CS795-1.a.

April 19, 2022

[1]: import sys

```
%pip install torch
    Requirement already satisfied: torch in ./opt/anaconda3/lib/python3.8/site-
    packages (1.11.0)
    Requirement already satisfied: typing-extensions in
    ./opt/anaconda3/lib/python3.8/site-packages (from torch) (3.7.4.3)
    WARNING: You are using pip version 21.2.4; however, version 22.0.4 is
    available.
    You should consider upgrading via the
    '/Users/pankajjatav/opt/anaconda3/bin/python -m pip install --upgrade pip'
    command.
    Note: you may need to restart the kernel to use updated packages.
[2]: import torch
[3]: x = torch.tensor(1.0, requires_grad=True)
     y = torch.tensor(1.0, requires_grad=True)
     f = x*y
     print(x)
     print(y)
     print(f)
     for i in range(100):
         x = x - (1 * y)
         y = y - (1 * x)
         print("Partial derivative with respect to x: ", x)
         print("Partial derivative with respect to y: ", y)
    tensor(1., requires_grad=True)
    tensor(1., requires_grad=True)
    tensor(1., grad_fn=<MulBackward0>)
    Partial derivative with respect to x:
                                           tensor(0., grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                           tensor(1., grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                           tensor(-1., grad_fn=<SubBackward0>)
```

```
tensor(2., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                       tensor(-3., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(5., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-8., grad_fn=<SubBackward0>)
                                       tensor(13., grad fn=<SubBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                       tensor(-21., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(34., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-55., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(89., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-144., grad_fn=<SubBackward0>)
                                       tensor(233., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                       tensor(-377., grad_fn=<SubBackward0>)
                                       tensor(610., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                       tensor(-987., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(1597., grad_fn=<SubBackward0>)
                                       tensor(-2584., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
Partial derivative with respect to y:
                                       tensor(4181., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-6765., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(10946., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-17711., grad fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(28657., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-46368., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(75025., grad_fn=<SubBackward0>)
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Partial derivative with respect to x:
Partial derivative with respect to y:
                                       tensor(196418., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-317811., grad_fn=<SubBackward0>)
                                       tensor(514229., grad_fn=<SubBackward0>)
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Partial derivative with respect to x:
                                       tensor(-832040., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(1346269., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-2178309., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(3524578., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-5702887., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(9227465., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-14930352.,
grad fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(24157816., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-39088168.,
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(63245984., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-1.0233e+08,
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(1.6558e+08,
grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-2.6791e+08,
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(4.3349e+08,
grad_fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-7.0141e+08,
```

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grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(1.1349e+09,
grad_fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-1.8363e+09,
grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(2.9712e+09,
grad fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-4.8075e+09,
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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grad_fn=<SubBackward0>)
Partial derivative with respect to x:
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grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(5.3316e+10,
grad_fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-8.6268e+10,
grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(1.3958e+11,
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Partial derivative with respect to y: tensor(4.4946e+13,
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Partial derivative with respect to x: tensor(-7.2723e+13,
```

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Partial derivative with respect to x: tensor(-1.9039e+14,
grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(3.0806e+14,
grad fn=<SubBackward0>)
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Partial derivative with respect to x: tensor(-8.9444e+15,
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Partial derivative with respect to y: tensor(1.4472e+16,
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Partial derivative with respect to x: tensor(-2.3417e+16,
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
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Partial derivative with respect to x:
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Partial derivative with respect to y: tensor(6.7989e+17,
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Partial derivative with respect to y:
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Partial derivative with respect to y: tensor(4.6600e+18,
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Partial derivative with respect to x: tensor(-7.5401e+18,
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Partial derivative with respect to x: tensor(-1.9740e+19,
grad fn=<SubBackward0>)
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Partial derivative with respect to y:
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                                      tensor(-2.4279e+21,
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grad fn=<SubBackward0>)
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Partial derivative with respect to x: tensor(-7.8177e+23,
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Partial derivative with respect to x: tensor(-2.0467e+24,
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Partial derivative with respect to y: tensor(3.3116e+24,
grad fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-5.3584e+24,
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Partial derivative with respect to y:
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Partial derivative with respect to x:
                                       tensor(-1.4028e+25,
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Partial derivative with respect to y: tensor(2.2698e+25,
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Partial derivative with respect to x:
                                       tensor(-3.6727e+25,
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                                      tensor(-2.5173e+26,
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Partial derivative with respect to x:
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Partial derivative with respect to y: tensor(2.7917e+27,
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Partial derivative with respect to x: tensor(-4.5171e+27,
grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(7.3088e+27,
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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Partial derivative with respect to y: tensor(5.0095e+28,
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Partial derivative with respect to x: tensor(-8.1056e+28,
```

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grad_fn=<SubBackward0>)
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grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(3.4336e+29,
grad fn=<SubBackward0>)
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Partial derivative with respect to y:
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Partial derivative with respect to x: tensor(-9.9692e+30,
grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(1.6131e+31,
grad_fn=<SubBackward0>)
                                      tensor(-2.6100e+31,
Partial derivative with respect to x:
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
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grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                       tensor(-6.8330e+31,
grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                       tensor(1.1056e+32,
grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                      tensor(-1.7889e+32,
grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(2.8945e+32,
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Partial derivative with respect to x: tensor(-4.6834e+32,
grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(7.5779e+32,
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Partial derivative with respect to x: tensor(-1.2261e+33,
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(5.1940e+33,
grad_fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-8.4040e+33,
```

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grad_fn=<SubBackward0>)
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grad_fn=<SubBackward0>)
Partial derivative with respect to x: tensor(-2.2002e+34,
grad fn=<SubBackward0>)
Partial derivative with respect to y: tensor(3.5600e+34,
grad fn=<SubBackward0>)
Partial derivative with respect to x:
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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Partial derivative with respect to x:
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grad_fn=<SubBackward0>)
Partial derivative with respect to y: tensor(1.6724e+36,
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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Partial derivative with respect to y:
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Partial derivative with respect to y:
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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Partial derivative with respect to y:
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Partial derivative with respect to x:
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                                       tensor(inf, grad_fn=<SubBackward0>)
Partial derivative with respect to y:
```

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Partial derivative with respect to x:
                                            tensor(-inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                            tensor(-inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                            tensor(-inf, grad fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                            tensor(-inf, grad fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                            tensor(-inf, grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(inf, grad_fn=<SubBackward0>)
[4]: x = torch.tensor(1.0, requires_grad=True)
     y = torch.tensor(1.0, requires grad=True)
     f = x*y
     print(x)
     print(y)
     print(f)
     for i in range(100):
         x_half = x - (1 * y)
         y_half = y + (1 * x)
         x = x - (1 * y_half)
         y = y + (1 * x half)
         print("Partial derivative with respect to x: ", x)
         print("Partial derivative with respect to y: ", y)
    tensor(1., requires_grad=True)
    tensor(1., requires_grad=True)
    tensor(1., grad_fn=<MulBackward0>)
    Partial derivative with respect to x:
                                            tensor(-1., grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(1., grad fn=<AddBackward0>)
    Partial derivative with respect to x:
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    Partial derivative with respect to y:
                                            tensor(-1., grad_fn=<AddBackward0>)
    Partial derivative with respect to x:
                                            tensor(1., grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(-1., grad_fn=<AddBackward0>)
    Partial derivative with respect to x:
                                            tensor(1., grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(1., grad_fn=<AddBackward0>)
                                            tensor(-1., grad_fn=<SubBackward0>)
    Partial derivative with respect to x:
                                            tensor(1., grad_fn=<AddBackward0>)
    Partial derivative with respect to y:
    Partial derivative with respect to x:
                                            tensor(-1., grad_fn=<SubBackward0>)
                                            tensor(-1., grad_fn=<AddBackward0>)
    Partial derivative with respect to y:
    Partial derivative with respect to x:
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                                            tensor(-1., grad_fn=<AddBackward0>)
    Partial derivative with respect to y:
    Partial derivative with respect to x:
                                            tensor(1., grad_fn=<SubBackward0>)
    Partial derivative with respect to y:
                                            tensor(1., grad_fn=<AddBackward0>)
```

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Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(1., grad_fn=<AddBackward0>)
Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
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                                        tensor(1., grad fn=<SubBackward0>)
Partial derivative with respect to x:
Partial derivative with respect to y:
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Partial derivative with respect to x:
                                        tensor(1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(1., grad_fn=<AddBackward0>)
Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(1., grad_fn=<AddBackward0>)
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<AddBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                        tensor(1., grad_fn=<SubBackward0>)
                                        tensor(-1., grad_fn=<AddBackward0>)
Partial derivative with respect to y:
Partial derivative with respect to x:
                                        tensor(1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(1., grad_fn=<AddBackward0>)
Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(1., grad_fn=<AddBackward0>)
Partial derivative with respect to x:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
                                        tensor(-1., grad fn=<AddBackward0>)
                                        tensor(1., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
Partial derivative with respect to y:
                                        tensor(-1., grad_fn=<AddBackward0>)
Partial derivative with respect to x:
                                        tensor(1., grad_fn=<SubBackward0>)
Partial derivative with respect to y:
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Partial derivative with respect to x:
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                                        tensor(1., grad_fn=<AddBackward0>)
Partial derivative with respect to y:
                                        tensor(-1., grad_fn=<SubBackward0>)
Partial derivative with respect to x:
Partial derivative with respect to y:
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Partial derivative with respect to x:
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