

## AI Assignment

1) Convert FOL to CNF

$$\forall x [\exists z \text{ animal}(z) \wedge \text{kills}(x, z)]$$

$$\Rightarrow [\forall y \rightarrow \text{loves}(y, x)]$$

2) Eliminate implication:  $A \Rightarrow B \equiv \neg A \vee B$ 

$$\forall x [\neg \exists z \text{ Animal}(z) \wedge \text{kills}(x, z)] \vee$$

$$\forall y \rightarrow \text{loves}(y, x)$$

3) Move  $\neg$  inwards:  $\neg \exists x P \equiv \forall x \neg P$ 

$$\forall x [\forall z \neg (\text{Animal}(z) \wedge \text{kills}(x, z))] \vee$$

$$\forall y \rightarrow \text{loves}(y, x)$$

4) Prep universal quantifiers:

$$[\neg \text{Animal}(z) \vee \neg \text{kills}(x, z)] \vee \rightarrow \text{loves}(y, x)$$

5) CNF:

$$\neg \text{Animal}(z) \vee \neg \text{kills}(x, z) \vee \rightarrow \text{loves}(y, x)$$



Regt..

II) Convert to FOL & prove using resolution

→ Cold & precipitation  $\rightarrow$  snow

$$\text{cold}(x) \wedge \text{precipitation}(x) \Rightarrow \text{snow}(x)$$

$$\neg \text{cold}(x) \vee \neg \text{precipitation}(x) \vee \text{snow}(x)$$

$$\neg \text{cold}(x) \vee \neg \text{precipitation}(x) \vee \text{snow}(x)$$

ii) → January  $\rightarrow$  cold

$$\text{January}(x) \Rightarrow \text{cold}(x)$$

$$\neg \text{January}(x) \vee \text{cold}(x)$$

iii) clouds  $\rightarrow$  ppt

$$\text{clouds}(x) \Rightarrow \text{ppt}(x)$$

$$\neg \text{clouds}(x) \vee \text{ppt}(x)$$

iv) January(x)

v) ~~January(x)~~ clouds(x)

To prove: snow(x)

→ Resolution of (i) & (ii)

$$\text{vi) } \neg \text{ppt}(x) \vee \text{snow}(x) \vee \neg \text{January}(x)$$

→ Resolution of (vi) & (iv)

$$\text{vii) } \neg \text{ppt}(x) \vee \text{snow}(x)$$

□

Q.E.D.

→ resolution of (vii) & (iii)

(viii) snow(x)  $v \rightarrow$  clouds

→ resolution of (viii) & (v)

~~is~~ snow(x)

Proved