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DEPARTMENT OF ELECTRONICS ENGINEERING
ELECTRONIC CIRCUITS
DC CIRCUITS

Numerical 1: Calculate V_o and I_o for the circuit shown in Figure 1.

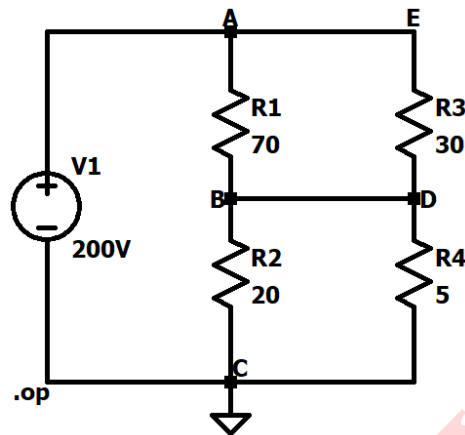


Figure 1: Circuit 1

Solution:

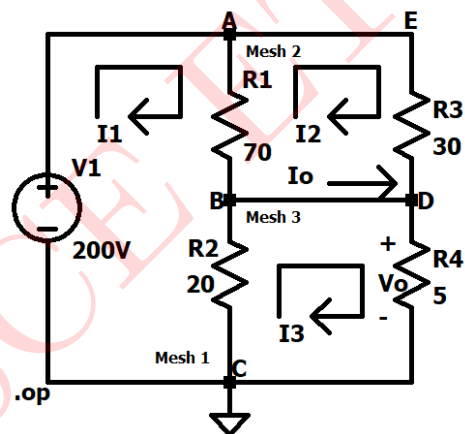


Figure 2: Simplified circuit

Consider I_1 , I_2 and I_3 flowing through mesh 1, 2 and 3 clockwise.

Applying KVL to mesh 1,

$$200 - 70(I_1 - I_2) - 20(I_1 - I_3) = 0$$

$$90I_1 - 70I_2 - 20I_3 = 200$$

—(i)

Applying KVL to mesh 2,

$$-70(I_2 - I_1) - 30I_2 = 0$$

$$70I_1 - 100I_2 = 0$$

—(ii)

Applying KVL to mesh 3,

$$-20(I_3 - I_1) - 5I_3 = 0$$

$$20I_1 - 25I_3 = 0$$

—(iii)

From Eqs. (i), (ii) and (iii) we get,

$$I_1 = 8A$$

$$I_2 = 5.6A$$

$$I_3 = 6.4A$$

$$\text{Hence, } I_o = -I_2 = -5.6A$$

$$\begin{aligned} V_o &= V_{R4} = I_{R4} \times R4 \\ &= 6.4A \times 5\Omega \\ &= 32V \end{aligned}$$

$$V_o = 32V \quad I_o = -5.6 \text{ A}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

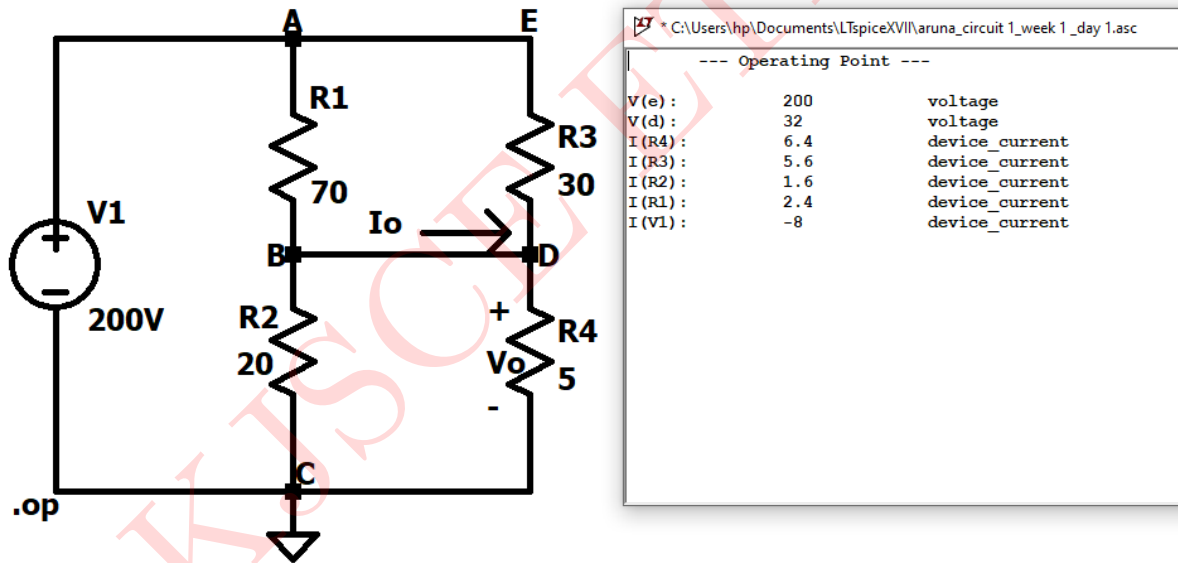


Figure 3: Circuit Schematic and Simulated Results

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| V_o | 32 V | 32 V |
| I_o | -5.6 A | -5.6 A |

Table 1: Numerical 1

Numerical 2: Calculate equivalent resistance R_{ab} at terminals a-b for each of the following circuits in Figure 4 and Figure 5.

(a)

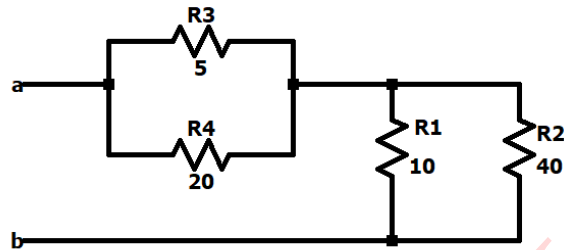


Figure 4: Circuit 2

(b)

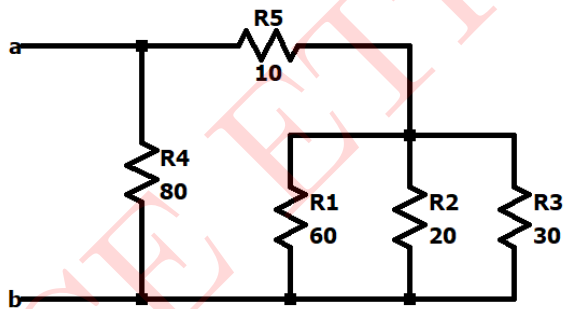


Figure 5: Circuit 3

Solution:

(a)

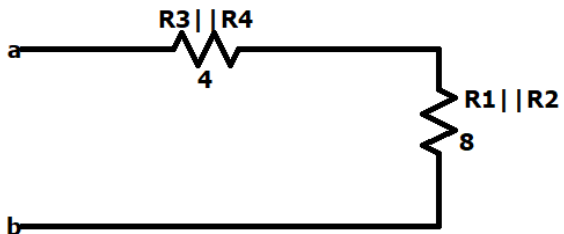


Figure 6: Circuit 2 Simplified Circuit (1)

$$R1 || R2 = 10 \, \Omega || 40 \, \Omega \\ = 8 \, \Omega$$

$$R3 || R4 = 5 \, \Omega || 20 \, \Omega \\ = 4 \, \Omega$$

$$R1 || R2 + R3 || R4 = 10 \, \Omega || 40 \, \Omega + 5 \, \Omega || 20 \, \Omega \\ = 12 \, \Omega$$

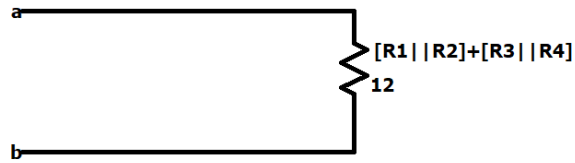


Figure 7: Circuit 2 Simplified Circuit (2)

$$R_{ab} = 12 \, \Omega$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

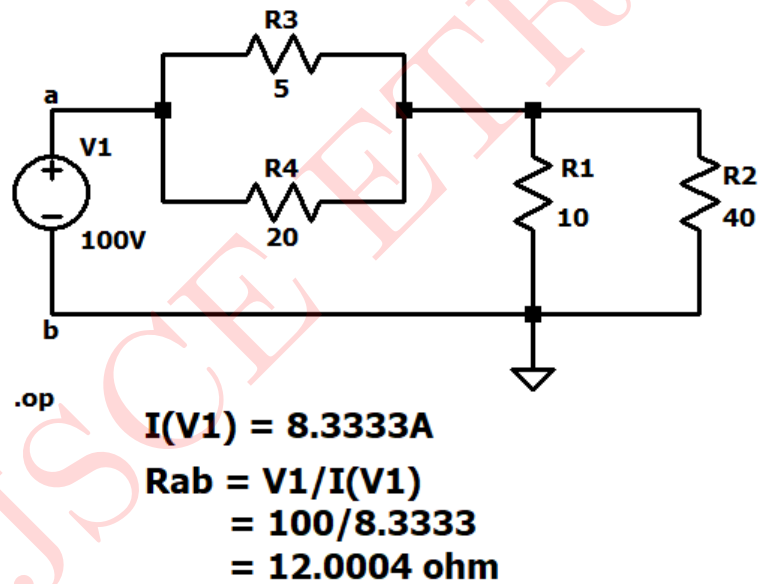


Figure 8: Circuit Schematic

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| R_{ab} | 12 Ω | 12.0004 Ω |

Table 2: Numerical 2 (a)

(b)

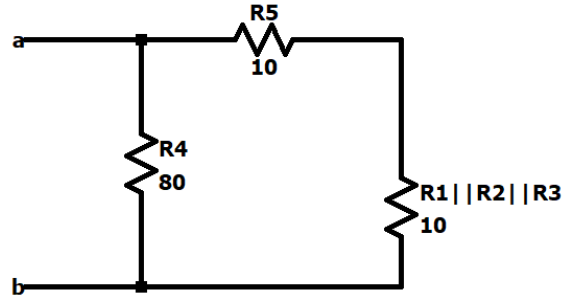


Figure 9: Circuit 3 Simplified Circuit (1)

$$\begin{aligned} R1||R2||R3 &= 60\ \Omega \parallel 20\ \Omega \parallel 30\ \Omega \\ &= 10\ \Omega \end{aligned}$$

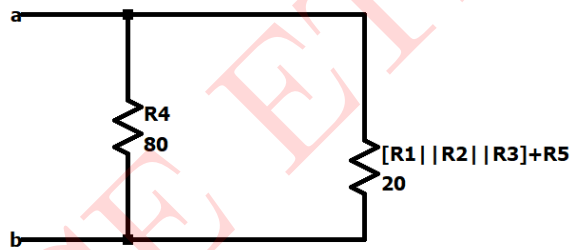


Figure 10: Circuit 3 Simplified Circuit (2)

$$\begin{aligned} R1||R2||R3 + R5 &= 10\ \Omega + 10\ \Omega \\ &= 20\ \Omega \end{aligned}$$

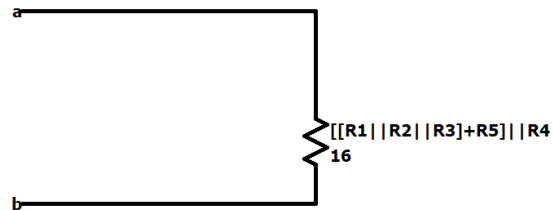


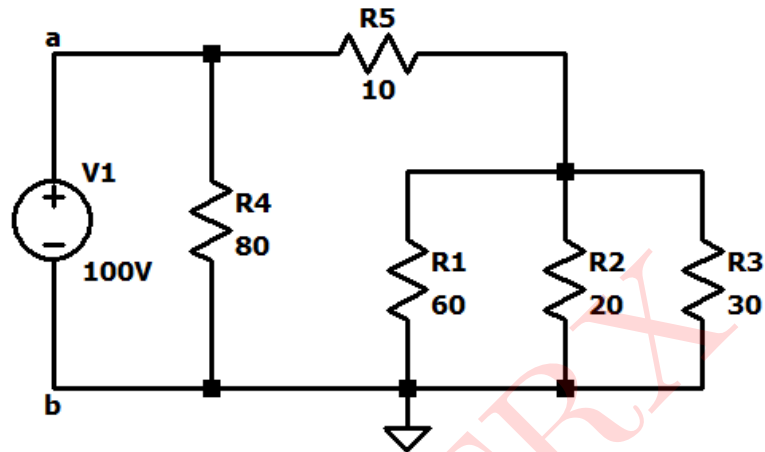
Figure 11: Circuit 3 Simplified Circuit (3)

$$\begin{aligned} R1||R2||R3 + R5 \parallel R4 &= 20\ \Omega \parallel 80\ \Omega \\ &= 16\ \Omega \end{aligned}$$

$$R_{ab} = 16\ \Omega$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:



$$\begin{aligned} I(V1) &= 6.25A \\ R_{ab} &= V1/I(V1) \\ &= 100/6.25 \\ &= 16 \text{ ohm} \end{aligned}$$

Figure 12: Circuit Schematic

Comparison of theoretical and Simulated Results

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| R_{ab} | 16 Ω | 16 Ω |

Table 3: Numerical 2 (b)

Numerical 3: Apply Superposition theorem to compute current across 2Ω resistor in figure 13

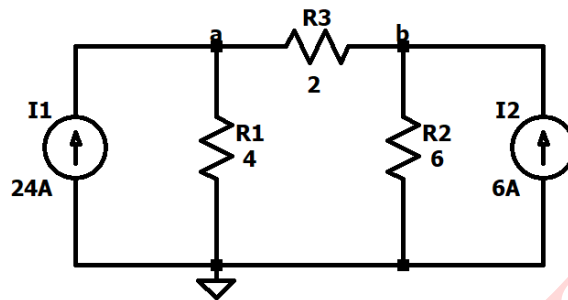


Figure 13: Circuit 4

Solution:

Case 1:

Taking I_1 as the source, I_2 will be open circuited, figure 14

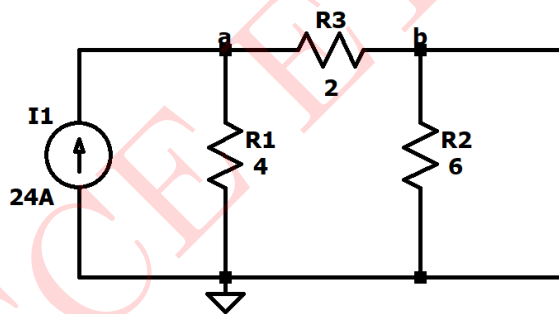


Figure 14: Circuit 4 keeping I_1 as source

Current through 2Ω resistor = i_1

Total current through the circuit $I_T = 24A$

$$\begin{aligned} R_{eq} &= R_2 + R_3 \\ &= 2\Omega + 6\Omega \\ &= 8\Omega \end{aligned}$$

$$\begin{aligned} i_1 &= I_T \frac{R_1}{R_1 + R_{eq}} \\ &= 24 \times \frac{4}{4 + 8} \\ &= 8A \end{aligned}$$

$i_1 = 8A$ (clockwise)

Case 2:

Taking I_2 as the source, I_1 will be open circuited, figure 15

Current through 2Ω resistor = i_2

Total current through the circuit $I_T = 6A$

$$R_{eq} = R_1 + R_2$$

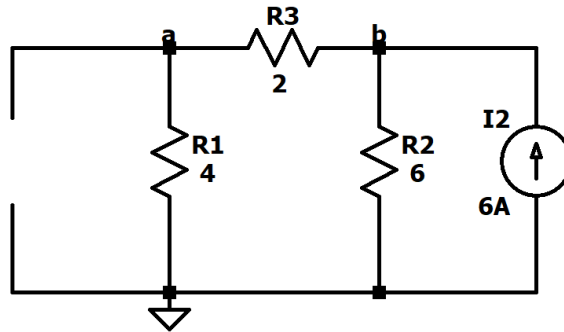


Figure 15: Circuit 4 keeping I_2 as source

$$\begin{aligned}
 &= 4\Omega + 2\Omega \\
 &= 6\Omega \\
 i_2 &= I_T \frac{R_1}{R_1 + R_{eq}} \\
 &= 6 \times \frac{6}{6 + 6} \\
 &= 3A
 \end{aligned}$$

$i_2 = 3A$ (anticlockwise)

From Case 1 and Case 2,

$$\begin{aligned}
 I_{2\Omega} &= i_1 + i_2 \\
 &= 8A - 3A \\
 &= 5A \text{ (clockwise)}
 \end{aligned}$$

$I_{2\Omega} = 5A$ (clockwise)

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

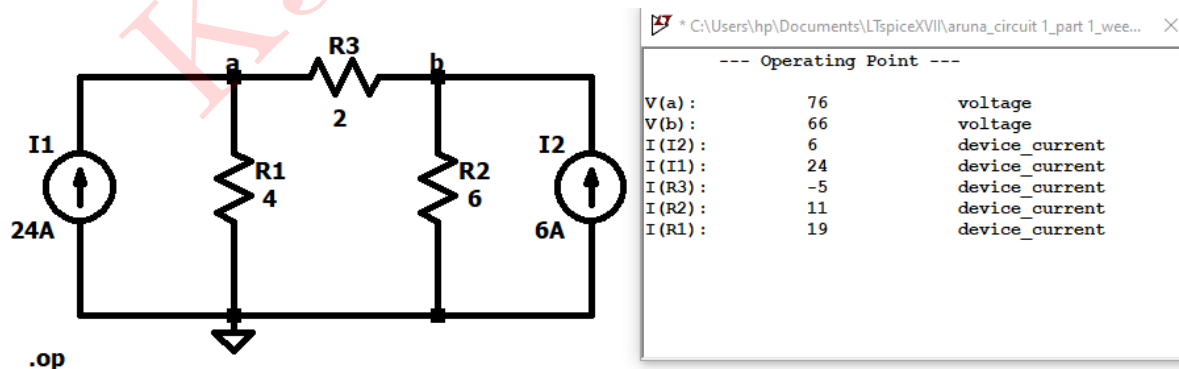


Figure 16: Circuit Schematic and Simulated Results

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|---------------|--------------------|------------------|
| $I_{2\Omega}$ | 5A | 5A |

Table 4: Numerical 3

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Numerical 4: Use Superposition theorem to calculate voltage across 3Ω resistor in figure 17

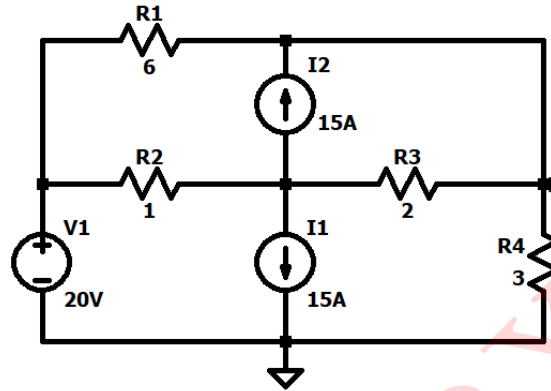


Figure 17: Circuit 5

Solution:

Case 1:

Taking V_1 as the source, I_1 and I_2 will be open circuited, figure 18

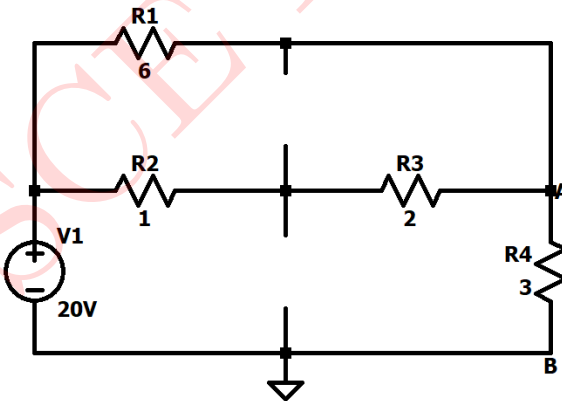


Figure 18: Circuit 5 keeping V_1 as source

$$\begin{aligned} R_{eq} &= (R_1 \parallel (R_2 + R_3)) + R_4 \\ &= (6 \parallel (1 + 2)) + 3 \\ &= 5\Omega \end{aligned}$$

$$I_T = \frac{V_1}{R_{eq}} = \frac{20}{5} = 4A$$

$$\begin{aligned} V_{A1} &= I_T \times R_4 \\ &= 4 \times 3 \\ &= 12V \end{aligned}$$

Case 2:

Taking I_1 as the source, V_1 will be short circuited and I_2 will be open circuited, figure 19

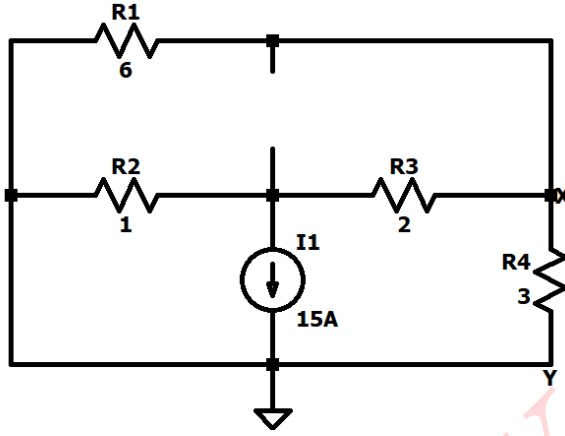


Figure 19: Circuit 5 keeping I_1 as source

Using Mesh analysis in Mesh 1, 2 and 3 we get,

Applying KVL in Mesh 1,

$$-6I_1 - 2(I_1 - I_2) - 1(I_1 - I_3) = 0$$

$$-9I_1 + 3I_2 + I_3 = 0$$

—(i)

Applying KVL in Supermesh,

$$-2(I_2 - I_1) - 3I_2 - 1(I_3 - I_1) = 0$$

$$3I_1 - 5I_2 - I_3 = 0$$

—(ii)

From the figure 7,

$$-I_1 + I_2 = -15$$

—(iii)

From Eqs. (i), (ii) and (iii) we get,

$$I_1 = 1A$$

$$I_2 = -2A$$

$$I_3 = 17A$$

Current through 3Ω resistor = $-2A$

Voltage across 3Ω resistor $V_{A2} = -2 \times 3 = -6V$

Case 3:

Taking I_2 as the source, V_1 will be short circuited and I_1 will be open circuited, figure 20

Using Mesh analysis in Mesh 1, 2 and 3 we get,

Applying KVL in Mesh 3,

$$-3I_3 - 1(I_3 - I_1) - 2(I_3 - I_2) = 0$$

$$I_1 + 2I_2 - 6I_3 = 0$$

—(i)

Applying KVL in Supermesh,

$$-1(I_1 - I_3) - 6I_1 - 2(I_2 - I_3) = 0$$

$$-7I_1 - 2I_2 + 3I_3 = 0$$

—(ii)

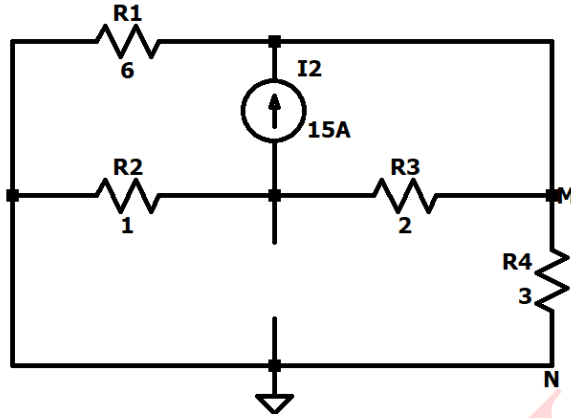


Figure 20: Circuit 5 keeping I_2 as source

From the figure 20,

$$-I_1 + I_2 = -15$$

—(iii)

From Eqs. (i), (ii) and (iii) we get,

$$I_1 = 2A$$

$$I_2 = -13A$$

$$I_3 = 4A$$

Current through 3Ω resistor = $4A$

$$\text{Voltage across } 3\Omega \text{ resistor } V_{A3} = 4 \times 3 = 12V$$

From Case 1, Case 2 and Case 3,

$$\begin{aligned} \text{Net voltage across } R_4 &= V_{A1} + V_{A2} + V_{A3} \\ &= 12V - 6V - 12V \\ &= 18V \text{ (clockwise)} \end{aligned}$$

$$V_{3\Omega} = 18V(\text{clockwise})$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

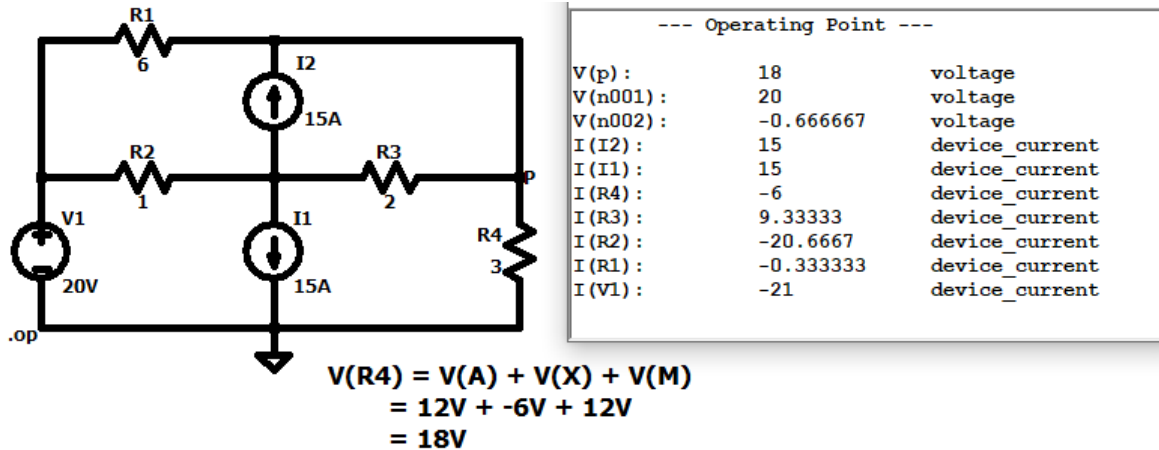


Figure 21: Circuit Schematic and Simulated Results

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|---------------|--------------------|------------------|
| $V_{3\Omega}$ | 18V | 18V |

Table 5: Numerical 4

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Numerical 5: Find the Thevenin's equivalent of the circuit as seen by looking into terminals A-B in figure 22.

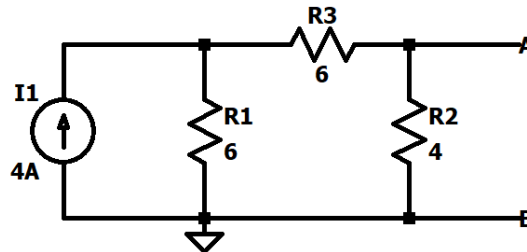


Figure 22: Circuit 6

Solution:

Step 1: Calculation of V_{th}

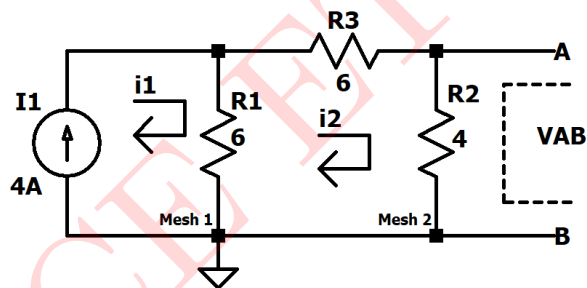


Figure 23: Finding V_{th}

Apply KVL to mesh 1,

$$i_1 = 4A \text{ (anticlockwise)} \quad \text{---(i)}$$

Apply KVL to mesh 2,

$$-6i_2 - 4i_2 - 6(i_2 - i_1) = 0$$

$$-16i_2 - 6i_1 = 0$$

$$\text{---(ii)}$$

Solving (i) and (ii),

$$i_2 = 1.5A \text{ (anticlockwise)}$$

$$V_{AB} = i_2 \times R_2 = 6V$$

$$V_{th} = V_{AB} = 6V$$

$$V_{th} = \mathbf{6V}$$

Step 2: Calculation of R_{th}

For finding R_{th} , deactivate all the independent sources,

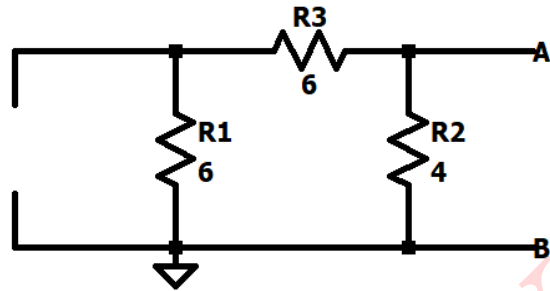


Figure 24: Finding R_{th}

$$\begin{aligned}\text{Equivalent resistance across AB} = R_{th} &= (R_1 + R_3) \parallel R_2 \\ &= (6 + 6) \parallel 4 \\ &= 3\Omega\end{aligned}$$

$$R_{th} = 3\Omega$$

Thevenin's Equivalent Circuit

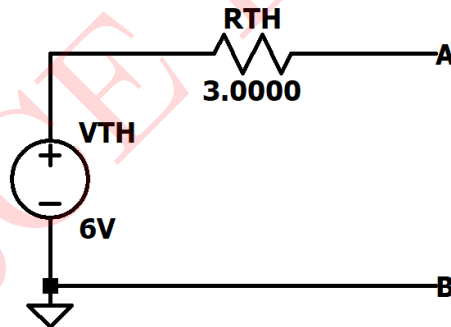


Figure 25: Thevenin's equivalent circuit

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

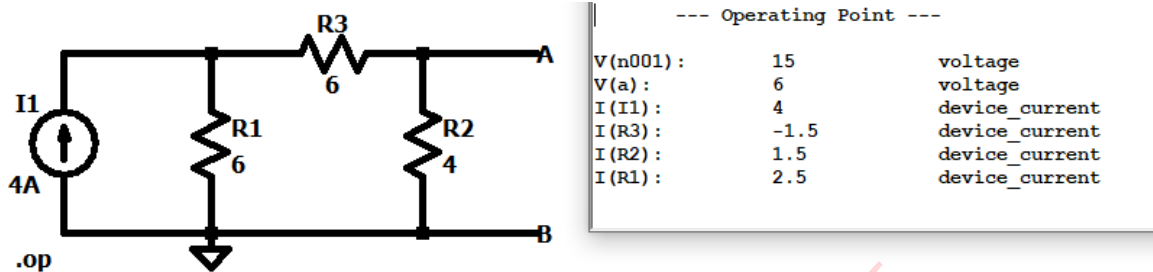


Figure 26: Circuit Schematic and Simulated Results for V_{th}

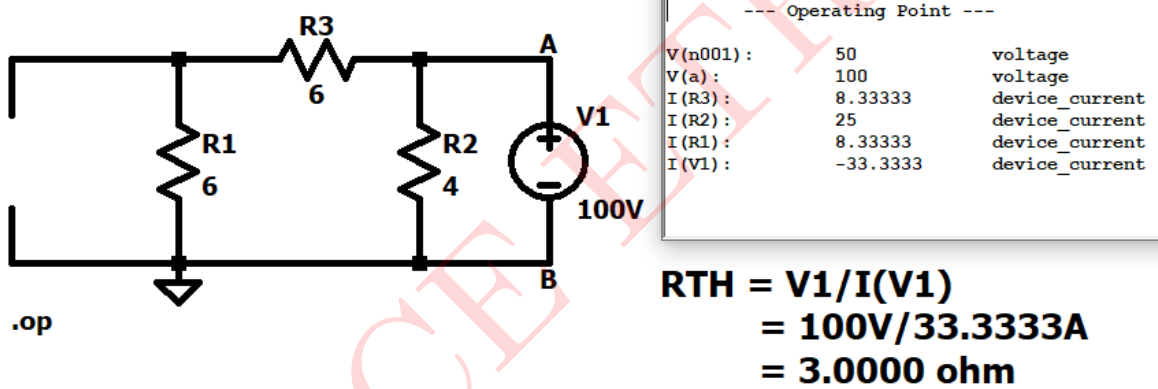


Figure 27: Circuit Schematic and Simulated Results for R_{th}

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| V_{th} | 6V | 6V |
| R_{th} | 3Ω | 3.00Ω |

Table 6: Numerical 5

Numerical 6: For the circuit in figure 28, find the Thevenin's equivalent of the circuit across terminals A-B.

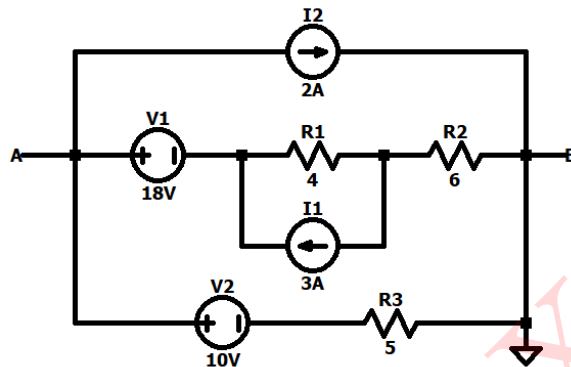


Figure 28: Circuit 7

Solution:

Step 1: Calculation of V_{th}

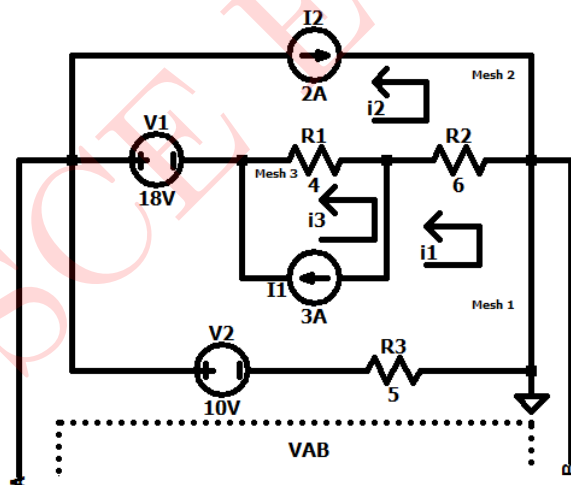


Figure 29: Finding V_{th}

From figure 29,

$$i_1 - i_3 = 3A \quad \text{---(i)}$$

$$i_2 = -2A \quad \text{---(ii)}$$

Applying KVL in Supermesh,

$$-10 - 5i_1 - 6(i_1 - i_2) - 4(i_3 - i_2) + 18 = 0$$

$$11i_1 - 10 - i_2 + 4i_3 = 8 \quad \text{---(iii)}$$

Solving (i), (ii) and (iii),

$$i_1 = 0A, i_3 = -3A$$

$$\begin{aligned} V_{th} &= V_2 + i_1 \times R_2 \\ &= 10 + 0 \times 5 \\ &= 10V \end{aligned}$$

Step 2: Calculation of R_{th}

For finding R_{th} , deactivate all the independent sources,

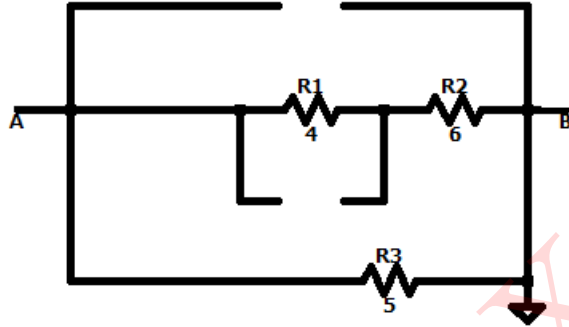


Figure 30: Finding R_{th}

$$\begin{aligned}\text{Equivalent resistance across AB} = R_{th} &= (R_1 + R_2) \parallel R_3 \\ &= (4+6) \parallel 5 \\ &= 3.3333\Omega\end{aligned}$$

$$R_{th} = 3.3333\Omega$$

Thevenin's Equivalent Circuit

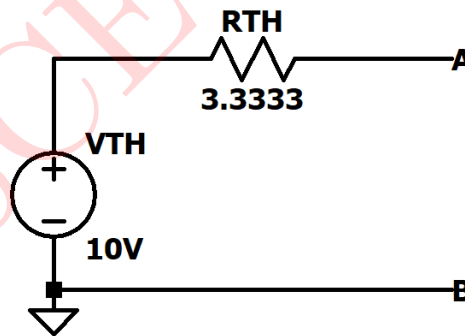


Figure 31: Thevenin's equivalent circuit

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

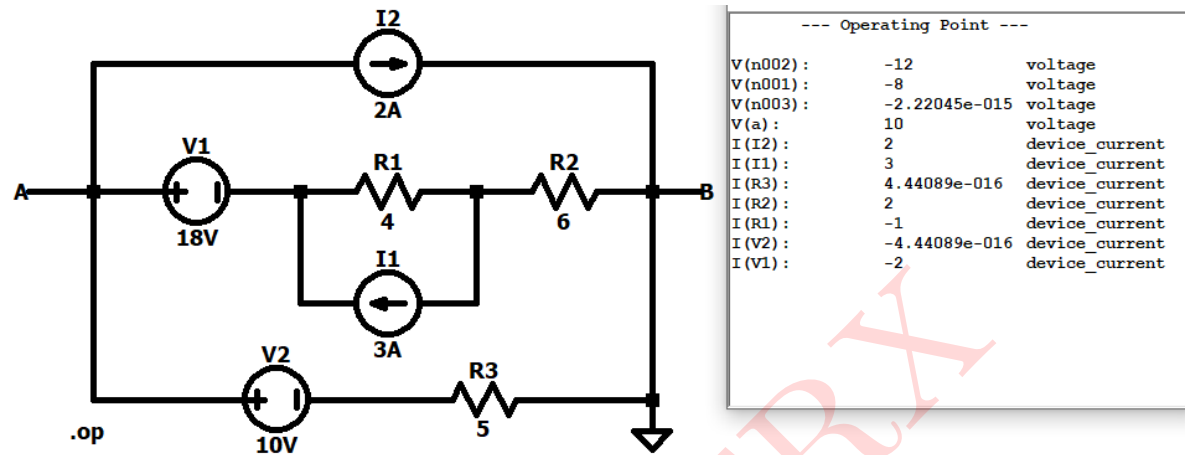


Figure 32: Circuit Schematic and Simulated Results for V_{th}

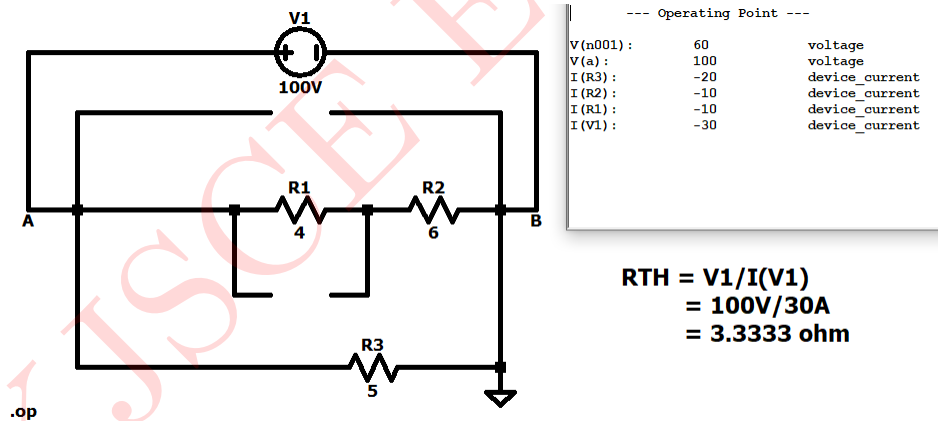


Figure 33: Circuit Schematic and Simulated Results for R_{th}

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| V_{th} | 10V | 10V |
| R_{th} | 3.3333Ω | 3.3333Ω |

Table 7: Numerical 6

Numerical 7: Using Norton's theorem, find the current which would flow in a 25Ω resistor connected between points N and O in figure 34.

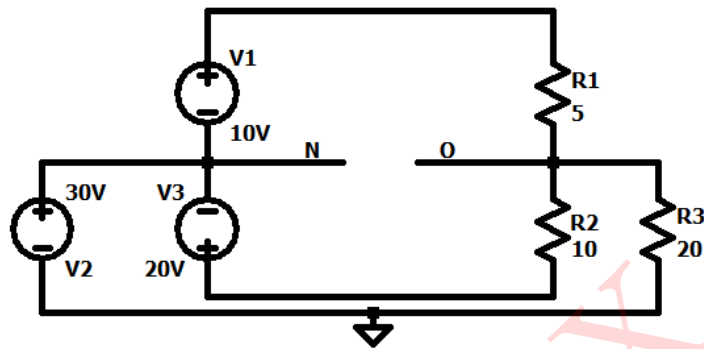


Figure 34: Circuit 8

Solution:

Step 1: Calculation of I_{sc}

Short Circuit NO to find I_{sc}

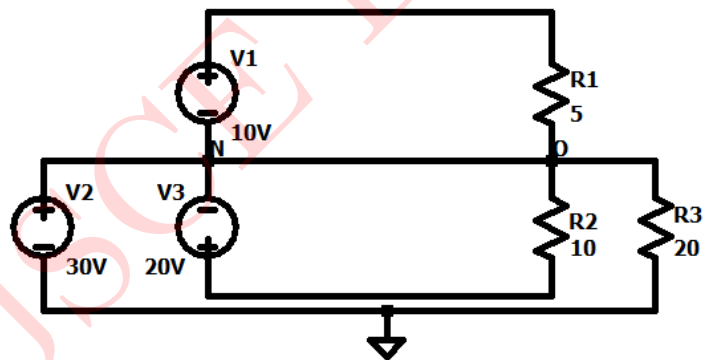


Figure 35: Finding I_{sc}

$$\begin{aligned}
 I_{sc} &= \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \\
 &= \frac{10}{5} + \frac{30}{10} - \frac{20}{20} \\
 &= 2.5\text{A}
 \end{aligned}$$

$$I_{sc} = 2.5\text{A}$$

Step 2: Calculation of R_N

Deactivate all independent sources to find R_N

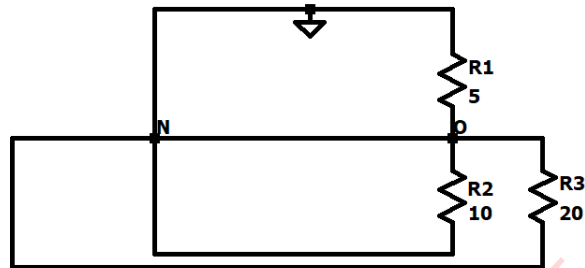


Figure 36: Finding R_N

$$\begin{aligned}\frac{1}{R_N} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \\ &= \frac{1}{5} + \frac{1}{10} + \frac{1}{20} \\ &= \frac{7}{20}\end{aligned}$$

$$R_N = 2.857\Omega$$

Norton's Equivalent Circuit

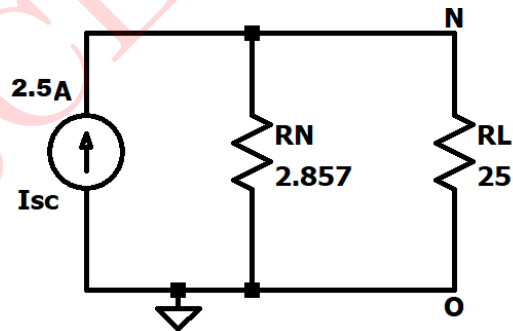


Figure 37: Norton's equivalent circuit

For finding current across 25Ω resistor

Open circuit voltage through NO

$$\begin{aligned}V_{NO} &= I_{sc} \times R_N \\ &= 2.5 \times 2.857 \\ &= 7.1425\text{V}\end{aligned}$$

Current through 25Ω resistor across NO

$$\begin{aligned}I_{RL} &= \frac{V_{NO}}{R_L} \\ &= \frac{7.1425}{25} \\ &= 0.2857\text{A}\end{aligned}$$

$$I_{25\Omega} = 0.2857\text{A}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

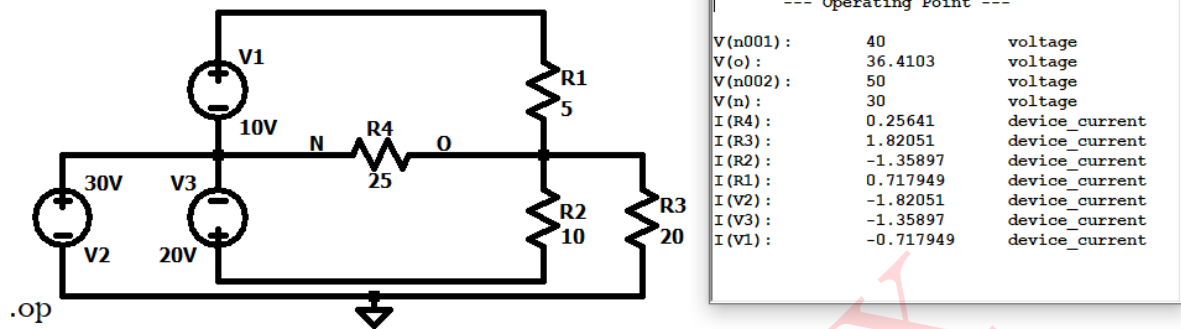


Figure 38: Circuit Schematic and Simulated Results for $I_{25\Omega}$

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|----------------|--------------------|------------------|
| $I_{25\Omega}$ | 0.2857A | 0.2564A |

Table 8: Numerical 7

Numerical 8 : Find the Norton's equivalent and Thevenin's equivalent of the circuit across terminals A-B of the circuit in figure 39.

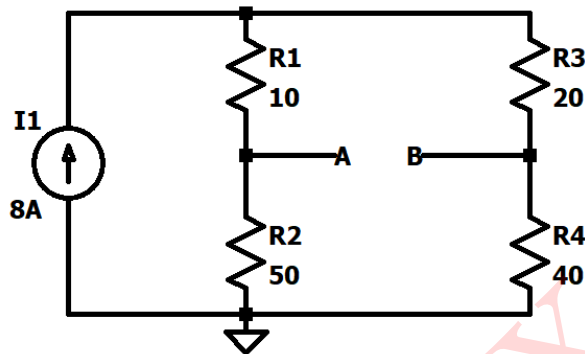


Figure 39: Circuit 9

Solution:

Step 1: Calculation of I_{sc}

Short Circuit AB to find I_{sc}

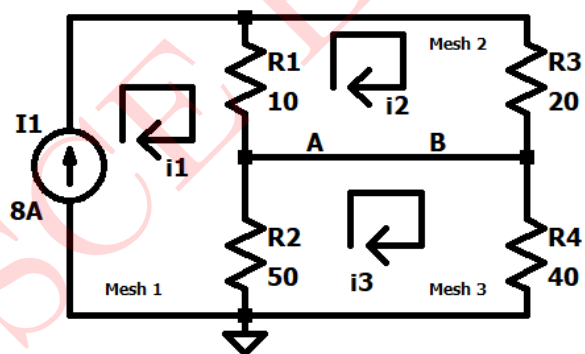


Figure 40: Finding I_{sc}

Apply KVL to mesh 1,

$$i_1 = 8A \text{ (clockwise)} \quad \text{---(i)}$$

Apply KVL to mesh 2,

$$\begin{aligned} -20i_2 - 10(i_2 - i_1) &= 0 \\ i_2 &= 2.667A \text{ (clockwise)} \end{aligned} \quad \text{---(ii)}$$

Apply KVL to mesh 3,

$$\begin{aligned} -40i_3 - 50(i_3 - i_1) &= 0 \\ i_3 &= 4.444A \text{ (clockwise)} \end{aligned} \quad \text{---(iii)}$$

From (ii) and (iii),

$$\begin{aligned} I_{sc} &= i_3 - i_2 \\ &= 4.444 - 2.667 \\ &= 1.777A \text{ (clockwise)} \end{aligned}$$

$$I_{sc} = 1.777A \text{ (clockwise)}$$

Step 2: Calculation of R_N

Deactivate all independent sources to find R_N

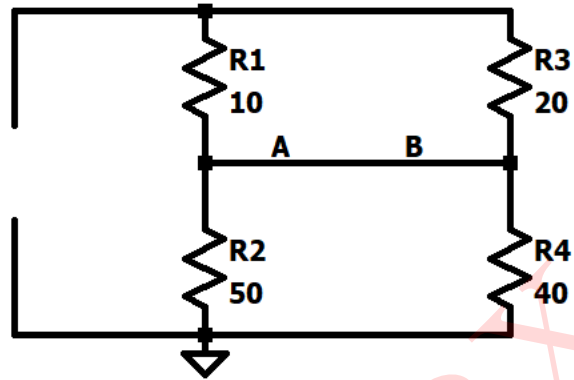


Figure 41: Finding R_N

$$\begin{aligned} R_N &= (R_1 + R_3) \parallel (R_2 + R_4) \\ &= (10 + 20) \parallel (50 + 40) \\ &= 22.5\Omega \end{aligned}$$

$$R_N = 22.5\Omega$$

Norton's Equivalent Circuit

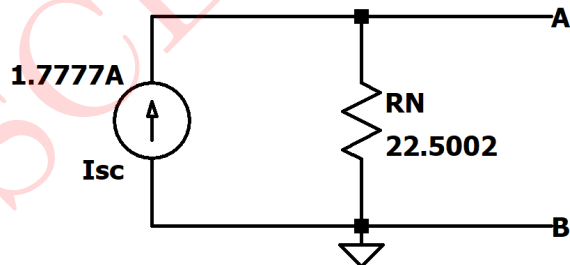


Figure 42: Norton's equivalent circuit

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

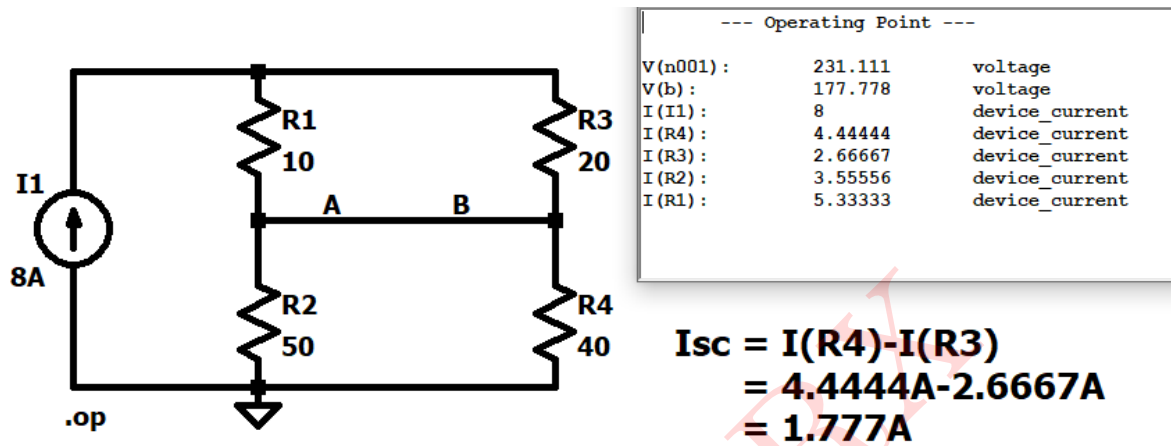


Figure 43: Circuit Schematic and Simulated Results for I_{sc}

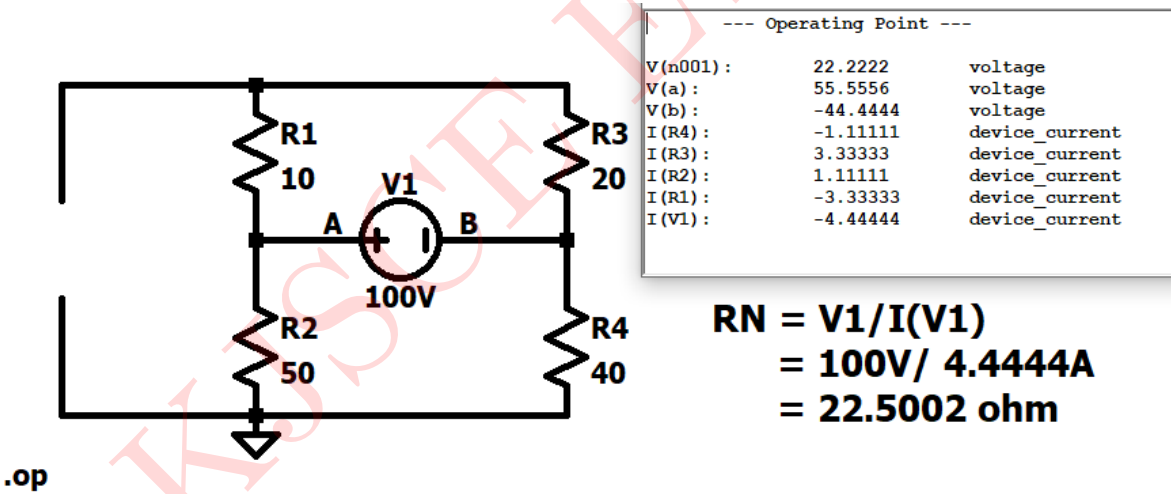


Figure 44: Circuit Schematic and Simulated Results for R_N

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| I_{sc} | 1.777A | 1.7777A |
| R_N | 22.5Ω | 22.5002Ω |

Table 9: Numerical 8 Norton's Theorem

Thevenin's Theorem

Step 1: Calculation of V_{th}

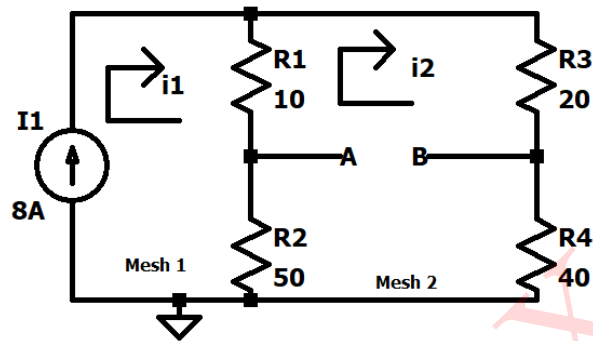


Figure 45: Finding V_{th}

Apply KVL to mesh 1,

$$i_1 = 8A \text{ (clockwise)} \quad \text{---(i)}$$

Apply KVL to mesh 2,

$$\begin{aligned} -20i_2 - 40i_2 - 4i_2 - 10(i_2 - i_1) - 50(i_2 - i_1) &= 0 \\ 60i_1 - 120i_2 &= 0 \end{aligned} \quad \text{---(ii)}$$

Solving (i) and (ii),

$$i_2 = 4A \text{ (anticlockwise)}$$

$$\begin{aligned} V_B &= i_2 \times R_3 \\ &= 4 \times 20 \\ &= 80 \end{aligned}$$

$$\begin{aligned} V_A &= i_2 \times R_1 \\ &= 4 \times 10 \\ &= 40 \end{aligned}$$

$$\begin{aligned} V_{AB} &= V_B - V_A \\ &= 80 - 40 \\ &= 40 \end{aligned}$$

$$V_{th} = V_{AB} = 40V$$

$$V_{th} = \mathbf{40V}$$

Step 2: Calculation of R_{th}

For finding R_{th} , deactivate all the independent sources,

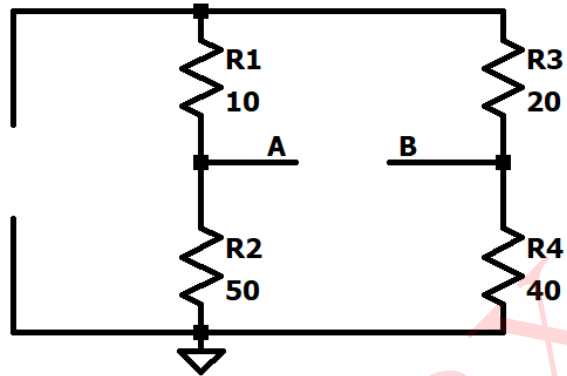


Figure 46: Finding R_{th}

$$\begin{aligned} R_{th} &= (R_1 + R_3) \parallel (R_2 + R_4) \\ &= (10 + 20) \parallel (50 + 40) \\ &= 22.5\Omega \end{aligned}$$

$$R_{th} = 22.5\Omega$$

Thevenin's Equivalent Circuit

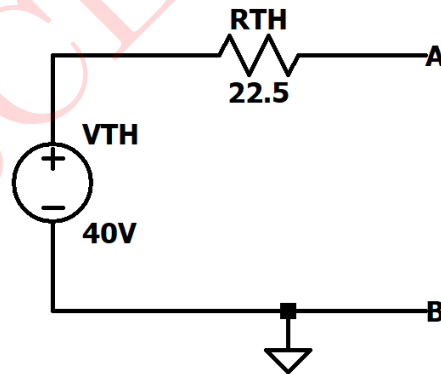


Figure 47: Thevenin's equivalent circuit

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

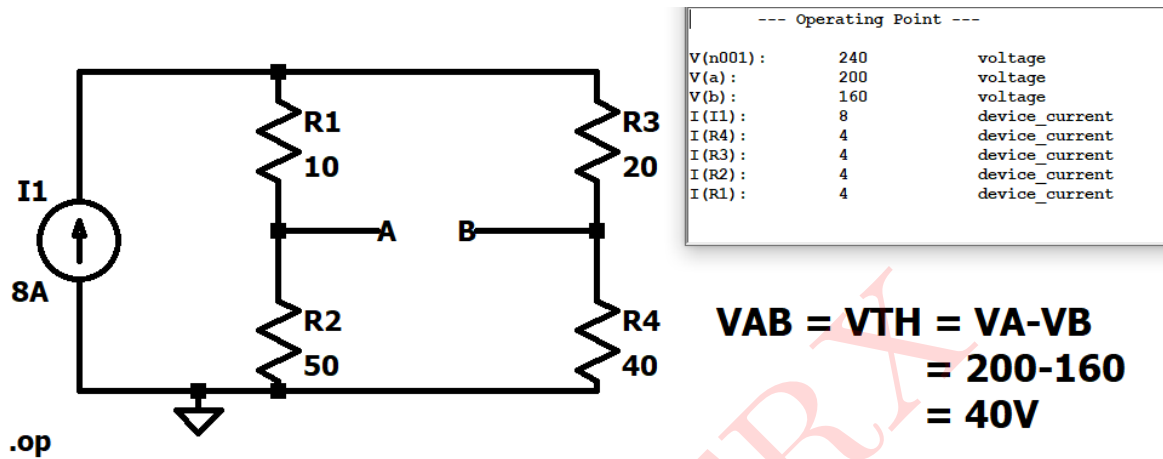


Figure 48: Circuit Schematic and Simulated Results for V_{th}

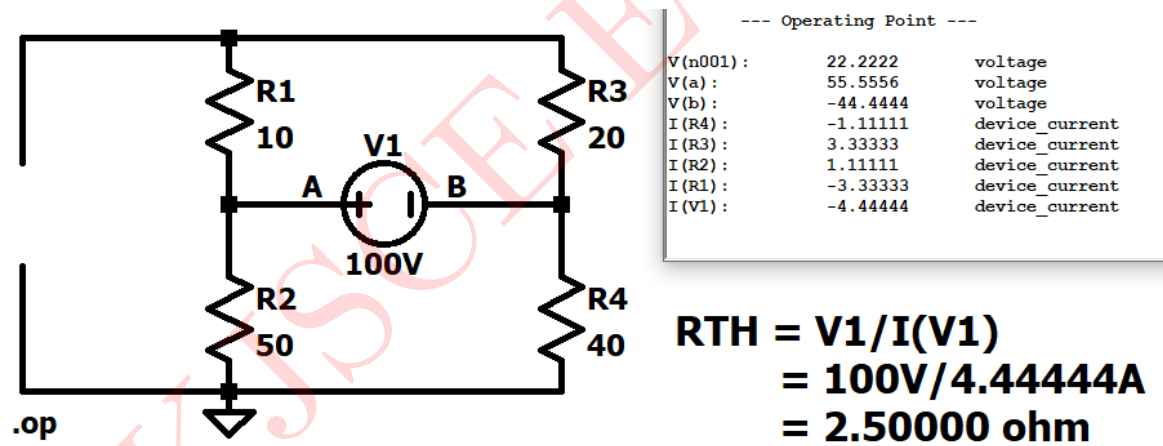


Figure 49: Circuit Schematic and Simulated Results for R_{th}

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| V_{th} | 40V | 40V |
| R_{th} | 22.5Ω | 22.500Ω |

Table 10: Numerical 8 Thevenin's theorem

Numerical 9: For the circuit in figure 50, find the Norton's equivalent circuit at terminals A-B.

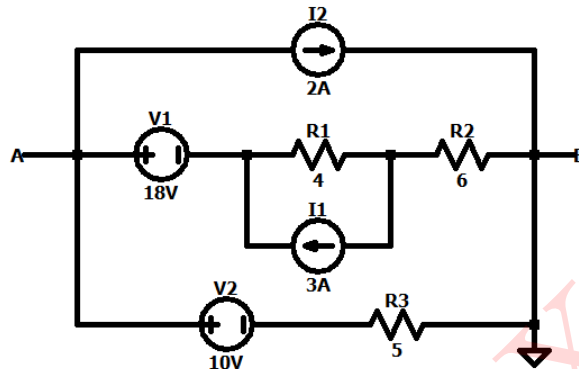


Figure 50: Circuit 10

Solution:

Step 1: Calculation of I_{sc}

Short Circuit AB to find I_{sc}

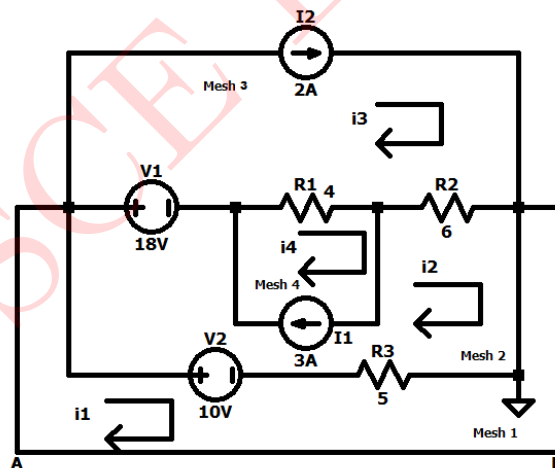


Figure 51: Finding I_{sc}

From figure 51,

$$i_3 = 2A \quad \text{---(i)}$$

$$i_4 - i_3 = 3A \quad \text{---(ii)}$$

Applying KVL in Mesh 1,

$$\begin{aligned} -10 - 5(i_1 - i_2) &= 0 \\ -5i_1 + 5i_2 &= 10 \end{aligned} \quad \text{---(iii)}$$

Applying KVL in Supermesh,

$$\begin{aligned} -18 - 4(i_4 - i_3) - 6(i_2 - i_3) - 5(i_2 - i_1) + 10 &= 0 \\ 5i_1 - 11i_2 + 10i_3 - 4i_4 &= 10 \end{aligned} \quad \text{---(iv)}$$

Solving (i), (ii), (iii) and (iv),

$$i_1 = 3\text{A}, i_2 = -1\text{A}$$

$$I_{sc} = i_1 = 3\text{A}$$

$$I_{sc} = 3\text{A}$$

Step 2: Calculation of R_N

Deactivate all independent sources to find R_N

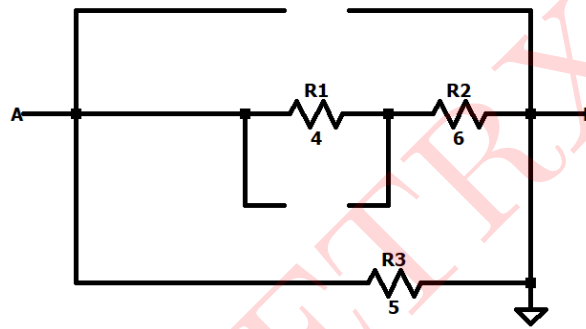


Figure 52: Finding R_N

$$\begin{aligned} \text{Equivalent resistance across AB} = R_N &= (R_1 + R_2) \parallel R_3 \\ &= (4+6) \parallel 5 \\ &= 3.3333\Omega \end{aligned}$$

$$R_N = 3.3333\Omega$$

Norton's Equivalent Circuit

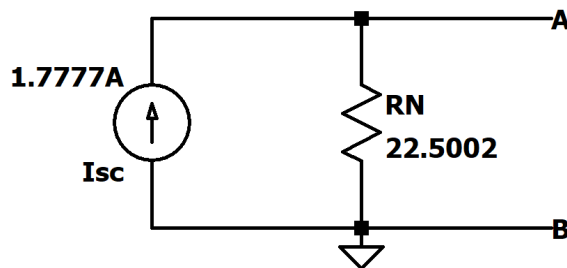


Figure 53: Norton's equivalent circuit

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

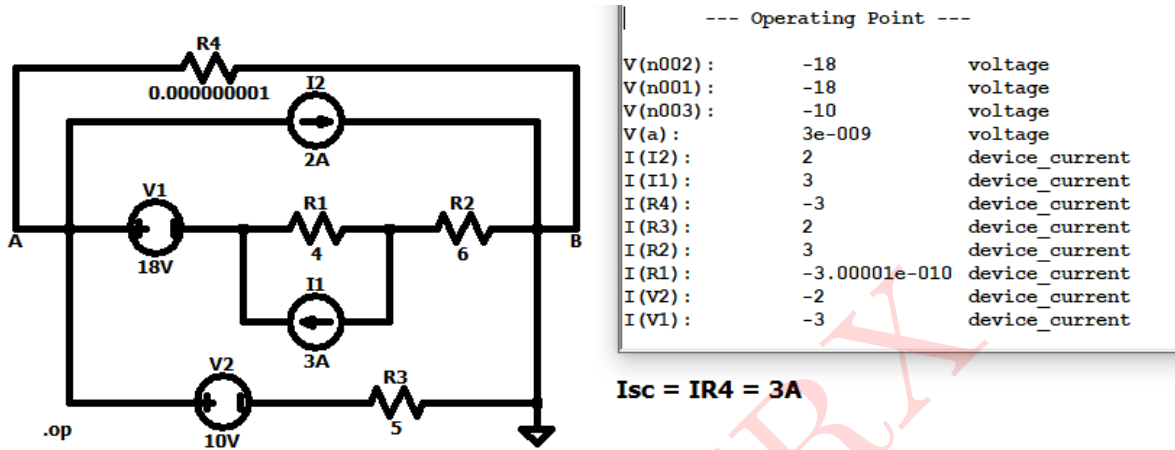


Figure 54: Circuit Schematic and Simulated Results for I_{sc}

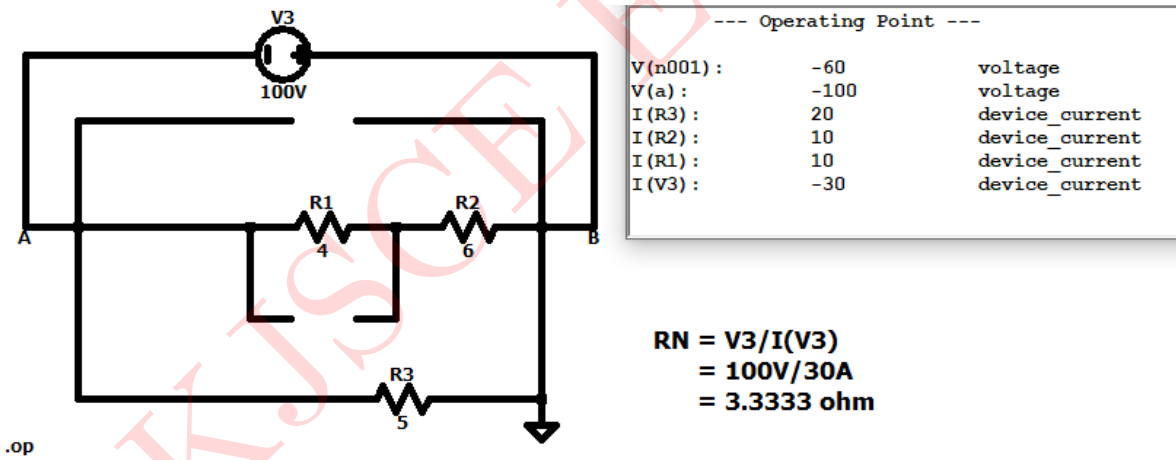


Figure 55: Circuit Schematic and Simulated Results for R_N

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|------------|--------------------|------------------|
| I_{sc} | 3A | 3A |
| R_N | 3.33Ω | 3.33Ω |

Table 11: Numerical 9

Numerical 10: Calculate the value of R_L which will absorb maximum power from the circuit in figure 56. Also compute the value of maximum power.

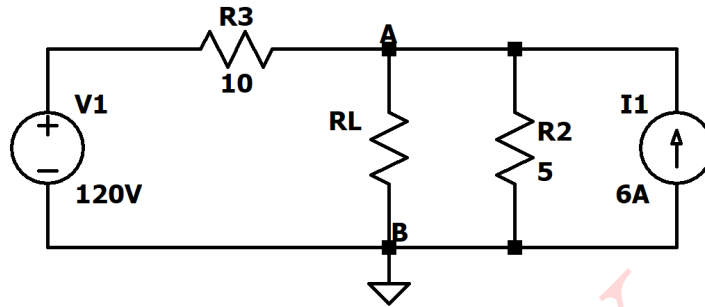


Figure 56: Circuit 11

Solution:

Step 1: Calculation of V_{th}

For finding V_{th} , remove resistor R_L and find voltage across AB.

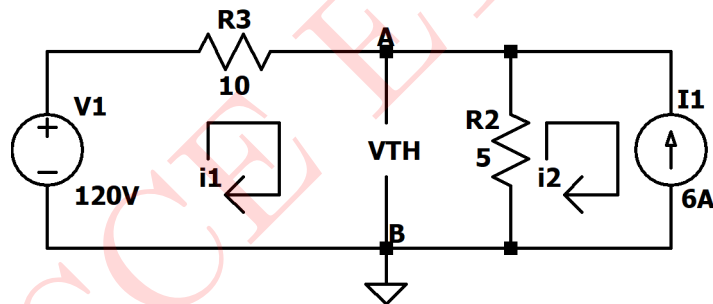


Figure 57: Finding V_{th}

Apply KVL to loop 1,

$$120 - 10i_1 - 5(i_1 - i_2) = 0$$

$$15i_1 - 5i_2 = 120$$

—(i)

Apply KVL to loop 2,

$$i_2 = -6A$$

—(ii)

From (i) and (ii),

$$i_1 = 6A$$

$$V_{th} = V_{AB} = 120 - 6 \times 10 - 5(6 - 6) = 60$$

$$V_{th} = 60V$$

Step 2: Calculation of R_{th}

For finding R_{th} , deactivate all the independent sources,

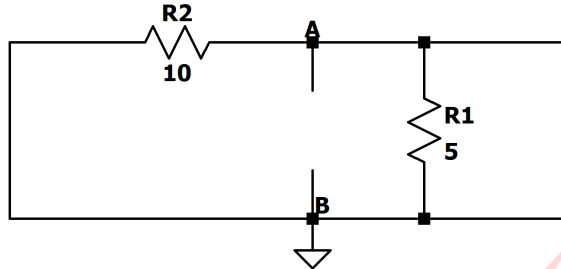


Figure 58: Finding R_{th}

$$\begin{aligned}\text{Equivalent resistance across AB} = R_{th} &= R_1 || R_2 \\ &= 5 || 10 \\ &= 3.333\Omega\end{aligned}$$

$$R_{th} = 3.333\Omega$$

Thevenin's Equivalent Circuit

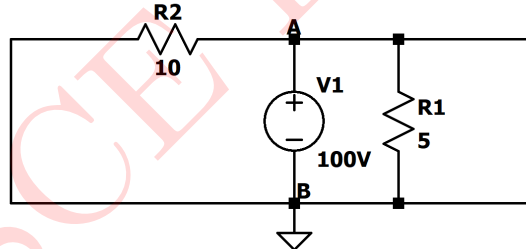


Figure 59: Thevenin's equivalent circuit

For maximum power transfer $R_L = R_{th} = 3.333\Omega$

$$R_L = 3.333\Omega$$

Maximum power can be calculated as

$$\begin{aligned}P_{max} &= \frac{V_{th}^2}{4R_{th}} \\ &= \frac{60^2}{4 \times 3.333} \\ &= 270.0027W\end{aligned}$$

$$\text{Maximum Power} = 270.0027W$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

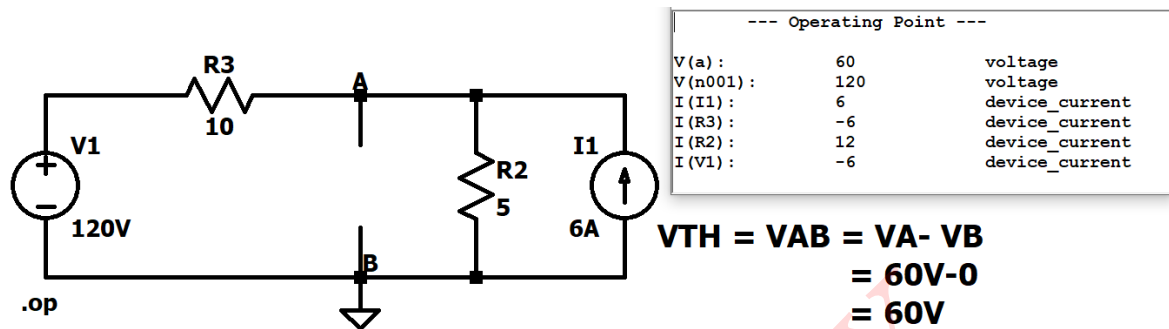


Figure 60: Circuit Schematic and Simulated Results for V_{th}

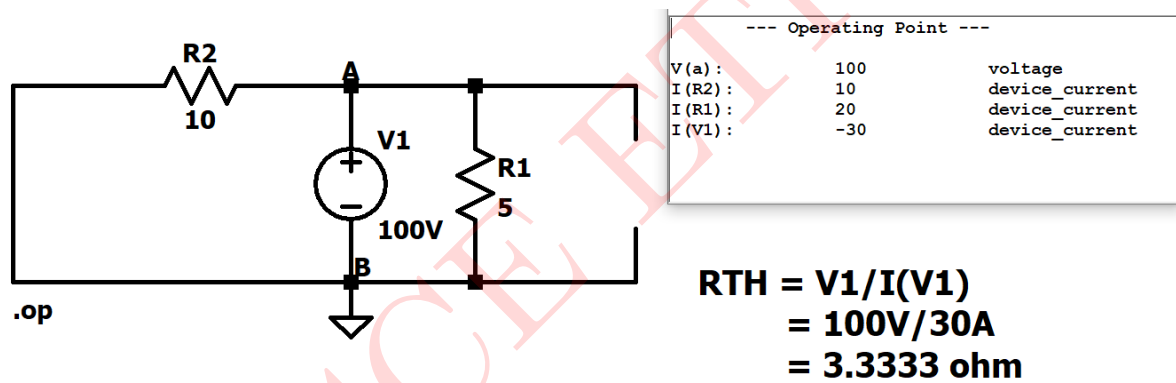


Figure 61: Circuit Schematic and Simulated Results for R_{th}

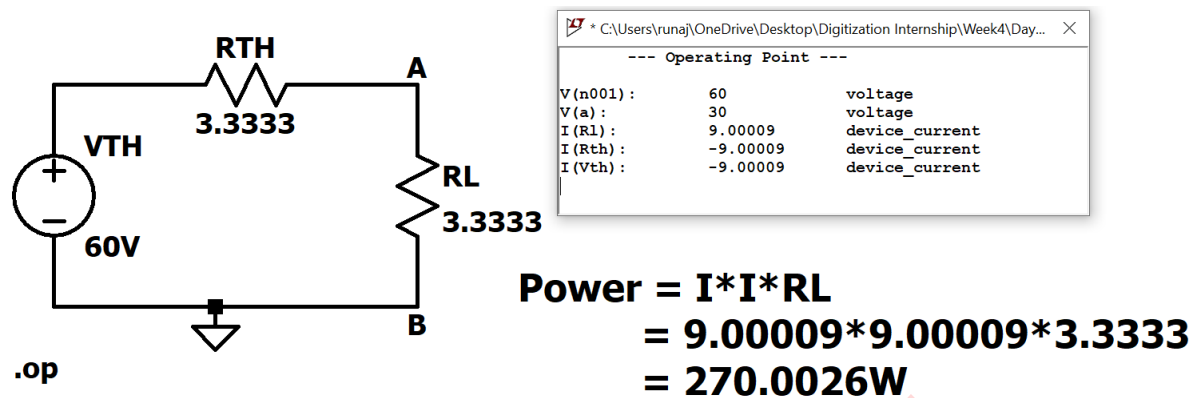


Figure 62: Circuit Schematic and Simulated Results for Maximum Power

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|---------------|--------------------|------------------|
| V_{th} | 60V | 60V |
| R_{th} | 3.333Ω | 3.333Ω |
| Maximum Power | 270.0027W | 270.0026W |

Table 12: Numerical 10

Numerical 11: Calculate the value of R_L which will absorb maximum power from the circuit in figure 63. Also compute the value of maximum power.

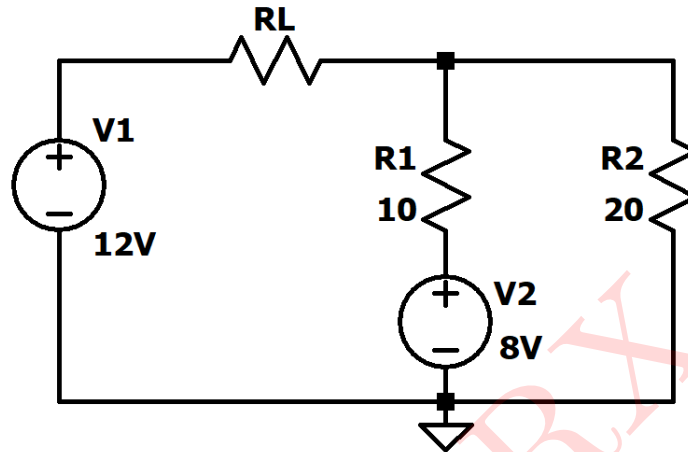


Figure 63: Circuit 12

Solution:

Step 1: Calculation of V_{th}

For finding V_{th} , remove resistor R_L and find voltage across AB.

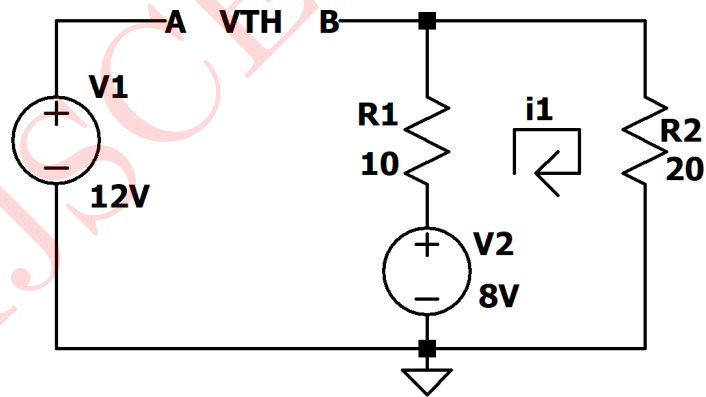


Figure 64: Finding V_{th}

Applying Mesh analysis,

$$8 - 10i_1 - 20i_1 = 0$$

$$i_1 = 0.2667\text{A}$$

$$\begin{aligned} V_{th} = V_{AB} &= 12 - 8 + 10 \times i_1 \\ &= 12 - 8 + 10 \times 0.2667 \\ &= 6.6667\text{V} \end{aligned}$$

$$V_{th} = \mathbf{6.6667\text{V}}$$

Step 2: Calculation of R_{th}

For finding R_{th} , deactivate all the independent sources,

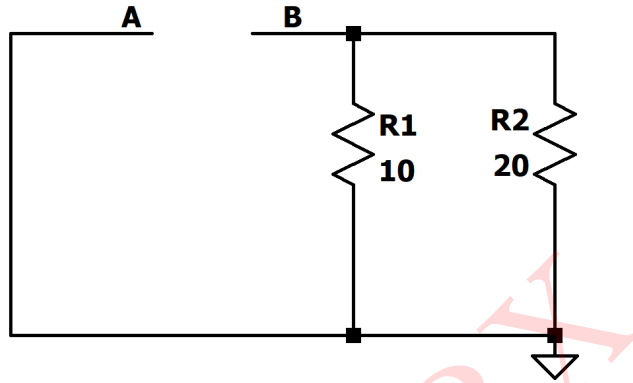


Figure 65: Finding R_{th}

$$\begin{aligned}\text{Equivalent resistance across AB} &= R_{th} = R_1 || R_2 \\ &= 10 || 20 \\ &= 6.6667\Omega\end{aligned}$$

$$R_{th} = 6.6667\Omega$$

Thevenin's Equivalent Circuit

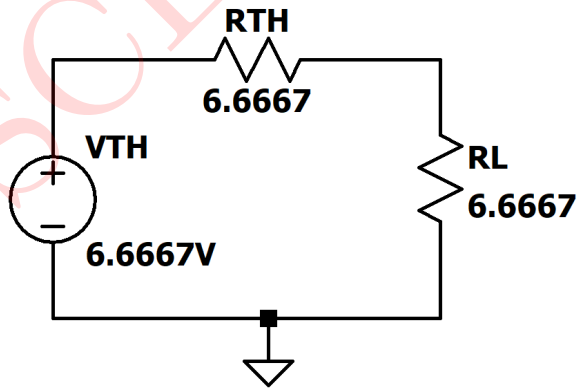


Figure 66: Thevenin's equivalent circuit

For maximum power transfer $R_L = R_{th} = 6.6667\Omega$

$$R_L = 6.6667\Omega$$

Maximum power can be calculated as

$$\begin{aligned}P_{max} &= \frac{V_{th}^2}{4R_{th}} \\ &= \frac{6.6667^2}{4 \times 6.6667} \\ &= 1.666675W\end{aligned}$$

$$\text{Maximum Power} = 1.666675W$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

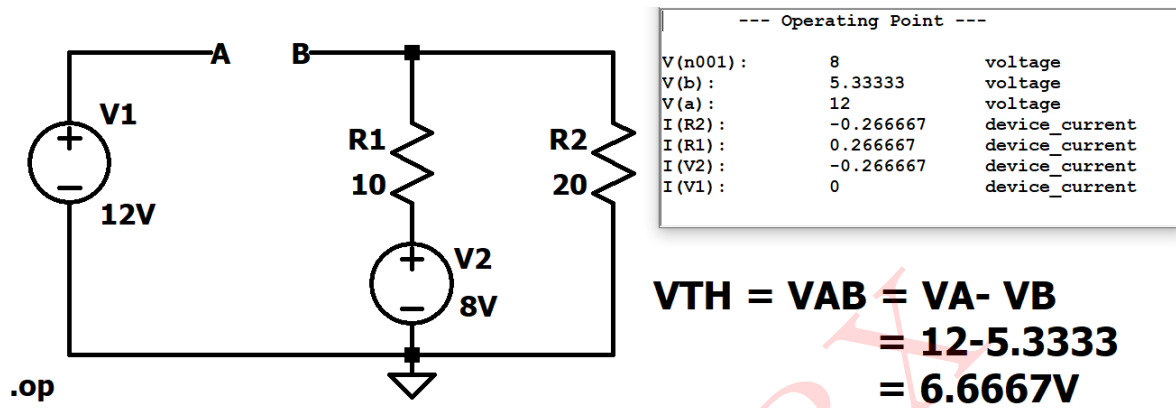


Figure 67: Circuit Schematic and Simulated Results for V_{th}

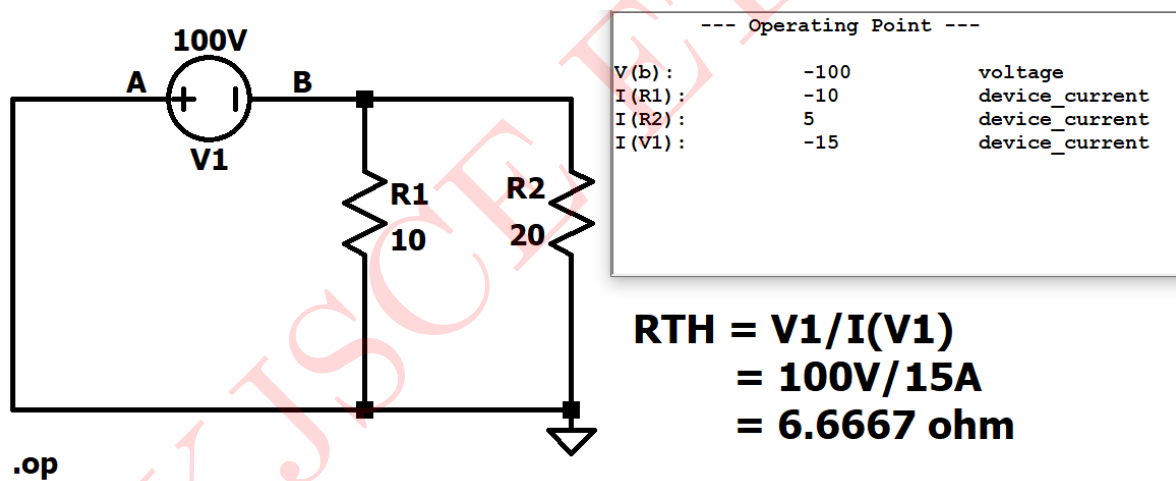


Figure 68: Circuit Schematic and Simulated Results for R_{th}

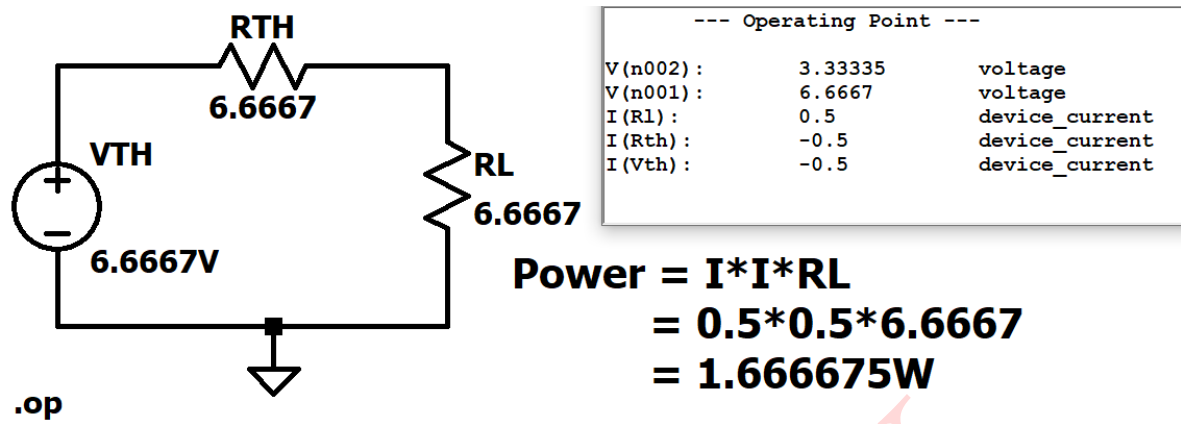


Figure 69: Circuit Schematic and Simulated Results for Maximum Power

Comparison of theoretical and simulated values:

| Parameters | Theoretical Values | Simulated Values |
|---------------|--------------------|------------------|
| V_{th} | 6.6667V | 6.6667V |
| R_{th} | 6.6667Ω | 6.6667Ω |
| Maximum Power | 1.666675W | 1.666675W |

Table 13: Numerical 11