# Assignment 1

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#### Question taken from

cbse/math/10/2006/set2-Q17

## 1 Question 1

Find the value of p for which the points

$$\mathbf{A} = \begin{pmatrix} -5 \\ 1 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ p \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 4 \\ -2 \end{pmatrix}$$
 are collinear

#### 2 Solution

Given:- Given:-  $\mathbf{A} = \begin{pmatrix} -5 \\ 1 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ p \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 4 \\ -2 \end{pmatrix}$ 

Given that the points are collinear, so we create a matrix

$$\mathbf{M} = \begin{pmatrix} \mathbf{B} - \mathbf{A} & \mathbf{C} - \mathbf{A} \end{pmatrix}^{\mathsf{T}} \tag{2.0.1}$$

where  $rank(\mathbf{M}) = 1$ . We have the matrix  $\mathbf{M}$  as,

$$\mathbf{M} = \begin{pmatrix} 1+5 & p-1 \\ 4+5 & -2-1 \end{pmatrix} \tag{2.0.2}$$

$$\implies \mathbf{M} = \begin{pmatrix} 6 & p-1 \\ 9 & -3 \end{pmatrix} \tag{2.0.3}$$

Now we row reduce the matrix M,

$$\begin{pmatrix} 6 & p-1 \\ 9 & -3 \end{pmatrix} \stackrel{R_1 \leftrightarrow R_2}{\longleftrightarrow} \begin{pmatrix} 9 & -3 \\ 6 & p-1 \end{pmatrix} \tag{2.0.4}$$

$$\stackrel{R_1 \to \frac{R_1}{3}}{\longleftrightarrow} \begin{pmatrix} 3 & -1 \\ 6 & p-1 \end{pmatrix} \tag{2.0.5}$$

$$\stackrel{R_2 \to R_2 - 2R_1}{\longleftrightarrow} \begin{pmatrix} 3 & -1 \\ 0 & p+1 \end{pmatrix} \tag{2.0.6}$$

$$\stackrel{R_1 \to \frac{R_1}{3}}{\longleftrightarrow} \begin{pmatrix} 1 & \frac{-1}{3} \\ 0 & p+1 \end{pmatrix} \tag{2.0.7}$$

Since  $rank(\mathbf{M}) = 1$ , we have

$$p + 1 = 0 (2.0.8)$$

$$\implies p = -1 \tag{2.0.9}$$

Fig.2.1 verifies that the points are indeed collinear for p = -1

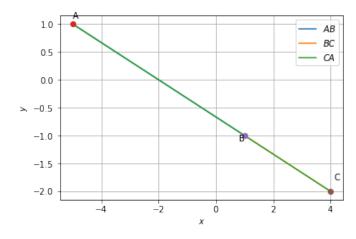


Fig. 2.1: Collinear