K. J. SOMAIYA COLLEGE OF ENGINEERING DEPARTMENT OF ELECTRONICS ENGINEERING ELECTRONIC CIRCUITS

Darlington Amplifier

Q1. Calculate DC voltages at each mode and DC currents in the give circuit.

Given: $R_1 = 82k\Omega$, $R_2 = 39k\Omega$, $R_E = 820\Omega$, $C_{C1} = 10\mu F$, $C_{C2} = 10\mu F$, $V_{CC} = 10V$, $\beta = 100$.

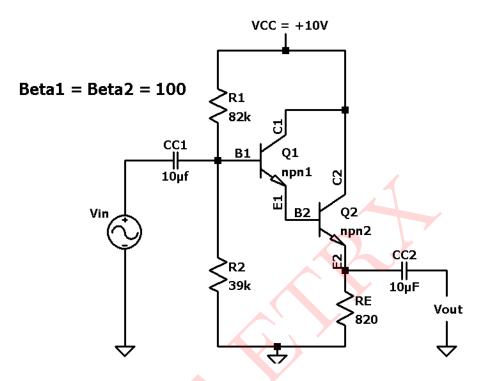


Figure 1: Circuit 1

Solution:

DC Analysis:

$$V_{BE} = V_{BE1} + V_{BE2} = 0.7 + 0.7 = 1.4V$$

$$V_{TH} = \left(\frac{R_2}{R_1 + R_2}\right) \times V_{CC} = \left(\frac{39k}{82k + 39k}\right) 10 = \mathbf{3.223V}$$

$$R_{TH} = R_1 \mid\mid R_2 = 82k \mid\mid 39k = \mathbf{26.429k}\Omega$$

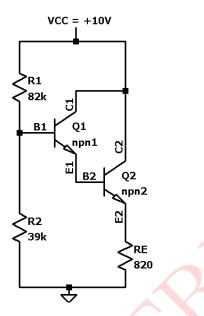


Figure 2: DC equivalent circuit

By thevenins equivalent circuit

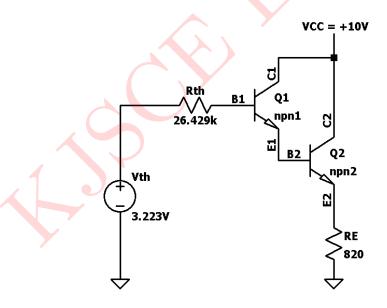


Figure 3: The venins equivalent circuit

$$\begin{split} I_{BQ} &= \frac{V_{TH} - V_{BE}}{R_{TH} + (1+\beta)^2 R_E} = \frac{3.223 - 1.4}{26.429k + (101)^2 \times 820} = \textbf{0.18149} \textbf{\mu} \textbf{A} \\ I_{C1} &= \beta I_{B1} = \textbf{0.018149} \textbf{m} \textbf{A} \\ I_{E1} &= I_{B1} + I_{C1} = \textbf{0.01833} \textbf{m} \textbf{A} \\ \text{Now, } I_{E1} &= I_{B2} = \textbf{0.01833} \textbf{m} \textbf{A} \\ I_{C2} &= \beta I_{B2} = \textbf{1.83304} \textbf{m} \textbf{A} \\ I_{E2} &= I_{C2} + I_{B2} = 1.83304 + 0.01833 = \textbf{1.85137} \textbf{m} \textbf{A} \\ V_{E2} &= I_{E2} R_E = 1.85137 m A \times 820\Omega = \textbf{1.5181V} \end{split}$$

$$V_{C2}$$
= 10V
 $V_{CE2} = V_{C2} - V_{E2} = 10 - 1.5181 = 8.4819$ V
Q point = (I_C, V_{CE}) = (1.83304mA , 8.4819V)

Small signal parameters:

$$\begin{split} r_{\pi 1} &= \frac{\beta V_T}{I_{C1}} = \frac{100 \times 26mV}{0.018149mA} = \mathbf{143.258k}\Omega \\ r_{\pi 2} &= \frac{\beta V_T}{I_{C2}} = \frac{100 \times 26mV}{1.83305mA} = \mathbf{1.418k}\Omega \end{split}$$

Mid frequency equivalent circuit:

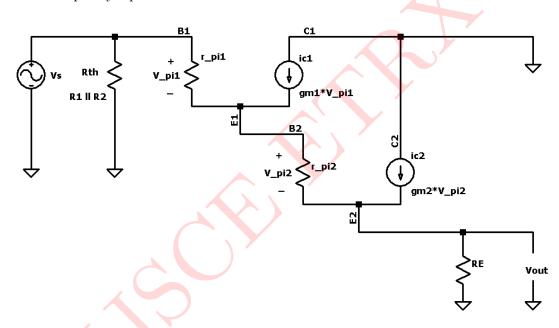


Figure 4: Mid frequency equivalent circuit

$$Z_{i2} = r_{\pi} + (1+\beta)R_E = 1.418k + (101) \times 820 = 82.238k\Omega$$

 $Z_{i1} = r_{\pi} + (1+\beta)Z_{i2} = 143.258k + (101) \times 82.238k = 8.449M\Omega$ (very high)

 $Z_i = R_1 \parallel R_2 \parallel Z_{i1} = 82$ k | | 39k | | 8.449M = **26.3465**k Ω (R_1 and R_2 decreases input impedence)

$$Z_{o2} = \frac{Z_{o1} + r_{\pi 2}}{1 + \beta}$$

$$Z_{o1} = \frac{(R1||R_2) + r_{\pi}}{1 + \beta} = \frac{26.429k + 143.258k}{101} = \mathbf{1.680 \ k\Omega}$$

$$Z_{o2} = \frac{1.680k + 1.418K}{101} = \mathbf{30.6732} \ \Omega \ \text{(Very low)}$$

$$Z_{o} = Z_{o2}||R_E = 30.6732||820 = \mathbf{29.5671} \ \Omega \ \text{(very low)}$$

$$A_i$$
 Current gain:

$$\begin{split} A_{i_1} &= \frac{I_{E1}}{I_{B1}} = (1+\beta) = \textbf{101} \\ A_{i_2} &= \frac{I_{E2}}{I_{B2}} = (1+\beta) = \textbf{101} \\ A_{i_t} &= A_{i2} \times A_{i1} = 101 \times 101 = \textbf{10201} \text{ (very high)} \\ A_{i_s} &= \frac{I_o}{I_i} = \frac{I_o}{I_{B2}} \times \frac{I_{B2}}{I_{B1}} \times \frac{I_{B1}}{I_i} \\ \frac{I_{B1}}{I_i} &= \frac{R_{TH}}{R_{TH} + Z_i} = \frac{26.429k}{26.429k + 8.449M} = \textbf{3.1183mA} \\ A_{i_s} &= 101.118mA = \textbf{31.8097} \text{ (Presence of } R_{TH} \text{ reduces current gain)} \end{split}$$

 A_v Voltage Gain:

$$A_{V_2} = \frac{V_o}{V_1} = \frac{R_E}{Z_{i2}} \times A_{i_2} = 101 \times \frac{820}{82.238k} = \mathbf{1.007}$$

$$A_{V_1} = \frac{V_1}{V_i} = \frac{Z_{i1}}{Z_{i2}} \times A_{i_1} = 101 \times \frac{82.238k}{8.449M} = \mathbf{0.98307}$$

$$A_{V_T} = A_{V_2} \times A_{V_1} = 1.0070 \times 0.98307 = \mathbf{0.98995}$$

$$A_{V_{Ts}} = A_{V_T} \times \frac{Z_i}{Z_i + R_{sig}} = \mathbf{0.98997} \; (\because R_{sig} = 0)$$

$$A_{V_{Ts}} indB = 20 \log_{10}(0.98995) = -\mathbf{0.08775dB}$$

SIMULATED RESULTS:

Above circuit was simulated in LTSpice and results are presented below:

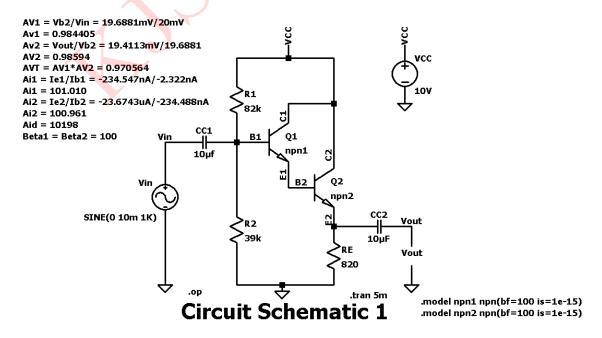


Figure 5: Circuit Schematic

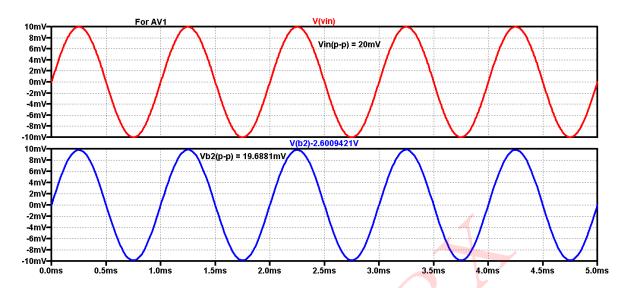


Figure 6: Input output waveform for A_{V_1}

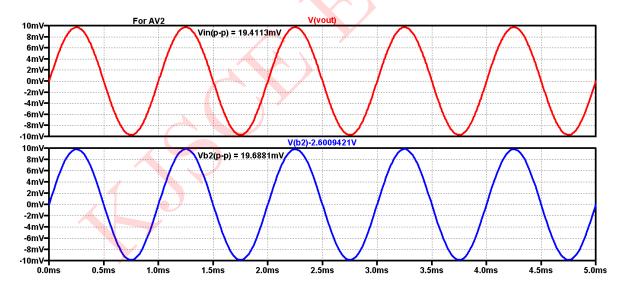


Figure 7: Input output waveform for A_{V_2}

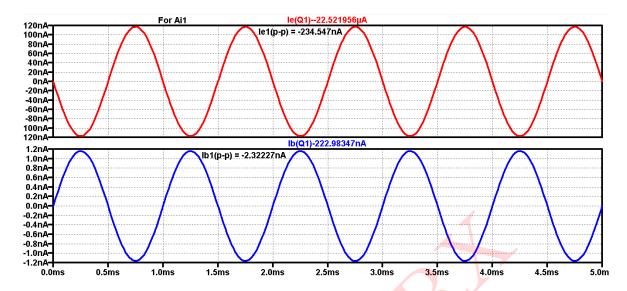


Figure 8: Input output waveform for A_{i_1}

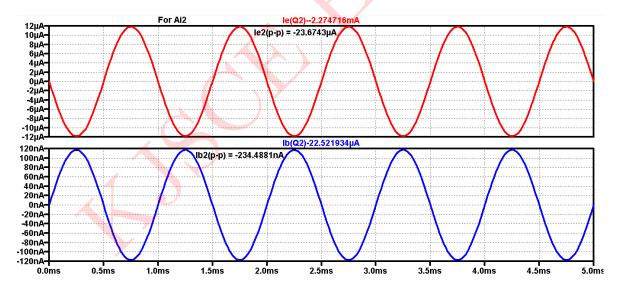


Figure 9: Input output waveform for A_{i_2}

${\bf Comparison\ of\ Theoretical\ and\ Simulated\ Values:}$

Parameters	Simulated	Theoretical
Stage 1:		
I_{B1}, I_{C1}	$0.2229\mu A, 0.0222mA$	$0.18149\mu A, 0.018149mA$
I_{E1}	$0.02252 \mathrm{mA}$	0.01833 mA
Stage 2:		
I_{B2}, I_{C2}	0.02252mA, 2.225mA	0.01833mA, 1.83304mA
I_{E2},V_{E2}	2.274mA, 1.865V	1.85137mA, 1.5181V
V_{C2}, V_{CE2}	10V, 8.135V	10V, 8.4819V
A_{V_1}	0.984404	0.98307
A_{V_2}	0.98594	1.0070
A_{V_T}	0.97056	0.98995
A_{i_1}	101.010	101
A_{i_2}	100.961	101
A_{i_T}	10198	10201
Z_i	_	$26.3456 \mathrm{k}\Omega$
Z_o	_	29.5671Ω

Table 1: Numerical 1
