# K. J. SOMAIYA COLLEGE OF ENGINEERING DEPARTMENT OF ELECTRONICS ENGINEERING ELEMENTS OF ELECTRICAL AND ELECTRONICS ENGINEERING DC CRICUITS

**Numerical 1:** Find the current  $I_0$  in Circuit 1.

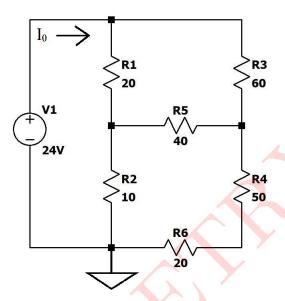


Figure 1: Circuit 1

#### **Solution:**

By using delta to star conversion,

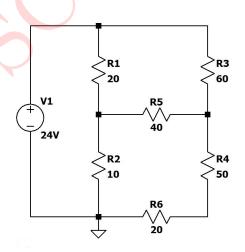


Figure 2: Modified circuit for figure 1

By further simplyfing we get,

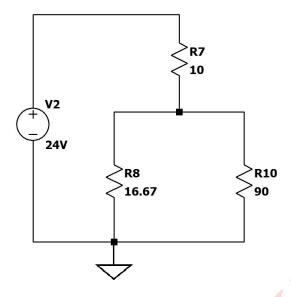


Figure 3: Modified circuit for figure 2

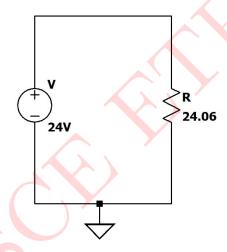


Figure 4: Modified circuit for figure 3

$$\therefore I_0 = \frac{V}{R}$$

$$\therefore I_0 = \frac{24}{24.064}$$

$$I_0 = 0.9973 \text{ A}$$

The above circuit is simulated in LTspice. The results are presented below.

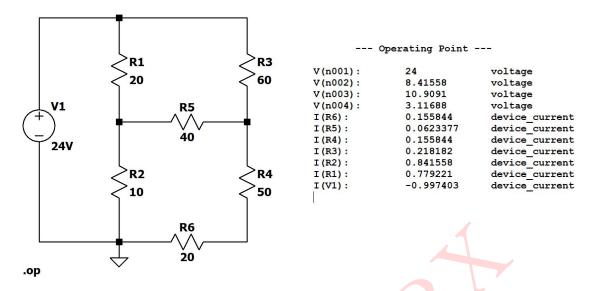


Figure 5: Circuit schematic and simulated results

Here,  $I_{V1} = I_0 = 0.9974$ A

Parameter	Theoretical value	Simulated values
$I_0$	0.9973A	0.9974A

Table 1: Numerical 1

Numerical 2: Find  $R_{ab}$  in the four way power divider circuit. Assume each element is  $1\Omega$ .

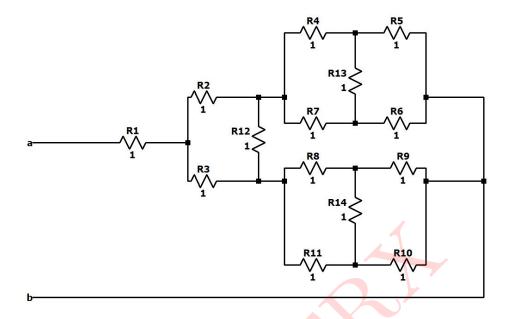


Figure 6: Circuit 2

## Solution:

Since loop 1 and loop 2 form a wheatstone's bridge, current through  $R_{13}$  and  $R_{14}$  becomes zero. Therefore,  $R_{13}$  and  $R_{14}$  becomes open i.e. gets removed.

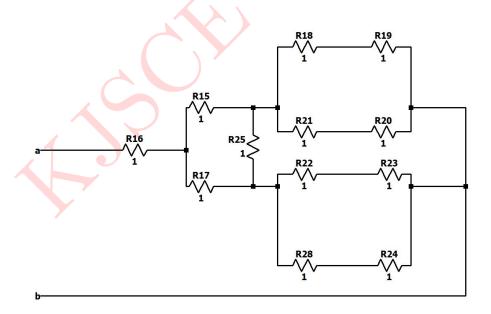


Figure 7: Modified circuit for figure 6

After simplifying the circuit we get, Now, this loop also forms a wheatstone's bridge

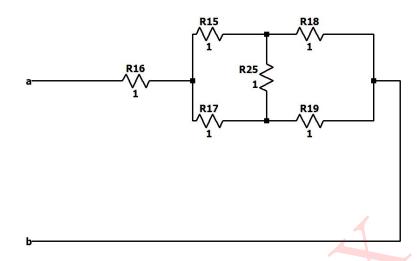


Figure 8: Modified circuit for figure 7

Therefore the resistance  $R_{25}$  gets removed.

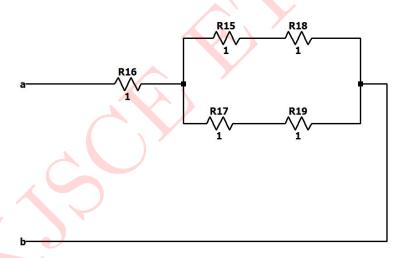


Figure 9: Modified circuit for figure 8

After simplyfing the circuit we get,

$$R_{ab} = 2\Omega$$

The above circuit is simulated in LTspice. The results are presented below.

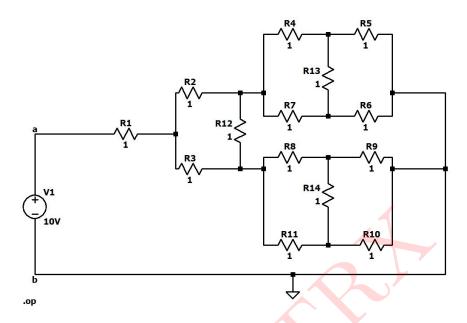


Figure 10: Circuit schematic

Î		Operating	Point	<del>/-</del>
V(n001)	:	2.5		voltage
V(n004)	:	5		voltage
V(a):		10		voltage
V(n005)		2.5		voltage
V(n002)	:	1.25		voltage
V(n003)	:	1.25		voltage
V(n006)	:	1.25		voltage
V(n007)		1.25		voltage
I (R11):		-1.25	i	device current
I (R14):		0		device current
I (R13):		0		device current
I (R12):		0		device current
I(R10):		-1.25	i e	device_current
I(R9):		-1.25	i	device_current
I(R8):		-1.25	i	device_current
I(R7):		-1.25	5	device_current
I(R6):		-1.25	i	device_current
I(R5):		-1.25	i	device_current
I(R4):		-1.25	i e	device_current
I(R3):		-2.5		device_current
I(R1):		-5		device_current
I(R2):		-2.5		device_current
I(V1):		-5		device current

Figure 11: Simulated results

$${\rm Here},$$

$$R_{ab} = \frac{V_1}{I_V}$$

$$R_{ab} = \frac{10}{5}$$

$$R_{ab} = 2\Omega$$

Parameter	Theoretical value	Simulated values
$R_{ab}$	$2 \Omega$	$2 \Omega$

Table 2: Numerical 2

# Numerical 3: Using superposition, find $V_0$ in the circuit 3.

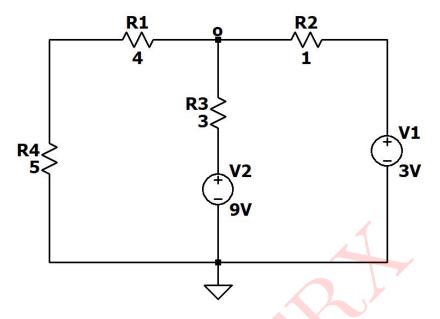


Figure 12: Circuit 3

## Solution:

Step 1: When 3V source is acting alone,

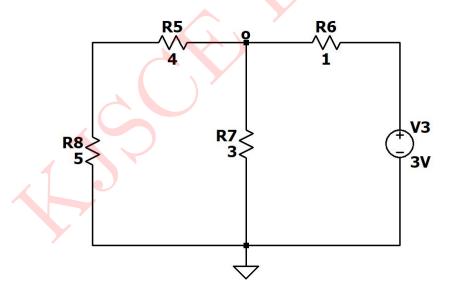


Figure 13: Modified circuit for figure 12

By further simplyfing we get,

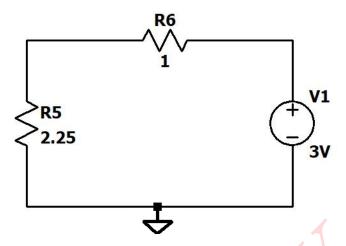


Figure 14: Modified circuit for figure 13

$$I_{ckt} = \frac{3}{3.25} = 0.9230$$
  
 $I_1 = 0.9230 \times \frac{3}{3+9}$   
 $I_1 = 0.2307A(\leftarrow)$ 

Step 2: When 9V source is acting alone,

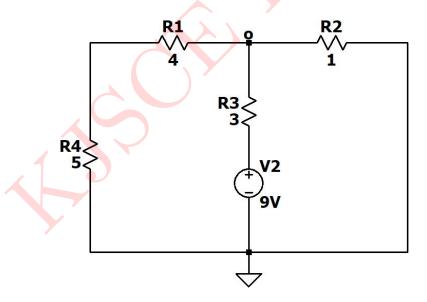


Figure 15: Modified circuit for figure 12

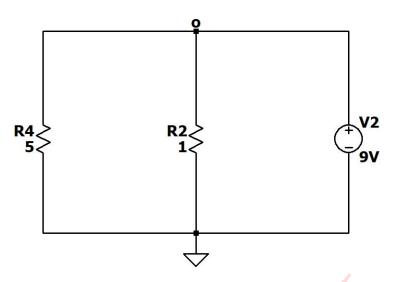


Figure 16: Modified circuit for figure 15

$$I_{ckt} = \frac{9}{3.9} = 2.3076A$$
  

$$\therefore I_2 = 2.3076 \times \frac{1}{1+9}$$

$$I_2 = 2.3076 \times \frac{1}{1+9}$$

$$\therefore I_2 = 0.23076A(\leftarrow)$$

By Superposition Theorem,

$$I : I = I_1 + I_2$$

$$I = 0.2307 + 0.2307$$

$$\therefore I = 0.4615A(\rightarrow)$$

$$\therefore V_0 - 0 = I \times R$$

$$V_0 = 0.4615 \times (4+5)$$

$$\therefore V_0 = \mathbf{4.1526V}$$

The above circuit is simulated in LTspice. The results are presented below.

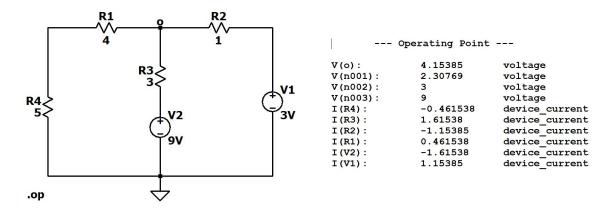


Figure 17: Circuit schematic and simulated results

Here,  $V_0 = 4.15385V$ 

Parameter	Theoretical value	Simulated values
$V_0$	4.1526V	4.1538V

Table 3: Numerical 3

# Numerical 4: Determine $V_0$ in circuit 4 using superposition principle.

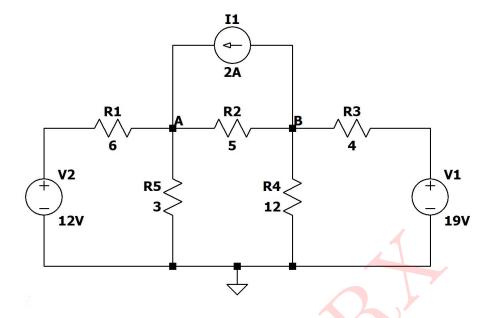


Figure 18: Circuit 4

## Solution:

Step 1: When 2A source is acting alone,

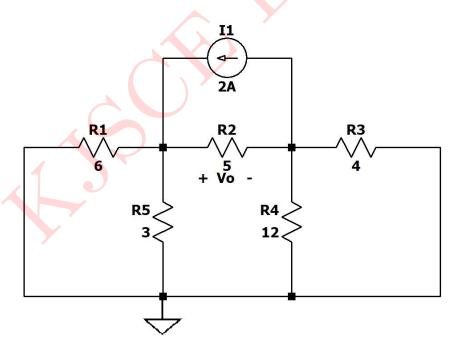


Figure 19: Modified circuit for figure 18

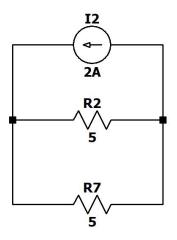


Figure 20: Modified circuit for figure 19

$$\therefore I_1 = 2 \times \frac{5}{10}$$
$$\therefore I_1 = 1A(\rightarrow)$$

$$I_1 = 1A(\rightarrow)$$

Step 2: When 12V source is acting alone,

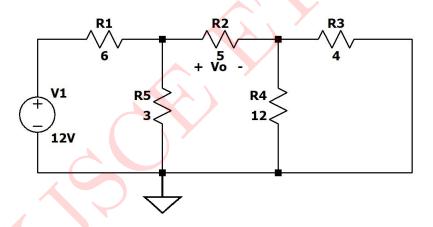


Figure 21: Modified circuit for figure 18

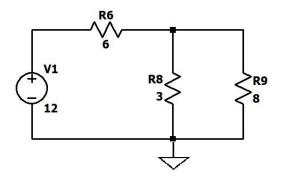


Figure 22: Modified circuit for figure 21

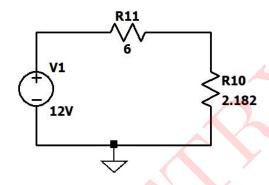


Figure 23: Modified circuit for figure 22

$$I_{ckt} = \frac{12}{6 + 2.182}$$

$$I_{12} = 1.467 \times \frac{3}{3 + 8}$$

$$I_{12} = 0.4A(\rightarrow)$$

Step 3: When 19V source is acting alone,

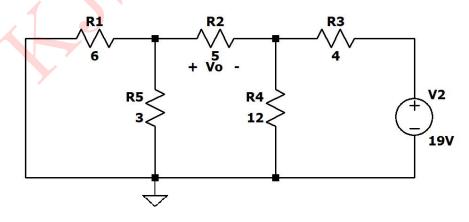


Figure 24: Modified circuit for figure 18

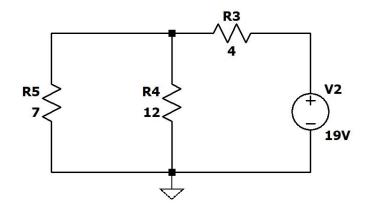


Figure 25: Modified circuit for figure 24

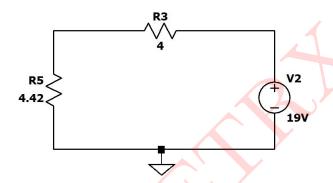


Figure 26: Modified circuit for figure 25

$$I_{ckt} = \frac{19}{8.42} = 2.256A$$
  
 $\therefore I_3 = 2.256 \times \frac{12}{7 + 12}$   
 $\therefore I_3 = 1.425A \leftarrow$   
 $\therefore I_3 = -1.425 \rightarrow$ 

By Superposition Theorem,

$$I_{5\Omega} = I_1 + I_2 + I_3$$

$$I_{5\Omega} = I_1 + I_2 + I_3$$
  
 $\therefore I_{5\Omega} = 1 + 0.4 - 1.425$   
 $\therefore I_{5\Omega} = -0.025(\rightarrow)$   
 $\therefore I_{5\Omega} = 0.025(\leftarrow)$ 

$$I_{50} = -0.025 \rightarrow$$

$$I_{50} = 0.025(\leftarrow)$$

$$V_0 = I_{5\Omega} \times R_{5\Omega}$$

$$\therefore V_0 = 0.025 \times 5$$

$$V_0 = 0.125V$$

The above circuit is simulated in LTspice. The results are presented below.

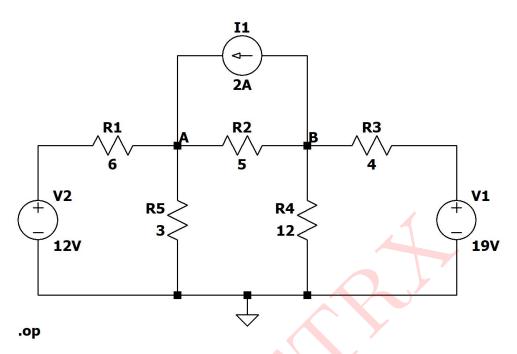


Figure 27: Circuit schematic

## --- Operating Point ---

V(a):	8.05	voltage
V(n001):	12	voltage
V(b):	8.175	voltage
V(n002):	19	voltage
I(I1):	2	device_current
I(R5):	-2.68333	device_current
I(R4):	-0.68125	device_current
I(R3):	2.70625	device_current
I(R2):	0.025	device_current
I(R1):	-0.658333	device_current
I(V2):	-0.658333	device_current
I(V1):	-2.70625	device current

Figure 28: Simulated results

Here,  $V_0 = V_B - V_A = 8.175 - 8.050$  $\therefore V_0 = \mathbf{0.125V}$ 

Parameter	Theoretical value	Simulated values
$V_0$	0.125V	0.125 V

Table 4: Numerical 4



**Numerical 5:** Use Thevenin's theorem to find current in the branch AB of the network shown in Figure 29. All resistances are in ohms.

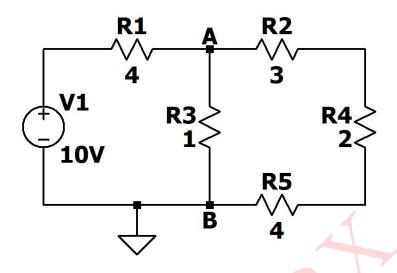


Figure 29: Circuit 5

## Solution:

Step 1: Finding  $R_{TH}$ ,

Here, we need to replace the voltage source by a short circuit as shown in figure 30.

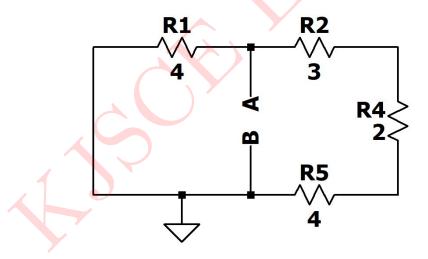


Figure 30: Modified circuit for figure 29 to find  $R_{TH}$ 

After simplifying the circuit we get,

 $R_{AB} = R_{TH} = 2.769\Omega$ 

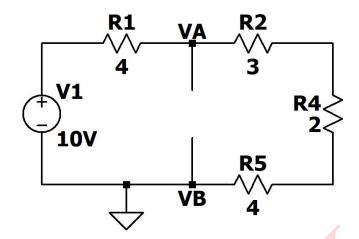


Figure 31: Modified circuit for figure 30 to find  $V_{TH}$ 

By using nodal analysis,

$$\therefore \frac{V_A - 10}{4} + \frac{V_A}{9} = 0$$

$$\therefore 13V_A - 90 = 0$$

$$\therefore V_{TH} = V_A = 6.9230V$$

Step 3: Thevenin's equivalent circuit,

The circuit consists of resistance  $R_{TH}$  and  $R_L$  in series with voltage source  $V_{TH}$  as shown in figure 32.

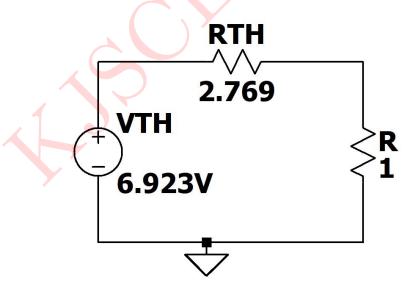


Figure 32: The venin's equivalent circuit

$$I_{1\Omega} = \frac{6.923}{2.769 + 1} = 1.8368A$$
  
 $I_{AB} = I_{1\Omega} = \mathbf{1.8368A}$ 

The above circuit is simulated in LTspice. The results are presented below.

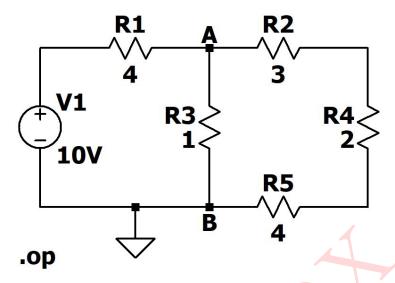


Figure 33: Circuit schematic

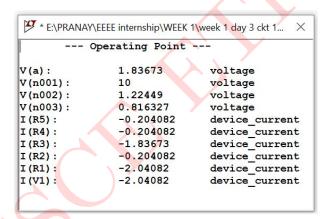


Figure 34: Simulated results

Here,  $I_{1\Omega} = I_{AB} = 1.83673 \text{A}$ 

Parameter	Theoretical value	Simulated values
$I_{1\Omega}$	1.8369A	1.83673A

Table 5: Numerical 5

**Numerical 6**: Find the current that would flow if  $2\Omega$  resistor was connected between A and B as shown in figure 35. All resistances are in ohms.

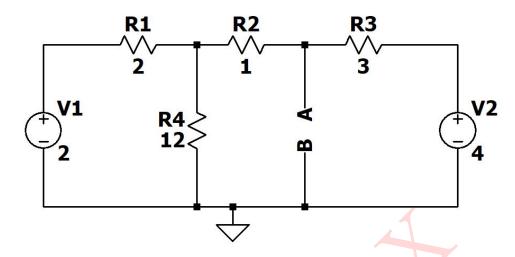


Figure 35: Circuit 6

## Solution:

Step 1: Find  $R_{TH}$  or  $R_{AB}$ ,

Here, we need to replace voltage source with short circuit as shown in figure 35.

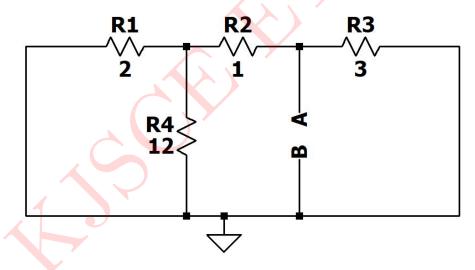


Figure 36: Modified circuit for figure 35 to find  $R_{TH}$ 

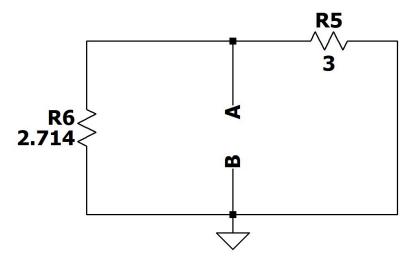


Figure 37: Modified circuit for figure 36 to find  $R_{TH}$ 

 $R_{AB} = R_{TH} = 1.425\Omega$ 

Step 2: Find  $V_{TH}$  or  $V_{AB}$ ,

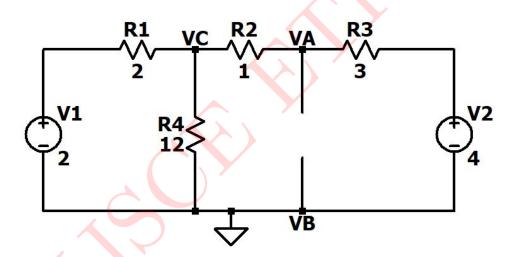


Figure 38: Modified circuit for figure 35 to find  $V_{TH}$ 

By Nodal analysis,

Considering node  $V_C$ ,

$$\therefore \frac{V_C - V_A}{1} + \frac{V_C - 2}{2} + \frac{V_C}{12} = 0$$

$$\therefore -12V_A + 19V_C = 12 \qquad \dots (1)$$

Considering node  $V_A$ ,

$$\therefore \frac{V_A - 4}{3} + \frac{V_A - V_C}{1} = 0$$

$$\therefore 4V_A - 3V_C = 4$$
.....(2)

After solving equation (1) and (2) we get,  $V_A = 2.8V$ 

Step 3: Thevenin's equivalent circuit,

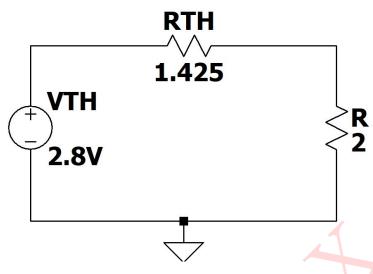


Figure 39: Thevenin's equivalent circuit

$$I_{AB} = \frac{2.8}{1.425 + 2} = 0.8175A$$
  
 $I_{Ab} = I_{2\Omega} = \mathbf{0.8175A}$ 

The above circuit is simulated in LTspice. The results are presented below.

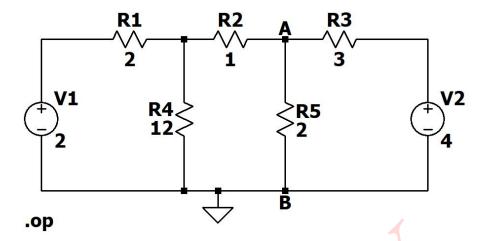


Figure 40: Circuit schematic

(	Operating Point	
V(n002):	1.66423	voltage
V(n001):	2	voltage
V(a):	1.63504	voltage
V(n003):	4	voltage
I(R5):	0.817518	device current
I(R4):	-0.138686	device current
I(R3):	0.788321	device current
I(R2):	-0.0291971	device current
I(R1):	-0.167883	device current
I(V2):	-0.788321	device current
I(V1):	-0.167883	device current

Figure 41: Simulated results

Here,  $I_{R5} = I_{AB} = \mathbf{0.8175A}$ 

Parameter	Theoretical value	Simulated values
$I_{AB}$	0.8175A	0.8175A

Table 6: Numerical 6

**Numerical 7:** Find the Thevenin and Norton equivalent circuits for the active network shown in Figure 42. All resistance are in ohms.

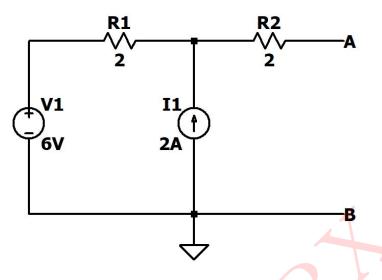


Figure 42: Circuit 7

# 1] For Thevenin's circuit:

Step 1: Finding  $V_{TH}$ ,

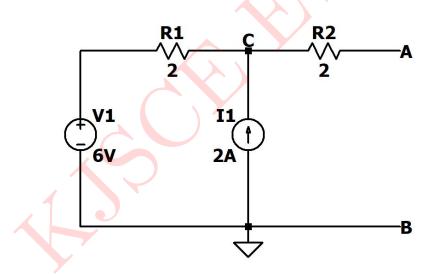


Figure 43: Modified circuit for figure 42 to find  $V_{TH}$ 

By nodal analysis, Considering node C,

$$\frac{V_C - V_A}{2} - 2 + \frac{V_C - 6}{2} = 0$$

$$\therefore 2V_C - V_A - 6 = 4$$

$$\therefore -V_A + 2V_C = 10$$
 ......(1)

Considering node A,

$$V_A - V_C = 0$$
 ......(2)

On solving (1) and (2) we get,

$$V_A = V_{TH} = \mathbf{10V}$$

## Step 2: Finding $R_{AB}$ ,

Here, we replace the voltage source by short circuit and current source by open circuit. Therefore the circuit gets reduced to figure 44.

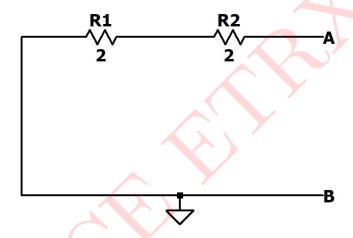


Figure 44: Modified circuit for figure 42 to find  $R_{TH}$ 

Here, we replace the voltage source by short circuit and current source by open circuit.  $R_{AB}=4\Omega$ 

## Step 3: Thevenin's equivalent circuit,

The circuit consists of  $R_{TH}$  in series with voltage source  $V_{TH}$  as shown in figure 45,

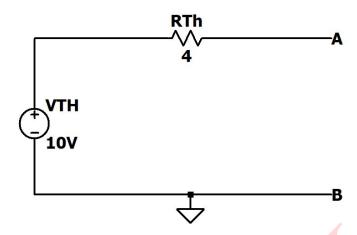


Figure 45: Thevenin's equivalent circuit

## 2] For Norton's circuit:

Step 1: Finding  $I_{SC}$ ,

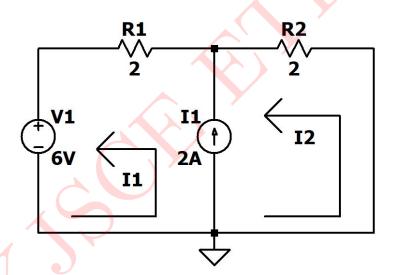


Figure 46: Modified circuit for figure 42 to find  $I_{SC}$ 

By supermesh,

Supermesh equation,

$$I_1 - I_2 = 2$$
 ......(3)

Applying mesh analysis to outer loop,

$$I_1 + I_2 = 3$$
 ......(4)

On solving equation (3) and (4) we get,

$$I_2 = I_{SC} = 2.5A$$

Step 2: Norton's equivalent circuit,

We know,

$$R_{th} = R_N = 4\Omega$$

The circuit consists of  $R_N$  in parallel with current source  $I_{SC}$  as shown in the figure 47,

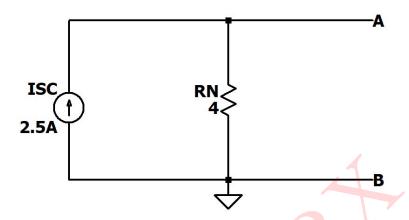


Figure 47: Norton's equivalent circuit

## SIMULATED RESULTS:

The above circuit is simulated in LTspice. The results are presented below.

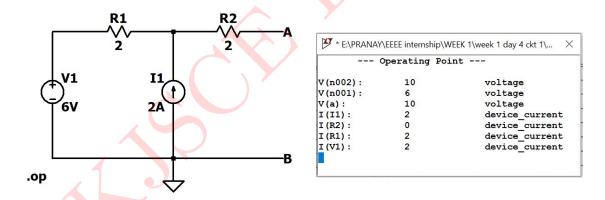


Figure 48: Circuit schematic and simulated results: To find  $V_{TH}$ 

Here, 
$$V_{TH} = V_A = 10V$$

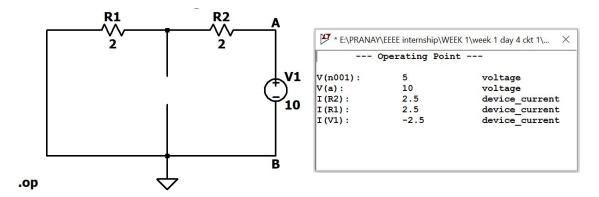


Figure 49: Circuit schematic and simulated results: To find  $R_{TH}$ 

Here,

$$R_{TH} = R_{AB} = \frac{V_A}{I_{V1}}$$

$$\therefore R_{TH} = R_{AB} = \frac{10}{2.5}$$

$$\therefore R_{TH} = R_{AB} = 4\Omega$$

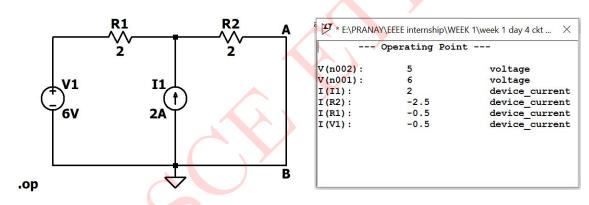


Figure 50: Circuit schematic and simulated results: To find  $I_{SC}$ 

Here,  $I_{SC} = I_{R2} = 2.5$ A

Parameter	Theoretical value	Simulated values
$V_{TH}$	10V	10V
$I_{SC}$	2.5A	2.5A
$R_{AB}$	$4\Omega$	$4\Omega$

Table 7: Numerical 7

Numerical 8: Determine current and voltage across  $3k\Omega$  resistor in Figure 51.

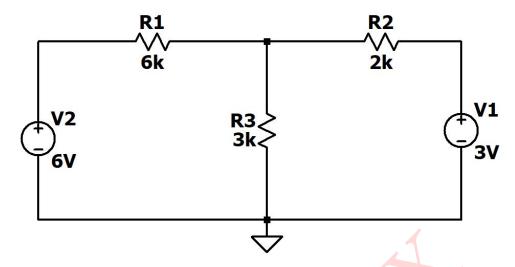


Figure 51: Circuit 8

Step 1: Finding  $I_{SC}$  or  $I_N$ ,

Here, we need to replace  $3k\Omega$  resistor with a short circuit.

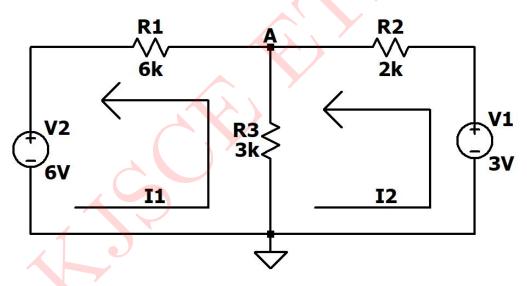


Figure 52: Modified circuit for figure 51 to find  $I_{SC}$ 

By applying mesh analysis we get,

$$-10^3 \times 6I_1 = 6$$

$$I_1 = -1 \times 10^{-3} = -1mA$$

$$-10^3 \times 2I_2 = 3$$

$$\therefore I_1 = 1.5mA$$

$$I_{SC} = I_2 - I_1$$

$$I_{SC} = 1.5 - (-1)$$

 $I_{SC} = 2.5mA$ 

## Step 2: Finding $R_{AB}$ or $R_N$ ,

Here, we need to replace both the voltage source with short circuit. As shown in the figure 53.

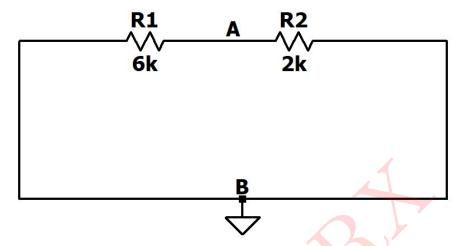


Figure 53: Modified circuit for figure 51 to find  $R_{TH}$ 

After solving we get,

$$R_{AB} = 6\Omega \mid\mid 2\Omega$$

$$\therefore R_{AB} = 1.5 \text{k}\Omega$$

## Step 3: Norton's equivalent circuit,

The circuit consists of  $R_N$  in parallel with current source  $I_{SC}$  as shown in the figure 54.

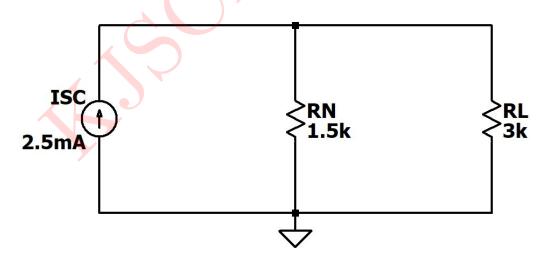


Figure 54: Norton's equivalent circuit

By using current division formula,

$$I_{3k\Omega} = 2.5 \times 10^{-3} \times \frac{1.5 \times 10^{3}}{(1.5+3) \times 10^{3}}$$
  
 $\therefore I_{3k\Omega} = \mathbf{0.8333mA}$   
 $V_{3k\Omega} = I \times R = 0.8333 \times 10^{-3} \times 3 \times 10^{3}$ 

$$\therefore V_{3k\Omega} = 2.5\mathbf{V}$$

#### SIMULATED RESULTS:

The above circuit is simulated in LTspice. The results are presented below. Here,

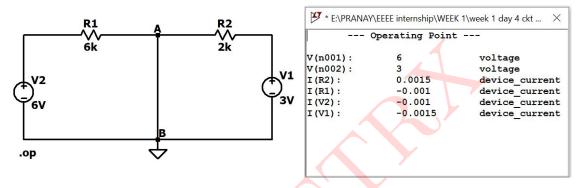


Figure 55: Circuit schematic and simulated results: To find  $V_{TH}$ 

$$I_{SC} = I_{AB} = I_{R2} - I_{R1}$$
  

$$\therefore I_{SC} = I_{AB} = 0.0015 - (-0.001)$$
  

$$\therefore I_{SC} = I_{AB} = 0.0025 = 2.5 mA$$

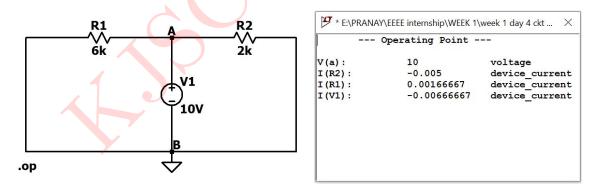


Figure 56: Circuit schematic and simulated results: To find  $R_{TH}$ 

Here,
$$R_N = R_{AB} = \frac{V1}{I_{V1}}$$
 $\therefore R_N = R_{AB} = \frac{10}{0.006667}$ 
 $\therefore R_N = R_{AB} = 1.5k\Omega$ 

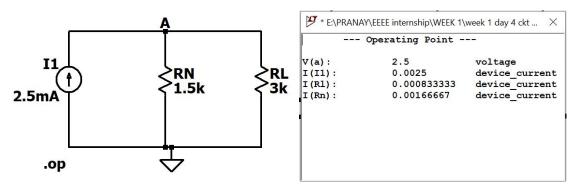


Figure 57: Circuit schematic and simulated results: To find  $I_{SC}$ 

Here,  $V_A = V_{3\Omega} = \mathbf{2.5V}$   $I_{RL} = I_{3\Omega} = \mathbf{0.8333mA}$ 

Parameter	Theoretical value	Simulated values
$I_{3k\Omega}$	$0.8333 \mathrm{mA}$	0.8333 mA
$V_{3k\Omega}$	2.5V	2.5V

Table 8: Numerical 8

**Numerical 9:** Find the value of  $R_L$  for maximum power transfer in the Figure 58. Find the maximum power.

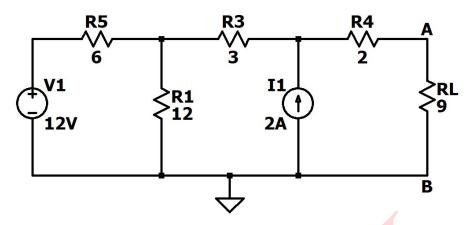


Figure 58: Circuit 9

## Solution:

Step 1: Finding  $R_{TH}$ ,

Here, we need to replace the voltage source by a short circuit and current source by open circuit as shown in figure 59.

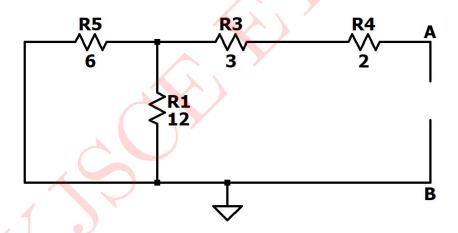


Figure 59: Modified circuit for figure 58 to find  $R_{TH}$ 

After simplifying the circuit we get,

$$R_{AB} = R_{TH} = 6||12 + 3 + 2$$

$$R_{AB} = R_{TH} = 4 + 5$$

$$R_{AB} = R_{TH} = 9\Omega$$

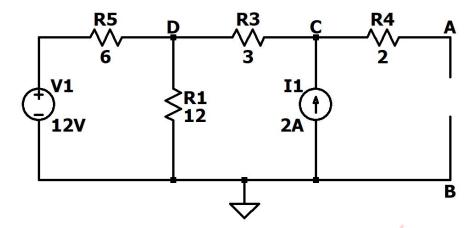


Figure 60: Modified circuit for figure 58 to find  $V_{TH}$ 

By using nodal analysis,

Considering node A,

$$\therefore \frac{V_A - V_C}{2} = 0$$

$$\therefore V_A - V_C = 0$$
.....(1)

Considering node C,

$$\therefore \frac{V_C - V_A}{2} + \frac{V_C - V_D}{3} = 2$$

$$\therefore -3V_A + 5V_C - 2V_D = 12$$
......(2)

Considering node D,

$$\therefore \frac{V_D - 12}{6} + \frac{V_D}{12} + \frac{V_D - V_C}{3} = 0$$

$$\therefore -4V_C + 7V_D = 0$$
......(3)

On solving equations (1),(2) and (3) we get,

$$V_A = 22V$$

For maximum power transfer,

$$R_L = R_{TH} = 9\Omega$$

Maximum power,

$$P_{max} = \frac{(V_{TH})^2}{4R_L}$$
$$P_{max} = \frac{(22)^2}{4 \times 9}$$

 $P_{max} = 13.44$ W

The above circuit is simulated in LTspice. The results are presented below.

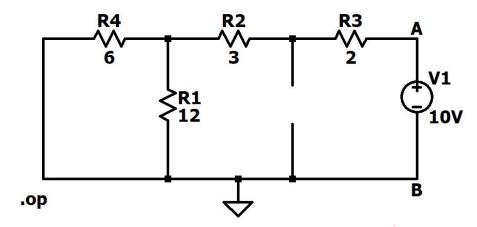


Figure 61: Circuit schematic for finding  $R_{TH}$ 

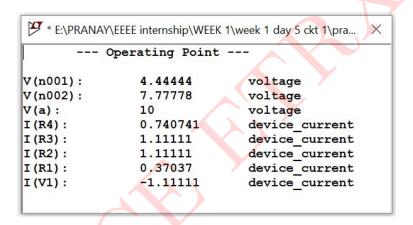


Figure 62: Simulated results for finding  $R_{TH}$ 

Here, 
$$I_{V_1} = 1.111A$$
 
$$R_{AB} = \frac{V_1}{I_{V_1}} = \frac{10}{1.111}$$
 
$$R_{AB} = R_{TH} = 9.00\Omega$$

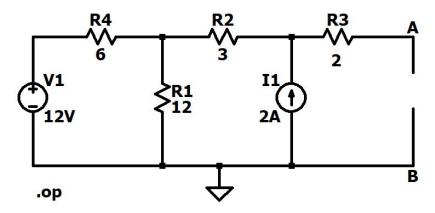


Figure 63: Circuit schematic for finding  $V_{TH}$ 

(	Operating Point	
V(n002):	16	voltage
V(n003):	22	voltage
V(a):	22	voltage
V(n001):	12	voltage
I(I1):	2	device current
I(R4):	0.666667	device current
I(R3):	0	device current
I(R2):	2	device current
I(R1):	1.33333	device current
I(V1):	0.666667	device current

Figure 64: Simulated results for finding  $V_{TH}$ 

Here,  $V_{TH} = V_{AB} = 22V$ 

For maximum power transfer,

$$R_L = R_{TH} = 9\Omega$$

Maximum power,

$$P_{max} = \frac{(V_{TH})^2}{4R_L}$$
$$P_{max} = \frac{(22)^2}{4 \times 9}$$

$$P_{max} = \frac{(22)^2}{4 \times 9}$$

$$P_{max} = 13.44$$
W

Parameter	Theoretical value	Simulated values
$R_L$	$9\Omega$	$9\Omega$
$P_{max}$	13.44W	13.44W

Table 9: Numerical 9

Numerical 10: Consider the bridge circuit. Is the bridge balanced? If the  $10k\Omega$  resistance is replaced by an  $18k\Omega$  resistor, what resistor connected between A-B absorbs the maximum power? What is the power?

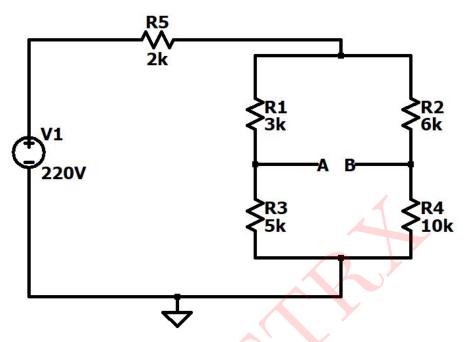


Figure 65: Circuit 10

#### Solution:

Part 1: To find whether the bridge is balanced or not.

$$\therefore \frac{R_1}{R_2} = \frac{3 \times 10^3}{5 \times 10^3} = 0.6$$

$$\therefore \frac{R_3}{R_4} = \frac{6 \times 10^3}{10 \times 10^3} = 0.6$$

$$\therefore \frac{R_1}{R_2} = \frac{R_3}{R_4}$$

Since the ratio of resistances is equal the bridge is balanced.

Part 2: Solving futher by replacing  $10k\Omega$  resistor with  $18k\Omega$  resistor.

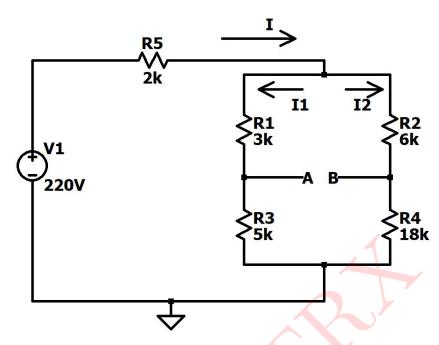


Figure 66: Modified circuit for figure 65 to solve part 2

Step 1: Find  $V_{TH}$  or  $V_{AB}$ ,

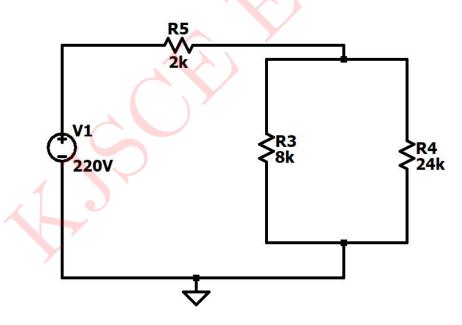


Figure 67: Modified circuit for figure 66 to find  $V_{TH}$ 

$$I = \frac{200}{8 \times 10^3}$$

$$I = 27.5mA$$

$$I_2 = 27.5 \times \frac{8}{8 + 24} = 6.875mA$$

$$I_1 = 27.5 \times \frac{24}{8 + 24} = 20.625mA$$

Writing  $V_{TH}$  equation,

 $V_{TH} - 3 \times 20.625 + 6 \times 6.875 = 0$ 

 $V_{TH} = V_{AB} = 20.625V$ 

# Step 2: Find $R_{TH}$ or $R_{AB}$ ,

Here, we need to replace voltage source with short circuit as shown in figure 68.

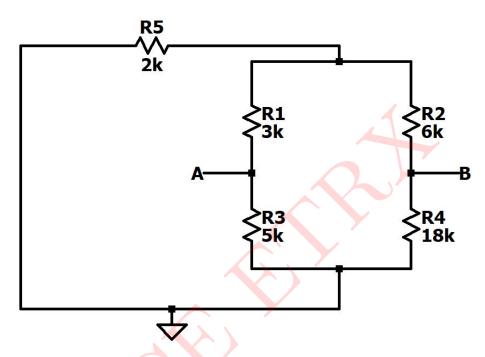


Figure 68: Modified circuit for figure 65 to find  $R_{TH}$ 

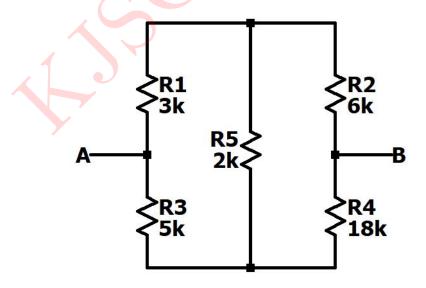


Figure 69: Modified circuit for figure 68 to find  $R_{TH}$ 

Using delta to star conversion,

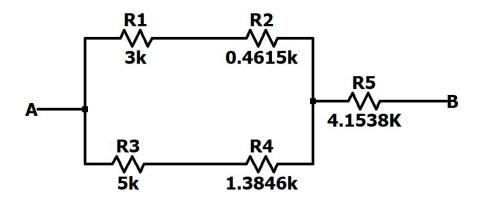


Figure 70: Modified circuit for figure 69 to find  $R_{TH}$ 

After simplifing we get,

$$R_{TH} = 6.3846k\Omega$$

For maximum power transfer,

$$R_{AB} = R_{Th} = 6.3846k\Omega$$

Maximum power,

$$P_{max} = \frac{(V_{TH})^2}{4R_L}$$

$$P_{max} = \frac{(20.625)^2}{4 \times 6.346 \times 10^3}$$

$$P_{max} = 16.656 \text{mW}$$

The above circuit is simulated in LTspice. The results are presented below.

Part 1: To find whether the bridge is balanced or not.

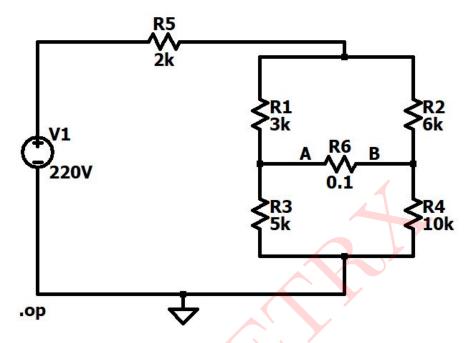


Figure 71: Circuit schematic

(	Operating Poin	t
V(n002):	160	voltage
V(a):	100	voltage
V(b):	100	voltage
V(n001):	220	voltage
I (R6):	0	device current
I (R5):	-0.03	device current
I (R4):	0.01	device current
I (R3):	0.02	device current
I(R2):	0.01	device current
I(R1):	0.02	device current
I(V1):	-0.03	device current

Figure 72: Simulated results

Since, current in the branch AB is zero the circuit forms a Wheatstone's bridge. Hence the bridge is balanced.

Part 2: Solving futher by replacing  $10k\Omega$  resistor with  $18k\Omega$  resistor.

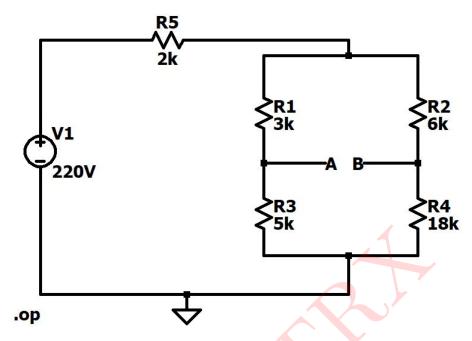


Figure 73: Circuit schematic for finding  $V_{TH}$ 

(	Operating Point	<del></del>
V(n002):	165	voltage
V(a):	103.125	voltage
V(b):	123.75	voltage
V(n001):	220	voltage
I(R5):	-0.0275	device current
I(R4):	0.006875	device current
I(R3):	0.020625	device current
I (R2):	0.006875	device current
I(R1):	0.020625	device current
I(V1):	-0.0275	device current

Figure 74: Simulated results for finding  $V_{TH}$ 

Here,

 $V_A = 103.125V$ 

 $V_B = 123.75V$ 

 $\therefore V_{TH} = V_{BA} = V_B - V_A$ 

 $\therefore V_{TH} = V_{BA} = 123.75 - 103.125$ 

 $V_{TH} = V_{BA} = 20.625V$ 

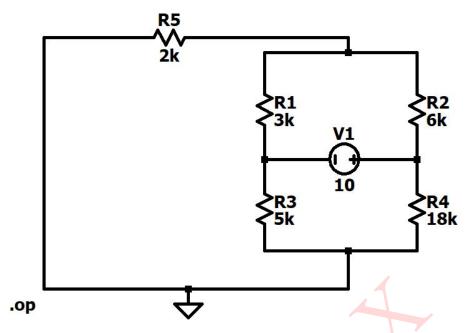


Figure 75: Circuit schematic for finding  $R_{TH}$ 

c	perating Point -	-
V(n001):	0.29304	voltage
V(n002):	-2.74725	voltage
V(n003):	7.25275	voltage
I(R5):	0.00014652	device current
I(R4):	0.00040293	device current
I(R3):	-0.000549451	device current
I(R2):	-0.00115995	device current
I(R1):	0.00101343	device current
I (V1):	-0.00156288	device_current

Figure 76: Simulated results for finding  $R_{TH}$ 

Here,

$$I_{V_{e}} = 0.00156288A$$

$$I_{V_1} = 0.00156288A$$

$$R_{AB} = R_{TH} = \frac{V_1}{I_{V_1}}$$

$$R_{AB} = R_{TH} = \frac{10}{0.00156288}$$

$$R_{AB} = R_{TH} = 6.39844\Omega$$

For maximum power transfer,

$$R_{AB} = R_{Th} = 6.3846k\Omega$$

Maximum power,

$$P_{max} = \frac{(V_{TH})^2}{4R_L}$$
 
$$P_{max} = \frac{(20.625)^2}{4 \times 6.346 \times 10^3}$$
 
$$P_{max} = \mathbf{16.656mW}$$

Parameter	Theoretical value	Simulated values
$R_{AB}$	$6.3846\Omega$	$6.3844\Omega$
$P_{max}$	16.656 mW	$16.657 \mathrm{mW}$

Table 10: Numerical 10