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## The Experiment Report of Machine Learning

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**SCHOOL: SCHOOL OF SOFTWARE ENGINEERING**

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# Recommender System Based on Matrix Decomposition

**Abstract**—This experiment intends to use ALS or SGD or other methods to implement a recommender system based on matrix decomposition.

## I. INTRODUCTION

Recommender system is a common technique to recommend something such as movies, goods for us based on our favourites. In the experiment, I use SGD to implement a small recommender system based on matrix decomposition.

## II. METHODS AND THEORY

### A. Collaborative Filtering

Make automatic predictions (filtering) about the interests of a user by collecting preferences or taste information from many other users (collaboration).

There are some types of collaborative filtering.

- Memory-based CF: utilize the entire user-item database to generate a prediction.
- Model-based CF: build a model from the rating data (Matrix factorization, etc.) and use this model to predict missing ratings.

In this experiment, I use model-based CF.

### B. Matrix Factorization

- Give a rating matrix  $\mathbf{R} \in \mathbb{R}^{m \times n}$ , with sparse ratings from  $m$  users to  $n$  items.
- Assume rating matrix  $\mathbf{R}$  can be factorized into the multiplication of two low-rank feature matrices  $\mathbf{P} \in \mathbb{R}^{m \times k}$  And  $\mathbf{Q} \in \mathbb{R}^{k \times n}$

### C. Stochastic Gradient Descent(SGD) in Matrix Factorization

- SGD is to minimize the following objective function:

$$\mathcal{L} = \sum_{u,i \in \Omega} (r_{u,i} - \mathbf{p}_u^T \mathbf{q}_i)^2 + \lambda_p \|\mathbf{p}_u\|^2 + \lambda_q \|\mathbf{q}_i\|^2$$

Notes:

$$\mathbf{P} = [\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_m]^T \in \mathbb{R}^{m \times k}$$

$$\mathbf{Q} = [\mathbf{q}_1, \mathbf{q}_2, \dots, \mathbf{q}_n] \in \mathbb{R}^{k \times n}$$

$r_{u,i}$  denotes the actual rating of user  $u$  for item  $i$

$\Omega$  denotes the set of observed samples from rating matrix  $\mathbf{R}$

$\lambda_p, \lambda_q$  are regularization parameters to avoid overfitting

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### Algorithm 3 General Steps of SGD

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- 1: **Require** feature matrices  $\mathbf{P}, \mathbf{Q}$ , observed set  $\Omega$ , regularization parameters  $\lambda_p, \lambda_q$  and learning rate  $\alpha$ .
  - 2: **Randomly** select an observed sample  $r_{u,i}$  from observed set  $\Omega$ .
  - 3: Calculate the **gradient** w.r.t to the objective function.
  - 4: **Update** the feature matrices  $\mathbf{P}$  and  $\mathbf{Q}$  with learning rate  $\alpha$  and gradient.
  - 5: **Repeat** the above processes until **convergence**.
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- Calculate the gradient and update the feature matrices
- Objective function:

$$\mathcal{L} = (r_{u,i} - \mathbf{p}_u^T \mathbf{q}_i)^2 + \lambda_p \|\mathbf{p}_u\|^2 + \lambda_q \|\mathbf{q}_i\|^2$$

We randomly select an observed sample  $r_{u,i}$

And then we calculate the prediction error:

$$E_{u,i} = r_{u,i} - \mathbf{p}_u^T \mathbf{q}_i$$

Also, we calculate the gradient:

$$\frac{\partial \mathcal{L}}{\partial \mathbf{p}_u} = E_{u,i}(-\mathbf{q}_i) + \lambda_p \mathbf{p}_u$$

$$\frac{\partial \mathcal{L}}{\partial \mathbf{q}_i} = E_{u,i}(-\mathbf{p}_u) + \lambda_q \mathbf{q}_i$$

Finally, we update the feature matrices  $\mathbf{P}$  and  $\mathbf{Q}$  with **learning rate**  $\alpha$ :

$$\mathbf{p}_u = \mathbf{p}_u + \alpha(E_{u,i}\mathbf{q}_i - \lambda_p \mathbf{p}_u)$$

$$\mathbf{q}_i = \mathbf{q}_i + \alpha(E_{u,i}\mathbf{p}_u - \lambda_q \mathbf{q}_i)$$

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### Algorithm 4 SGD Algorithm

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- 1: **Require** feature matrices  $\mathbf{P}, \mathbf{Q}$ , observed set  $\Omega$ , regularization parameters  $\lambda_p, \lambda_q$  and learning rate  $\alpha$ .
  - 2: **Randomly** select an observed sample  $r_{u,i}$  from observed set  $\Omega$ .
  - 3: Calculate the **gradient** w.r.t to the objective function:
 
$$E_{u,i} = r_{u,i} - \mathbf{p}_u^T \mathbf{q}_i$$

$$\frac{\partial \mathcal{L}}{\partial \mathbf{p}_u} = E_{u,i}(-\mathbf{q}_i) + \lambda_p \mathbf{p}_u$$

$$\frac{\partial \mathcal{L}}{\partial \mathbf{q}_i} = E_{u,i}(-\mathbf{p}_u) + \lambda_q \mathbf{q}_i$$
  - 4: **Update** the feature matrices  $\mathbf{P}$  and  $\mathbf{Q}$  with learning rate  $\alpha$  and gradient:
 
$$\mathbf{p}_u = \mathbf{p}_u + \alpha(E_{u,i}\mathbf{q}_i - \lambda_p \mathbf{p}_u)$$

$$\mathbf{q}_i = \mathbf{q}_i + \alpha(E_{u,i}\mathbf{p}_u - \lambda_q \mathbf{q}_i)$$
  - 5: **Repeat** the above processes until **convergence**.
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## III. EXPERIMENT

### A. Dataset

This dataset is MovieLens-100k dataset. u.data in the dataset contains 10000 ratings on 1682 movies from 943 users. Each user has rated at least 20 movies. user\_id and item\_id are marked with the beginning of number 1. Also, the data is distributed randomly.



## B. Implementation

### (1) Initialization

In this experiment, I initialize the initial rating matrix with all zero and I initialize users matrix P and items matrix Q by random distribution method.

### (2) Parameters

Table 1 shown below shows all the parameters in the experiment.

Table 1-SGD on matrix decomposition

Parameters	Values
Learning rate	0.0002
Number of iterations	50
Penalty factor	100
Number of potential features	150

### (3) Results

Figure 1 shown below shows the result using the parameters listed above.

Figure 1-Loss value result

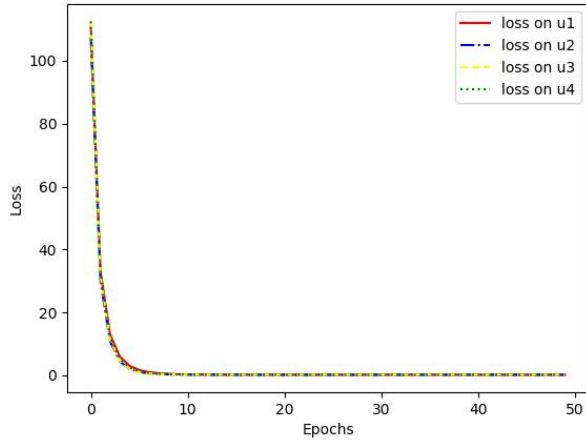


Figure 2 shown below shows the result using a smaller potential features. Here, potential features is 50. Initial loss value is small.

Figure 2-Loss value result(Smaller potential features)

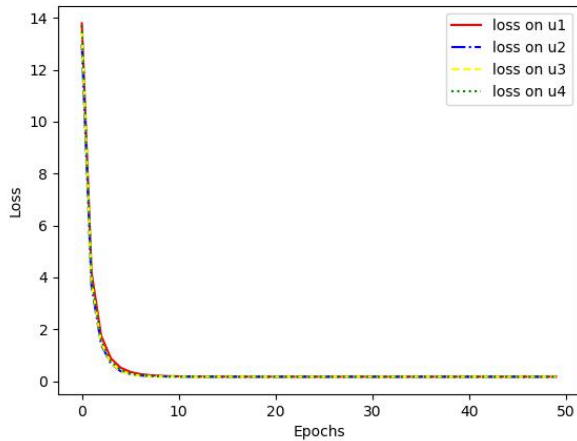


Figure 3 shown below shows the result using a larger potential features. Here, potential features is 350. Initial loss value is large.

Figure 3-Loss value result(Larger potential features)

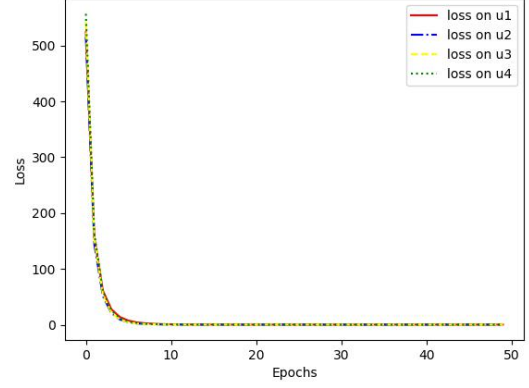


Figure 4 shown below shows the result using a larger penalty factor. Here, penalty factor is 800. Initial loss value is very small and it is very fast to converge.

Figure 4-Loss value result (Larger penalty factor)

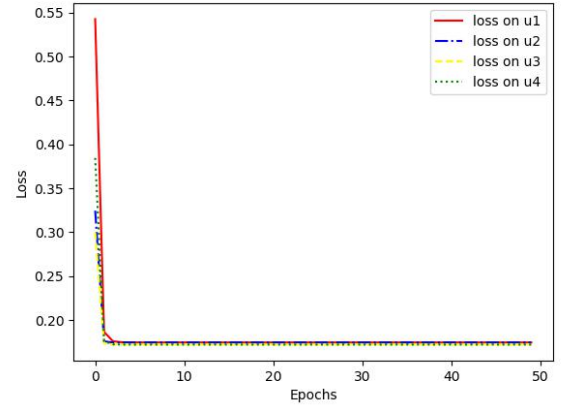


Figure 5 shown below shows the result using a smaller penalty factor. Here, penalty factor is 0.5. Initial loss value is large and it is slow to converge.

Figure 5-Loss value result(Smaller penalty factor)

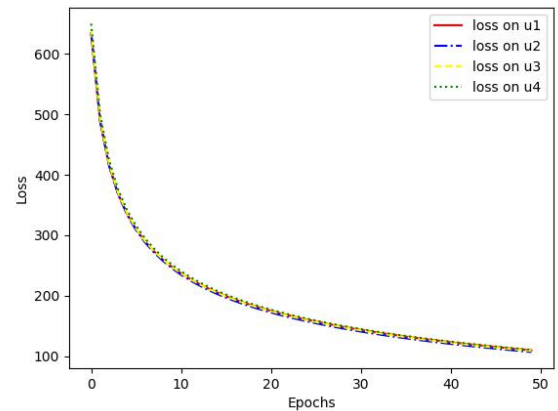




Figure 6 shown below shows the result using a smaller learning rate(LR). Here, learning rate is  $1e-7$ . Initial loss value is very large and it is very slow to converge.

Figure 6-Loss value result(Smaller learning rate)

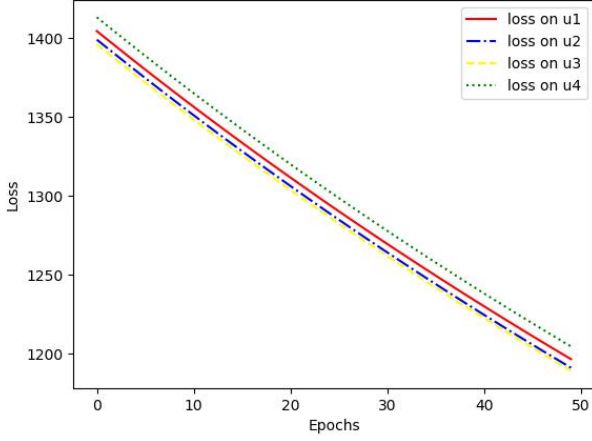
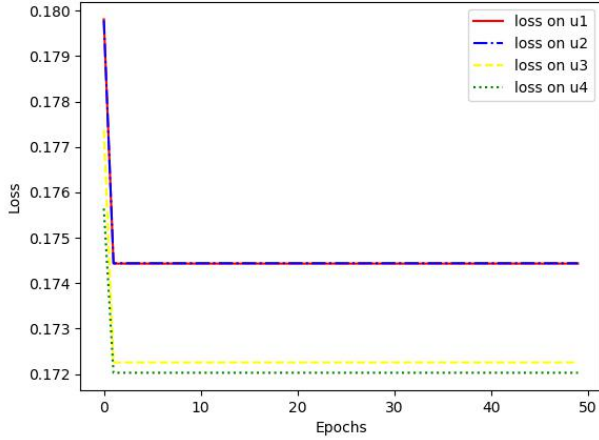


Figure 7 shown below shows the result using a larger learning rate(LR). Here, learning rate is 0.01. Initial loss value is very small and it is very fast to converge.

Figure 7-Loss value result(Larger learning rate)



#### IV. CONCLUSION

- (1) Recommender system is a common technique to recommend something useful for users. There are many methods and models to implement a recommender system such as ALS, SGD, SVD.
- (2) Parameters will play an important role in the performance of the models. A large learning rate will make the loss function faster to converge or it won't be converged. A small learning rate will make the loss function slower to converge. A large potential features will make the initial loss value larger. A small potential features will make the initial loss value smaller. Also, a large penalty factor will make the initial loss value smaller and it will be faster to converge in this experiment. A small penalty factor will make the initial loss value larger and it will be much slower to converge.