Different MLP Arcitectures on MNIST dataset

Loading data

```
In [2]: # if you keras is not using tensorflow as backend set "KERAS_BACKEND=tensorflow"
    from keras.utils import np_utils
    from keras.datasets import mnist
    import seaborn as sns
    from keras.initializers import RandomNormal
Using TensorFlow backend.
```

```
In [0]: import matplotlib.pyplot as plt
import numpy as np
import time
# https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4
# https://stackoverflow.com/a/14434334
# this function is used to update the plots for each epoch and error
def plt_dynamic(x, vy, ty, ax, colors=['b']):
    ax.plot(x, vy, 'b', label="Validation Loss")
    ax.plot(x, ty, 'r', label="Train Loss")
    plt.legend()
    plt.grid(True)
    fig.canvas.draw()
```

```
In [5]: print("Number of training examples :", X_train.shape[0], "and each image is of sh
print("Number of training examples :", X_test.shape[0], "and each image is of sha
```

Number of training examples: 60000 and each image is of shape (28, 28) Number of training examples: 10000 and each image is of shape (28, 28)

```
In [0]: # if you observe the input shape its 3 dimensional vector
# for each image we have a (28*28) vector
# we will convert the (28*28) vector into single dimensional vector of 1 * 784

X_train = X_train.reshape(X_train.shape[0], X_train.shape[1]*X_train.shape[2])
X_test = X_test.reshape(X_test.shape[0], X_test.shape[1]*X_test.shape[2])
```

In [7]: # after converting the input images from 3d to 2d vectors

print("Number of training examples :", X_train.shape[0], "and each image is of shaprint("Number of training examples :", X_test.shape[0], "and each image is of shape is of shape it.")

Number of training examples: 60000 and each image is of shape (784) Number of training examples: 10000 and each image is of shape (784)

In [8]: # An example data point
 print(X_train[0])

```
In [0]: | # if we observe the above matrix each cell is having a value between 0-255
          # before we move to apply machine learning algorithms lets try to normalize the d
          \# X \Rightarrow (X - Xmin)/(Xmax-Xmin) = X/255
          X train = X train/255
          X_{\text{test}} = X_{\text{test}}/255
In [10]: # example data point after normlizing
          print(X_train[0])
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In [11]: # here we are having a class number for each image
          print("Class label of first image :", y_train[0])
          # lets convert this into a 10 dimensional vector
          # ex: consider an image is 5 convert it into 5 => [0, 0, 0, 0, 0, 1, 0, 0, 0, 0]
          # this conversion needed for MLPs
          Y_train = np_utils.to_categorical(y_train, 10)
          Y_test = np_utils.to_categorical(y_test, 10)
          print("After converting the output into a vector : ",Y_train[0])
          Class label of first image : 5
          After converting the output into a vector : [0. 0. 0. 0. 0. 1. 0. 0. 0. 0.]
In [0]: from keras.models import Sequential
          from keras.layers import Dense, Activation
          # some model parameters
          output dim = 10
          input_dim = X_train.shape[1]
          batch size = 128
          nb epoch = 20
```

[1] MLP with 2 hidden layers

[1.1] Without Batch Normalization and Dropout

```
In [15]: # Multilayer perceptron

model = Sequential()
model.add(Dense(364, activation='relu', input_shape=(input_dim,), kernel_initiali
model.add(Dense(52, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(output_dim, activation='softmax'))

model.summary()
```

Layer (type)	Output Shape	Param #
dense_4 (Dense)	(None, 364)	285740
dense_5 (Dense)	(None, 52)	18980
dense_6 (Dense)	(None, 10)	530

Total params: 305,250 Trainable params: 305,250 Non-trainable params: 0

Non-trainable parails. 0

```
In [16]: model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accura
        history = model.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ver
       Train on 60000 samples, validate on 10000 samples
       Epoch 1/20
       c: 0.9213 - val loss: 0.1435 - val acc: 0.9563
       60000/60000 [=============== ] - 4s 74us/step - loss: 0.1041 - ac
       c: 0.9690 - val_loss: 0.0936 - val_acc: 0.9729
       c: 0.9796 - val loss: 0.0862 - val acc: 0.9755
       Epoch 4/20
       60000/60000 [============= ] - 4s 72us/step - loss: 0.0468 - ac
       c: 0.9855 - val loss: 0.0678 - val acc: 0.9787
       Epoch 5/20
       60000/60000 [=============== ] - 4s 72us/step - loss: 0.0343 - ac
       c: 0.9892 - val_loss: 0.0663 - val_acc: 0.9803
       Epoch 6/20
       60000/60000 [============= ] - 4s 73us/step - loss: 0.0247 - ac
       c: 0.9924 - val_loss: 0.0746 - val_acc: 0.9777
       Epoch 7/20
       60000/60000 [=============== ] - 4s 72us/step - loss: 0.0221 - ac
       c: 0.9933 - val loss: 0.0642 - val acc: 0.9820
       Epoch 8/20
       60000/60000 [============= ] - 4s 74us/step - loss: 0.0161 - ac
       c: 0.9946 - val loss: 0.0775 - val acc: 0.9788
       Epoch 9/20
       60000/60000 [============ ] - 4s 73us/step - loss: 0.0134 - ac
       c: 0.9957 - val loss: 0.0802 - val acc: 0.9788
       Epoch 10/20
       60000/60000 [============= ] - 5s 75us/step - loss: 0.0113 - ac
       c: 0.9964 - val_loss: 0.0733 - val_acc: 0.9803
        Epoch 11/20
       60000/60000 [=============== ] - 4s 74us/step - loss: 0.0126 - ac
       c: 0.9960 - val loss: 0.0737 - val acc: 0.9807
       Epoch 12/20
       60000/60000 [============= ] - 4s 73us/step - loss: 0.0090 - ac
       c: 0.9973 - val loss: 0.0772 - val acc: 0.9816
       Epoch 13/20
       c: 0.9971 - val loss: 0.0790 - val acc: 0.9812
       Epoch 14/20
       60000/60000 [============= ] - 4s 73us/step - loss: 0.0079 - ac
       c: 0.9975 - val loss: 0.0877 - val acc: 0.9808
       Epoch 15/20
       60000/60000 [================ ] - 4s 72us/step - loss: 0.0071 - ac
       c: 0.9976 - val loss: 0.0893 - val acc: 0.9781
       Epoch 16/20
       60000/60000 [============= ] - 4s 72us/step - loss: 0.0113 - ac
       c: 0.9965 - val loss: 0.0975 - val acc: 0.9787
       Epoch 17/20
       60000/60000 [=============== ] - 4s 73us/step - loss: 0.0045 - ac
       c: 0.9986 - val loss: 0.0982 - val acc: 0.9792
       Epoch 18/20
```

```
60000/60000 [=============] - 4s 73us/step - loss: 0.0110 - ac c: 0.9965 - val_loss: 0.0809 - val_acc: 0.9820 Epoch 19/20 60000/60000 [==============] - 4s 73us/step - loss: 0.0037 - ac c: 0.9990 - val_loss: 0.0829 - val_acc: 0.9831 Epoch 20/20 60000/60000 [=================] - 4s 72us/step - loss: 0.0056 - ac c: 0.9982 - val_loss: 0.0965 - val_acc: 0.9793
```

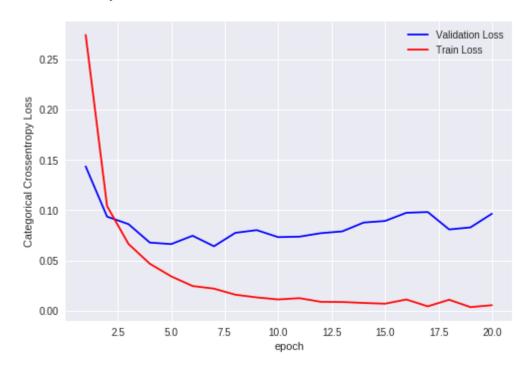
```
In [18]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

# List of epoch numbers
    x = list(range(1,nb_epoch+1))

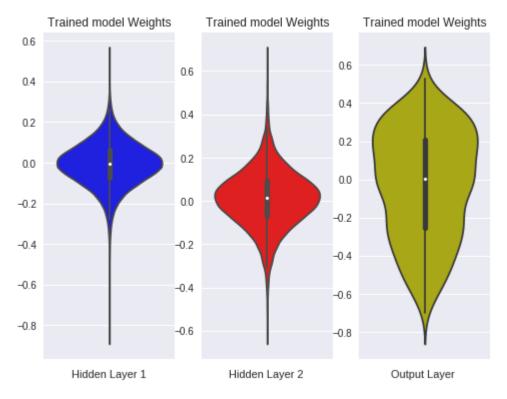
vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

Test score: 0.09650619211766216



```
In [19]: | w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out w = w after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2 w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



In [0]:

[1.2] With Batch Normalization and Dropout

```
In [21]: from keras.layers.normalization import BatchNormalization
    from keras.layers import Dropout

model = Sequential()
    model.add(Dense(364, activation='relu', input_shape=(input_dim,), kernel_initiali
    model.add(BatchNormalization())
    model.add(Dropout(0.5))
    model.add(Dense(52, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
    model.add(Dropout(0.5))
    model.add(Dropout(0.5))
    model.add(Dense(output_dim, activation='softmax'))

model.summary()
```

Layer (type)	Output	Shape	Param #
dense_7 (Dense)	(None,	364)	285740
batch_normalization_1 (Batch	(None,	364)	1456
dropout_1 (Dropout)	(None,	364)	0
dense_8 (Dense)	(None,	52)	18980
batch_normalization_2 (Batch	(None,	52)	208
dropout_2 (Dropout)	(None,	52)	0
dense_9 (Dense)	(None,	10)	530

Total params: 306,914 Trainable params: 306,082 Non-trainable params: 832

```
In [22]: model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accura
       history = model.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ver
       Train on 60000 samples, validate on 10000 samples
       Epoch 1/20
       cc: 0.8330 - val loss: 0.1736 - val acc: 0.9462
       Epoch 2/20
       60000/60000 [================ ] - 6s 96us/step - loss: 0.2584 - ac
       c: 0.9258 - val_loss: 0.1278 - val_acc: 0.9600
       60000/60000 [============= ] - 6s 95us/step - loss: 0.2003 - ac
       c: 0.9423 - val loss: 0.1044 - val acc: 0.9666
       Epoch 4/20
       c: 0.9502 - val loss: 0.0951 - val acc: 0.9706
       Epoch 5/20
       60000/60000 [=============== ] - 6s 96us/step - loss: 0.1487 - ac
       c: 0.9580 - val_loss: 0.0830 - val_acc: 0.9750
       Epoch 6/20
       60000/60000 [=============== ] - 6s 96us/step - loss: 0.1339 - ac
       c: 0.9607 - val_loss: 0.0770 - val_acc: 0.9758
       Epoch 7/20
       60000/60000 [=============== ] - 6s 96us/step - loss: 0.1257 - ac
       c: 0.9637 - val loss: 0.0756 - val acc: 0.9786
       Epoch 8/20
       60000/60000 [============= ] - 6s 97us/step - loss: 0.1200 - ac
       c: 0.9646 - val loss: 0.0714 - val acc: 0.9774
       Epoch 9/20
       60000/60000 [============ ] - 6s 97us/step - loss: 0.1103 - ac
       c: 0.9667 - val loss: 0.0714 - val acc: 0.9779
       Epoch 10/20
       60000/60000 [=============== ] - 6s 98us/step - loss: 0.1035 - ac
       c: 0.9689 - val_loss: 0.0715 - val_acc: 0.9781
       Epoch 11/20
       cc: 0.9704 - val loss: 0.0673 - val acc: 0.9794
       Epoch 12/20
       c: 0.9718 - val loss: 0.0667 - val acc: 0.9806
       Epoch 13/20
       60000/60000 [=============== ] - 6s 94us/step - loss: 0.0905 - ac
       c: 0.9728 - val_loss: 0.0634 - val_acc: 0.9803
       Epoch 14/20
       60000/60000 [============== ] - 6s 95us/step - loss: 0.0890 - ac
       c: 0.9733 - val loss: 0.0647 - val acc: 0.9805
       Epoch 15/20
       c: 0.9753 - val loss: 0.0686 - val acc: 0.9796
       Epoch 16/20
       60000/60000 [============= ] - 6s 97us/step - loss: 0.0787 - ac
       c: 0.9765 - val loss: 0.0614 - val acc: 0.9815
       Epoch 17/20
       60000/60000 [================ ] - 6s 96us/step - loss: 0.0801 - ac
       c: 0.9764 - val loss: 0.0632 - val acc: 0.9816
       Epoch 18/20
```

```
60000/60000 [=============] - 6s 95us/step - loss: 0.0736 - ac c: 0.9782 - val_loss: 0.0661 - val_acc: 0.9808 Epoch 19/20 60000/60000 [==============] - 6s 96us/step - loss: 0.0753 - ac c: 0.9775 - val_loss: 0.0642 - val_acc: 0.9819 Epoch 20/20 60000/60000 [=================] - 6s 96us/step - loss: 0.0719 - ac c: 0.9784 - val loss: 0.0645 - val acc: 0.9819
```

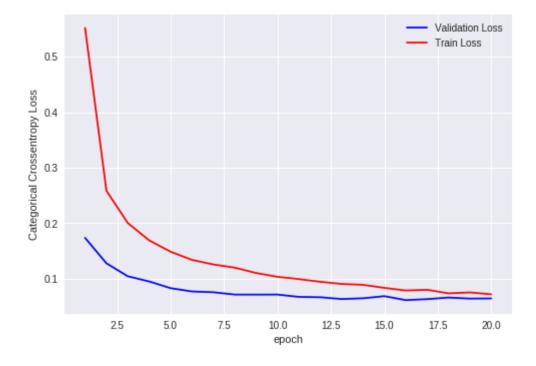
```
In [23]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

# list of epoch numbers
    x = list(range(1,nb_epoch+1))

vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

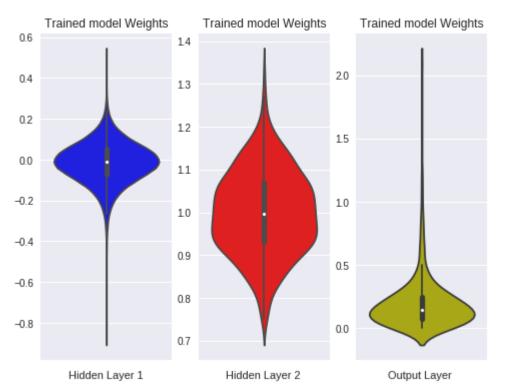
Test score: 0.06447895890461514



1/12/2019

```
In [24]: w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out w = w after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2 w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



[2] MLP with 3 hidden layers

[2.1] Without Batch Normalization and Dropout

```
In [25]: # Multilayer perceptron

model = Sequential()
model.add(Dense(392, activation='relu', input_shape=(input_dim,), kernel_initiali
model.add(Dense(196, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(98, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(output_dim, activation='softmax'))

model.summary()
```

Layer (type)	Output Shape	Param #
dense_10 (Dense)	(None, 392)	307720
dense_11 (Dense)	(None, 196)	77028
dense_12 (Dense)	(None, 98)	19306
dense_13 (Dense)	(None, 10)	990

Total params: 405,044 Trainable params: 405,044 Non-trainable params: 0

```
In [26]: model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accura
        history = model.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ver
       Train on 60000 samples, validate on 10000 samples
       Epoch 1/20
       cc: 0.9268 - val_loss: 0.1271 - val_acc: 0.9592
       60000/60000 [================ ] - 6s 95us/step - loss: 0.0884 - ac
       c: 0.9727 - val_loss: 0.0834 - val_acc: 0.9732
       c: 0.9820 - val loss: 0.0759 - val acc: 0.9760
       Epoch 4/20
       60000/60000 [================ ] - 6s 96us/step - loss: 0.0415 - ac
       c: 0.9869 - val loss: 0.0653 - val acc: 0.9793
       Epoch 5/20
       60000/60000 [================ ] - 6s 96us/step - loss: 0.0305 - ac
       c: 0.9900 - val_loss: 0.0713 - val_acc: 0.9800
       Epoch 6/20
       60000/60000 [============= ] - 6s 97us/step - loss: 0.0247 - ac
       c: 0.9919 - val_loss: 0.0776 - val_acc: 0.9788
       Epoch 7/20
       60000/60000 [================ ] - 6s 96us/step - loss: 0.0207 - ac
       c: 0.9929 - val loss: 0.0804 - val acc: 0.9792
       60000/60000 [============= ] - 6s 97us/step - loss: 0.0184 - ac
       c: 0.9938 - val loss: 0.0773 - val acc: 0.9804
       Epoch 9/20
       60000/60000 [============ ] - 6s 95us/step - loss: 0.0194 - ac
       c: 0.9934 - val loss: 0.0800 - val acc: 0.9778
       Epoch 10/20
       60000/60000 [============= ] - 6s 95us/step - loss: 0.0143 - ac
       c: 0.9951 - val loss: 0.0821 - val acc: 0.9789
        Epoch 11/20
       60000/60000 [=============== ] - 6s 96us/step - loss: 0.0133 - ac
       c: 0.9956 - val loss: 0.0781 - val acc: 0.9820
       Epoch 12/20
       60000/60000 [============= ] - 6s 95us/step - loss: 0.0141 - ac
       c: 0.9951 - val loss: 0.0954 - val acc: 0.9775
       Epoch 13/20
       60000/60000 [================ ] - 6s 97us/step - loss: 0.0108 - ac
       c: 0.9967 - val loss: 0.0913 - val acc: 0.9775
       Epoch 14/20
       60000/60000 [============== ] - 6s 96us/step - loss: 0.0141 - ac
       c: 0.9954 - val loss: 0.0915 - val acc: 0.9779
       Epoch 15/20
       c: 0.9968 - val loss: 0.0893 - val acc: 0.9795
       Epoch 16/20
       60000/60000 [============= ] - 6s 95us/step - loss: 0.0101 - ac
       c: 0.9970 - val loss: 0.0920 - val acc: 0.9800
       Epoch 17/20
       60000/60000 [=============== ] - 6s 96us/step - loss: 0.0116 - ac
       c: 0.9965 - val loss: 0.0950 - val acc: 0.9808
       Epoch 18/20
```

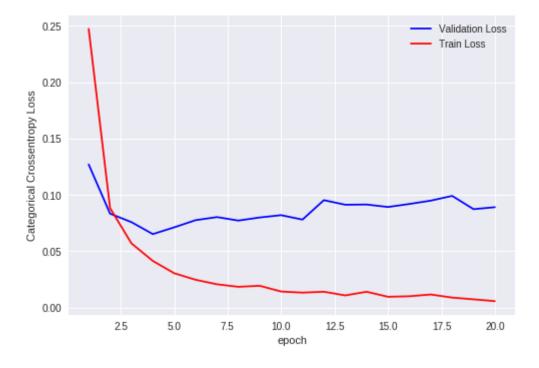
```
In [27]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

# list of epoch numbers
    x = list(range(1,nb_epoch+1))

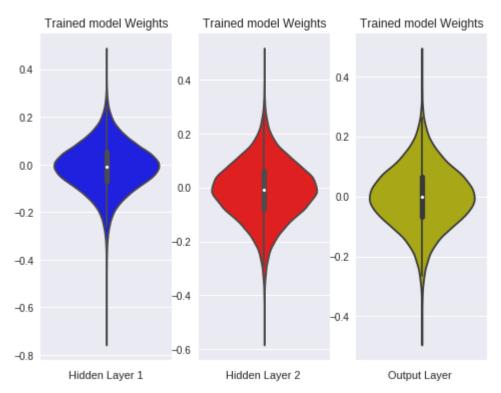
vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

Test score: 0.08915272126807804



```
In [28]: w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out w = w after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2 w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



[2.2] With Batch Normalization and Dropout

```
In [29]: from keras.layers.normalization import BatchNormalization
    from keras.layers import Dropout

model = Sequential()
    model.add(Dense(364, activation='relu', input_shape=(input_dim,), kernel_initiali
    model.add(BatchNormalization())
    model.add(Dropout(0.5))
    model.add(Dense(52, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
    model.add(Dropout(0.5))
    model.add(Dense(64, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
    model.add(BatchNormalization())
    model.add(Dropout(0.5))
    model.add(Dense(output_dim, activation='softmax'))

model.summary()
```

Layer (type)	Output	Shape	Param #
dense_14 (Dense)	(None,	364)	285740
batch_normalization_3 (Batch	(None,	364)	1456
dropout_3 (Dropout)	(None,	364)	0
dense_15 (Dense)	(None,	52)	18980
batch_normalization_4 (Batch	(None,	52)	208
dropout_4 (Dropout)	(None,	52)	0
dense_16 (Dense)	(None,	64)	3392
batch_normalization_5 (Batch	(None,	64)	256
dropout_5 (Dropout)	(None,	64)	0
dense_17 (Dense)	(None,	10)	650
Total params: 310,682	=====:		======

Total params: 310,682 Trainable params: 309,722 Non-trainable params: 960

http://localhost:8888/notebooks/Desktop/MLP_on_MNIST.ipynb

```
In [31]: model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accura
        history = model.fit(X train, Y train, batch size=batch size, epochs=nb epoch, ver
        Train on 60000 samples, validate on 10000 samples
        Epoch 1/20
        60000/60000 [================= ] - 8s 127us/step - loss: 0.8095 - a
        cc: 0.7476 - val loss: 0.2088 - val acc: 0.9344
        Epoch 2/20
        60000/60000 [================ ] - 6s 107us/step - loss: 0.3403 - a
        cc: 0.9033 - val_loss: 0.1457 - val_acc: 0.9562
        60000/60000 [=============== ] - 6s 106us/step - loss: 0.2610 - a
        cc: 0.9285 - val loss: 0.1263 - val acc: 0.9634
        Epoch 4/20
        cc: 0.9390 - val loss: 0.1025 - val acc: 0.9711
        Epoch 5/20
        60000/60000 [================ ] - 6s 104us/step - loss: 0.1953 - a
        cc: 0.9472 - val_loss: 0.0967 - val_acc: 0.9721
        Epoch 6/20
        60000/60000 [============= ] - 6s 105us/step - loss: 0.1848 - a
        cc: 0.9492 - val_loss: 0.0968 - val_acc: 0.9724
        Epoch 7/20
        60000/60000 [============== ] - 6s 104us/step - loss: 0.1687 - a
        cc: 0.9546 - val loss: 0.0914 - val acc: 0.9737
        Epoch 8/20
        60000/60000 [============== ] - 6s 106us/step - loss: 0.1545 - a
        cc: 0.9578 - val loss: 0.0838 - val acc: 0.9762
        Epoch 9/20
        60000/60000 [================ ] - 6s 104us/step - loss: 0.1435 - a
        cc: 0.9606 - val loss: 0.0879 - val acc: 0.9756
        Epoch 10/20
        60000/60000 [============= ] - 6s 106us/step - loss: 0.1431 - a
        cc: 0.9607 - val loss: 0.0794 - val acc: 0.9787
        Epoch 11/20
        60000/60000 [================ ] - 7s 109us/step - loss: 0.1350 - a
        cc: 0.9622 - val loss: 0.0813 - val acc: 0.9769
        Epoch 12/20
        60000/60000 [============= ] - 6s 107us/step - loss: 0.1268 - a
        cc: 0.9652 - val loss: 0.0741 - val acc: 0.9799
        Epoch 13/20
        60000/60000 [=============== ] - 6s 106us/step - loss: 0.1232 - a
        cc: 0.9660 - val loss: 0.0773 - val acc: 0.9792
        Epoch 14/20
        60000/60000 [============= ] - 6s 105us/step - loss: 0.1180 - a
        cc: 0.9678 - val loss: 0.0735 - val acc: 0.9793
        Epoch 15/20
        60000/60000 [============= ] - 6s 107us/step - loss: 0.1122 - a
        cc: 0.9694 - val loss: 0.0723 - val acc: 0.9808
        Epoch 16/20
        60000/60000 [============= ] - 6s 108us/step - loss: 0.1082 - a
        cc: 0.9704 - val loss: 0.0732 - val acc: 0.9804
        Epoch 17/20
        60000/60000 [================ ] - 6s 107us/step - loss: 0.1081 - a
        cc: 0.9701 - val loss: 0.0731 - val acc: 0.9805
        Epoch 18/20
```

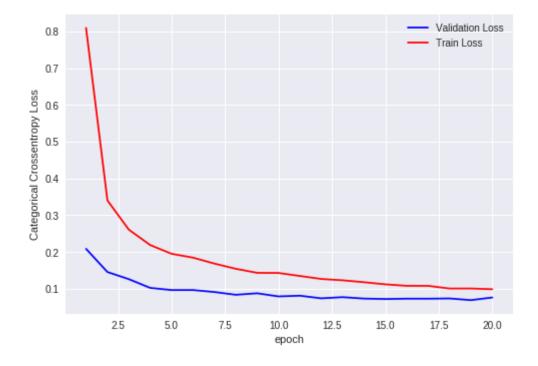
```
In [32]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

# list of epoch numbers
    x = list(range(1,nb_epoch+1))

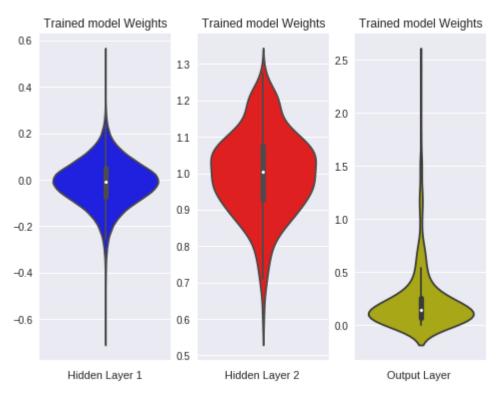
vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

Test score: 0.07640664648028324



```
In [33]: w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out w = w after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2 w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



[2] MLP with 5 hidden layers

[3.1] Without Batch Normalization and Dropout

```
In [34]: # Multilayer perceptron

model = Sequential()
model.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initiali
model.add(Dense(256, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(128, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(64, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(32, activation='relu', kernel_initializer=RandomNormal(mean=0.0,
model.add(Dense(output_dim, activation='softmax'))
```

Layer (type)	Output Shape	Param #
dense_18 (Dense)	(None, 512)	401920
dense_19 (Dense)	(None, 256)	131328
dense_20 (Dense)	(None, 128)	32896
dense_21 (Dense)	(None, 64)	8256
dense_22 (Dense)	(None, 32)	2080
dense_23 (Dense)	(None, 10)	330

Total params: 576,810 Trainable params: 576,810 Non-trainable params: 0

```
In [35]: model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accura
        history = model.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ver
        Train on 60000 samples, validate on 10000 samples
        Epoch 1/20
        60000/60000 [================ ] - 9s 142us/step - loss: 0.3075 - a
        cc: 0.9062 - val loss: 0.1160 - val acc: 0.9641
        Epoch 2/20
        cc: 0.9698 - val_loss: 0.1045 - val_acc: 0.9681
        60000/60000 [=============== ] - 8s 129us/step - loss: 0.0650 - a
        cc: 0.9800 - val loss: 0.0769 - val acc: 0.9760
        Epoch 4/20
        60000/60000 [================ ] - 8s 137us/step - loss: 0.0453 - a
        cc: 0.9860 - val loss: 0.0769 - val acc: 0.9772
        Epoch 5/20
        60000/60000 [================ ] - 8s 139us/step - loss: 0.0388 - a
        cc: 0.9875 - val_loss: 0.0905 - val_acc: 0.9762
        Epoch 6/20
        60000/60000 [=============== ] - 8s 132us/step - loss: 0.0311 - a
        cc: 0.9901 - val_loss: 0.0786 - val_acc: 0.9794
        Epoch 7/20
        60000/60000 [=============== ] - 8s 132us/step - loss: 0.0260 - a
        cc: 0.9920 - val loss: 0.0770 - val acc: 0.9793
        Epoch 8/20
        60000/60000 [============= ] - 8s 131us/step - loss: 0.0215 - a
        cc: 0.9934 - val loss: 0.0936 - val acc: 0.9768
        Epoch 9/20
        60000/60000 [=============== ] - 8s 133us/step - loss: 0.0196 - a
        cc: 0.9937 - val loss: 0.0951 - val acc: 0.9768
        Epoch 10/20
        60000/60000 [============= ] - 8s 135us/step - loss: 0.0166 - a
        cc: 0.9945 - val loss: 0.0862 - val acc: 0.9799
        Epoch 11/20
        60000/60000 [=============== ] - 8s 130us/step - loss: 0.0169 - a
        cc: 0.9948 - val loss: 0.0959 - val acc: 0.9774
        Epoch 12/20
        cc: 0.9948 - val loss: 0.0949 - val acc: 0.9774
        Epoch 13/20
        60000/60000 [=============== ] - 8s 132us/step - loss: 0.0137 - a
        cc: 0.9956 - val loss: 0.0884 - val acc: 0.9803
        Epoch 14/20
        60000/60000 [============= ] - 8s 129us/step - loss: 0.0127 - a
        cc: 0.9960 - val loss: 0.0816 - val acc: 0.9808
        Epoch 15/20
        60000/60000 [=============== ] - 8s 130us/step - loss: 0.0139 - a
        cc: 0.9958 - val loss: 0.1052 - val acc: 0.9788
        Epoch 16/20
        60000/60000 [============= ] - 8s 130us/step - loss: 0.0130 - a
        cc: 0.9963 - val loss: 0.0854 - val acc: 0.9832
        Epoch 17/20
        60000/60000 [=============== ] - 8s 132us/step - loss: 0.0104 - a
        cc: 0.9971 - val loss: 0.0868 - val acc: 0.9818
        Epoch 18/20
```

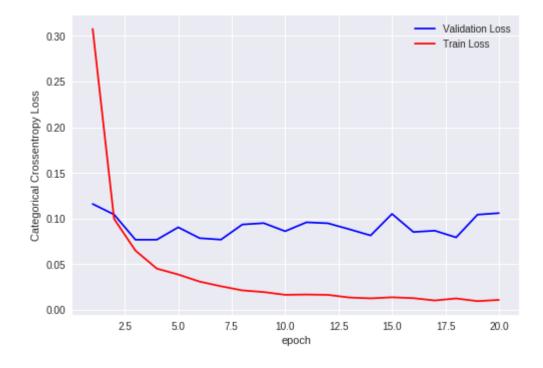
```
In [36]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch') ; ax.set_ylabel('Categorical Crossentropy Loss')

# list of epoch numbers
    x = list(range(1,nb_epoch+1))

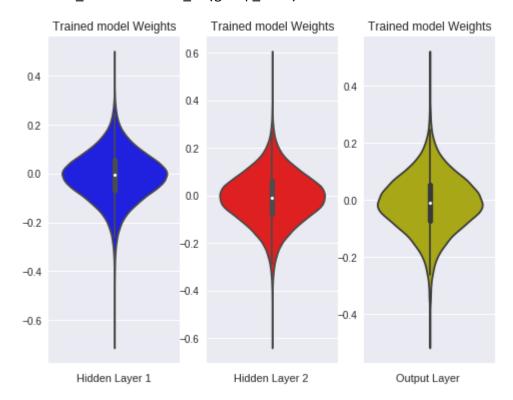
vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

Test score: 0.10602583270173854



```
In [37]: w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out_w = w_after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1 w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2_w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



[3.2] With Batch Normalization and Dropout

```
In [38]:
         from keras.layers.normalization import BatchNormalization
         from keras.layers import Dropout
         model = Sequential()
         model.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initiali
         model.add(BatchNormalization())
         model.add(Dropout(0.5))
         model.add(Dense(256, activation='relu', kernel initializer=RandomNormal(mean=0.0,
         model.add(BatchNormalization())
         model.add(Dropout(0.5))
         model.add(Dense(128, activation='relu', kernel initializer=RandomNormal(mean=0.0,
         model.add(BatchNormalization())
         model.add(Dropout(0.5))
         model.add(Dense(64, activation='relu', kernel initializer=RandomNormal(mean=0.0,
         model.add(BatchNormalization())
         model.add(Dropout(0.5))
         model.add(Dense(32, activation='relu', kernel initializer=RandomNormal(mean=0.0,
         model.add(BatchNormalization())
         model.add(Dropout(0.5))
         model.add(Dense(output dim, activation='softmax'))
         model.summary()
```

Layer (type)	Output	Shape	Param #
dense_24 (Dense)	(None,		401920
batch_normalization_6 (Batch	(None,	512)	2048
dropout_6 (Dropout)	(None,	512)	0
dense_25 (Dense)	(None,	256)	131328
batch_normalization_7 (Batch	(None,	256)	1024
dropout_7 (Dropout)	(None,	256)	0
dense_26 (Dense)	(None,	128)	32896
batch_normalization_8 (Batch	(None,	128)	512
dropout_8 (Dropout)	(None,	128)	0
dense_27 (Dense)	(None,	64)	8256
batch_normalization_9 (Batch	(None,	64)	256
dropout_9 (Dropout)	(None,	64)	0
dense_28 (Dense)	(None,	32)	2080
batch_normalization_10 (Batc	(None,	32)	128
dropout_10 (Dropout)	(None,	32)	0

dense_29 (Dense) (None, 10) 330

Total params: 580,778
Trainable params: 578,794
Non-trainable params: 1,984

```
In [39]: | model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accura
      history = model.fit(X train, Y train, batch size=batch size, epochs=nb epoch, ver
      Train on 60000 samples, validate on 10000 samples
      Epoch 1/20
      acc: 0.5948 - val loss: 0.2912 - val acc: 0.9224
      Epoch 2/20
      acc: 0.8618 - val_loss: 0.1788 - val_acc: 0.9523
      60000/60000 [========================= ] - 11s 190us/step - loss: 0.3592 -
      acc: 0.9095 - val loss: 0.1466 - val acc: 0.9610
      Epoch 4/20
      60000/60000 [============= ] - 11s 188us/step - loss: 0.2985 -
      acc: 0.9285 - val loss: 0.1363 - val acc: 0.9660
      Epoch 5/20
      acc: 0.9387 - val loss: 0.1195 - val acc: 0.9697
      Epoch 6/20
      60000/60000 [============= ] - 11s 190us/step - loss: 0.2315 -
      acc: 0.9456 - val_loss: 0.1222 - val_acc: 0.9695
      Epoch 7/20
      acc: 0.9487 - val loss: 0.1162 - val acc: 0.9709
      Epoch 8/20
      60000/60000 [============= ] - 12s 192us/step - loss: 0.2027 -
      acc: 0.9530 - val loss: 0.0990 - val acc: 0.9757
      Epoch 9/20
      acc: 0.9557 - val loss: 0.0959 - val acc: 0.9758
      Epoch 10/20
      60000/60000 [============= ] - 11s 190us/step - loss: 0.1793 -
      acc: 0.9581 - val loss: 0.0988 - val acc: 0.9770
      Epoch 11/20
      acc: 0.9602 - val loss: 0.0918 - val acc: 0.9790
      Epoch 12/20
      60000/60000 [============= ] - 11s 189us/step - loss: 0.1606 -
      acc: 0.9622 - val loss: 0.0887 - val acc: 0.9801
      Epoch 13/20
      acc: 0.9647 - val loss: 0.0910 - val acc: 0.9787
      Epoch 14/20
      60000/60000 [============= ] - 11s 190us/step - loss: 0.1521 -
      acc: 0.9651 - val loss: 0.0865 - val acc: 0.9796
      Epoch 15/20
      60000/60000 [============== ] - 11s 189us/step - loss: 0.1467 -
      acc: 0.9675 - val loss: 0.0810 - val acc: 0.9808
      Epoch 16/20
      60000/60000 [============== ] - 11s 189us/step - loss: 0.1424 -
      acc: 0.9677 - val loss: 0.0794 - val acc: 0.9807
      Epoch 17/20
      acc: 0.9695 - val loss: 0.0847 - val acc: 0.9816
      Epoch 18/20
```

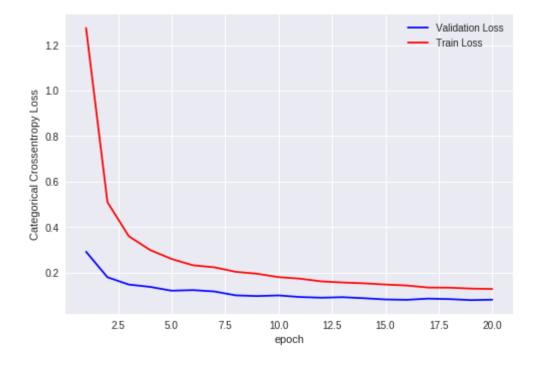
```
In [40]: score = model.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
    print('Test accuracy:', score[1])

fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')

# list of epoch numbers
    x = list(range(1,nb_epoch+1))

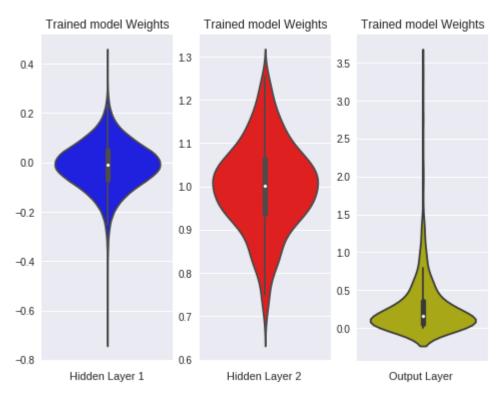
vy = history.history['val_loss']
    ty = history.history['loss']
    plt_dynamic(x, vy, ty, ax)
```

Test score: 0.08005840601597447



```
In [41]: w after = model.get weights()
         h1 w = w after[0].flatten().reshape(-1,1)
         h2 w = w after[2].flatten().reshape(-1,1)
         out w = w after[4].flatten().reshape(-1,1)
         fig = plt.figure(figsize=(8, 6))
         plt.title("Weight matrices after model trained")
         plt.subplot(1, 3, 1)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h1_w,color='b')
         plt.xlabel('Hidden Layer 1')
         plt.subplot(1, 3, 2)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=h2 w, color='r')
         plt.xlabel('Hidden Layer 2 ')
         plt.subplot(1, 3, 3)
         plt.title("Trained model Weights")
         ax = sns.violinplot(y=out_w,color='y')
         plt.xlabel('Output Layer ')
         plt.show()
```

/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816: FutureWarnin
g: remove_na is deprecated and is a private function. Do not use.
 violin_data = remove_na(group_data)



MLP WITH DIFFERNET ARCHITECTURES				
+ TEST_ACCURACY	MLP_MODEL	•	IN_ACCURA	·
+				
0.875 l	MLP(2-hidden layers)	ļ	0.87	I
	ayers) With Dropout and Batch Normalization	1	0.978	1
0.982	MLP(3-hidden layers)	I	0.998	1
MLP(3-hidden 0.979	Layers) With Dropout and Batch Normalization		0.972	
Ι ΄	MLP(5-hidden layers)		0.996	
0.978				
MLP(5-hidden 1 0.981	Layers) With Dropout and Batch Normalization	•	0.971	I

Conclusion

- 1. The Best train and test (0.998 | 0.982) accuracy is obtained by MLP(3-hidden layers) without Dropout and Batch Normalization.
- 2. With Dropout and Batch Normalization the NN is less overfitted than the NN without Dropout and Batch Normalization.