will iterate from $0 \sim n-1$ each i, it take n^2 times

k will iterate from $0 \sim n-1$ each j, it take n^3 times

total cost $n^3 + n^2 + n$

when $c = 2, n_0 = 2$

$$n^3 + n^2 + n \leq cn^3, \text{ when } n \geq n_0$$

So the time complexity is $O(n^3)$

(2) $O(n^3)$

i will iterate from $0 \sim n-1$, it take n times

j will iterate from $0 \sim n-1$ each i, it take $\sum_{t=1}^n t = \frac{(n+1)n}{2}$ times

k will iterate from $0 \sim n-1$ each j, it take $\sum_{t=1}^n \frac{(t+1)t}{2} = \frac{\sum_{t=1}^n t^2 + t}{2} = \frac{2n^3 + 6n^2 + 2n}{12}$ times

$$\text{total cost } \frac{1}{6}n^3 + n^2 + \frac{10}{6}n$$

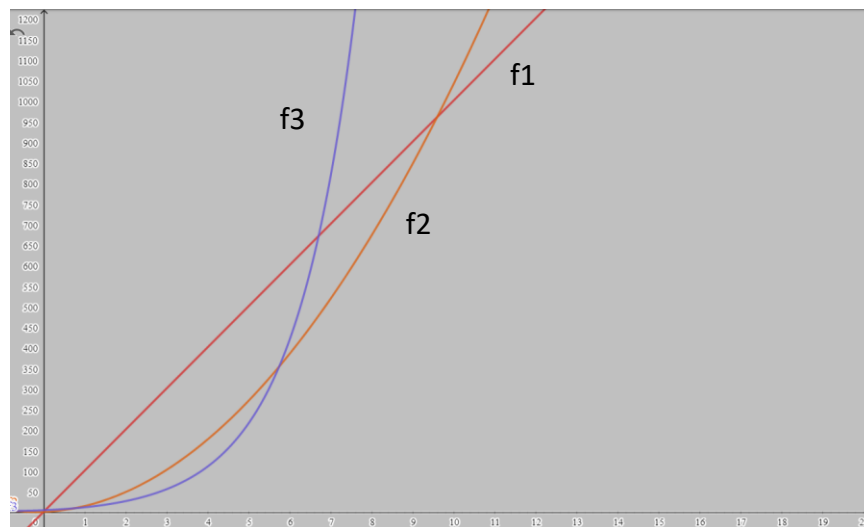
when $c = \frac{2}{6}, n_0 = 8$

$$\frac{1}{6}n^3 + n^2 + \frac{10}{6}n \leq cn^3, \text{ when } n \geq n_0$$

So the time complexity is $O(n^3)$

4.

(1)



(2) $f_3'(n) > f_2'(n) > f_1'(n)$, when $n \geq 4.8$

$$O(f_1(n)) = O(n)$$

$$O(f_2(n)) = O(n^2)$$

$$O(f_3(n)) = O(2^n)$$

(3) $O(n^t)$ is meaning $f(n) \leq c * n^t$, when $n \leq n_0$ $f(n)$ is n – polynomial,
so the constant can put into c

(4) $n^2 + n < cn^2$, when $n \leq n_0$

let $c = 2$, $n_0 = 0$, then $n^2 + n$'s time complexity is $O(n^2)$