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DEPARTMENT OF ELECTRONICS ENGINEERING
ELECTRONIC CIRCUITS
DC CIRCUITS

Numerical 1: Find voltage across $35\ \Omega$ resistance. Solve analytically using mesh analysis

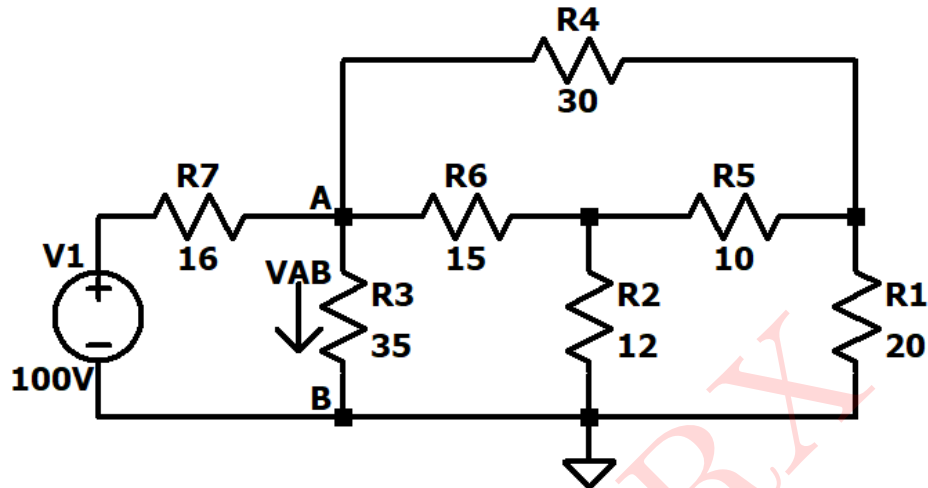


Figure 1: Circuit 1

Solution:

Applying KVL to mesh 1:

$$100 - (16 + 35)I_1 + 35I_2 = 0$$

$$100 - 51I_1 + 35I_2 = 0$$

$$51I_1 - 35I_2 = 100 \quad \dots\dots\dots(1)$$

Applying KVL to mesh 2:

$$35I_1 - (35 + 15 + 12)I_2 + 12I_3 + 15I_4 = 0$$

$$35I_1 - 62I_2 + 12I_3 + 15I_4 = 0 \quad \dots\dots\dots(2)$$

Applying KVL to mesh 3:

$$12I_2 - (12 + 20 + 10)I_3 + 10I_4 = 0$$

$$12I_2 - 42I_3 + 10I_4 = 0 \quad \dots\dots\dots(3)$$

Applying KVL to mesh 4:

$$15I_2 + 10I_3 - (15 + 10 + 30)I_4 = 0$$

$$15I_2 + 10I_3 - 55I_4 = 0 \quad \dots\dots\dots(4)$$

Solving equation (1), (2), (3) and (4) simultaneously, we get

$$I_1 = 3.6138\text{A}$$

$$I_2 = 2.4086\text{A}$$

$$I_3 = 0.8828\text{A}$$

$$I_4 = 0.8174\text{A}$$

$$V_{AB} = (3.6138 - 2.4086) \times 35$$

$$V_{AB} = 42.182\text{V}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

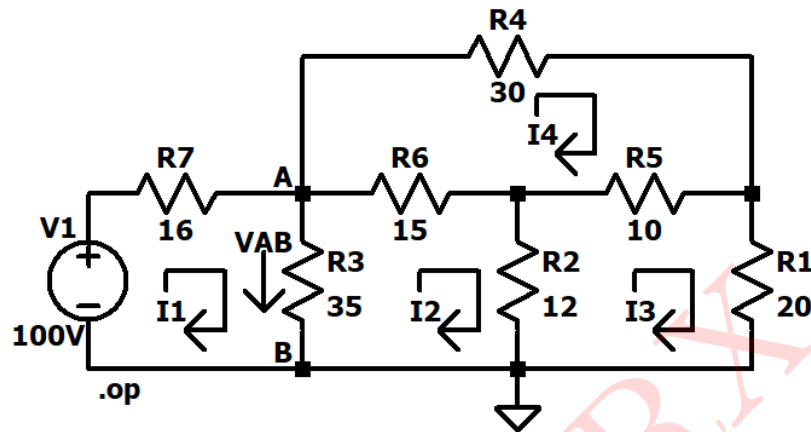


Figure 2: Circuit Schematic

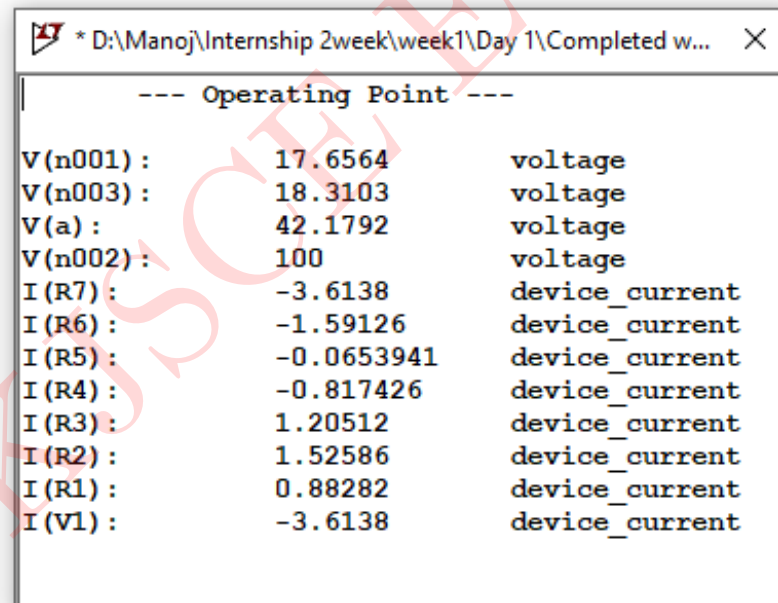


Figure 3: Simulated Results

Comparison of Theoretical and Simulated Values:-

Parameters	Theoretical Values	Simulated Values
V_{AB}	42.182V	42.1792V

Table 1: Numerical 1

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Numerical 2: Find equivalent resistance at terminals

a) a – b

b) c – d

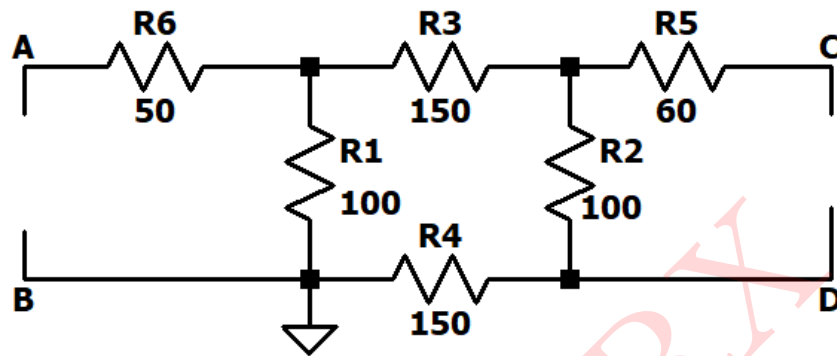


Figure 4: Circuit 2

Solution:

a) a – b

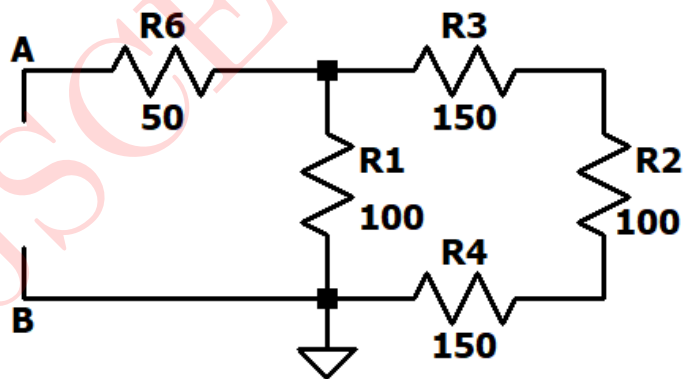


Figure 5: Equivalent circuit for a – b section

$$\begin{aligned}
 R_{AB} &= 50 + \frac{100 \times 400}{100 + 400} \\
 &= 50 + \frac{4 \times 10^4}{500} \\
 &= 50 + \frac{400}{5} \\
 &= 50 + 80 \\
 \therefore R_{AB} &= 130 \, \Omega
 \end{aligned}$$

b) c – d

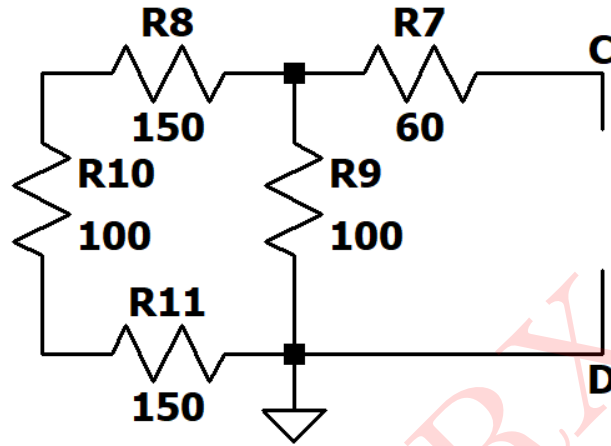


Figure 6: Equivalent circuit for c – d section

$$\begin{aligned}
 R_{CD} &= 60 + \frac{100 \times 400}{100 + 400} \\
 &= 60 + \frac{4 \times 10^4}{500} \\
 &= 60 + \frac{400}{5} \\
 &= 60 + 80 \\
 \therefore R_{CD} &= 140 \, \Omega
 \end{aligned}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

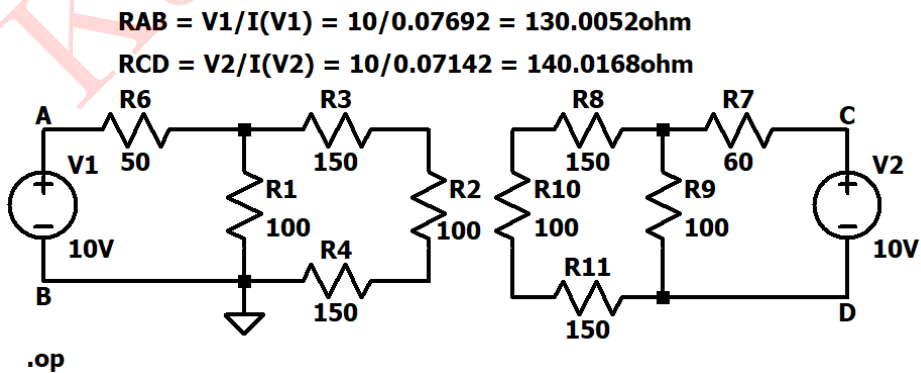


Figure 7: Circuit Schematic

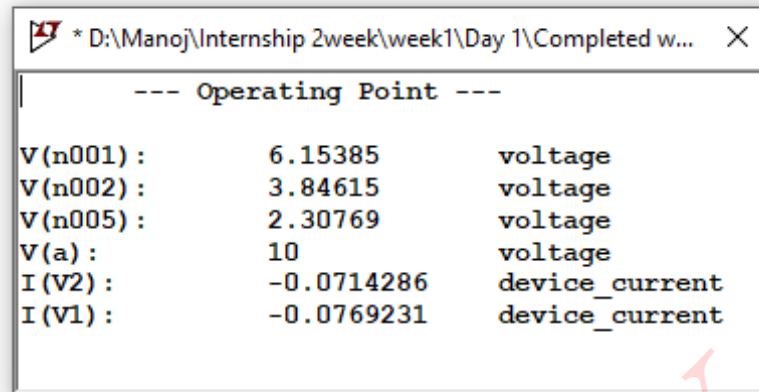


Figure 8: Simulated Results

Comparison of Theoretical and Simulated Values:-

Parameters	Theoretical Values	Simulated Values
R_{AB}	130 Ω	130.0052 Ω
R_{CD}	140 Ω	140.0168 Ω

Table 2: Numerical 2

Numerical 3: Find current in 2Ω resistor by using Thevenin's Theorem.

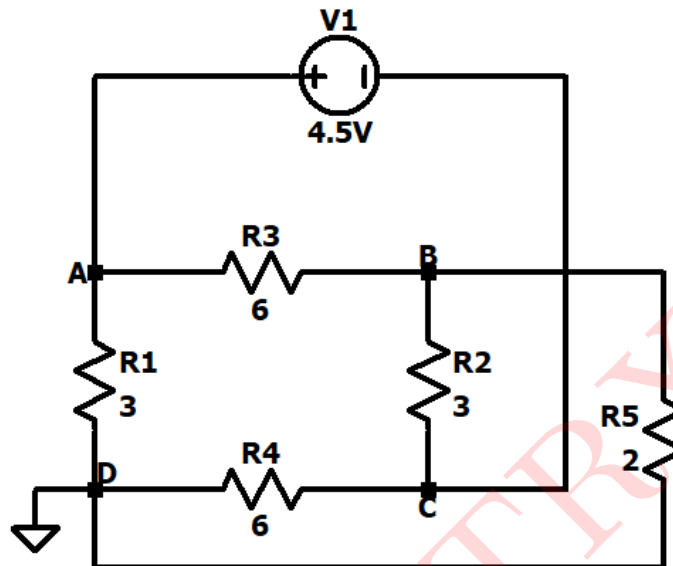


Figure 9: Circuit 3

Solution:

1) Calculation of V_{TH} :-

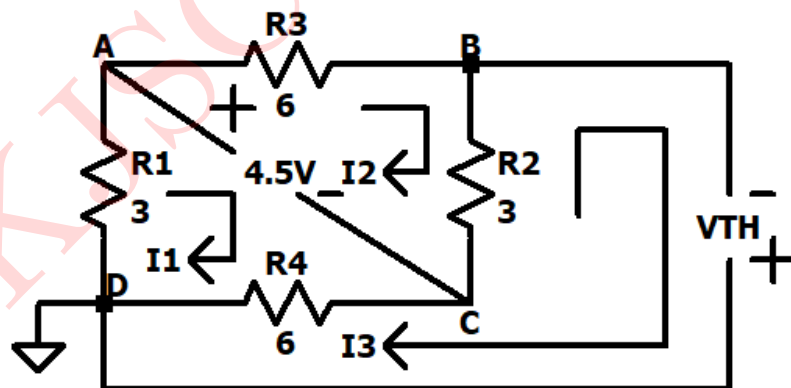


Figure 10: Circuit for V_{TH}

Applying KVL to mesh 1:

$$-6I_1 - 3I_1 - 4.5 = 0$$

$$-9I_1 = 4.5$$

$$I_1 = \frac{-4.5}{9}$$

$$I_1 = -0.5A \quad \text{.....(1)}$$

Applying KVL to mesh 2:

$$-6I_2 - 3I_2 + 4.5 = 0$$

$$9I_2 = 4.5$$

$$I_2 = \frac{4.5}{9}$$

$$I_2 = 0.5\text{A} \quad \dots\dots\dots(2)$$

Applying KVL to mesh 3:

$$V_{TH} = 6I_1 + 3I_2$$

$$= 6 \times (-0.5) + 3 \times 0.5 \quad \dots\dots\dots\text{From (1) and (2)}$$

$$= -1.5\text{V}$$

2) Calculation of R_{TH} :-

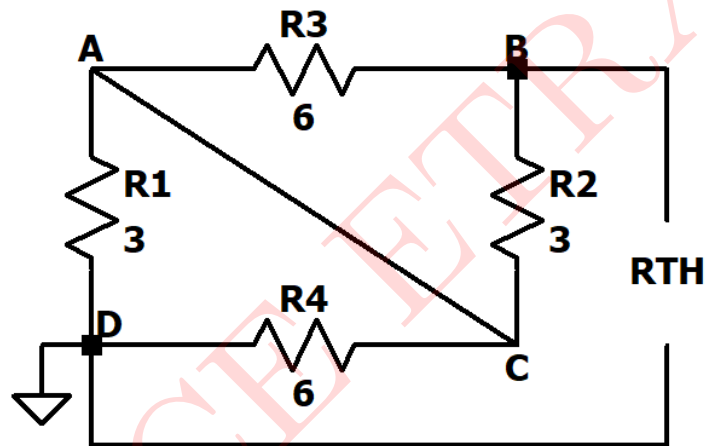


Figure 11: Circuit for R_{TH}

From the above circuit 3Ω and 6Ω are parallel with each other in loop ADC and ABC

$$\therefore R_{TH} = \frac{3 \times 6}{3 + 6} + \frac{3 \times 6}{3 + 6}$$

$$= \frac{6}{3} + \frac{6}{3}$$

$$= 2 + 2$$

$$\therefore R_{TH} = 4\Omega$$

3) Calculation of load current :-

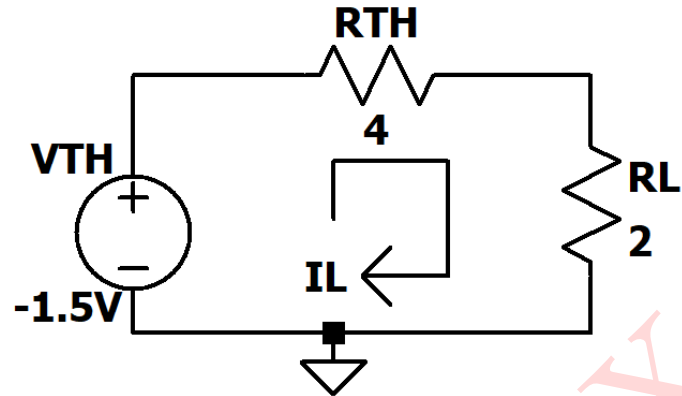


Figure 12: Thevenin's equivalent circuit

Applying KVL to mesh 1:

$$-6I_L - 1.5 = 0$$

$$\therefore I_L = -0.25\text{A}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

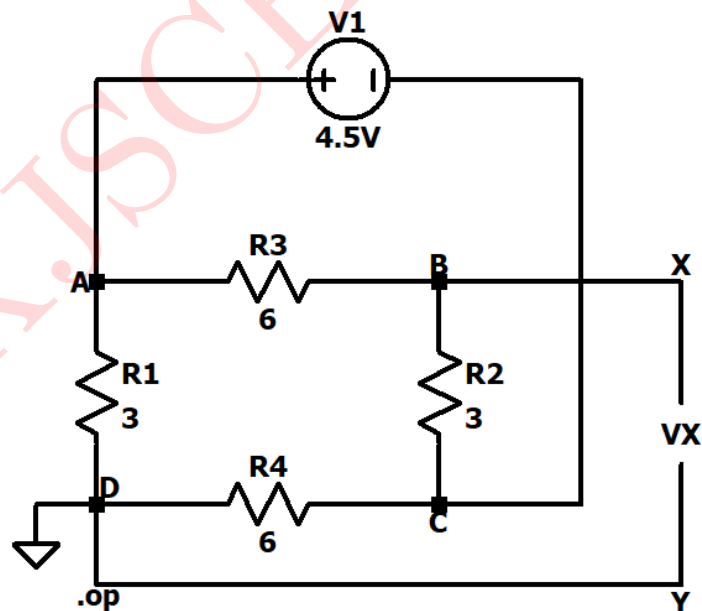


Figure 13: Circuit Schematic for V_{TH}

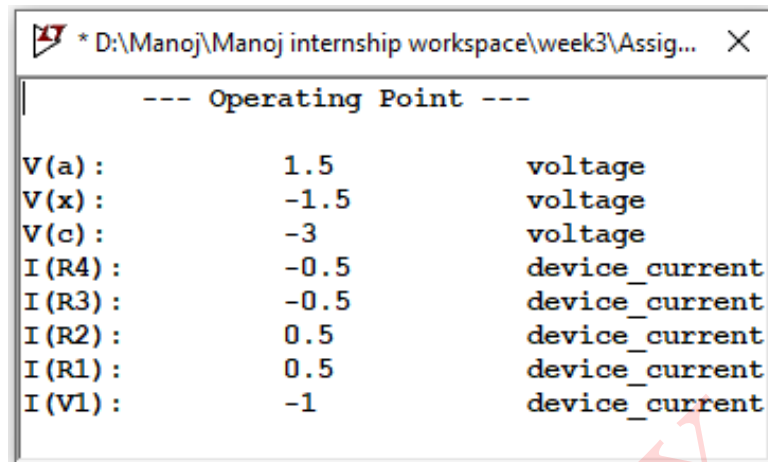


Figure 14: Simulated Results for V_{TH}

$$\mathbf{R_{XY} = R_{TH} = V1/I(V1) = 10/2.5 = 4ohms}$$

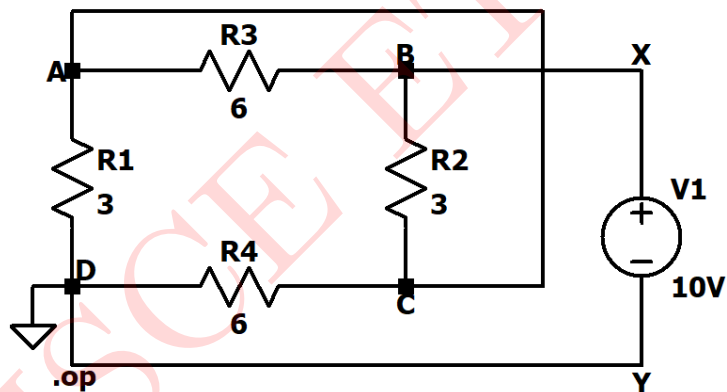


Figure 15: Circuit Schematic for R_{TH}

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--- Operating Point ---		
V(c) :	5	voltage
V(x) :	10	voltage
I(R4) :	0.833333	device_current
I(R3) :	0.833333	device_current
I(R2) :	1.66667	device_current
I(R1) :	1.66667	device_current
I(V1) :	-2.5	device_current

Figure 16: Simulated Results for R_{TH}

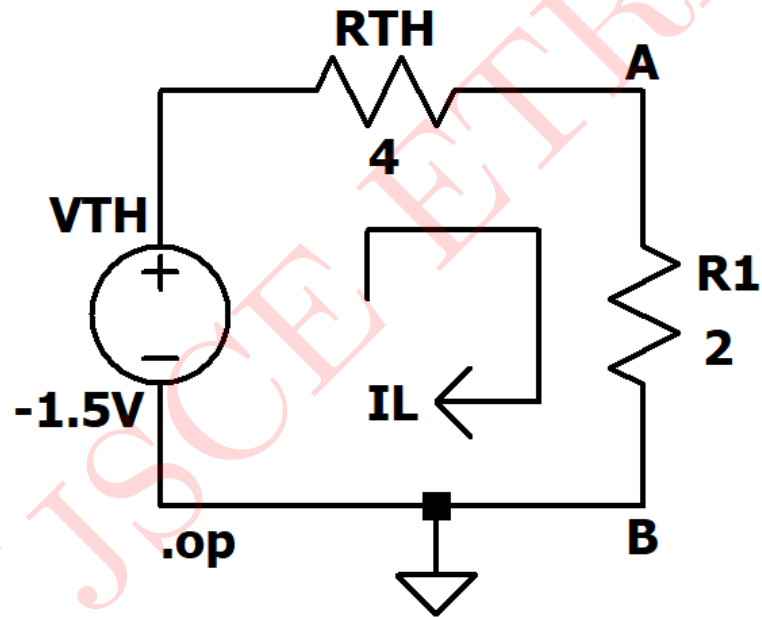


Figure 17: Circuit Schematic for I_L

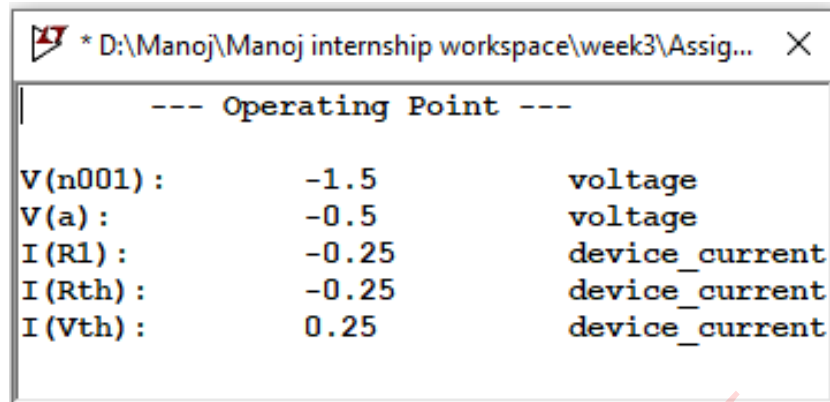


Figure 18: Simulated Results for I_L

Comparison of Theoretical and Simulated Values:-

Parameters	Theoretical Values	Simulated Values
V_{TH}	$-1.5V$	$-1.5V$
R_{TH}	4Ω	4Ω
I_L	$-0.25A$	$-0.25A$

Table 3: Numerical 3

Numerical 4: Find current in 5Ω resistor by using Thevenin's Theorem.

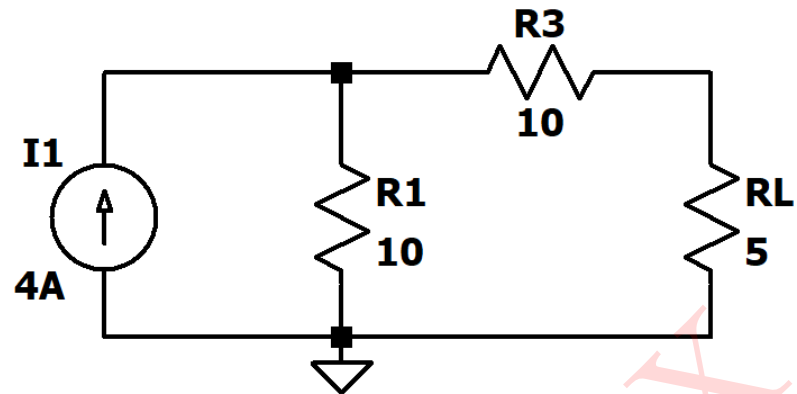


Figure 19: Circuit 4

Solution:

1) Calculation of V_{TH} :-

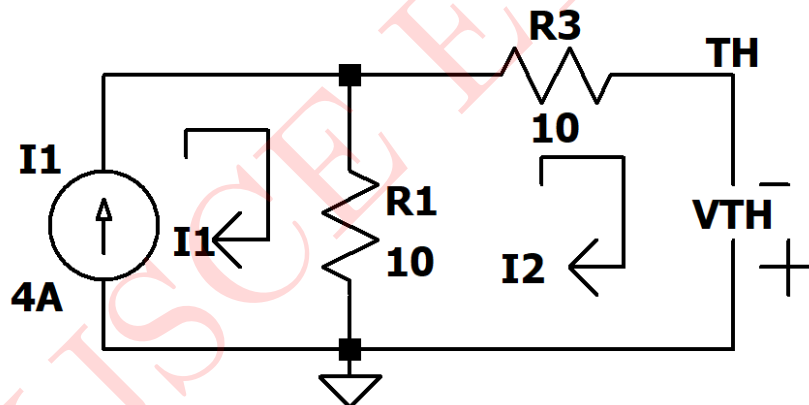


Figure 20: Circuit for V_{TH}

4A current source is in uncommon branch

$$\therefore I_1 = 4A$$

Applying KVL to mesh 2:

$$V_{TH} = 10 \times I_1 + 10 \times 0$$

$$\therefore V_{TH} = 40V$$

2) Calculation of R_{TH} :-

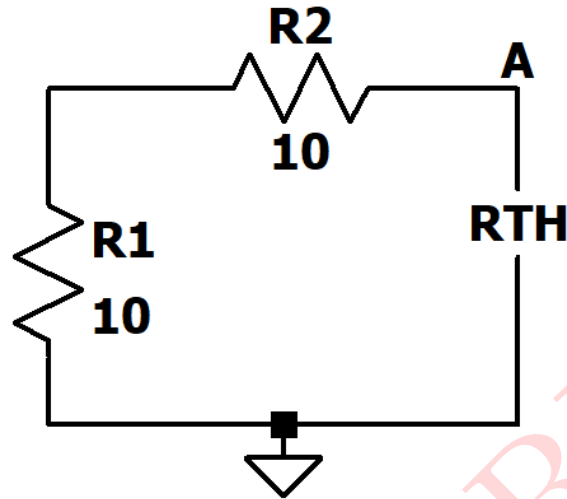


Figure 21: Circuit for R_{TH}

R_1 and R_2 are series with each other

$$\therefore R_{TH} = 10 + 10$$

$$R_{TH} = 20\Omega$$

3) Calculation of load current :-

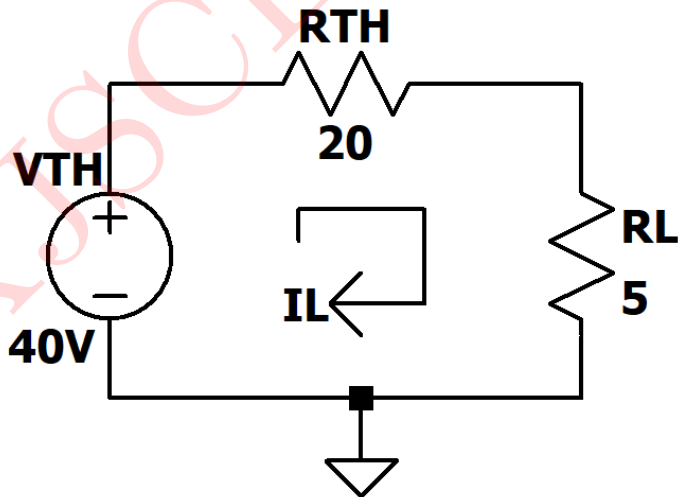


Figure 22: Thevenin's equivalent circuit

Applying KVL to mesh 1:

$$40 - 20I_L - 5I_L = 0$$

$$40 - 25I_L = 0$$

$$I_L = \frac{40}{25}$$

$$\therefore I_L = 1.6A$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

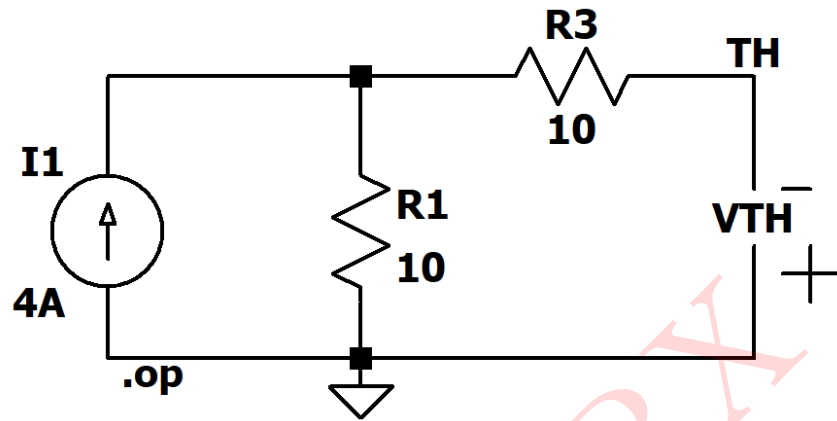


Figure 23: Circuit Schematic for V_{TH}

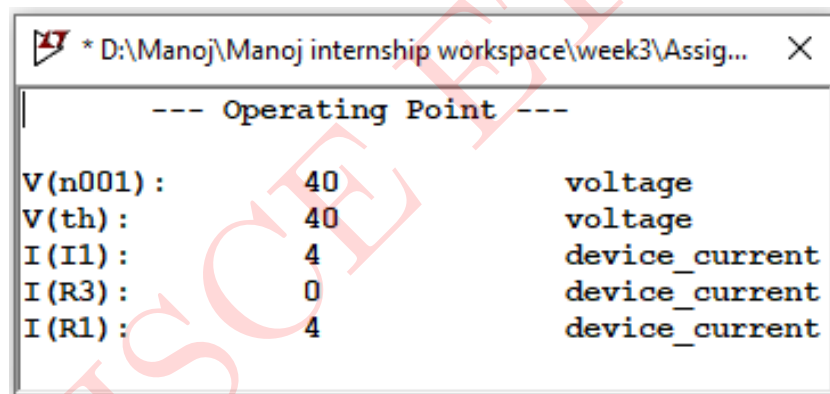
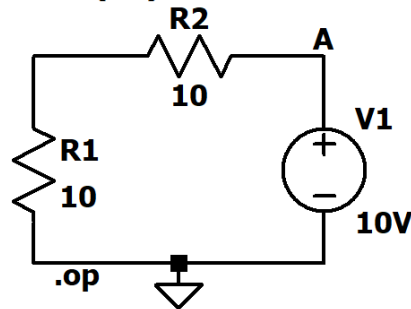


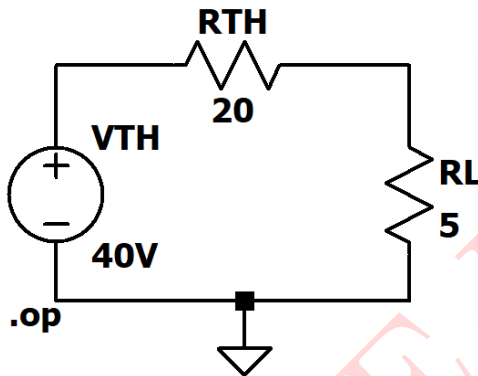
Figure 24: Simulated Results for V_{TH}

$$R_{TH} = V_1/I(R_1) = 10/0.5 = 20\text{ohms}$$



--- Operating Point ---		
V(n001):	5	voltage
V(a):	10	voltage
I(R2):	0.5	device_current
I(R1):	0.5	device_current
I(V1):	-0.5	device_current

Figure 25: Circuit Schematic and Simulated Results for R_{TH}



--- Operating Point ---		
V(n001):	40	voltage
V(n002):	8	voltage
I(R1):	1.6	device_current
I(Rth):	1.6	device_current
I(Vth):	-1.6	device_current

Figure 26: Circuit Schematic and Simulated Results for I_L

Comparison of Theoretical and Simulated Values:-

Parameters	Theoretical Values	Simulated Values
V_{TH}	40V	40V
R_{TH}	20Ω	20Ω
I_L	1.6A	1.6A

Table 4: Numerical 4

Numerical 5: For the circuit shown in figure 27, find the value of R_L for the maximum power transefer and also find maximum power P_{Max}

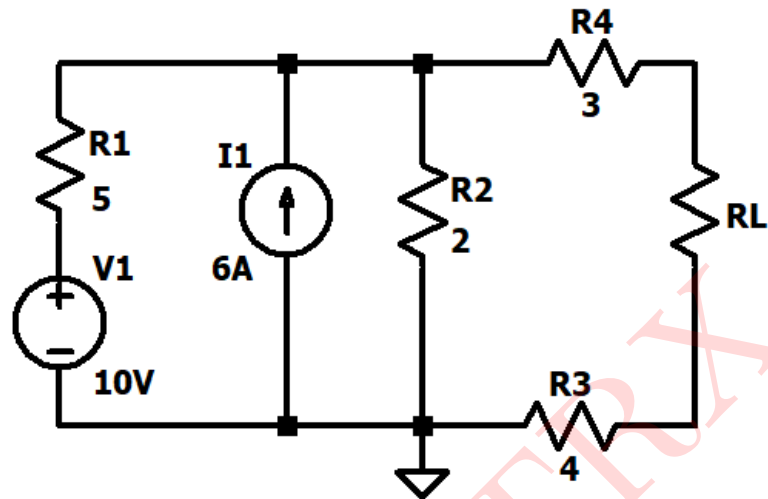


Figure 27: Circuit 5

Solution:

1) Calculation of V_{TH} :-

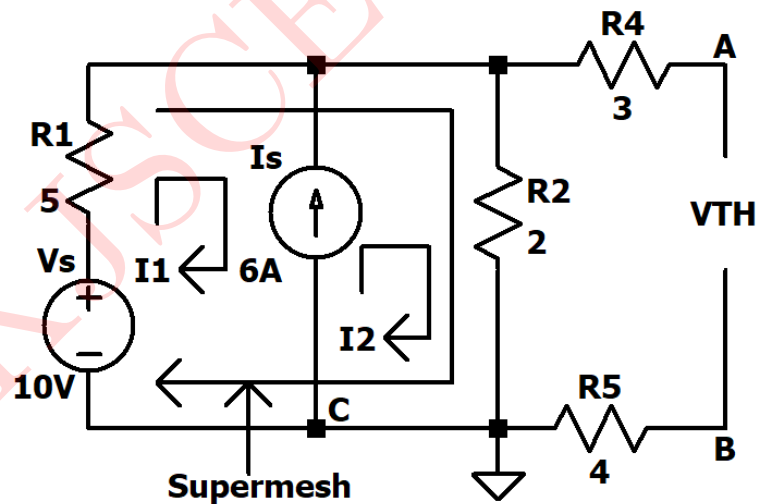


Figure 28: Circuit for V_{TH}

6A current source is in common branch

By applying KCL to node C, we get

$$I_1 + 6 = I_2$$

$$-I_1 + I_2 = 6 \quad \dots\dots\dots(1)$$

Applying KVL to supermesh:

$$10 - 5I_1 - 2I_2 = 0$$

$$5I_1 + 2I_2 = 10 \quad \dots\dots\dots(2)$$

Solving equation (1) and (2) simultaneously

$$I_1 = -0.2857\text{A and } I_2 = 5.7142\text{A}$$

$$\begin{aligned}
 \therefore V_{TH} &= 2I_2 \\
 &= 2 \times 5.7142 \\
 &= 11.4284\text{V}
 \end{aligned}$$

2) Calculation of R_{TH} :-

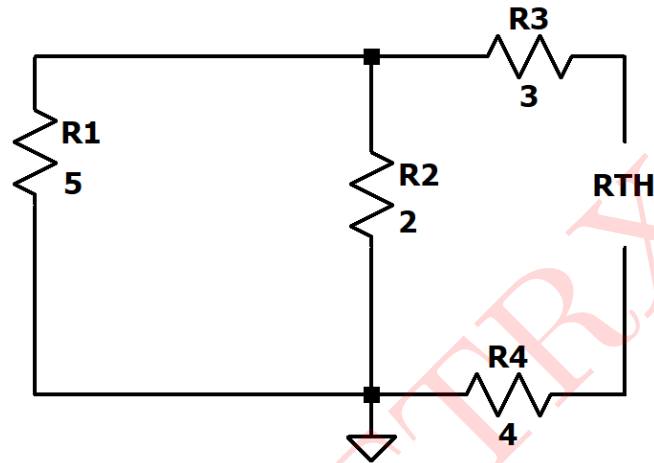


Figure 29: Circuit for R_{TH}

R_1 and R_2 resistor are parallel with each other and series with R_3 and R_4

$$\therefore R_{TH} = \frac{5 \times 2}{5 + 2} + 3 + 4$$

$$R_{TH} = \frac{10}{7} + 3 + 4$$

$$R_{TH} = 1.4285 + 3 + 4$$

$$\therefore R_{TH} = 8.4285\Omega$$

3) Calculation of load current :-

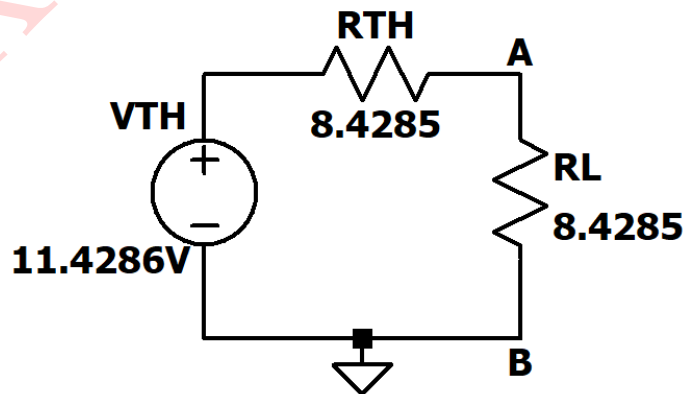


Figure 30: Thevenin's equivalent circuit

For Maximum Power:

$$R_L = R_{TH} = 8.4285\Omega$$

By Maximum Power Transfer Theorem

$$\begin{aligned}
 \therefore P_{Max} &= \frac{V_{TH}^2}{4R_{TH}} \\
 &= \frac{(11.4284)^2}{4 \times 8.4285} \\
 &= \frac{130.6083}{33.714} \\
 \therefore P_{Max} &= 3.8740W
 \end{aligned}$$

SIMULATED RESULTS:

The given circuit is simulated in LTspice and the results obtained are as follows:

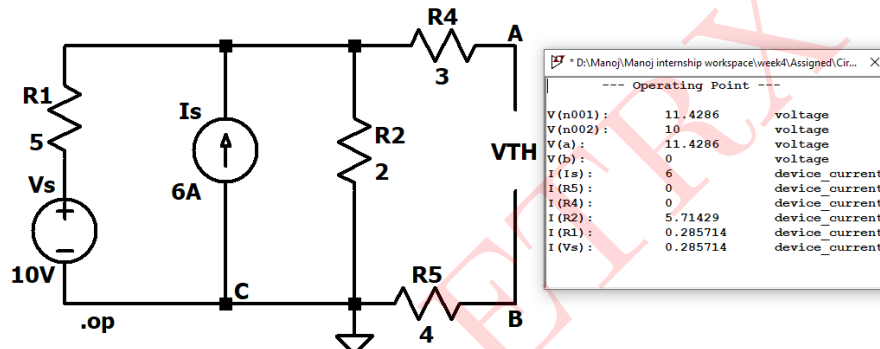


Figure 31: Circuit Schematic for V_{TH}

$$R_{TH} = V_1 / I(V_1) = 10 / 1.18644 = 8.4285 \text{ ohm}$$

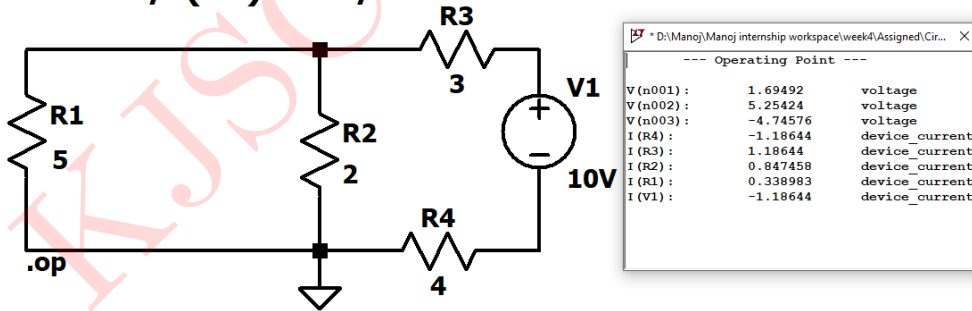


Figure 32: Circuit Schematic and Simulated Results for R_{TH}

$$P_{max} = (11.4286)^2 / (4 \times 8.4285) = 3.8741W$$

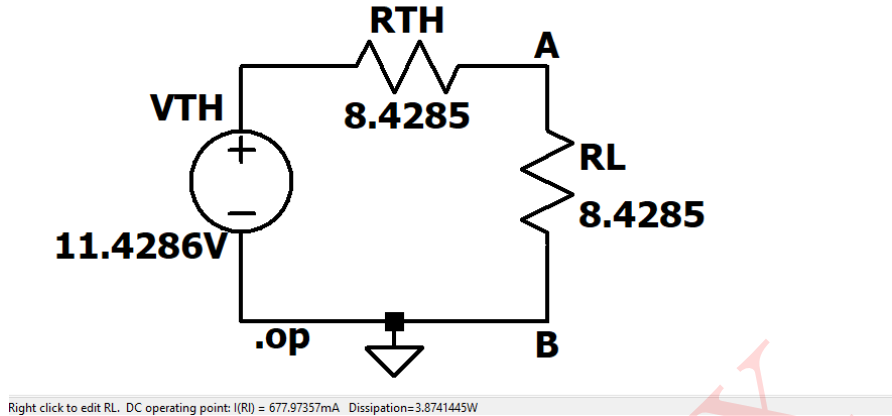


Figure 33: Circuit Schematic for P_{Max}

Comparison of Theoretical and Simulated Values:-

Parameters	Theoretical Values	Simulated Values
V_{TH}	11.4284V	11.4286V
R_{TH}	8.4285Ω	8.4285Ω
P_{Max}	3.8740W	3.8741W

Table 5: Numerical 5
