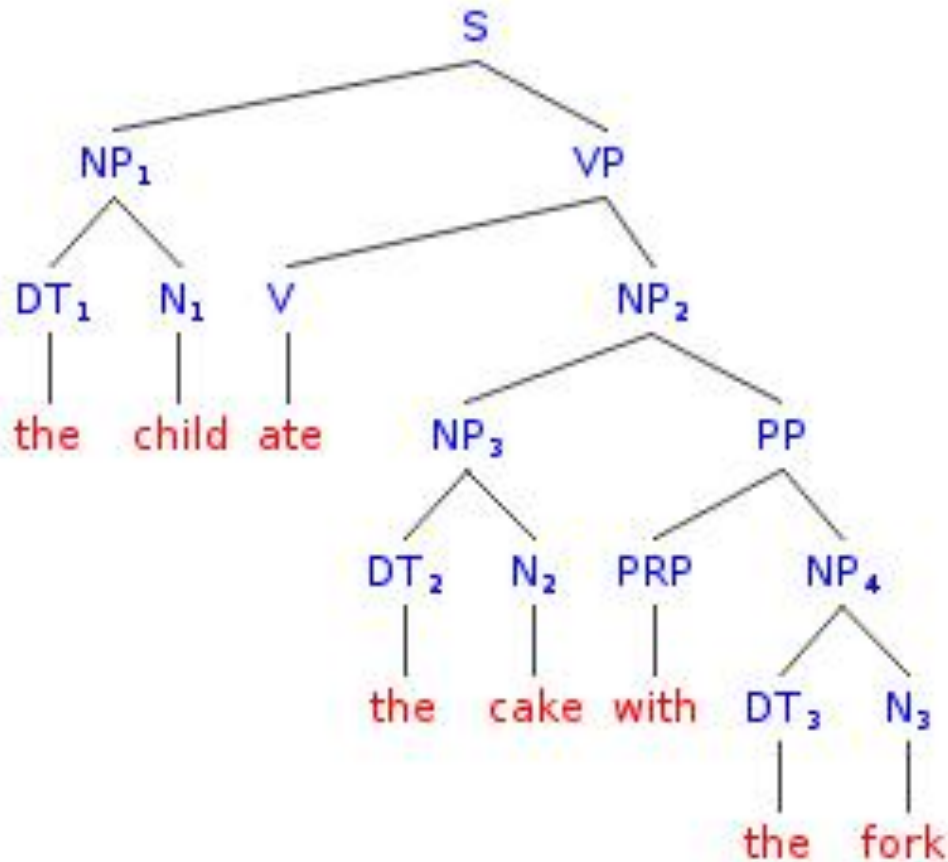


# NLP

# Introduction to NLP

*Classic parsing methods*



S → NP VP

NP → DT N | NP PP

PP → PRP NP

VP → V NP | VP PP

DT → 'a' | 'the'

N → 'child' | 'cake' | 'fork'

PRP → 'with' | 'to'

V → 'saw' | 'ate'

## Parsing as Search

- There are two types of constraints on the parses
  - From the input sentence
  - From the grammar
- Therefore, two general approaches to parsing
  - Top-down
  - Bottom-up

# Top Down Parsing

S

S → NP VP

NP → DT N | NP PP

PP → PRP NP

VP → V NP | VP PP

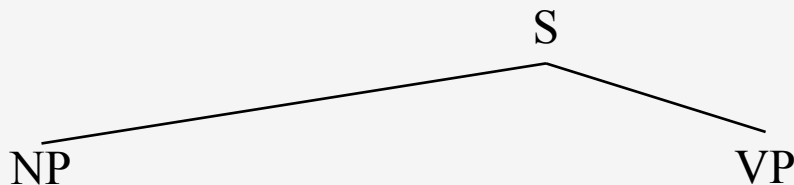
DT → 'a' | 'the'

N → 'child' | 'cake' | 'fork'

PRP → 'with' | 'to'

V → 'saw' | 'ate'

# Top Down Parsing



S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

DT -> 'a' | 'the'

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# Top Down Parsing



S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

DT -> 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

PRP -> 'with' | 'to'

V -> 'saw' | 'ate'



# Top Down Parsing



S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

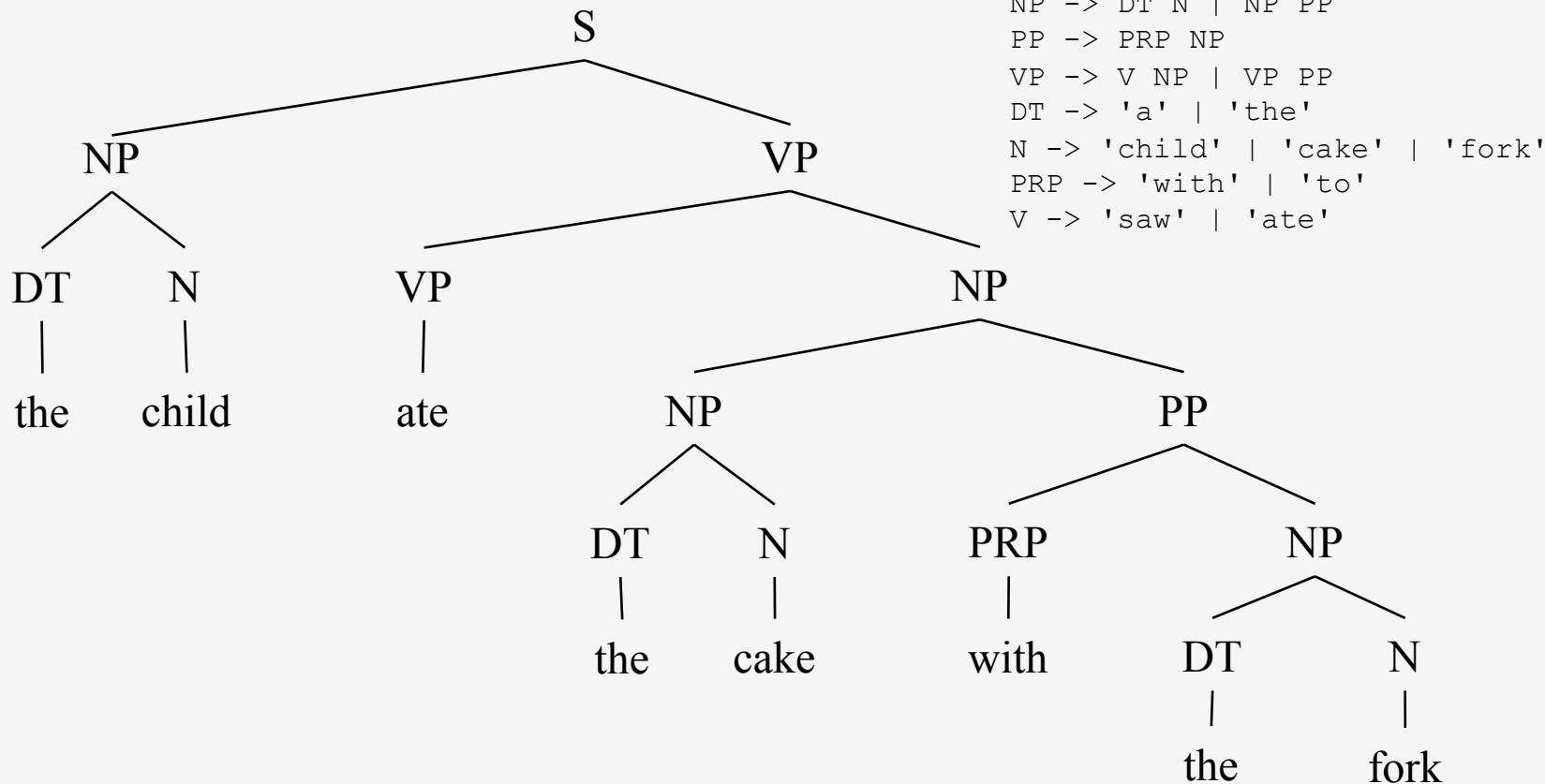
DT -> 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

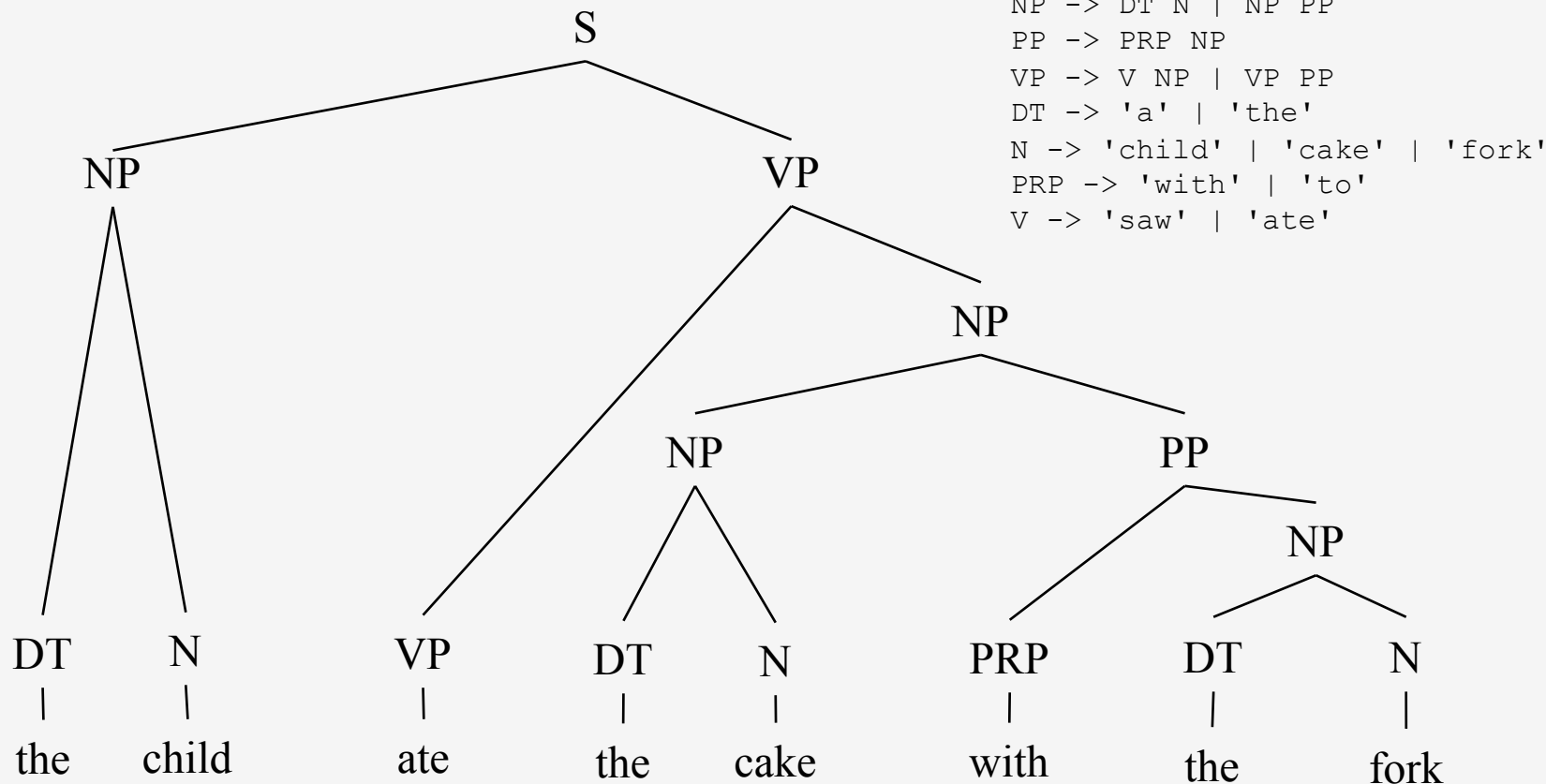
PRP -> 'with' | 'to'

V -> 'saw' | 'ate'

# Top Down Parsing



# Bottom Up Parsing



# Bottom Up Vs. Top Down Methods

- Bottom up
  - explores options that won't lead to a full parse.
- Top down
  - explores options that don't match the full sentence.
- Dynamic programming
  - caches of intermediate results (memoization)
- Cocke–Kasami–Younger (CKY) parser
  - based on dynamic programming

# Introduction to NLP

*Shift-reduce parsing*

# Shift-reduce Parsing

- A bottom-up parser
  - Tries to match the RHS of a production until it can build an S
- *Shift* operation
  - Each word in the input sentence is pushed onto a stack
- *Reduce* operation
  - If the top n words on the top of the stack match the RHS of a production, then they are popped and replaced by the LHS of the production
- Stopping condition
  - The process stops when the input sentence has been processed and S has been popped from the stack.

# Shift-reduce Parsing Example

[ \* the child ate the cake]

# Shift-reduce Parsing Example

```
[ * the child ate the cake]  
S [ 'the' * child ate the cake]
```



# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
```

# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
```

# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
R [ NP * ate the cake]
S [ NP 'ate' * the cake]
```

# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
R [ NP * ate the cake]
S [ NP 'ate' * the cake]
R [ NP V * the cake]
S [ NP V 'the' * cake]
R [ NP V DT * cake]
S [ NP V DT 'cake' * ]
```

# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
R [ NP * ate the cake]
S [ NP 'ate' * the cake]
R [ NP V * the cake]
S [ NP V 'the' * cake]
R [ NP V DT * cake]
S [ NP V DT 'cake' * ]
R [ NP V DT N * ]
R [ NP V NP * ]
R [ NP VP * ]
R [ S * ]
```

# Shift-reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
R [ NP * ate the cake]
S [ NP 'ate' * the cake]
R [ NP V * the cake]
S [ NP V 'the' * cake]
R [ NP V DT * cake]
S [ NP V DT 'cake' * ]
R [ NP V DT N * ]
R [ NP V NP * ]
R [ NP VP * ]
R [ S * ]
```

**(S (NP (DT the) (N child)) (VP (V ate) (NP (DT the) (N cake))))**

# NLP

# Introduction to NLP

*Cocke-Kasami-Younger (CKY) Parsing*



# Dynamic Programming

- **Motivation**
  - A lot of the work is repeated
  - Caching intermediate results improves the complexity
- **Dynamic programming**
  - Building a parse for a substring  $[i,j]$  based on all parses  $[i,k]$  and  $[k, j]$  that are included in it.
- **Complexity**
  - $O(n^3)$  for recognizing an input string of length  $n$

## Dynamic Programming

- CKY (Cocke–Kasami–Younger)
  - bottom-up
  - requires a normalized (binarized) grammar
- Earley parser
  - top-down
  - more complicated

## Example

["the", "child", "ate", "the", "cake", "with", "the", "fork"]

S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

DT -> 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

PRP -> 'with' | 'to'

V -> 'saw' | 'ate'



the

--	--	--	--	--	--	--	--

child

--	--	--	--	--	--	--	--

ate

--	--	--	--	--	--	--	--

the

--	--	--	--	--	--	--	--

cake

--	--	--	--	--	--	--	--

with

--	--	--	--	--	--	--	--

the

--	--	--	--	--	--	--	--

fork

--	--	--	--	--	--	--	--





the	DT						
child	N						
ate							
the							
cake							
with							
the							
fork							





the	DT — NP						
child	N						
ate							
the							
cake							
with							
the							
fork							





	the	DT	NP						
	child	N							
	ate	V							
	the	DT							
	cake								
	with								
	the								
	fork								



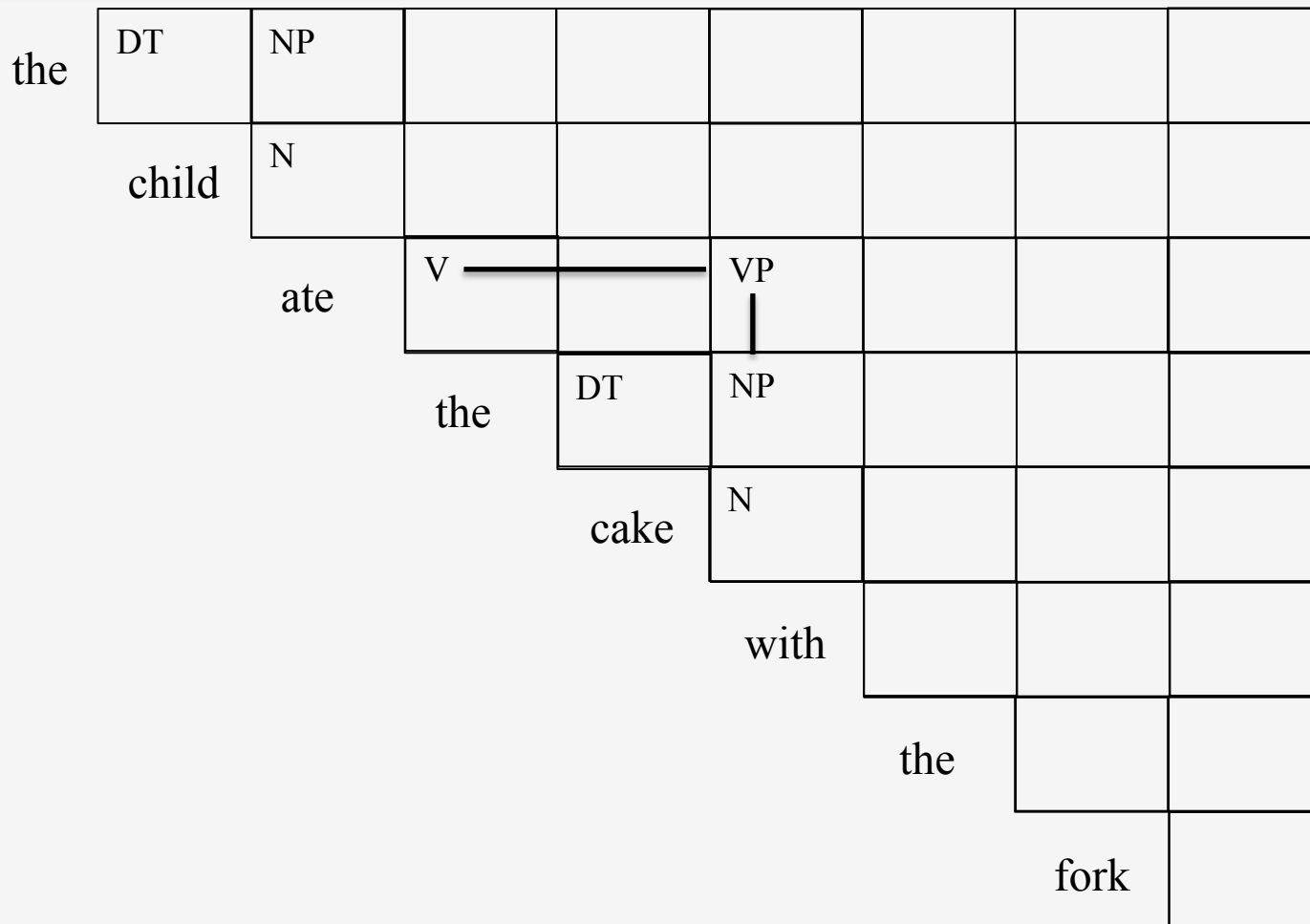




the	DT	NP					
child		N					
	ate		V				
		the		DT	NP		
			cake		N		
				with			
					the		
						fork	



the	DT	NP					
child	N						
ate	V			VP			
the	DT	NP					
cake	N						
with							
the							
fork							



	DT	NP		S			
the		N					
	child		V	VP			
		ate					
			the	DT	NP		
				cake	N		
					with		
						the	
							fork





the	DT	NP			S			
child		N						
ate			V		VP			
the				DT	NP			
cake					N			
with								
the								
fork								

	DT	NP		S			
the		N					
	child		V	VP			
		ate					
			the	DT	NP		
				cake	N		
					with	PRP	
						the	
							fork

the	DT	NP		S			
	child	N					
		ate	V	VP			
			the	DT	NP		NP
				cake	N		
					with	PRP	PP
						the	DT NP
							fork N

the	DT	NP		S			
child	N						
ate	V		VP			VP	
the	DT	NP				NP	
cake	N						
with	PRP					PP	
the	DT	NP					
fork	N						

the	DT	NP			S			
child		N						
	ate	V	VP					VP
	the		DT	NP				NP
		cake		N				
			with		PRP			PP
				the		DT		NP
					fork			N

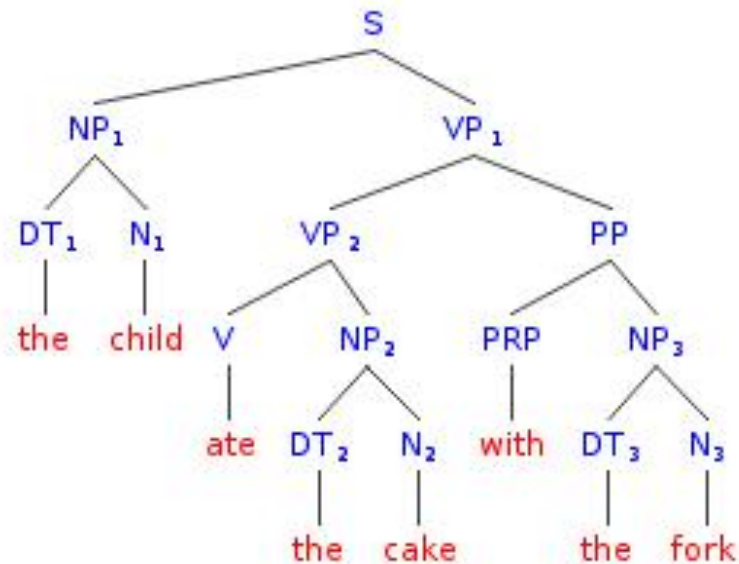
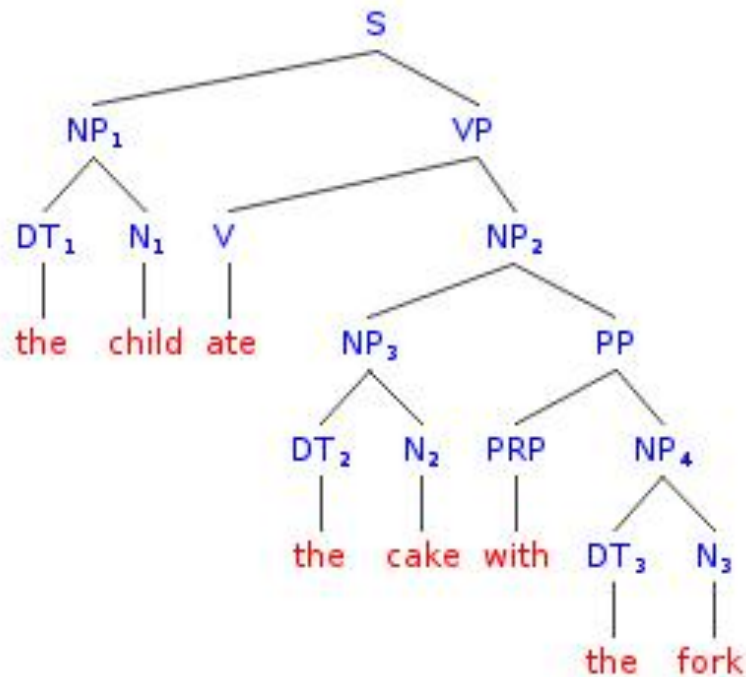


the	DT	NP			S		S
child		N					
ate			V		VP		VP
				DT	NP		NP
					N		
						PRP	PP
							DT NP
							N
							fork



the	DT	NP			S			S
child		N						
	ate		V		VP			VP
		the		DT	NP			NP
			cake		N			
				with		PRP		PP
					the		DT	NP
						fork		N

[0] DT [1] N [2] ==> [0] NP [2]  
[3] DT [4] N [5] ==> [3] NP [5]  
[6] DT [7] N [8] ==> [6] NP [8]  
[2] V [3] NP [5] ==> [2] VP [5]  
[5] PRP [6] NP [8] ==> [5] PP [8]  
[0] NP [2] VP [5] ==> [0] S [5]  
[3] NP [5] PP [8] ==> [3] NP [8]  
**[2] V [3] NP [8] ==> [2] VP [8]**  
**[2] VP [5] PP [8] ==> [2] VP [8]**  
[0] NP [2] VP [8] ==> [0] S [8]



What is the *meaning* of each of these sentences?



```
(S  
  (NP (DT the) (N child))  
  (VP  
    (VP (V ate) (NP (DT the) (N cake)))  
    (PP (PRP with) (NP (DT the) (N fork))))))
```

```
(S
  (NP (DT the) (N child))
  (VP
    (VP (V ate) (NP (DT the) (N cake)))
    (PP (PRP with) (NP (DT the) (N fork))))))
```

```
(S
  (NP (DT the) (N child))
  (VP
    (V ate)
    (NP
      (NP (DT the) (N cake))
      (PP (PRP with) (NP (DT the) (N fork)))))))
```

## Online Demo

- <http://www.diotavelli.net/people/void/demos/cky.html>

## Complexity of CKY

- There are  $O(n^2)$  cells in the table
- Single parse
  - Each cell requires a linear lookup.
  - Total time complexity is  $O(n^3)$
- All parses
  - Total time complexity is exponential

## A Longer Example

["take", "this", "book"]

S -> NP VP | Aux NP VP | VP

NP -> PRON | Det Nom

Nom -> N | Nom N | Nom PP

PP -> PRP NP

VP -> V | V NP | VP PP

Det -> 'the' | 'a' | 'this'

PRON -> 'he' | 'she'

N -> 'book' | 'boys' | 'girl'

PRP -> 'with' | 'in'

V -> 'takes' | 'take'

# Non-binary Productions

["take", "this", "book"]

S → NP VP | **Aux NP VP** | **VP**

NP → **PRON** | Det Nom

Nom → **N** | Nom N | Nom PP

PP → PRP NP

VP → **V** | V NP | VP PP

Det → 'the' | 'a' | 'this'

PRON → 'he' | 'she'

N → 'book' | 'boys' | 'girl'

PRP → 'with' | 'in'

V → 'takes' | 'take'

## Chomsky Normal Form

- All rules have to be in binary form:
  - $X \rightarrow YZ$  or  $X \rightarrow w$
- This introduces new non-terminals for
  - hybrid rules
  - n-ary rules
  - unary rules

# ATIS Grammar

## Original version

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow Verb$

$VP \rightarrow Verb NP$

$VP \rightarrow VP PP$

$PP \rightarrow Prep NP$



# ATIS Grammar In CNF

## Original version

$S \rightarrow NP VP$

$S \rightarrow \text{Aux } NP VP$

$S \rightarrow VP$

$NP \rightarrow \text{Pronoun}$

$NP \rightarrow \text{Proper-Noun}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{Noun}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{Verb}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

## CNF version

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow \text{Aux } NP$

$S \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$S \rightarrow \text{Verb } NP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid \text{he} \mid \text{she} \mid \text{me}$

$NP \rightarrow \text{Houston} \mid \text{NWA}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$VP \rightarrow \text{Verb } NP$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep } NP$

# ATIS Grammar In CNF

## Original version

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow \text{Pronoun}$

$NP \rightarrow \text{Proper-Noun}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{Noun}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{Verb}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

## CNF version

$S \rightarrow NP VP$

$S \rightarrow X_1 VP$

$X_1 \rightarrow Aux NP$

$S \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$S \rightarrow \text{Verb NP}$

$S \rightarrow VP PP$

$NP \rightarrow \text{I} \mid \text{he} \mid \text{she} \mid \text{me}$

$NP \rightarrow \text{Houston} \mid \text{NWA}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

# Chomsky Normal Form

- All rules have to be in binary form:
  - $X \rightarrow YZ$  or  $X \rightarrow w$
- New non-terminals for hybrid rules, n-ary and unary rules:
  - $INF-VP \rightarrow to VP$  *becomes*
    - $INF-VP \rightarrow TO$
    - $TO \rightarrow to$
  - $S \rightarrow Aux NP VP$  *becomes*
    - $S \rightarrow R1 VP$
    - $R1 \rightarrow Aux NP$
  - $S \rightarrow VP$      $VP \rightarrow Verb$      $VP \rightarrow Verb NP$      $VP \rightarrow Verb PP$  *becomes*
    - $S \rightarrow book$
    - $S \rightarrow buy$
    - $S \rightarrow R2 PP$
    - $S \rightarrow Verb PP$
  - etc.

## Issues with CKY

- Weak equivalence only
  - Same language, different structure
  - If the grammar had to be converted to CNF, then the final parse tree doesn't match the original grammar
  - However, it can be converted back using a specific procedure
- Syntactic ambiguity
  - (Deterministic) CKY has no way to perform syntactic disambiguation

# NLP