

**K. J. SOMAIYA COLLEGE OF ENGINEERING**  
**DEPARTMENT OF ELECTRONICS ENGINEERING**  
**ELECTRONIC CIRCUITS**  
**AC CIRCUITS**

**Numerical 1:** A series RLC circuit containing a resistance of  $20\Omega$ , an inductance of  $0.15H$  and a capacitor of  $75\mu F$  are connected in series across a  $120V$ ,  $60Hz$  supply.

Calculate:

- The current drawn by the circuit
- $V_R$ ,  $V_L$  and  $V_C$
- Power factor
- Draw the voltage phasor diagram

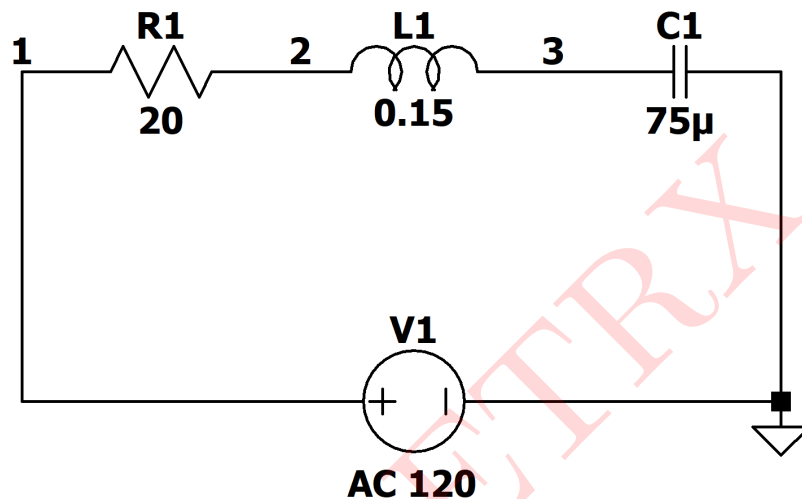


Figure 1: Circuit 1

**Solution:**

Frequency  $f = 60Hz$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi(60) = 120\pi \text{ rad/s}$$

Finding Inductive reactance  $X_L$ :

$$X_L = \omega L_1 = 120\pi \times 0.15 = 18\pi$$

$$X_L = 56.5487\Omega$$

Finding Capacitive reactance for  $X_C$ :

$$X_C = \frac{1}{\omega C_1} = \frac{1}{120\pi \times 75 \times 10^{-6}} = \frac{1000}{9\pi}\Omega$$

$$X_C = 35.3678\Omega$$

Net reactance,  $X$ :

$$X = X_L - X_C$$

$$X = 56.5487 - 35.3678$$

$$\therefore X = 21.1809\Omega$$

To find the phase angle  $\phi$ :

$$\phi = \tan^{-1} \left( \frac{X}{R_1} \right) = \tan^{-1} \left( \frac{21.1809}{20} \right)$$

$$\phi = 46.6426^\circ$$

To find total impedance,  $Z$ :

$$|Z| = \sqrt{R_1^2 + (X)^2} = \sqrt{25^2 + (21.1809)^2}$$

$$\therefore |Z| = 29.1313\Omega$$

$$Z = 29.1313\angle\phi$$

$$Z = 29.1313\angle 46.6426^\circ\Omega$$

a) Total current drawn by the circuit  $I$ ,

$$I = \frac{V_{in}}{Z} = \frac{120}{29.1313\angle 46.6426^\circ}$$

$$I = 4.1193\angle -46.6426^\circ A$$

b)  $V_R$ ,  $V_L$  and  $V_C$ ,

$$V_R = I \times R_1 = (4.1193\angle -46.6426^\circ) \times 20$$

$$\therefore V_R = 82.3856\angle -46.643^\circ V$$

$$V_L = I \times X_L = (4.1193\angle -46.6426^\circ) \times (56.5487\angle 90^\circ)$$

$$\therefore V_L = 232.924\angle 43.574^\circ V$$

$$V_C = I \times X_C = (4.1193\angle -46.6426^\circ) \times (35.3678\angle -90^\circ)$$

$$\therefore V_C = 145.6906\angle -136.643^\circ V$$

c) Power factor =  $\cos(\phi) = \cos(46.6426^\circ)$

$\therefore$  Power factor = 0.6865 lagging

d) Voltage Phasor diagram:

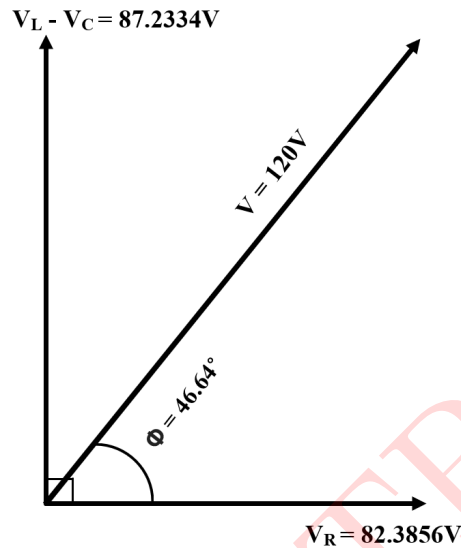


Figure 2: Voltage Phasor diagram

### SIMULATED RESULTS:

The following circuit has been simulated in LTspice and the graph obtained is as follows:

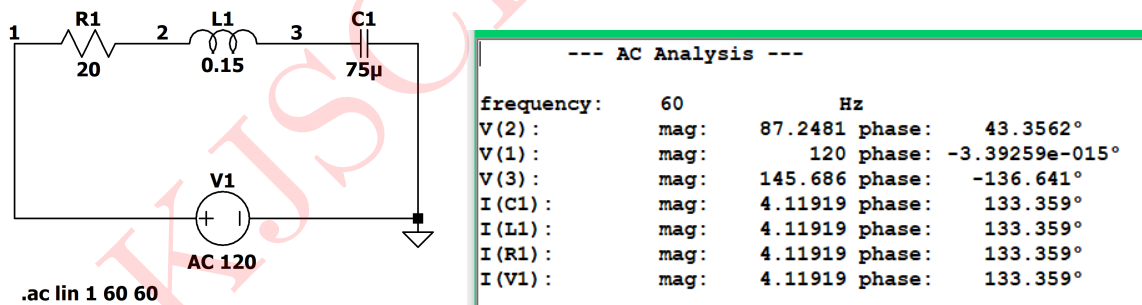


Figure 3: Circuit Schematic and Simulated Results

### Verifying the Calculated Values with Simulated Values:

Quantity	Calculated Value	Simulated Value
$I$	4.1193A	4.1192A
$V_R$	82.3856V	82.3838V
$V_L$	232.924	232.934
$V_C$	145.6906	145.686
$\phi$	46.6426°	46.6426°
Power Factor	0.6865	0.6865

Table 1: Comparison of calculated and simulated results

**Numerical 2:** In the R-L circuit given in Figure 4,  $R = 5\Omega$ ,  $L = 0.1H$  and a  $60Hz$  AC voltage  $V = 220\angle 60^\circ$ , find:

- Current through the circuit
- Power factor

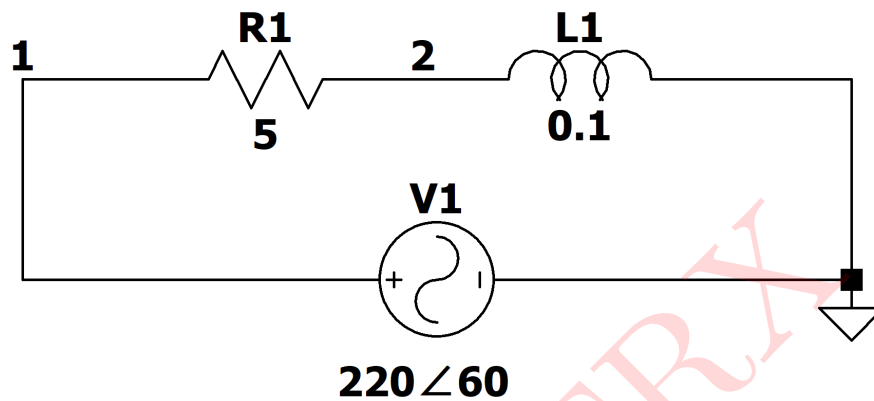


Figure 4: Circuit 2

**Solution:**

$$V_{rms} = \frac{220}{\sqrt{2}} = 155.5635V$$

Frequency  $f = 60Hz$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi(60) = 120\pi \text{ rad/s}$$

Finding Inductive reactance  $X_L$ :

$$X_L = \omega L_1 = 120\pi \times 0.1 = 12\pi$$

$$X_L = 37.699\Omega$$

To find the phase angle  $\phi$ :

$$\phi = \tan^{-1} \left( \frac{X_L}{R_1} \right) = \tan^{-1} \left( \frac{37.699}{5} \right)$$

$$\phi = 82.445^\circ$$

To find total impedance,  $Z$ :

$$|Z| = \sqrt{R_1^2 + (X_L)^2} = \sqrt{5^2 + (37.699)^2}$$

$$\therefore |Z| = 38.029\Omega$$

$$Z = 38.029\angle\phi$$

$$Z = 38.029\angle 82.445^\circ\Omega$$

Finding RMS current  $I_{rms}$ ,

$$I_{rms} = \frac{V_{rms}}{Z} = \frac{220\angle 60^\circ}{38.029\angle 82.445^\circ}$$

$$I_{rms} = 5.7851\angle -22.445^\circ A$$

a) Current through the circuit  $I$ ,

$$I = \frac{I_{rms}}{\sqrt{2}}$$

$$I = 4.0907\angle -22.445^\circ A$$

b) Power factor =  $\cos(\phi) = \cos(82.445^\circ)$

$\therefore$  Power factor = 0.1315 lagging

### SIMULATED RESULTS:

The following circuit has been simulated in LTspice and the graph obtained is as follows:

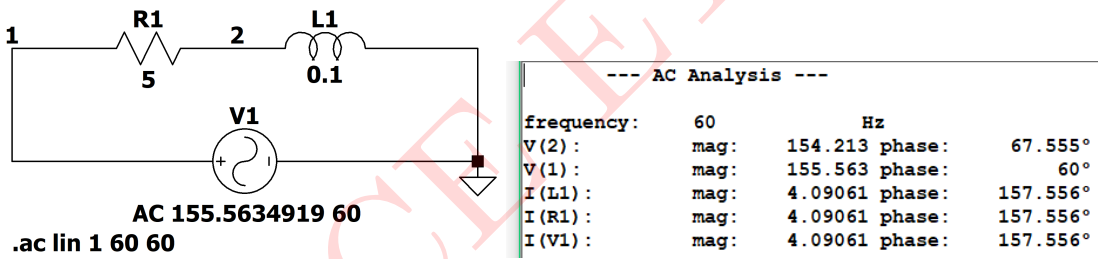


Figure 5: Circuit Schematic and Simulated Results

### Verifying the Calculated Values with Simulated Values:

Quantity	Calculated Value	Simulated Value
$I$	4.0907 A	4.09061 A
Power Factor	0.1315	0.1315

Table 2: Comparison of calculated and simulated results

**Numerical 3:** A voltage  $V = 120 \sin 314t$  is applied to a circuit consisting of a  $25\Omega$  resistor and an  $60\mu F$  capacitor in series. Determine:

- An expression for the value of the current flowing at any instant
- $V_R$  and  $V_C$
- Power factor

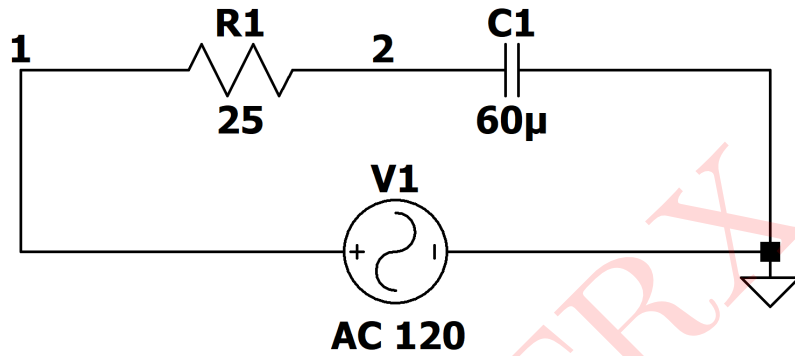


Figure 6: Circuit 3

**Solution:**

Angular frequency:  $\omega$

$$\omega = 314 \text{ rad/s}$$

Finding Capacitive reactance,  $X_C$ :

$$X_C = \frac{1}{\omega C_1} = \frac{1}{314 \times 60 \times 10^{-6}} = 53.079\Omega$$

$$X_C = 53.079\Omega$$

To find the phase angle  $\phi$ :

$$\phi = \tan^{-1} \left( \frac{-X_C}{R_1} \right) = \tan^{-1} \left( \frac{-53.079}{25} \right)$$

$$\phi = -64.7797^\circ$$

To find total impedance,  $Z$ :

$$|Z| = \sqrt{R_1^2 + (X_C)^2} = \sqrt{25^2 + (53.079)^2}$$

$$\therefore |Z| = 58.6718\Omega$$

$$Z = 58.6718 \angle \phi$$

$$Z = 58.6718 \angle -64.7797^\circ \Omega$$

- Current through the circuit  $I$ ,

$$I = \frac{V}{Z} = \frac{120}{58.6718 \angle -64.7797^\circ}$$

$$I = 2.045 \angle 64.7797^\circ \text{ A}$$

b) Voltage across resistor,  $V_R$ :

$$V_R = I \times R_1 = (2.045 \angle 64.7797^\circ) \times 25$$

$$\therefore V_R = 51.125 \angle 64.7797^\circ V$$

Voltage across Capacitor,  $V_C$

$$V_C = I \times X_C = (2.045 \angle 64.7797^\circ) \times (53.079 \angle -90^\circ)$$

$$\therefore V_C = 108.546 \angle -25.22^\circ V$$

c) Power factor =  $\cos(\phi) = \cos(-64.7797^\circ)$

$\therefore$  Power factor = 0.42609 leading

### SIMULATED RESULTS:

The following circuit has been simulated in LTspice and the graph obtained is as follows:

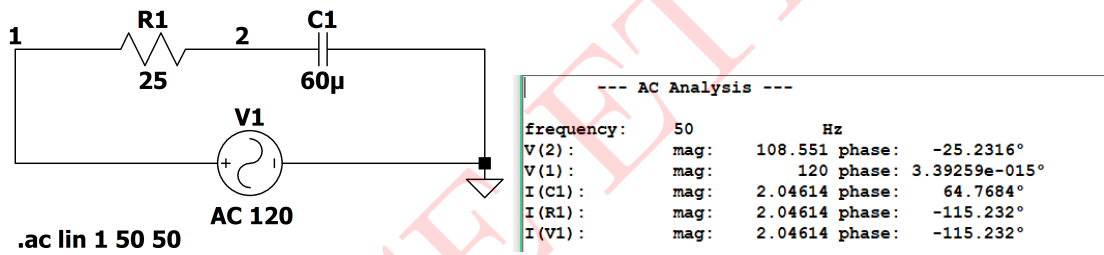


Figure 7: Circuit Schematic and Simulated Results

### Verifying the Calculated Values with Simulated Values:

Quantity	Calculated Value	Simulated Value
$I$	2.045A	2.046A
$V_R$	51.125V	51.15V
$V_C$	108.546V	108.551V
Power Factor	0.42609	0.42609

Table 3: Comparison of calculated and simulated results

**Numerical 4:** The Circuit given in Figure 8 consists of a resistance of  $5\Omega$ , an inductance of  $14mH$  and a capacitor of  $20\mu F$  are connected in parallel across a 110V, 50Hz supply. Calculate:

- Individual currents drawn by each element
- Total current drawn from the supply
- Overall power factor of the circuit
- Draw the phasor diagram

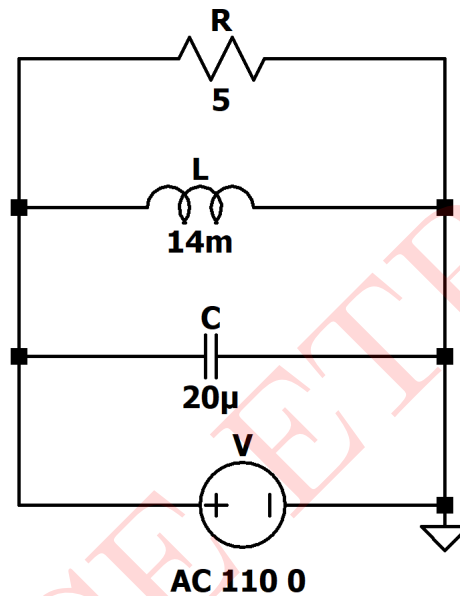


Figure 8: Circuit 4

**Solution:**

Frequency  $f = 50Hz$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi(50) = 100\pi \text{ rad/s}$$

Finding Inductive reactance  $X_L$ :

$$X_L = \omega L = 100\pi \times 14 \times 10^{-3} = 1.4\pi$$

$$X_L = 4.3982\Omega$$

Finding Capacitive reactance for  $X_C$ :

$$X_C = \frac{1}{\omega C} = \frac{1}{100\pi \times 20 \times 10^{-6}} = \frac{500}{\pi}\Omega$$

$$X_C = 159.1545\Omega$$



a) Individual currents drawn by each element:

Current through resistor,  $I_R$ :

$$I_R = \frac{V}{R} = \frac{110}{5}$$

$$I_R = 22A$$

Current through Inductor,  $I_L$ :

$$I_L = \frac{V}{X_L} = \frac{110}{4.3982j}$$

$$I_L = 25.0101 \angle -90^\circ A$$

Current through Capacitor,  $I_C$ :

$$I_C = \frac{V}{X_C} = \frac{110}{-159.1545j}$$

$$I_C = 0.6911 \angle 90^\circ A$$

b) Total current drawn from the supply,  $I_{V_1}$ :

$$I_{V_1} = I_R + I_C + I_L$$

$$I_{V_1} = 22 + 25.0101 \angle -90^\circ + 0.6911 \angle 90^\circ$$

$$I_{V_1} = 32.7934 \angle -47.866^\circ A$$

c) Overall power factor of the circuit:

Power factor of complete circuit =  $\cos \phi$  where,

$\phi$  = phase difference between  $I_{V_1}$  and  $V_1$

$$\phi = -47.866^\circ$$

$$\therefore \cos \phi = \cos -47.866^\circ$$

$$\cos \phi = 0.6709$$

Since  $X_C > X_L$ , power factor is leading

Hence, overall power factor =  $p.f. = 0.6709$  leading

d) Phasor diagram

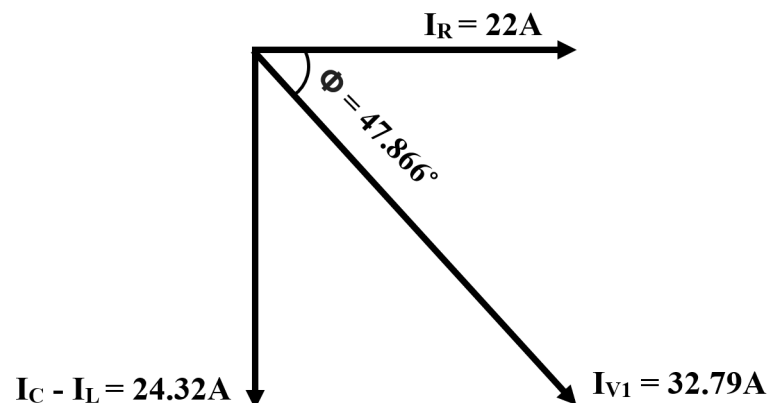


Figure 9: Phasor diagram

### SIMULATED RESULTS:

The following circuit has been simulated in LTspice and the readings obtained are as follows:

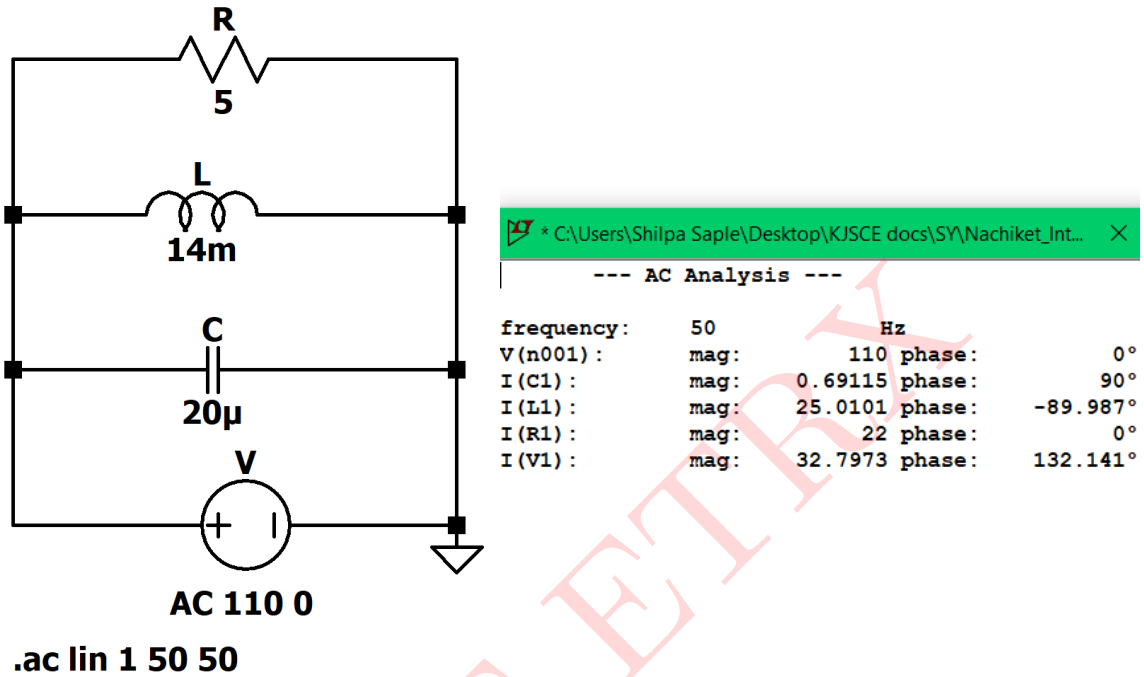


Figure 10: Circuit Schematic and Simulated Results

### Comparison of theoretical and simulated values:

Quantity	Calculated Value	Simulated Value
$I_R$	$22\angle 0^\circ A$	$22\angle 0^\circ A$
$I_L$	$25.01\angle -90^\circ A$	$25.01\angle -89.987^\circ A$
$I_C$	$0.6911\angle 90^\circ A$	$0.6911\angle 90^\circ A$
$I_{V_1}$	$32.7934\angle -47.866^\circ A$	$32.7973\angle -47.859^\circ A$
$\phi$	$47.866^\circ$	$47.859^\circ$
Power Factor	0.6709	0.6709

Table 4: Comparison of calculated and simulated results

**Numerical 5:** For the circuit given in Figure 11, find the current through all the branches  $I_1$ ,  $I_2$  and  $I_3$  and the voltage across all the branches if  $R_1 = 6\Omega$ ,  $L_1 = j4\Omega$ ,  $R_2 = 20\Omega$ ,  $L_2 = j8\Omega$ ,  $R_3 = 9\Omega$ ,  $C_1 = -j6\Omega$ ,  $V_1 = 100V$  and  $f = 50Hz$ .

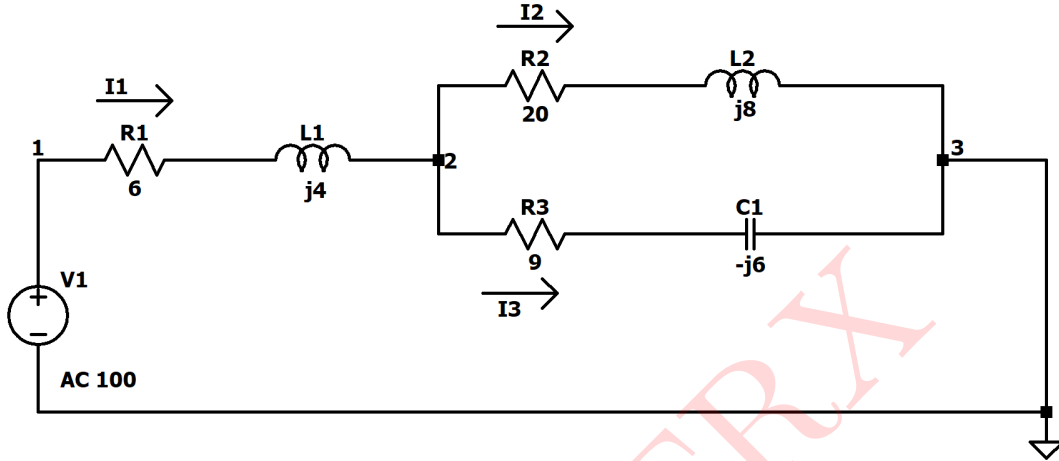


Figure 11: Circuit 5

**Solution:**

Frequency  $f = 50Hz$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi(50) = 100\pi \text{ rad/s}$$

Impedance of branch 1,  $Z_1 = 6 + j4\Omega$

Impedance of branch 2,  $Z_2 = 20 + j8\Omega$

Impedance of branch 3,  $Z_3 = 9 - j6\Omega$

Combined impedance of branch 2 and 3 after parallel combination,  $Z_4$ :

$$Z_4 = Z_2 || Z_3$$

$$Z_4 = \frac{Z_2 \times Z_3}{Z_2 + Z_3}$$

$$Z_4 = \frac{(20 + j8) \times (9 - j6)}{29 + j2}$$

$$Z_4 = 7.7112 - j2.1869\Omega$$

Total impedance of the circuit,  $Z$ :

$$Z = Z_1 + Z_4$$

$$Z = 13.7112 + j1.813\Omega$$

$$Z = 13.83 \angle 7.532^\circ \Omega$$

Total current through the circuit i.e. current through branch 1,  $I_1$ :

$$I_1 = \frac{V_1}{Z}$$

$$I_1 = \frac{100}{13.83 \angle 7.532^\circ}$$

$$I_1 = 7.23065 \angle -7.532^\circ A$$

Current through branch 2,  $I_2$ :

From current division rule:

$$I_2 = \frac{Z_3}{Z_2 + Z_3} \times I_1$$

$$I_2 = \frac{9 - j6}{20 + j8 + 9 - j6} \times (7.23065 \angle -7.532^\circ)$$

$$I_2 = 2.6906 \angle -45.167^\circ A$$

Current through branch 3,  $I_3$ :

From current division rule:

$$I_3 = I_1 - I_2$$

$$I_3 = (7.23065 \angle -7.532^\circ) - (2.6906 \angle -45.167^\circ)$$

$$I_3 = 5.3581 \angle 10.324^\circ A$$

Voltage across first branch,  $V_{12}$ :

From voltage division rule:

$$V_{12} = I_1 \times Z_1$$

$$V_{12} = (7.23065 \angle -7.532^\circ) \times (6 + j4)$$

$$V_{12} = (7.23065 \angle -7.532^\circ) \times (7.21 \angle 27^\circ)$$

$$V_{12} = 52.141 \angle 26.16^\circ V$$

Voltage across second and third branch,  $V_{23}$ :

$$V_{23} = V_1 - V_{12}$$

$$V_{23} = (100) - (52.141 \angle 26.16^\circ)$$

$$V_{23} = 57.953 \angle -23.34^\circ V$$

### SIMULATED RESULTS:

The following circuit has been simulated in LTspice and the readings obtained are as follows:

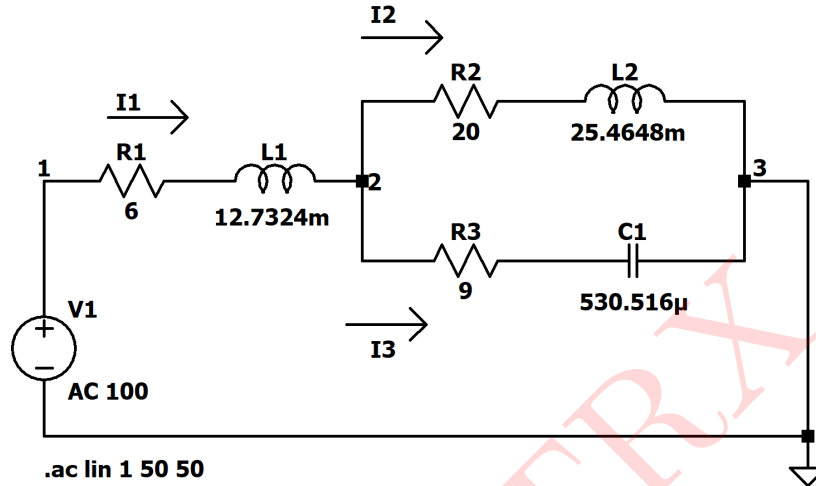


Figure 12: Circuit Schematic

frequency:	50	Hz
V(1) :	mag: 100	phase: 0°
V(n002) :	mag: 57.2782	phase: 5.69673°
V(2) :	mag: 57.9502	phase: -23.366°
V(n001) :	mag: 21.5213	phase: 44.8264°
V(n003) :	mag: 32.145	phase: -79.6759°
I(C1) :	mag: 5.3575	phase: 10.3241°
I(L2) :	mag: 2.69016	phase: -45.1665°
I(L1) :	mag: 7.22982	phase: -7.53132°
I(R3) :	mag: 5.3575	phase: 10.3241°
I(R2) :	mag: 2.69016	phase: -45.1665°
I(R1) :	mag: 7.22982	phase: -7.53132°
I(V1) :	mag: 7.22982	phase: 172.469°

Figure 13: Simulated Results

### Verifying the Calculated Values with Simulated Values:

Quantity	Calculated Value	Simulated Value
$I_1$	$7.23065 \angle -7.532^\circ A$	$7.22982 \angle -7.531^\circ A$
$I_2$	$2.6906 \angle -45.167^\circ A$	$2.69016 \angle -45.166^\circ A$
$I_3$	$5.3581 \angle 10.324^\circ A$	$5.3575 \angle 10.324^\circ A$
$V_{12}$	$52.141 \angle 26.16^\circ V$	$52.1409 \angle 26.15^\circ V$
$V_{23}$	$57.953 \angle -23.34^\circ V$	$57.9502 \angle -23.36^\circ V$
$\phi$	$7.532^\circ$	$7.531^\circ$

Table 5: Comparison of calculated and simulated results

**Numerical 6:** A  $50\text{Hz}$  sinusoidal voltage  $V = 100\sin\omega t$  is applied to a series R-L circuit. The values of the resistance and the inductance are  $22\Omega$  and  $0.0116\text{H}$  respectively.

Determine the following:

- Calculate the peak voltage across resistor and inductor and also find the peak value of source current in LTspice
- Plot input source voltage  $V_S(t)$  and input source current  $I_S(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  Vs  $I_S(t)$  in time and degrees
- Plot input source voltage  $V_S(t)$  and voltage across resistor  $V_R(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  vs  $V_R(t)$  in time and degrees
- Plot input source voltage  $V_S(t)$  and voltage across inductor  $V_L(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  vs  $V_L(t)$  in time and degrees
- Calculate the power factor of the circuit.

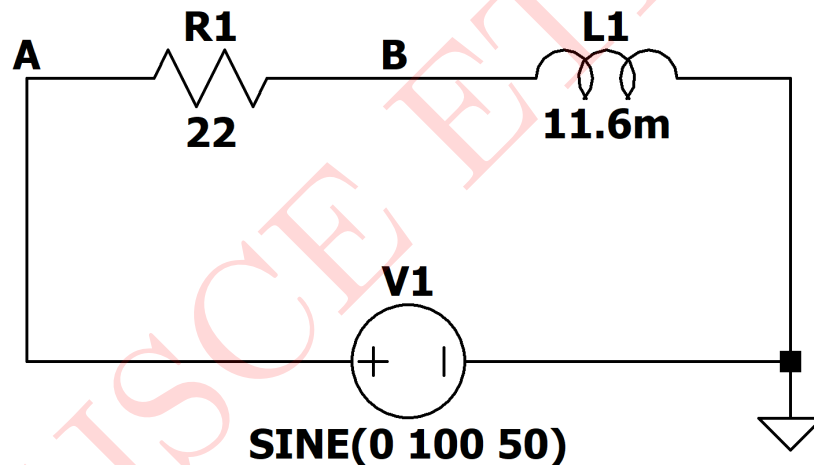


Figure 14: Circuit 6

**Solution:**

Frequency  $f = 50\text{Hz}$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi(50) = 100\pi \text{ rad/s}$$

Finding Inductive reactance  $X_L$ :

$$X_L = \omega L_1 = 100\pi \times 0.0116 = 1.16\pi$$

$$X_L = 3.6442\Omega$$

To find the phase angle  $\phi$ :

$$\phi = \tan^{-1} \left( \frac{X_L}{R_1} \right) = \tan^{-1} \left( \frac{3.6442}{22} \right)$$

$$\phi = 9.4054^\circ$$

To find total impedance,  $Z$ :

$$|Z| = \sqrt{R_1^2 + (X_L)^2} = \sqrt{22^2 + (3.6442)^2}$$

$$\therefore |Z| = 22.2998\Omega$$

$$Z = 22.2998\angle\phi$$

$$Z = 22.2998\angle 9.4054^\circ\Omega$$

Total source current in the circuit  $I$ ,

$$I = \frac{V_S}{Z} = \frac{100}{22.2998\angle 9.4054^\circ}$$

$$I = 4.4843\angle -9.4054^\circ A$$

Voltage across resistor,  $V_R$ :

$$V_R = I \times R_1 = (4.4843\angle -9.4054^\circ) \times 22$$

$$\therefore V_R = 98.6556\angle -9.4054^\circ V$$

Voltage across inductor,  $V_L$ :

$$V_L = I \times X_L = (4.4843\angle -9.4054^\circ) \times (3.6442\angle 90^\circ)$$

$$\therefore V_L = 16.3417\angle 80.59^\circ V$$

a) Peak values of  $V_R$ ,  $V_L$  and  $I$ :

$$\text{Peak voltage across resistor} = (V_R)_{max} = 98.6556V$$

$$\text{Peak voltage across inductor} = (V_L)_{max} = 16.3417V$$

$$\text{Peak value of source current} = (I)_{max} = 4.4843A$$

b) Plot of input source voltage  $V_S(t)$  and input source current  $I_S(t)$  in LTspice

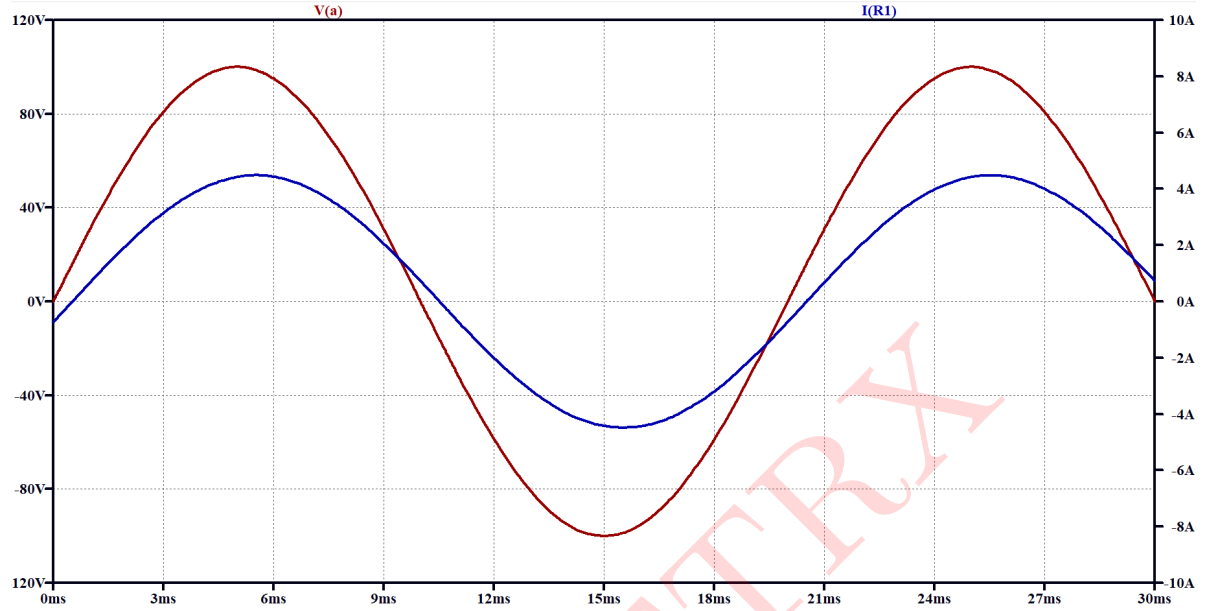


Figure 15:  $V_S(t)$  and  $I_S(t)$

c) Phase difference between  $V_S(t)$  and  $I_S(t)$  in time and degrees:

$$\Delta\phi_1 = 9.4054^\circ$$

$$\Delta t_1 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_1 = \frac{9.4054}{50 \times 360}$$

$$\Delta t_1 = 0.5225ms$$

Cursor 1			
V(a)			
Horz:	4.9830389ms	Vert:	99.9966V
Cursor 2			
I(R1)			
Horz:	5.5060071ms	Vert:	4.4838215A
Diff (Cursor2 - Cursor1)			
Horz:	522.9682μs	Vert:	-95.512779
Freq:	1.9121622KHz	Slope:	-182636

Figure 16: Phase difference from LTspice



d) Plot of input source voltage  $V_S(t)$  vs voltage across resistor  $V_R(t)$  in LTspice

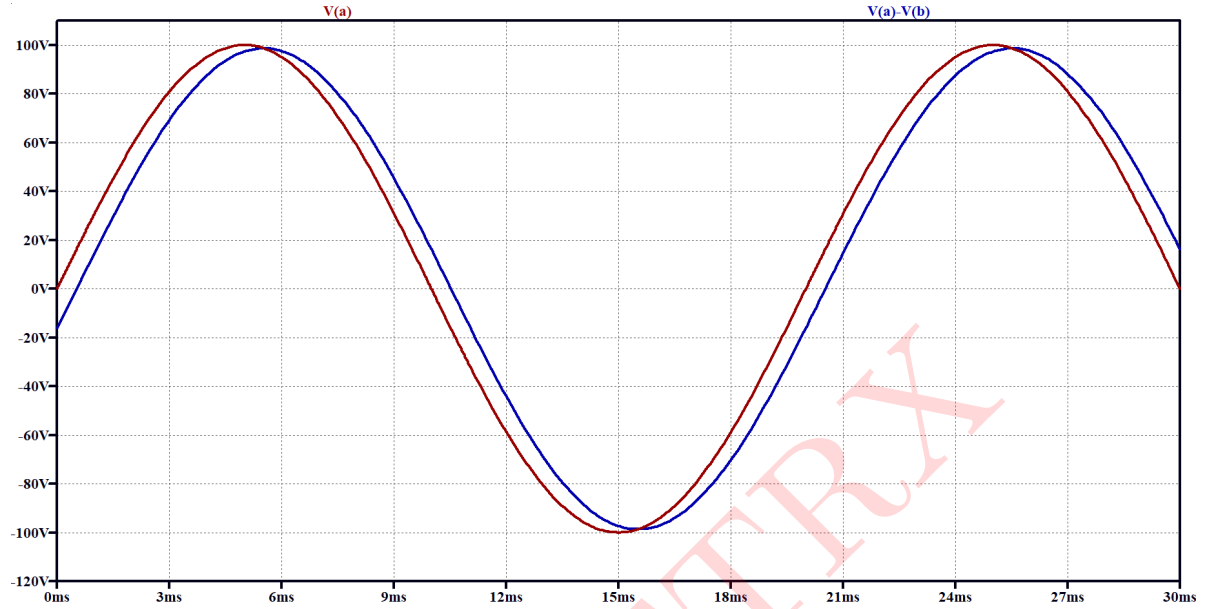


Figure 17:  $V_S(t)$  and  $V_R(t)$

e) Phase difference between  $V_S(t)$  and  $V_R(t)$  in time and degrees:

$$\Delta\phi_2 = 9.4054^\circ$$

$$\Delta t_2 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_2 = \frac{9.4054}{50 \times 360}$$

$$\Delta t_2 = 0.5225ms$$

Cursor 1	
V(a)	
Horz:	4.9988419ms
Vert:	99.998V
Cursor 2	
V(a)-V(b)	
Horz:	5.5233353ms
Vert:	98.651207V
Diff (Cursor2 - Cursor1)	
Horz:	524.49334μs
Vert:	-1.3467922V
Freq:	1.9066019KHz
Slope:	-2567.8

Figure 18: Phase difference from LTSpice

f) Plot of input source voltage  $V_S(t)$  vs voltage across inductor  $V_L(t)$  in LTSpice

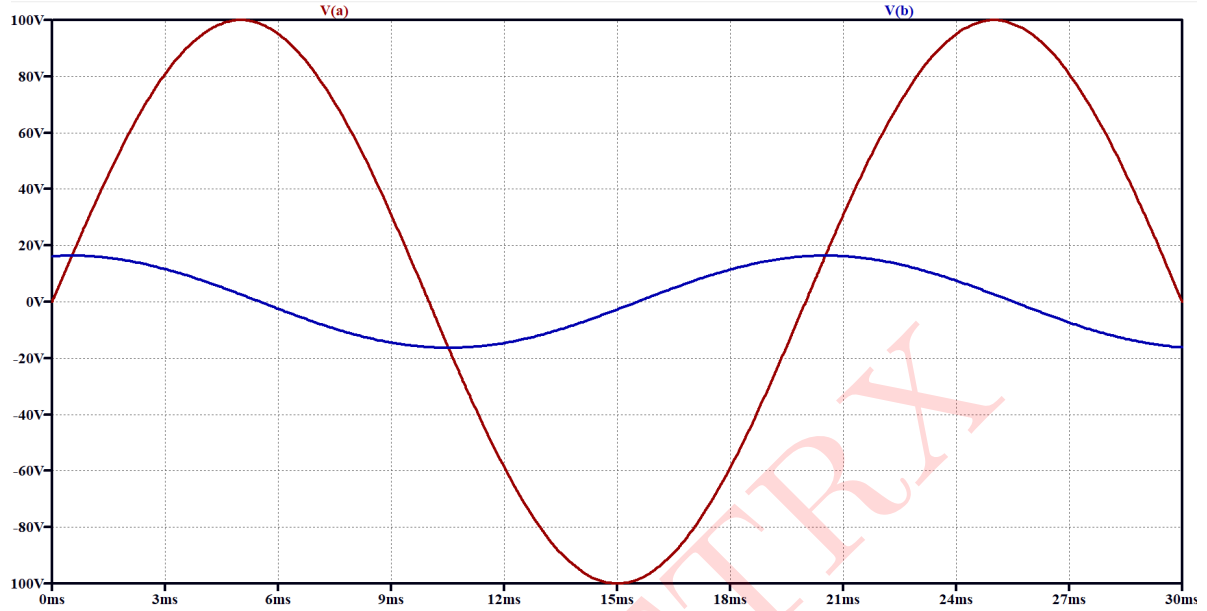


Figure 19:  $V_S(t)$  and  $V_L(t)$

g) Phase difference between  $V_S(t)$  and  $V_L(t)$  in time and degrees:

$$\Delta\phi_3 = 80.59^\circ$$

$$\Delta t_3 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_3 = \frac{80.59}{50 \times 360}$$

$$\Delta t_3 = 4.477ms$$

Cursor 1			
V(b)			
Horz:	20.465517ms	Vert:	16.337973V
Cursor 2			
V(a)			
Horz:	25.017241ms	Vert:	99.997794V
Diff (Cursor2 - Cursor1)			
Horz:	4.5517241ms	Vert:	83.659821V
Freq:	219.69697Hz	Slope:	18379.8

Figure 20: Phase difference from LTSpice

h) Power factor =  $\cos(\phi) = \cos(9.4054^\circ)$

$\therefore$  Power factor = 0.9866 lagging

**Verifying the Calculated Values with Simulated Values:**

Quantity	Calculated Value	Simulated Value
$(V_R)_{max}$	98.6556V	98.651V
$(V_L)_{max}$	16.3417V	16.3379V
$(I)_{max}$	4.4843A	4.4838A
$\Delta\phi_1$	9.4054°	9.4134°
$\Delta t_1$	0.5225ms	0.5229ms
$\Delta\phi_2$	9.4054°	9.441°
$\Delta t_2$	0.5225ms	0.5245ms
$\Delta\phi_3$	80.59°	80.58°
$\Delta t_3$	4.477ms	4.5517ms
Power Factor	0.9866	0.9865

Table 6: Comparison of calculated and simulated results

**Numerical 7:** A pure resistance of  $150\Omega$  is in series with a pure capacitance of  $220\mu F$ . The series combination is connected across  $120V$ ,  $50Hz$  supply.

Determine the following:

- Calculate the peak voltage across resistor and capacitor, also find the peak value of source current in LTspice
- Plot input source voltage  $V_S(t)$  and input source current  $I_S(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  and  $I_S(t)$  in time and degrees
- Plot input source voltage  $V_S(t)$  and voltage across resistor  $V_R(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  and  $V_R(t)$  in time and degrees
- Plot input source voltage  $V_S(t)$  and voltage across capacitor  $V_C(t)$  in LTspice
- Measure the phase delay/difference between  $V_S(t)$  and  $V_C(t)$  in time and degrees
- Calculate the power factor of the circuit.

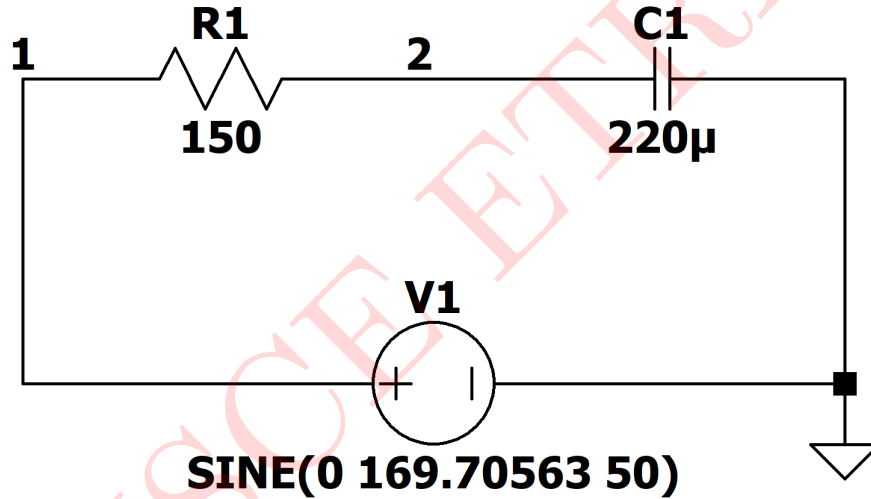


Figure 21: Circuit 7

**Solution:**

$$V_{max} = V_{rms} \times \sqrt{2}$$

$$V_{max} = 120 \times \sqrt{2} = 169.706V$$

Frequency  $f = 50Hz$ , angular frequency:  $\omega$

$$\omega = 2\pi f = 2\pi (50) = 100\pi rad/s$$

Finding Capacitive reactance  $X_C$ :

$$X_C = \frac{1}{\omega C_1} = \frac{1}{100\pi \times 220 \times 10^{-6}}$$

$$X_C = 14.469\Omega$$

To find the phase angle  $\phi$ :

$$\phi = \tan^{-1} \left( \frac{-X_C}{R_1} \right) = \tan^{-1} \left( \frac{-14.469}{150} \right)$$

$$\phi = -5.5096^\circ$$

To find total impedance,  $Z$ :

$$|Z| = \sqrt{R_1^2 + (X_C)^2} = \sqrt{150^2 + (14.469)^2}$$

$$\therefore |Z| = 150.696\Omega$$

$$Z = 150.696\angle\phi$$

$$Z = 150.696\angle - 5.5096^\circ\Omega$$

Finding RMS current  $I_{rms}$ ,

$$I_{rms} = \frac{V_{rms}}{Z} = \frac{120}{150.696\angle - 5.5096^\circ}$$

$$I_{rms} = 0.7963\angle 5.5096^\circ A$$

Source current,  $I$ :

$$I = I_{rms} \times \sqrt{2}$$

$$I = 0.7963\angle 5.5096^\circ \times \sqrt{2}$$

$$I = 1.1261\angle 5.5096^\circ A$$

Maximum voltage across resistor,  $V_R$ :

$$V_R = I \times R_1 = (1.1261\angle 5.5096^\circ) \times 150$$

$$\therefore V_R = 168.9218\angle 5.5096^\circ V$$

Voltage across capacitor,  $V_C$ :

$$V_C = I \times X_C = (1.1261\angle 5.5096^\circ) \times (14.469\angle - 90^\circ)$$

$$\therefore V_C = 16.294\angle - 84.49^\circ V$$

a) Peak values of  $V_R$ ,  $V_C$  and  $I$ :

$$\text{Peak voltage across resistor} = (V_R)_{max} = 168.9218V$$

$$\text{Peak voltage across capacitor} = (V_C)_{max} = 16.294V$$

$$\text{Peak value of source current} = (I)_{max} = 1.1261A$$

b) Plot of input source voltage  $V_S(t)$  and input source current  $I_S(t)$  in LTSpice

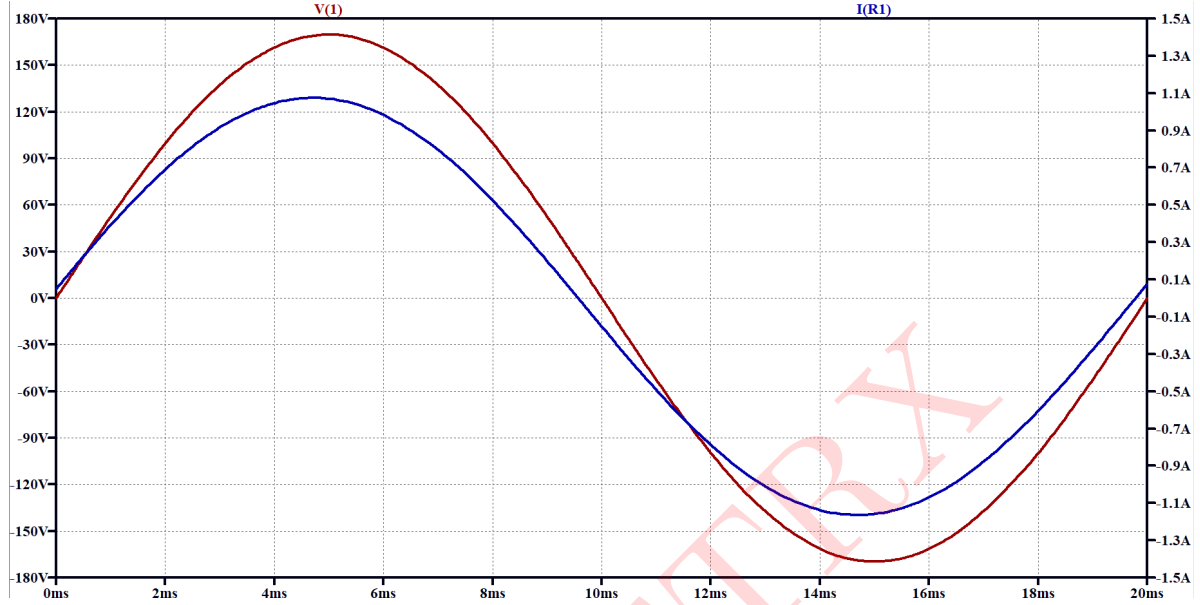


Figure 22:  $V_S(t)$  and  $I_S(t)$

c) Phase difference between  $V_S(t)$  and  $I_S(t)$  in time and degrees:

$$\Delta\phi_1 = 5.5096^\circ$$

$$\Delta t_1 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_1 = \frac{5.5096}{50 \times 360}$$

$$\Delta t_1 = 0.3061ms$$

Cursor 1			
I(R1)			
Horz:	4.6992933ms	Vert:	1.0748128A
Cursor 2			
V(1)			
Horz:	5.0024735ms	Vert:	169.69991V
Diff (Cursor2 - Cursor1)			
Horz:	303.18021μs	Vert:	168.6251
Freq:	3.2983683KHz	Slope:	556188

Figure 23: Phase difference from LTSpice

d) Plot of input source voltage  $V_S(t)$  vs voltage across resistor  $V_R(t)$  in LTSpice

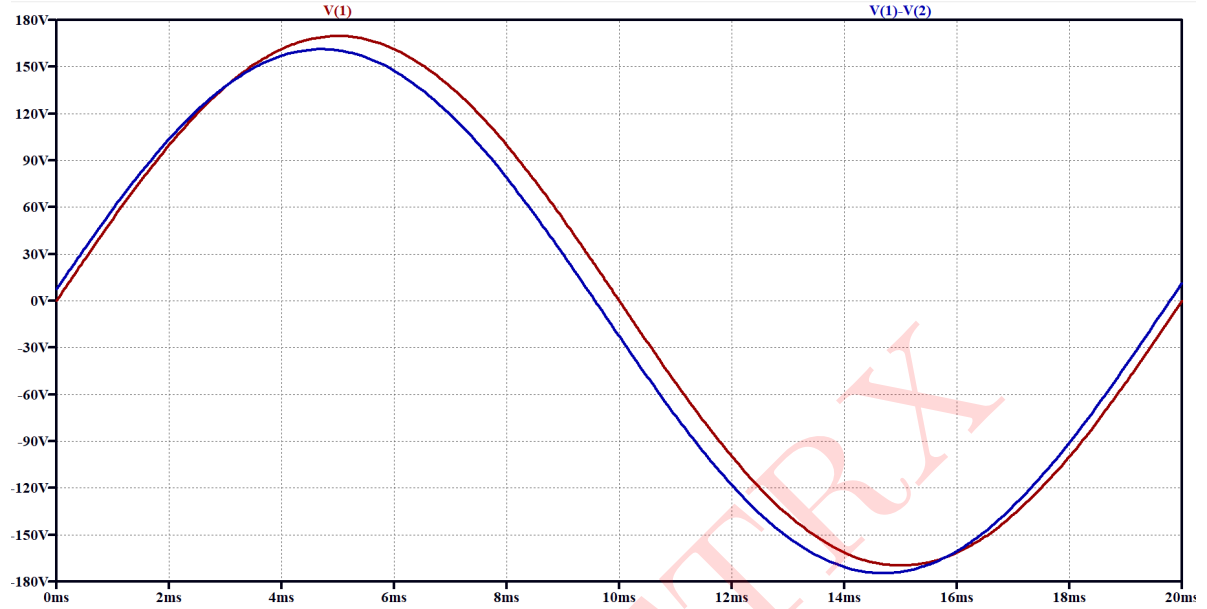


Figure 24:  $V_S(t)$  and  $V_R(t)$

e) Phase difference between  $V_S(t)$  and  $V_R(t)$  in time and degrees:

$$\Delta\phi_2 = 5.5096^\circ$$

$$\Delta t_2 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_2 = \frac{5.5096}{50 \times 360}$$

$$\Delta t_2 = 0.3061ms$$

Cursor 1			
V(1)-V(2)			
Horz:	4.7241379ms	Vert:	161.22668V
Cursor 2			
V(1)			
Horz:	5.0229885ms	Vert:	169.69571V
Diff (Cursor2 - Cursor1)			
Horz:	298.85057μs	Vert:	8.4690314V
Freq:	3.3461538KHz	Slope:	28338.7

Figure 25: Phase difference from LTSpice

f) Plot of input source voltage  $V_S(t)$  vs voltage across inductor  $V_C(t)$  in LTspice

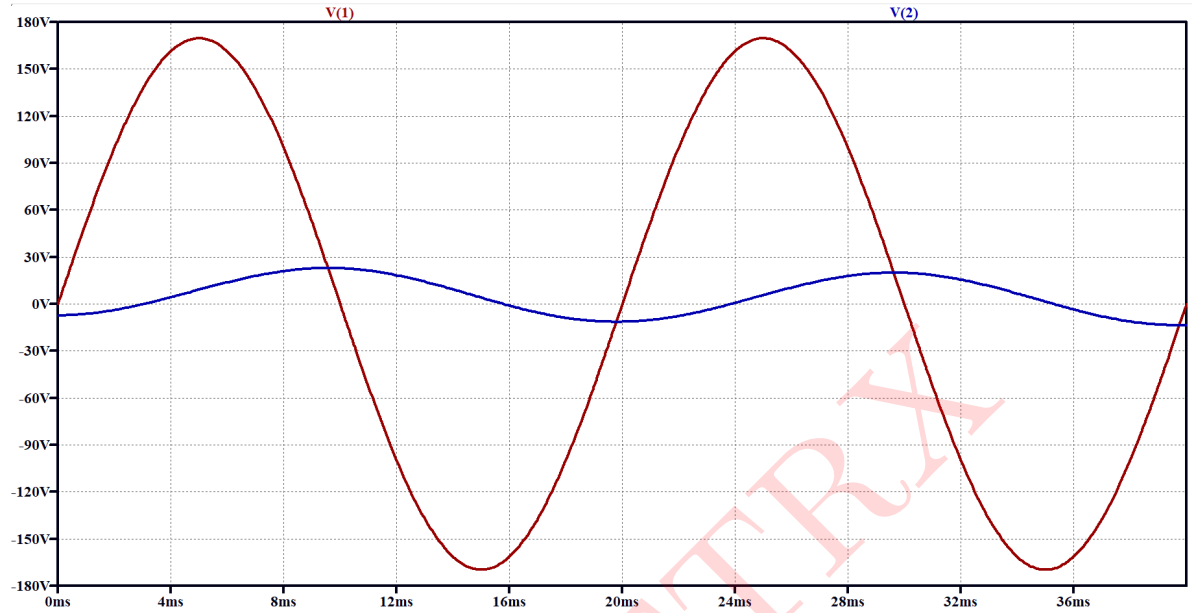


Figure 26:  $V_S(t)$  and  $V_C(t)$

g) Phase difference between  $V_S(t)$  and  $V_C(t)$  in time and degrees:

$$\Delta\phi_3 = 84.49^\circ$$

$$\Delta t_3 = \frac{\Delta\phi_1}{f \times 360}$$

$$\Delta t_3 = \frac{84.49}{50 \times 360}$$

$$\Delta t_3 = 4.694ms$$

Cursor 1			
V(1)			
Horz:	24.988506ms	Vert:	169.69343V
Cursor 2			
V(2)			
Horz:	29.632184ms	Vert:	19.893143V
Diff (Cursor2 - Cursor1)			
Horz:	4.6436782ms	Vert:	-149.80028V
Freq:	215.34653Hz	Slope:	-32259

Figure 27: Phase difference from LTspice



h) Power factor =  $\cos(\phi) = \cos(5.5096^\circ)$

$\therefore$  Power factor = 0.9954 leading

**Verifying the Calculated Values with Simulated Values:**

Quantity	Calculated Value	Simulated Value
$(V_R)_{max}$	168.922V	161.227V
$(V_C)_{max}$	16.294V	19.89V
$(I)_{max}$	1.1261A	1.0748A
$\Delta\phi_1$	$5.5096^\circ$	$5.4576^\circ$
$\Delta t_1$	0.3061ms	0.3032ms
$\Delta\phi_2$	$5.5096^\circ$	$5.380^\circ$
$\Delta t_2$	0.3061ms	0.2989ms
$\Delta\phi_3$	$84.49^\circ$	$83.59^\circ$
$\Delta t_3$	4.694ms	4.644ms
Power Factor	0.9954	0.9955

Table 7: Comparison of calculated and simulated results

**Numerical 8:** A series resonance network consisting of a resistor of  $24\Omega$ , a capacitor of  $1.8\mu F$  and an inductor of  $24mH$  is connected across a sinusoidal supply voltage which has a constant output of AC  $9V$  at all frequencies. Calculate:

- Resonant frequency
- Current at resonance
- The voltage across the inductor and capacitor at resonance
- The quality factor and the bandwidth of the circuit

Plot the resonance curve, the current at resonance, the voltage across the inductor and capacitor at resonance in LTspice.

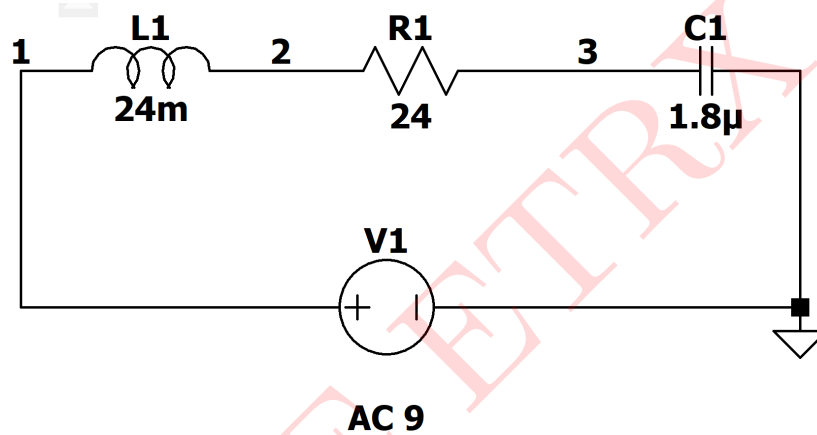


Figure 28: Circuit 8

**Solution:**

Resonant frequency  $f_r$ :

$$f_r = \frac{1}{2\pi\sqrt{L_1 C_1}}$$

$$f_r = \frac{1}{2\pi\sqrt{24 \times 10^{-3} \times 1.8 \times 10^{-6}}}$$

$$f_r = 765.735 Hz$$

a) Angular frequency at resonance,  $\omega_r$ :

$$\omega_r = 2\pi f_r$$

$$\omega_r = 2\pi \times 765.735$$

$$\omega_r = 4811.25 rad/s$$

At resonance,  $X_L = X_C$

$\therefore$  impedance,  $Z_r = R_1$

$$Z_r = 24\Omega$$

Since,  $X_C = X_L$  at resonance:

$$X_L = \omega L$$

$$X_L = 4811.25 \times 24 \times 10^{-3}$$

$$X_L = 115.47\Omega$$

$$X_C = X_L = 115.47\Omega$$

b) Current at resonance,  $I_r$ :

$$I_r = \frac{V}{Z_r}$$

$$I_r = \frac{9}{24}$$

$$I_r = 0.375A$$

c) Voltage across inductor,  $V_L$  and capacitor,  $V_C$ :

$$V_L = I \times X_L$$

$$V_L = 0.375 \times 115.47 \angle 90^\circ$$

$$V_L = 43.301 \angle 90^\circ V$$

$$V_C = 43.301 \angle -90^\circ V$$

d) Quality factor of the circuit,  $Q$

$$Q = \frac{X_L}{R_1}$$

$$Q = \frac{X_L}{24}$$

$$Q = 4.811$$

Bandwidth of the circuit,  $BW$

$$BW = \frac{f_r}{Q}$$

$$BW = \frac{765.735}{4.811}$$

$$BW = 159.16Hz$$

### SIMULATED RESULTS:

To obtain the resonance curve, the following circuit has been simulated in LTspice and the graph obtained is as follows:

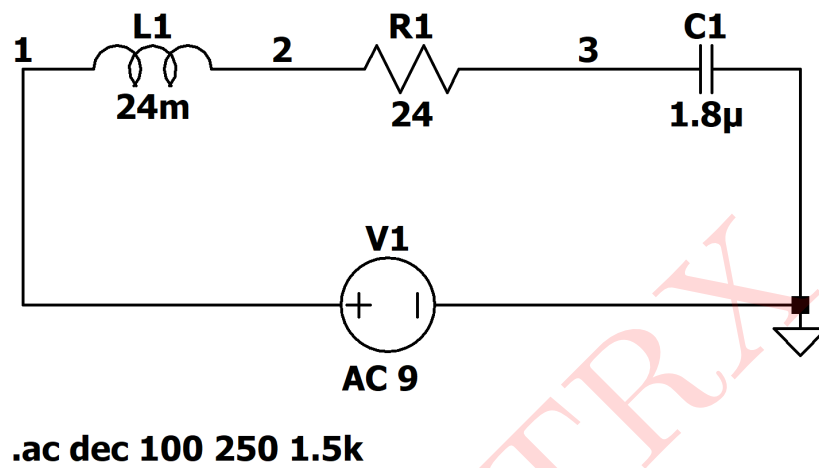


Figure 29: Circuit Schematic

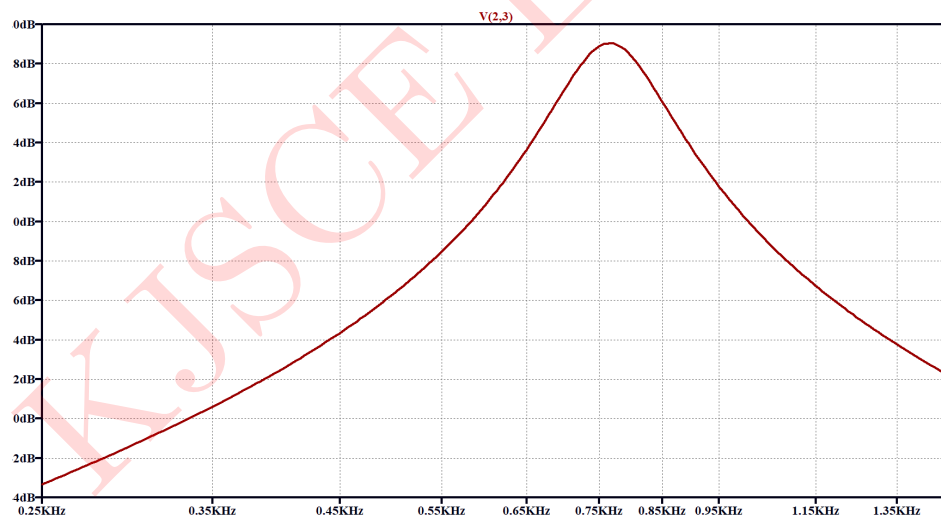


Figure 30: Resonance curve

To obtain the current, voltage across inductor and capacitor at resonance, the following circuit has been simulated in LTspice and the graph obtained is as follows:

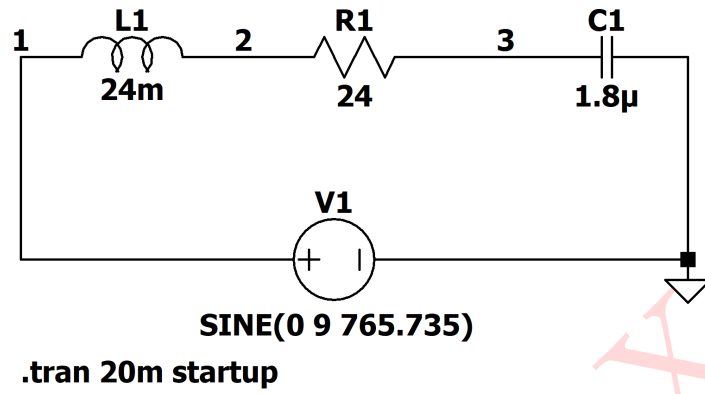


Figure 31: Circuit Schematic

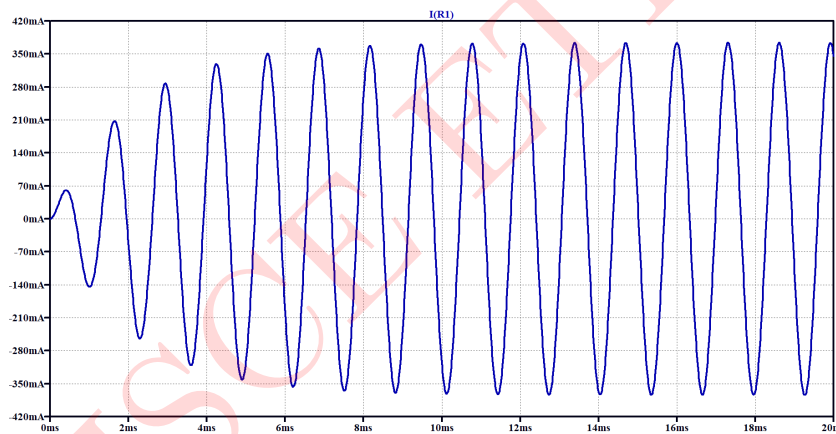


Figure 32: Current at resonance

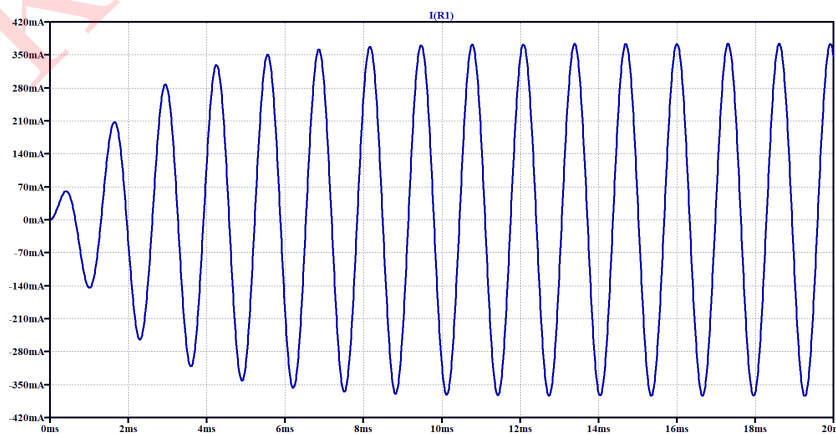


Figure 33:  $V_L$  and  $V_C$  at resonance

**Verifying the Calculated Values with Simulated Values:**

Quantity	Calculated Value	Simulated Value
$f_r$	$765.735Hz$	$764.0438Hz$
$I_r$	$0.375\angle 0^\circ A$	$0.370\angle 0^\circ A$
$V_L$	$43.301\angle 90^\circ V$	$42.9\angle 90^\circ V$
$V_C$	$43.301\angle -90^\circ V$	$42.89\angle -90^\circ V$
$Q$	$4.811$	$4.811$
$BW$	$159.16Hz$	$158.81Hz$

Table 8: Comparison of calculated and simulated results

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