

HOMEWORK-4

SOLUTIONS

3. It is desired to compute the sum of the first 10 terms of the series $14k^3 - 20k^2 + 5k, k = 1, 2, 3, \dots$
- Develop a pseudocode description of the required program.
 - Write and run the program described in part a.

Solution:

3a. Pseudocode:

Step 1: Initialize total to zero.

Step 2: Increment 'k' value from 1 to 10.

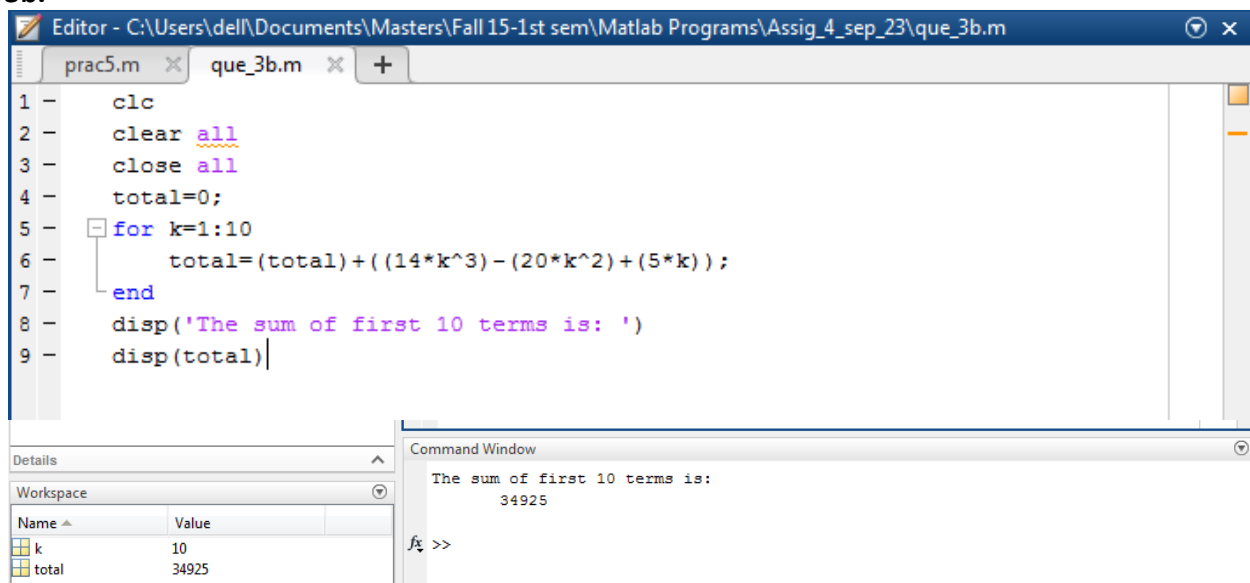
Step 3: For each 'k' value, compute the value for 'total' and update 'total' (by summing with previous value)

$\text{total} = (\text{total}) + ((14 * k^3) - (20 * k^2) + (5 * k));$

Step 4: Display the value for total (sum of first 10 terms)

Step 5: Stop.

3b.



The screenshot shows the MATLAB Editor window with a script named 'que_3b.m' open. The script contains the following code:

```
1 - clc
2 - clear all
3 - close all
4 - total=0;
5 - for k=1:10
6 -     total=(total)+((14*k^3)-(20*k^2)+(5*k));
7 - end
8 - disp('The sum of first 10 terms is: ')
9 - disp(total)
```

The Command Window shows the output of the script:

```
The sum of first 10 terms is:
34925
```

The Workspace window shows the variables 'k' and 'total' with their respective values:

Name	Value
k	10
total	34925

6.* Suppose that $x = [10, -2, 6, 5, -3]$ and $y = [9, -3, 2, 5, -1]$. Find the results of the following operations by hand and use MATLAB to check your results.

- a. $z = (x < 6)$
- b. $z = (x \leq y)$
- c. $z = (x == y)$
- d. $z = (x \sim y)$

Solution:

The image shows a MATLAB Editor window with a script named 'que_6.m' and a Command Window displaying the results of the operations.

Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_6.m

```
1 - clc
2 - clear all
3 - close all
4 - x=[10,-2,6,5,-3];
5 - y=[9,-3,2,5,-1];
6 - z1=(x<6)
7 - z2=(x<=y)
8 - z3=(x==y)
9 - z4=(x~y)
```

Command Window

```
z1 =
     0     1     0     1     1

z2 =
     0     0     0     1     1

z3 =
     0     0     0     1     0

z4 =
     1     1     1     0     1
```

Workspace

Name	Value
x	[10,-2,6,5,-3]
y	[9,-3,2,5,-1]
z1	1x5 logical
z2	1x5 logical
z3	1x5 logical
z4	1x5 logical

10. The arrays `price_A`, `price_B`, and `price_C` given below contain the price in dollars of three stocks over 10 days.

a. Use MATLAB to determine how many days the price of stock A was above both the price of stock B and the price of stock C.

b. Use MATLAB to determine how many days the price of stock A was above either the price of stock B or the price of stock C.

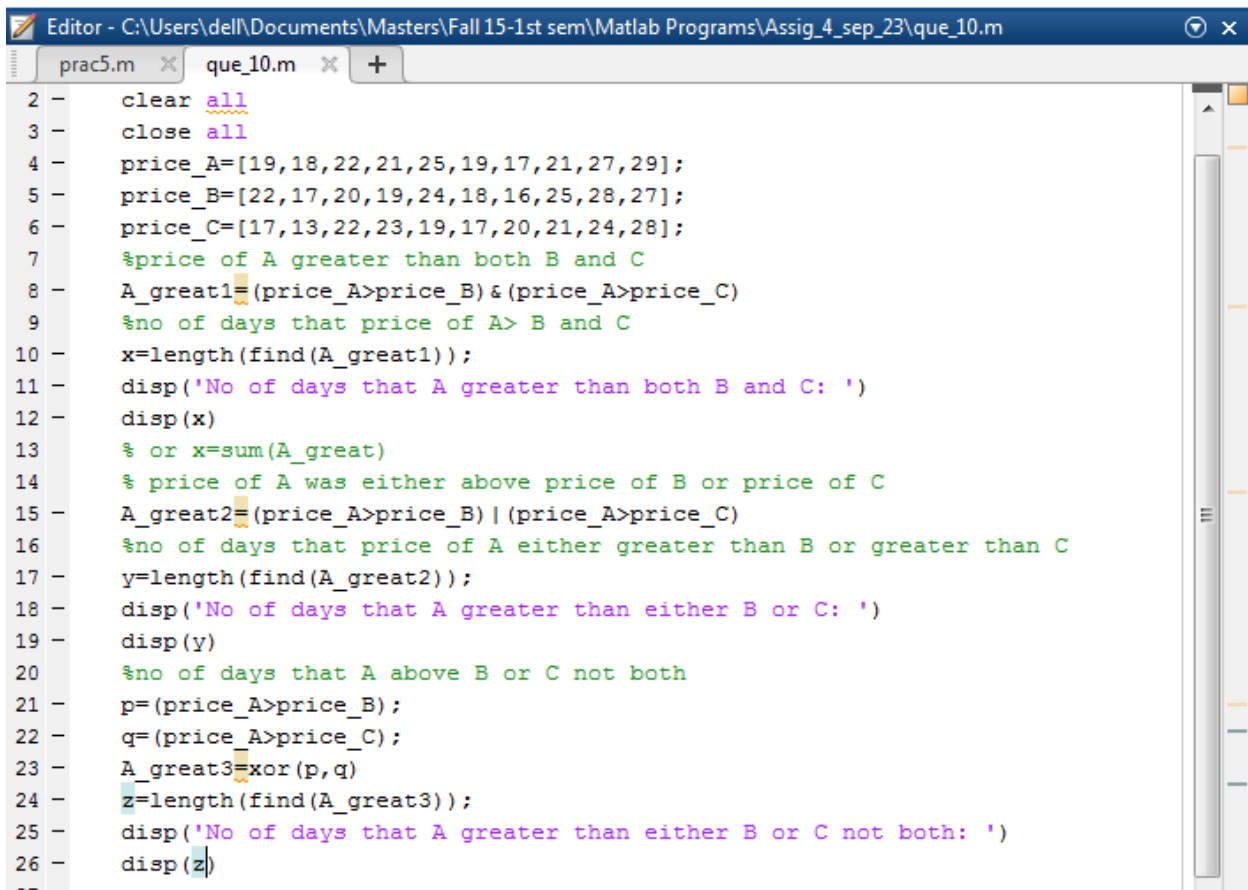
c. Use MATLAB to determine how many days the price of stock A was above either the price of stock B or the price of stock C, but not both.

```
price_A = [19, 18, 22, 21, 25, 19, 17, 21, 27, 29]
```

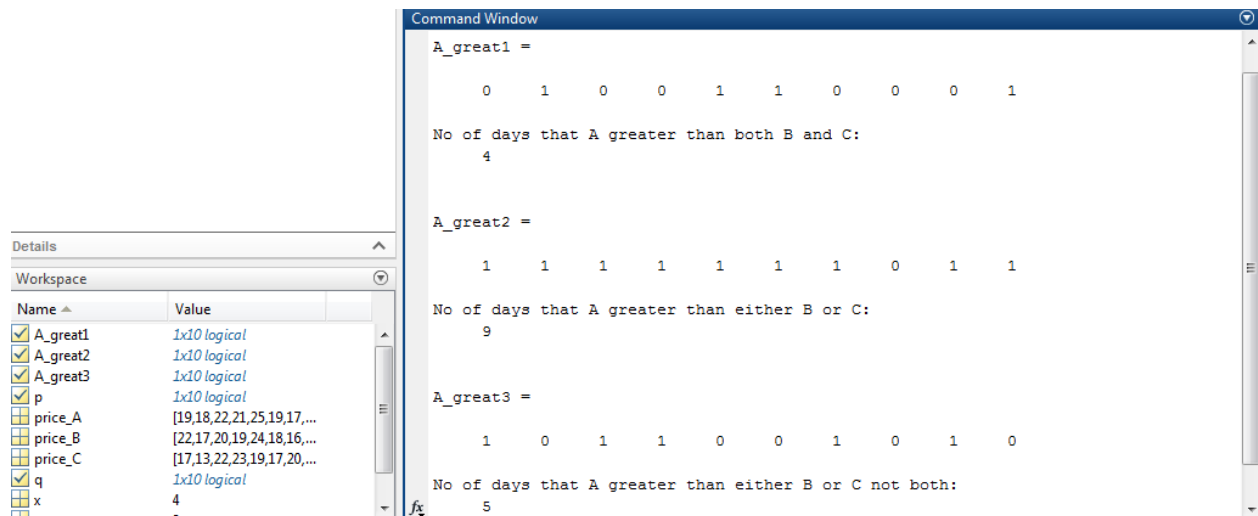
```
price_B = [22, 17, 20, 19, 24, 18, 16, 25, 28, 27]
```

```
price_C = [17, 13, 22, 23, 19, 17, 20, 21, 24, 28]
```

Solution:



```
Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_10.m
prac5.m  que_10.m  +
2 - clear all
3 - close all
4 - price_A=[19,18,22,21,25,19,17,21,27,29];
5 - price_B=[22,17,20,19,24,18,16,25,28,27];
6 - price_C=[17,13,22,23,19,17,20,21,24,28];
7 - %price of A greater than both B and C
8 - A_great1=(price_A>price_B)&(price_A>price_C)
9 - %no of days that price of A> B and C
10 - x=length(find(A_great1));
11 - disp('No of days that A greater than both B and C: ')
12 - disp(x)
13 - % or x=sum(A_great)
14 - % price of A was either above price of B or price of C
15 - A_great2=(price_A>price_B)|(price_A>price_C)
16 - %no of days that price of A either greater than B or greater than C
17 - y=length(find(A_great2));
18 - disp('No of days that A greater than either B or C: ')
19 - disp(y)
20 - %no of days that A above B or C not both
21 - p=(price_A>price_B);
22 - q=(price_A>price_C);
23 - A_great3=xor(p,q)
24 - z=length(find(A_great3));
25 - disp('No of days that A greater than either B or C not both: ')
26 - disp(z)
```



13.* The price, in dollars, of a certain stock over a 10-day period is given in the following array.

`price = [19, 18, 22, 21, 25, 19, 17, 21, 27, 29]`

Suppose you owned 1000 shares at the start of the 10-day period, and you bought 100 shares every day the price was below \$20 and sold 100 shares every day the price was above \$25. Use MATLAB to compute (a) the amount you spent in buying shares, (b) the amount you received from the sale of shares, (c) the total number of shares you own after the 10th day, and (d) the net increase in the worth of your portfolio.

Solution:


```

finamt =

    34800

net =

    15800

```

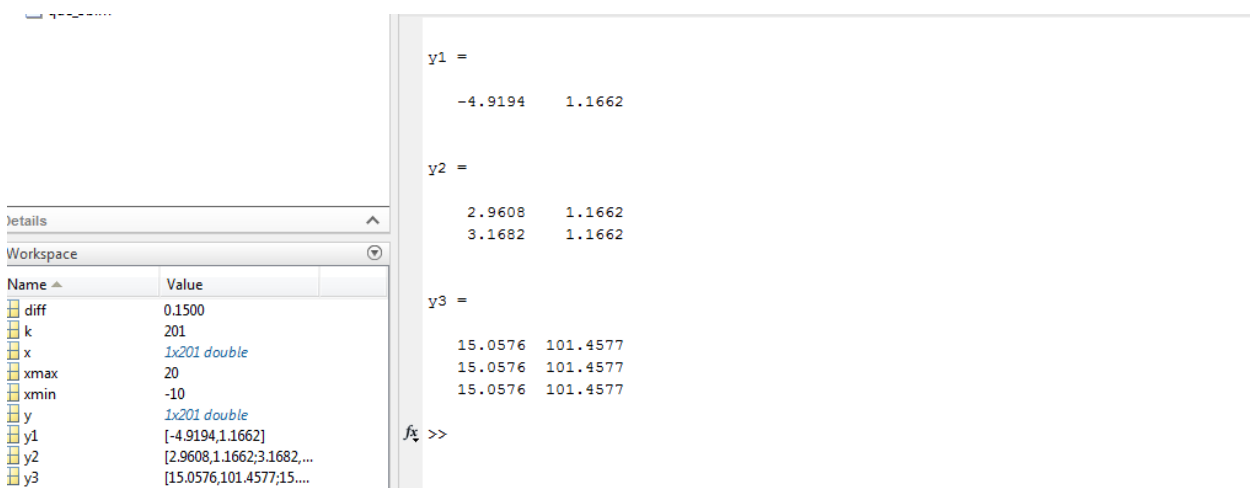
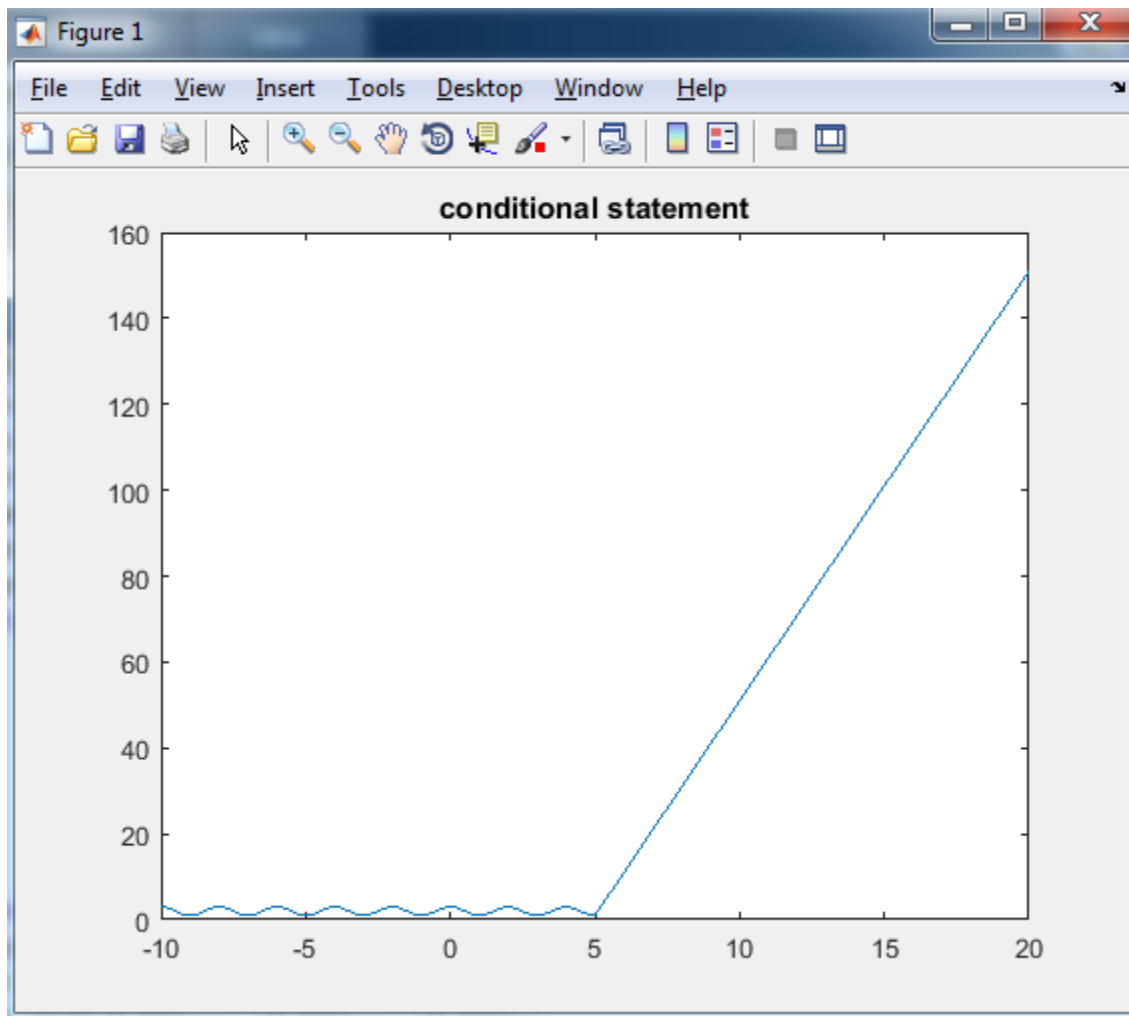
16. Write a script `le` using conditional statements to evaluate the following function, assuming that the scalar variable x has a value. The function is $y = e^{x+1}$ for $x < -1$, $y = 2 + \cos(\pi x)$ for $-1 \leq x < 5$, and $y = 10(x - 5) + 1$ for $x \geq 5$. Use your `le` to evaluate y for $x = -5$, $x = 3$, and $x = 15$, and check the results by hand.

Solution:

```

Editor - C:\Users\dell\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_16.m
+7  |  Prac_Chap4_test_understanding (1).m  |  Prac_for_loop.m  |  test_name_entering.m  |  que_16.m  |  +
1 -  |  clc
2 -  |  clear all
3 -  |  close all
4 -  |  xmax=20; xmin=-10;
5 -  |  diff=(xmax-xmin)/200;
6 -  |  x=xmin:diff:xmax;
7 -  |  for k=1:length(x)
8 -  |      if x(k) >= 5
9 -  |          y(k) = (10*(x(k)-5)) + 1;
10 - |      elseif -1 <= x(k) < 5
11 - |          y(k) = 2 + (cos(pi*x(k)));
12 - |      else
13 - |          y(k) = exp(x(k)+1);
14 - |      end
15 - |  end
16 - |  plot(x,y), title('conditional statement')
17 - |  % kk1=round((-5-xmin)/diff); kk2=round((3-xmin)/diff); kk3=round((15-xmin)/diff);
18 - |  % disp(x(kk1)), (x(kk2)), (x(kk3))
19 - |  % disp(y(kk1)), (y(kk2)), (y(kk3))
20 - |  %x=-5
21 - |  y1=ginput(1)
22 - |  %x=3
23 - |  y2=ginput(2)
24 - |  %x=15
25 - |  y3=ginput(3)

```



18. Write a program that accepts a numerical value x from 0 to 100 as input and computes and displays the corresponding letter grade given by the following table.

A $x \geq 90$

B $80 \leq x \leq 89$

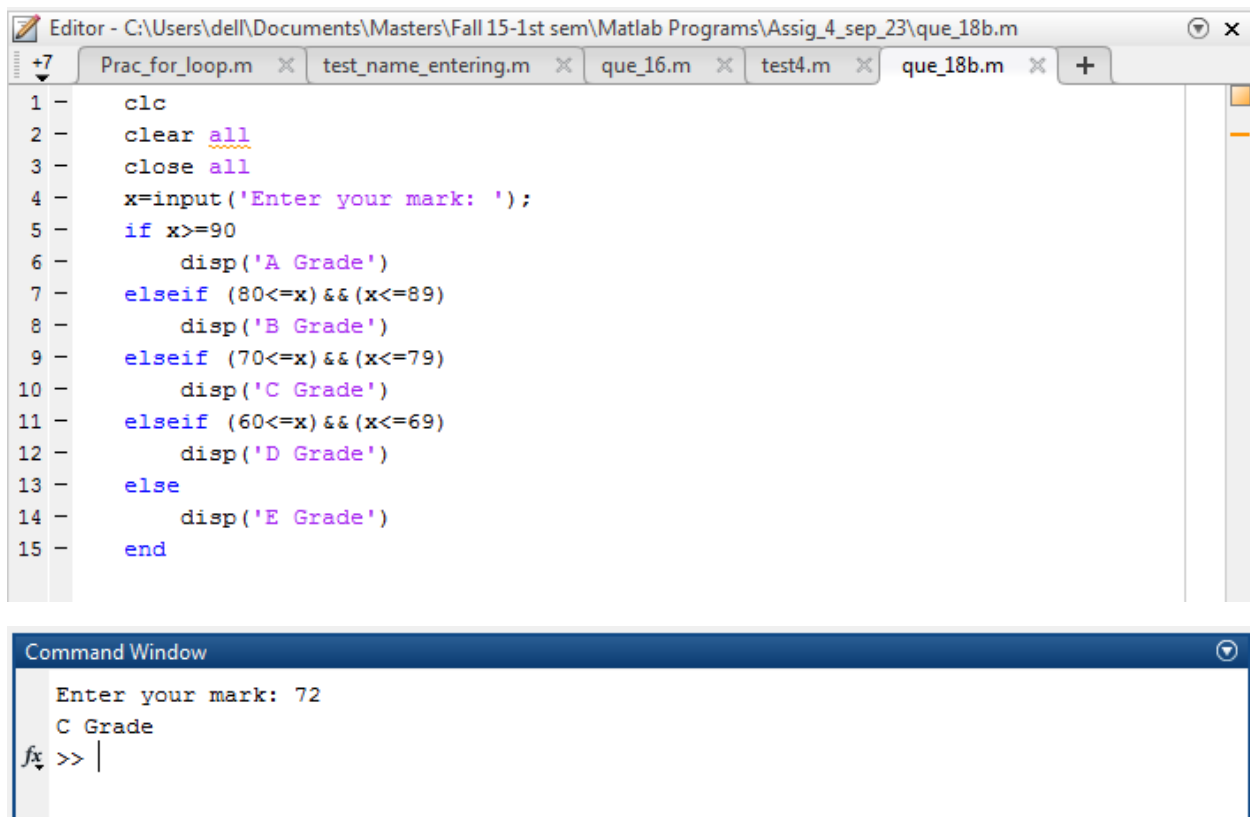
C $70 \leq x \leq 79$

D $60 \leq x \leq 69$

F $x < 60$

- Use nested if statements in your program (do not use elseif).
- Use only elseif clauses in your program.

Solution:

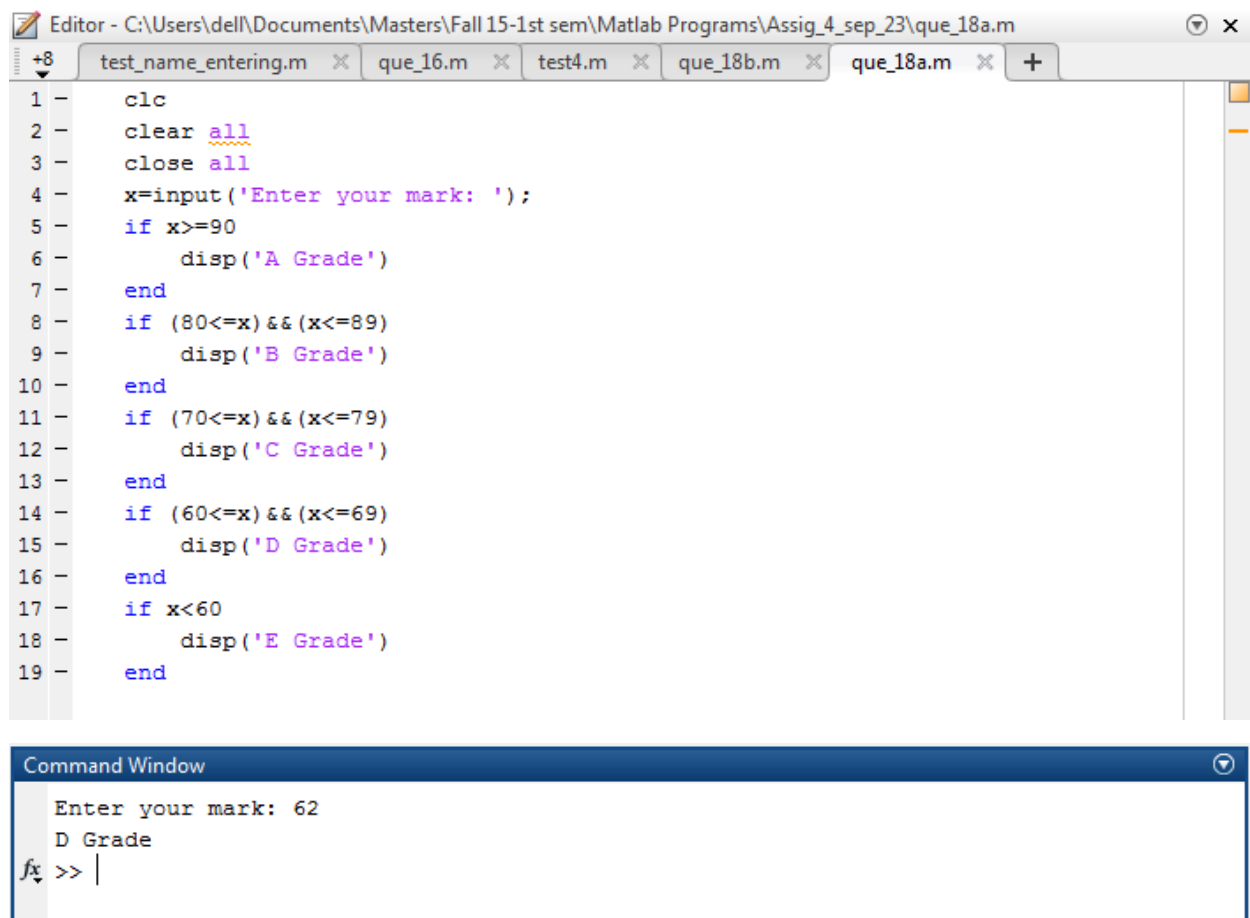


The screenshot shows the MATLAB Editor window with a script named 'que_18b.m'. The script uses elseif clauses to determine the letter grade based on the input mark. The Command Window shows the execution of the script, where the user enters '72' and the output is 'C Grade'.

```
Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_18b.m
+7  | 1 -   clc
    | 2 -   clear all
    | 3 -   close all
    | 4 -   x=input('Enter your mark: ');
    | 5 -   if x>=90
    | 6 -       disp('A Grade')
    | 7 -   elseif (80<=x) && (x<=89)
    | 8 -       disp('B Grade')
    | 9 -   elseif (70<=x) && (x<=79)
    |10 -       disp('C Grade')
    |11 -   elseif (60<=x) && (x<=69)
    |12 -       disp('D Grade')
    |13 -   else
    |14 -       disp('E Grade')
    |15 -   end

Command Window
Enter your mark: 72
C Grade
fx >> |
```


Without using else



The image shows a MATLAB Editor window with a script named 'que_18a.m'. The script uses a series of 'if' statements to determine a grade based on a user input 'x'. The grades are: A (x >= 90), B (80 <= x <= 89), C (70 <= x <= 69), D (60 <= x <= 59), and E (x < 60). The Command Window shows the execution of the script, where the user entered '62' and the output was 'D Grade'.

```
Editor - C:\Users\dell\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_18a.m
+8 test_name_entering.m x que_16.m x test4.m x que_18b.m x que_18a.m x +
1 - clc
2 - clear all
3 - close all
4 - x=input('Enter your mark: ');
5 - if x>=90
6 -     disp('A Grade')
7 - end
8 - if (80<=x) && (x<=89)
9 -     disp('B Grade')
10 - end
11 - if (70<=x) && (x<=69)
12 -     disp('C Grade')
13 - end
14 - if (60<=x) && (x<=59)
15 -     disp('D Grade')
16 - end
17 - if x<60
18 -     disp('E Grade')
19 - end

Command Window
Enter your mark: 62
D Grade
fx >> |
```

20. Figure P20 shows a mass-spring model of the type used to design packaging systems and vehicle suspensions, for example. The springs exert a force that is proportional to their compression, and the proportionality constant is the spring constant k . The two side springs provide additional resistance if the weight W is too heavy for the center spring. When the weight W is gently placed, it moves through a distance x before coming to rest. From statics, the weight force must balance the spring forces at this new position. Thus

$$\begin{aligned} W &= k_1 x & \text{if } x < d \\ W &= k_1 x + 2k_2(x - d) & \text{if } x \geq d \end{aligned}$$

These relations can be used to generate the plot of x versus W .

- a. Create a function `le` that computes the distance x , using the input parameters W , k_1 , k_2 , and d . Test your function for the following two cases, using the values $k_1 = 10^4$ N/m; $k_2 = 1.5 \times 10^4$ N/m; $d = 0.1$ m.

$$W = 500 \text{ N}$$

$$W = 2000 \text{ N}$$

- b. Use your function to plot x versus W for $0 \leq W \leq 3000$ N for the values of k_1 , k_2 , and d given in part a.

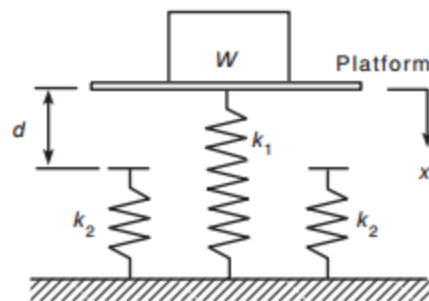


Figure P20

Solution:

```

Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_20a.m
+14  que_16.m  x  que_18b.m  x  que_18a.m  x  springdist.m  x  que_20a.m  x  +
1 -   clc
2 -   clear all
3 -   close all
4 -   d=0.1; k1=10^4;k2=1.5*10^4;
5 -   W=[500,2000];
6 -   % to find value for x
7 -   for i=1:length(W)
8 -       x=springdist(W(i),k1,k2,d)
9 -   end
10 -   W1=0:1:3000;
11 -   plot(springdist(W1,k1,k2,d),W1)
12
13

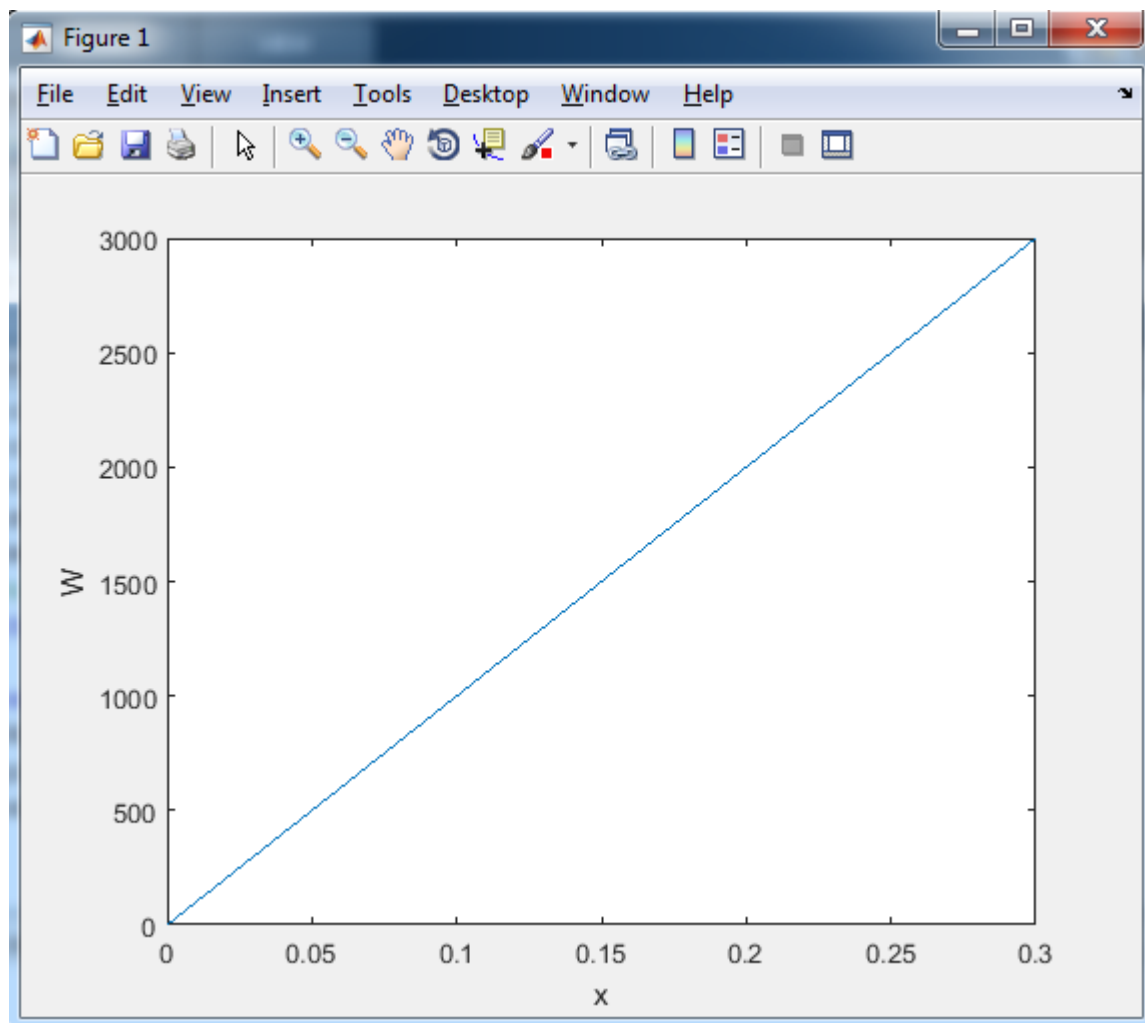
```

Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\springdist.m

```
1 function x=springdist(W,k1,k2,d)
2     x=W/k1;
3     if x>=d
4         x=(W+(2*k2*d))/(k1+2*k2);
5     end
6
7
8
```

Command Window

```
x =
    0.0500
|
x =
    0.1250
.
```



23. The (x, y) coordinates of a certain object as a function of time t are given by

$$x(t) = 5t - 10 \quad y(t) = 25t^2 - 120t + 144$$

for $0 \leq t \leq 4$. Write a program to determine the time at which the object is the closest to the origin at $(0, 0)$. Determine also the minimum distance. Do this in two ways:

- By using a `for` loop.
- By not using a `for` loop.

Solution:

```
Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_23.m
+12 que_20a.m x que_23.m x test1_28_09.m x que_26.m x que_36.m x que_23b.m x +
1 - clc
2 - clear all
3 - close all
4 - t=0:0.01:4;
5 - x=(5*t)-10;
6 - y=((25*t.^2)-(120.*t)+144);
7 - d=sqrt(x.^2+y.^2);
8 - mini=10
9 - % r=min(d)
10 - for k=1:length(t)
11 -     if d(k)<mini
12 -         mini=d(k);
13 -         tmin=t(k);
14 -     end
15 - end
16 - disp('Min distance is: ')
17 - disp(mini)
18 - disp('time: ')
19 - disp(tmin)
20
```

```
Editor - C:\Users\del\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_23b.m
+12 que_20a.m x que_23.m x test1_28_09.m x que_26.m x que_36.m x que_23b.m x +
1 - clc
2 - clear all
3 - close all
4 - t=0:0.01:4;
5 - x=(5*t)-10;
6 - y=((25*t.^2)-(120.*t)+144);
7 - d=sqrt(x.^2+y.^2);
8 - [dist,k]=min(d)
9 - tmin=t(k)
10 - disp('min distance: ')
11 - disp(dist)
12 - disp('time: ')
13 - disp(tmin)
```

```
Command Window

k =

    224

tmin =

    2.2300

min distance:

    1.3581

time:

    2.2300
```

26. Electrical resistors are said to be connected “in series” if the same current passes through each and “in parallel” if the same voltage is applied across each. If in series, they are equivalent to a single resistor whose resistance is given by

$$R = R_1 + R_2 + R_3 + \dots + R_n$$

If in parallel, their equivalent resistance is given by

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}$$

Write an M- file that prompts the user for the type of connection (series or parallel) and the number of resistors n and then computes the equivalent resistance.

Solution:

```
Editor - C:\Users\delh\Documents\Masters\Fall 15-1st sem\Matlab Programs\Assig_4_sep_23\que_26.m
+10 que_18a.m x springdist.m x que_20a.m x que_23.m x test1_28_09.m x que_26.m x +
1 - clc
2 - clear all
3 - close all
4 - R=1:1:20;
5 - x=input('Enter the connection type: ','s')
6 - if x=='S'
7 -     EqRes=sum(R);
8 - elseif x=='P'
9 -     EqRes=1./(sum(R));
10 - else
11 -     disp('Please Enter correct connection type')
12 - end
13 - disp(EqRes)
14
```

```
Command Window
Enter the connection type: S

x =

S

210
```

36.* In the structure in Figure P36a, six wires support three beams. Wires 1 and 2 can support no more than 1200 N each, wires 3 and 4 can support no more than 400 N each, and wires 5 and 6 can support no more than 200 N each. Three equal weights W are attached at the points shown. Assuming that the structure is stationary and that the weights of the wires and the beams are very small compared to W , the principles of statics applied to a particular beam state that the sum of vertical forces is zero and

Solution:

```
+11 springdist.m x que_20a.m x que_23.m x test1_28_09.m x que_26.m x que_36.m x +
1 - clc
2 - clear all
3 - close all
4 - X=[1,1,-1,-1,0,-1;1.4,-1,-0.8,0,-1,2;0,0,1,1,-1,0;
5   0,0,0,3,-2,0;0,0,0,0,1,1;0,0,0,0,0,3];
6 - for w=1:1200
7 -     W=[w;w;w;w;w;w];
8 -     T=X\W;
9 -     if T<=[1200;1200;400;400;200;200]
10 -         optimalwt= w;
11 -     end
12 - end
13 - % disp(optimalwt)
14 - w2=max(optimalwt)
15 - W=[w2;w2;w2;w2;w2;w2];
16 - T=X\W
17 -
```

Command Window

300

w2 =

300

T =

588.8889

311.1111

266.6667

233.3333

200.0000

100.0000

f_x >>