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DEPARTMENT OF ELECTRONICS ENGINEERING
ELECTRONIC CIRCUITS
DC Biasing Circuits

- Find the Q point for the following shown in circuit with given parameters:
 $R_1 = 87.4k\Omega$, $R_2 = 12.6k\Omega$, $R_D = 0.5k\Omega$, $R_S = 0.5k\Omega$, $V_{DD} = 5V$, $V_{SS} = -5V$,
 $V_P = -3.5V$, $I_{DSS} = 12mA$

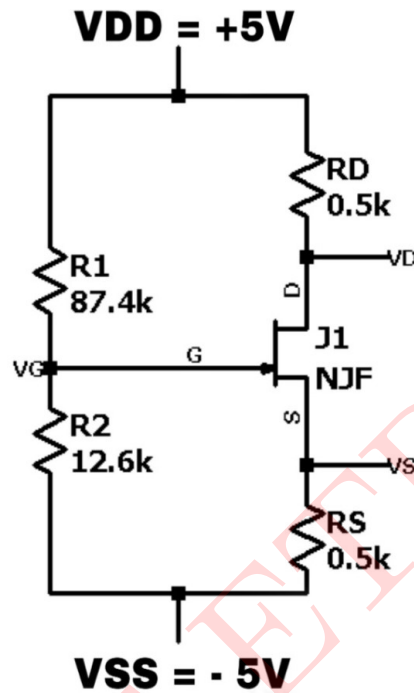


Figure 1: Circuit 1

Solution:

Assuming the transistor is biased in the saturation region, the DC drain current is given by:

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

Next we find the Q point i.e V_{DSQ} and I_{DQ}

$$V_G = V_{TH} = \frac{R_2}{R_1 + R_2} (5 - (-5)) - 5$$

$$V_G = \frac{12.6k\Omega}{87.4k\Omega + 12.6k\Omega} \times 10 - 5$$

$$V_G = V_{TH} = -3.75V$$

$$V_{GS} = V_G - V_S$$

$$V_{GS} = -3.74 - I_D R_S$$

$$V_{GS} = -3.74 - 500I_D \quad \text{--- (1)}$$

$$I_D = 12 \times 10^{-3} \left(1 - \frac{V_{GS}}{(-3.5)} \right)^2 \text{ ——— (2)}$$

Put (2) in (1)

$$V_{GS} = -3.74 - 6 \left(1 + \frac{2V_{GS}}{3.5} + \frac{V_{GS}^2}{3.5^2} \right)$$

$$V_{GS} = -9.74 - \frac{12V_{GS}}{3.5} - \frac{6V_{GS}^2}{3.5^2}$$

$$\frac{(V_{GS})^2}{(3.5)^2} + \frac{31V_{GS}}{7} + 9.74 = 0$$

$$V_{GS} = -5.26V \text{ or } -1.24V$$

We choose $-1.24V$ since $V_{GS} > V_P$

$$V_S = V_G - V_{GS}$$

$$V_S = -3.74 - (-1.24)$$

$$V_S = -2.5V$$

$$I_D = 12 \times 10^{-3} \left(1 + \left(\frac{-1.24}{3.5} \right) \right)^2$$

$$I_D = \mathbf{5mA}$$

Applying KVL to the drain source loop:

$$V_{DS} = 5 - I_D R_D - I_D R_S - (-5)$$

$$V_{DS} = 5 - 5 \times 0.5 - 5 \times 0.5 + 5$$

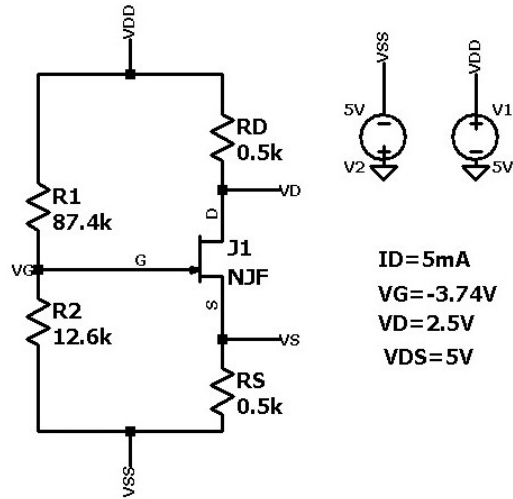
$$V_{DS} = \mathbf{5V}$$

$$Q \text{ point} = (V_{DS}, I_D)$$

$$Q \text{ point} = (\mathbf{5V}, \mathbf{5mA})$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows



`.model njf njf(vto=-3.5V beta=0.97e-3)`

JFETParameters: $V_p = -3.5\text{V}$ and $I_{DSS} = 12\text{mA}$
 $\beta = I_{DSS} / V_p^2 = 0.97\text{e-3}$

Figure 2: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
V_D	2.5V	2.5V
V_G	-3.74V	-3.74V
I_D	4.9mA	5mA
V_{DS}	5V	5V
V_S	-2.5V	-2.5V

Table 1: Numerical 1

2. Find V_G , V_{GS} , I_D and V_D for the circuit below:

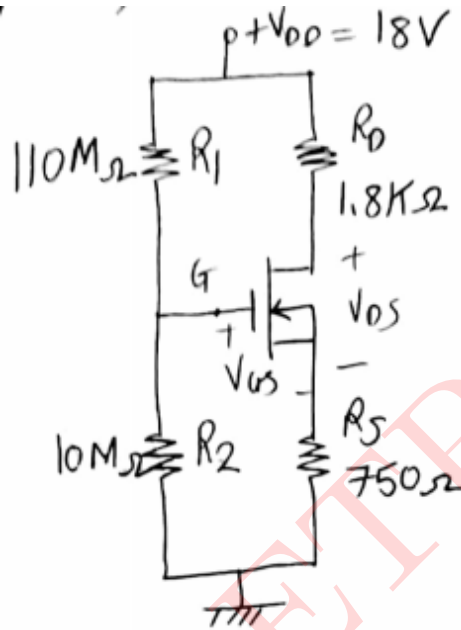


Figure 3: Circuit 2

Solution:

$$V_G = \frac{R_2}{R_1 + R_2} V_{DD} = 1.5V$$

$$V_S = I_D R_S$$

$$V_{GS} = V_G - V_S = V_G - I_D(750) \quad (1)$$

$$V_{GS} = 1.5 - I_D(750)$$

We assume that given NMOS D device is working in saturation region

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2 = 6 \left(1 + \frac{V_{GS}}{3}\right)^2 \quad (2)$$

Put (2) in (1)

$$V_{GS} = 1.5 - 750 \times 6 \left(1 + \frac{V_{GS}}{3}\right)^2$$

$$V_{GS} = 1.5 - 4.5 \left(1 + \frac{2V_{GS}}{3} + \frac{V_{GS}^2}{9}\right)$$

$$V_{GS} = 1.5 - 4.5 - 3V_{GS} - 0.5V_{GS}^2$$

$$0.5V_{GS}^2 + 4V_{GS} - 3 = 0$$

Solving the above quadratic equation, we get

$$V_{GS} = -0.8377V \text{ or } -7.16V$$

$$V_{GS} = -\mathbf{0.8377V} \quad \because (V_{GS} > V_P)$$

$$I_D = 6 \left(1 - \frac{(-0.8377)}{(-3)} \right)^2 = 3.11mA$$

$$I_D = \mathbf{3.11 \text{ mA}}$$

Applying KVL to D-S Loop:

$$V_{DD} - I_D R_D - V_{DS} - I_D R_S = 0$$

$$V_{DS} = V_{DD} - I_D (R_D + R_S)$$

$$V_{DS} = 18 - 3.11 \times 10^{-3} (1.8k\Omega + 750\Omega)$$

$$V_{DS} = \mathbf{10.07V}$$

3. Find the Q point, V_{DS} for the following shown in circuit with given parameter. Also find V_D , V_S and V_{DG} .
 $R_1 = 2.1\text{M}\Omega$, $R_2 = 270\text{K}\Omega$, $R_D = 2.4\text{K}\Omega$, $R_S = 1.5\text{K}\Omega$, $V_{DD} = 16\text{V}$,
 $V_P = -4\text{V}$, $I_{DSS} = 8\text{mA}$, $C_{C1} = 5\mu\text{F}$, $C_{C2} = 10\mu\text{F}$, $C_S = 20\mu\text{F}$.

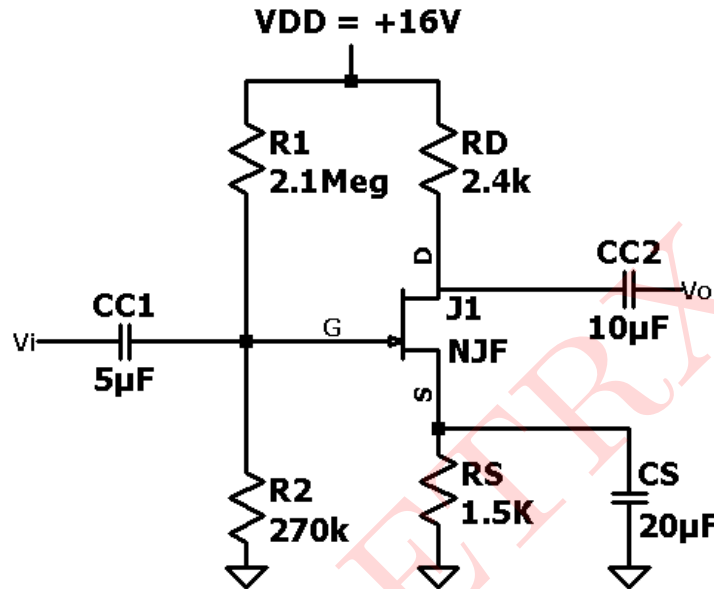


Figure 4: Circuit 3

Solution:

The above circuit is a voltage divider bias using a JFET.

For DC Analysis

$$V_G = \frac{R_2}{R_1 + R_2} V_{DD}$$

$$V_G = 1.82\text{V}$$

$$V_S = I_D R_S = (1.5\text{k}) I_D \quad \text{--- (1)}$$

$$V_{GS} = V_G - V_S$$

$$V_{GS} = 1.82 - (1.5\text{k}) I_D \quad \text{--- (2)}$$

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

$$I_D = 8\text{mA} \left(1 - \frac{V_{GS}}{4} \right)^2 \quad \text{--- (3)}$$

Solving equations (3) and (2)

$$V_{GS} = 1.82 - (1.5K) \times 8mA \left(1 + \frac{V_{GS}}{2} + \frac{(V_{GS})^2}{4^2} \right)$$

$$V_{GS} = 1.82 - 12 \left(1 + \frac{V_{GS}}{2} + \frac{(V_{GS})^2}{16} \right)$$

$$V_{GS} = 1.82 - 12 - 6V_{GS} - 0.75(V_{GS})^2$$

$$0.75(V_{GS})^2 + 7V_{GS} + 10.18 = 0$$

$$V_{GS} = -1.8V \text{ or } -7.53V$$

$$V_{GS} = -1.8V \quad \because (V_{GS} > V_P)$$

$$I_D = 8 \times 10^{-3} \left(1 - \frac{-1.8}{(-4)} \right)^2$$

$$I_{DQ} = \mathbf{2.42 \text{ mA}}$$

$$Q \text{ point } = (-1.82V, 2.42mA)$$

Applying KVL to the drain source loop:

$$V_{DS} = V_{DD} - I_D R_D - I_D R_S$$

$$V_{DS} = 16 - 2.42 \times 10^{-3} (2.4K + 1.5k)$$

$$V_{DS} = \mathbf{6.56V}$$

$$V_D = V_{DD} - I_D R_D$$

$$V_D = 16 - 2.42 \times 10^{-3} \times 2.4k$$

$$V_D = \mathbf{10.19V}$$

$$V_S = I_{DQ} R_S$$

$$V_S = 2.42 \times 10^{-3} \times 1.5k$$

$$V_S = \mathbf{3.63V}$$

$$V_{DG} = V_D - V_G$$

$$V_{DG} = 10.19 - 1.82$$

$$V_{DG} = \mathbf{8.37V}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

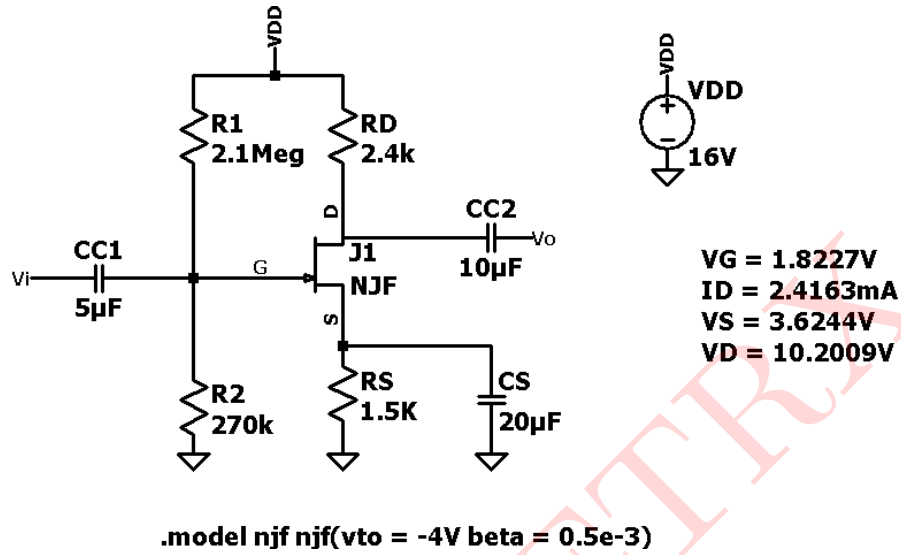


Figure 5: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
V_G	1.8227 V	1.82V
I_D	2.4163mA	2.42mA
V_{DS}	6.66V	6.55V
V_S	3.6244V	3.63V

Table 2: Numerical 3

4. Find V_{DS} for the following shown in circuit with given parameter, Also find V_{GS} and I_D
 $R_D = 10\text{M}\Omega$, $R_G = 2\text{K}\Omega$, $V_{DD} = 12\text{V}$, $V_{GS(on)} = 8\text{V}$, $V_{GS(th)} = 3\text{V}$, $I_{D(on)} = 6\text{mA}$,
 $C_{C1} = 1\mu\text{F}$, $C_{C2} = 1\mu\text{F}$.

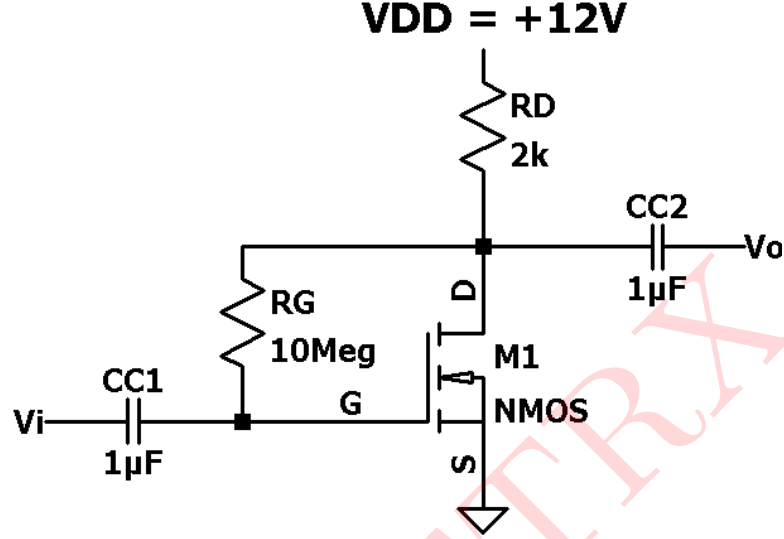


Figure 6: Circuit 4

Solution:

The above circuit is a drain feedback bias for E MOSFET.

$$k_n = \frac{I_{D(on)}}{(V_{GS(on)} - V_{GS(th)})^2} = \frac{6 \times 10^{-3}}{(8 - 3)^2}$$

$$k_n = 0.24 \times 10^{-3} \text{ A/V}^2$$

Applying KVL to the input loop:

$$V_{DD} - V_{GS} - I_D R_D - I_G R_G = 0$$

$$V_{GS} = V_{DD} - I_D R_D$$

$$V_{GS} = 12 - 2000 I_D \quad \because I_G = 0$$

$$I_D = k_n (V_{GS} - V_{GS(th)})^2$$

$$I_D = 0.24 \times 10^{-3} (12 - 2000 I_D - 3)^2$$

$$I_D = 0.24 \times 10^{-3} (81 - 3600 I_D + 4 \times 10^6 (I_D)^2)$$

$$960 I_D^2 - 9.64 I_D + 19.44 \times 10^3 = 0$$

$$I_D = 2.8\text{mA} \text{ or } 7.25\text{mA}$$

For $I_D = 7.25\text{mA}$

$$V_{DS} = V_{DD} - I_D R_D$$

$$V_{DS} = 12 - 7.25 \times 10^{-3} \times 2 \times 10^3$$

$$V_{DS} = 2.5V$$

Practically value of V_{DS} must be positive, Hence I_D cannot be 7.25mA

For $I_D = 2.8mA$

$$V_{DS} = V_{DD} - I_D R_D$$

$$V_{DS} = 12 - 2.8 \times 10^{-3} \times 2 \times 10^3$$

$$V_{DS} = 6.4V$$

$$V_{GS} = V_{DS} = 6.4V \quad \because \text{(Gate and Source terminals are connected)}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

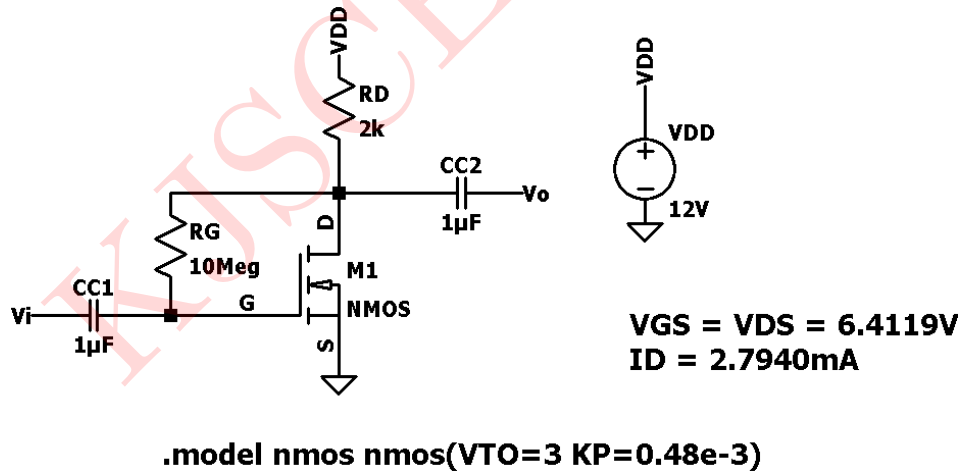


Figure 7: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
V_{GS}	6.4119 V	6.4V
I_D	2.794mA	2.8mA
V_{DS}	6.4119V	6.4V

Table 3: Numerical 4

5. Find I_B, I_C, V_{CE}, V_C for the following shown in circuit with given parameter.
 $R_B = 10k\Omega, R_C = 4k\Omega, R_E = 4k\Omega, \beta = 75, V_{CC} = 8V, V_{EE} = -8V$.

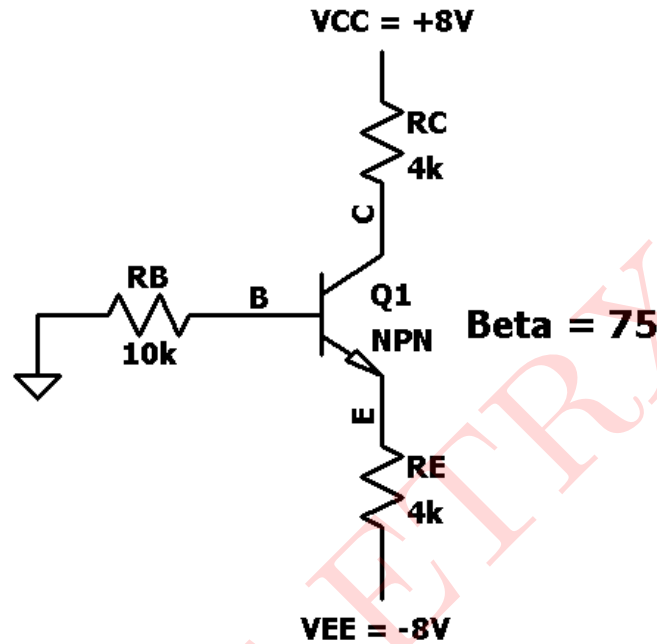


Figure 8: Circuit 5

Solution:

Applying KVL to the input loop.

$$-I_B R_B - V_{BE} - I_E R_E - V_{EE} = 0 \quad \text{--- (1)}$$

$$I_E = I_B + I_C$$

$$I_E = I_B + \beta I_B$$

$$I_E = (1 + \beta) I_B \quad \text{--- (2)}$$

Substituting equation (2) in equation (1)

$$0 = -I_B R_B - V_{BE} - (1 + \beta) I_B R_E - V_{EE}$$

$$I_B = \frac{-V_{EE} - V_{BE}}{R_B + (1 + \beta) R_E}$$

$$I_B = \frac{8 - 0.7}{10 \times 10^3 + (76)4 \times 10^3}$$

$$I_B = \mathbf{23.248 \mu A}$$

$$I_C = \beta I_B$$

$$I_C = \mathbf{1.743 mA}$$

Applying KVL to the output loop

$$-V_{CE} + V_{CC} - I_C R_C - I_E R_E - V_E = 0$$

$$V_{CE} = V_{CC} - I_C R_C - I_E R_E - V_E$$

$$V_{CE} = 8 - 1.743 \times 4 - (I_B + I_C) R_E = 8$$

$$V_{CE} = 8 - 6.972 - 6.9729$$

$$V_{CE} = \mathbf{2.055V}$$

$$V_C = I_C R_C + 8$$

$$V_C = -1.743 \times 4 \times 10^3 + V_{CC}$$

$$V_C = \mathbf{1.028V}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

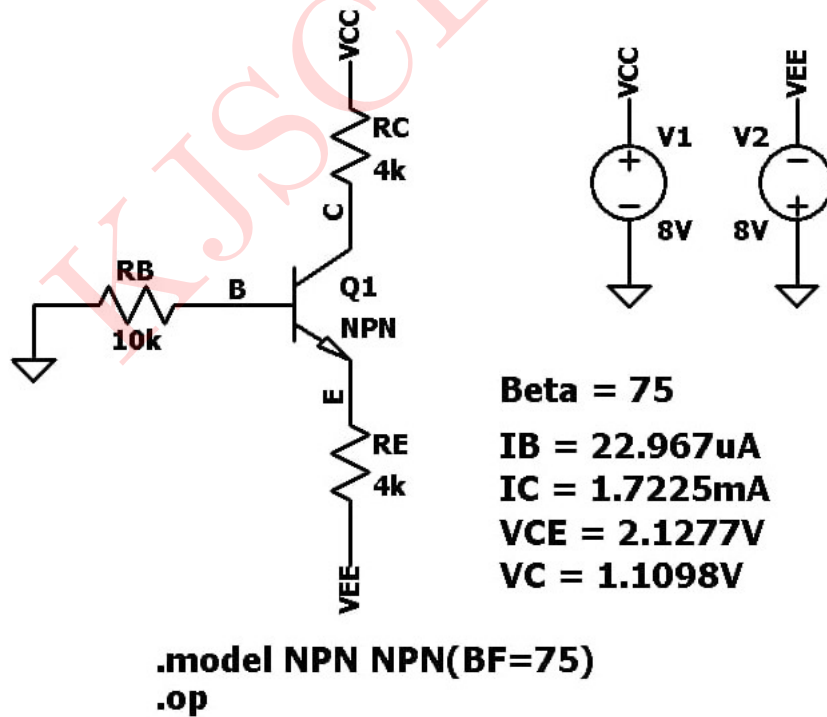


Figure 9: Circuit Schematic: Results

Comparsion between observed and theoretical values :

Parameters	Observed	Theoretical
I_B	$22.96\mu\text{A}$	$23.24\mu\text{A}$
I_C	1.7225mA	1.743mA
V_{CE}	2.1277V	2.055V
V_C	1.109V	1.028V

Table 4: Numerical 5

KJSCE ETRX

6. Find I_B, I_C, V_{CE}, V_C for the following shown in circuit with given parameter.
 $R_B = 20k\Omega, R_C = 10k\Omega, R_E = 2K\Omega, \beta = 75, V_{CC} = 5V$

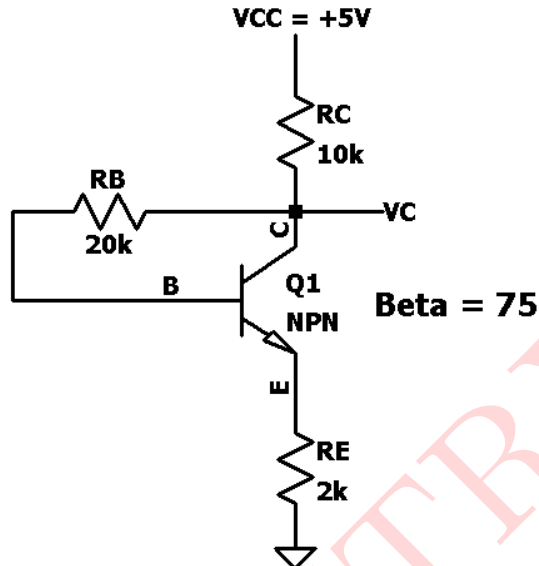


Figure 10: Circuit 6

Solution:

Applying KVL to the input feedback loop.

$$V_{CC} - (I_B + I_C)R_C - I_B R_B - V_{BE} - I_E R_E = 0 \quad (1)$$

$$I_E = I_B + I_C$$

$$I_E = I_B + \beta I_B$$

$$I_E = (1 + \beta)I_B \quad (2)$$

Substituting equation (2) in equation (1)

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + (1 + \beta)(R_E + R_C)}$$

$$I_B = \frac{5 - 0.7}{20k + (76)(4k + 10k)}$$

$$I_B = 4.6137\mu A$$

$$I_C = \beta I_B$$

$$I_C = 1.3460mA$$

Applying KVL to the output loop

$$V_{CE} = V_{CC} - (I_C + I_B)R_C - V_{CE} - (I_C + I_B)R_E = 0$$

$$V_{CE} = V_{CC} - (I_C + I_B) - (R_E + R_C) = 0$$

$$V_{CE} = 5 - (4.6137 \times 10^{-6} + 0.346 \times 10^{-3}) \times 12$$

$$V_{CE} = \mathbf{0.7056V}$$

$$V_C = 5 - (1 + \beta)I_B R_C$$

$$V_C = 5 - 76 \times 4.6137 \times 10^{-6} \times 10 \times 1000$$

$$V_C = \mathbf{1.4935V}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

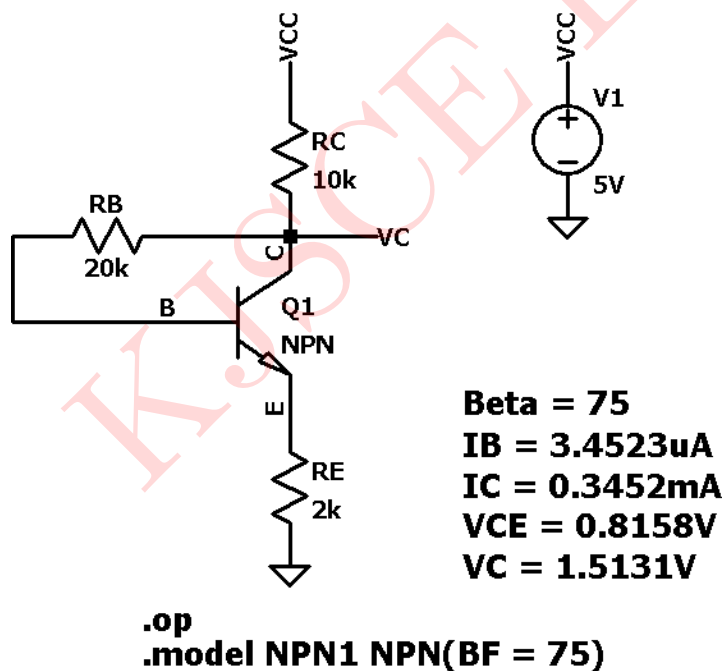


Figure 11: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
I_B	$3.4523\mu\text{A}$	$4.6137\mu\text{A}$
I_C	0.3452mA	0.3460mA
V_{CE}	0.8158V	0.7926V
V_C	1.5131V	1.4935V

Table 5: Numerical 6

7. Find I_C, V_{CE} for the following shown in circuit 7 with given parameter $\beta = 120, R_B = 250\text{k}\Omega, R_C = 1.5\text{k}\Omega, V_{CC} = -5\text{V}, V_{EE} = 5\text{V}$

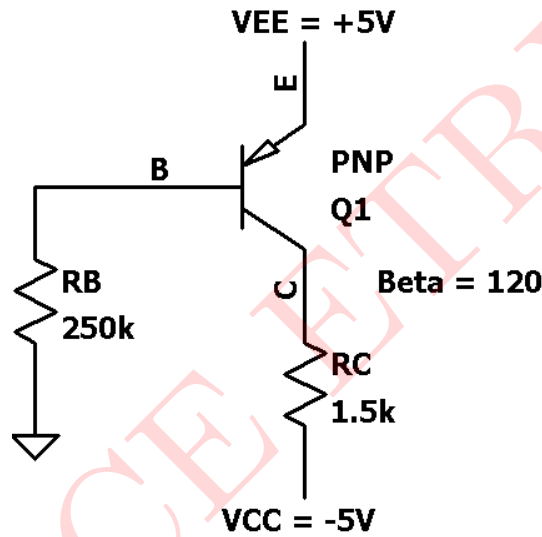


Figure 12: Circuit 7

Solution:

From circuit 7

$$I_C = \beta I_B$$

$$I_B = \frac{V_{EE} - V_{EB}}{R_B}$$

$$I_B = \frac{5 - 0.7}{250 \times 10^3}$$

$$I_B = 17.2\mu\text{A}$$

$$I_C = \beta I_B$$

$$I_C = 2.064\text{mA} \quad V_C = I_C R_C + V_{CC}$$

$$V_C = (2.064 \times 10^{-3} \times 1.5 \times 10^3) - 5$$

$$V_C = -1.904\text{V}$$

$$V_{EC} = V_E - V_C \quad V_{EC} = 5 - (-1.904) \quad V_{EC} = 6.904\text{V}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

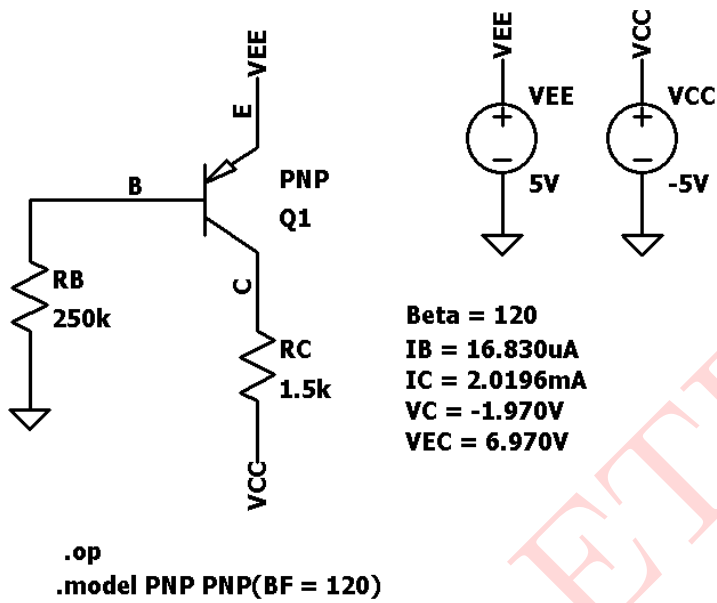


Figure 13: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
I_B	$16.830\mu A$	$17.2\mu A$
I_C	$2.0196mA$	$2.064mA$
V_{CE}	$6.970V$	$6.904V$
V_C	$-1.970V$	$-1.904V$

Table 6: Numerical 7

8. Find I_C , V_{BC} , I_E for the following shown in circuit with given parameter.
 $\alpha = 0.9920$, $R_C = 2.2\text{k}\Omega$, $R_E = 4\text{k}\Omega$, $V_{CC} = 9\text{V}$, $V_{EE} = 9\text{V}$

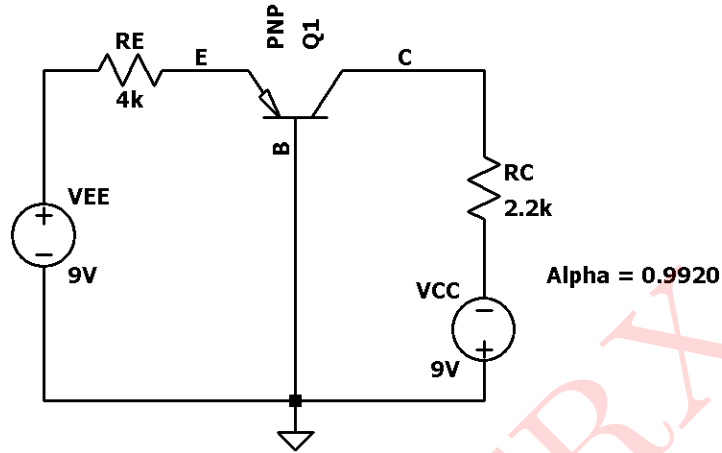


Figure 14: Circuit 8

Solution:

For circuit 8 applying KVL to emitter base loop

$$I_E = \frac{V_{EE} - V_{EB}}{R_E}$$

$$I_E = \frac{9 - 0.7}{4 \times 10^3}$$

$$I_E = \mathbf{2.075\text{mA}}$$

$$I_C = \alpha I_E$$

$$I_C = \mathbf{2.0584\text{mA}}$$

Applying KVL for circuit 8 to collector base loop

$$V_{BC} + I_C R_C = V_{CC}$$

$$V_{BC} = V_{CC} - I_C R_C$$

$$V_{BC} = 9 - (2.0584 \times 10^{-3} \times 2.2 \times 10^3)$$

$$V_{BC} = \mathbf{4.4715\text{V}}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

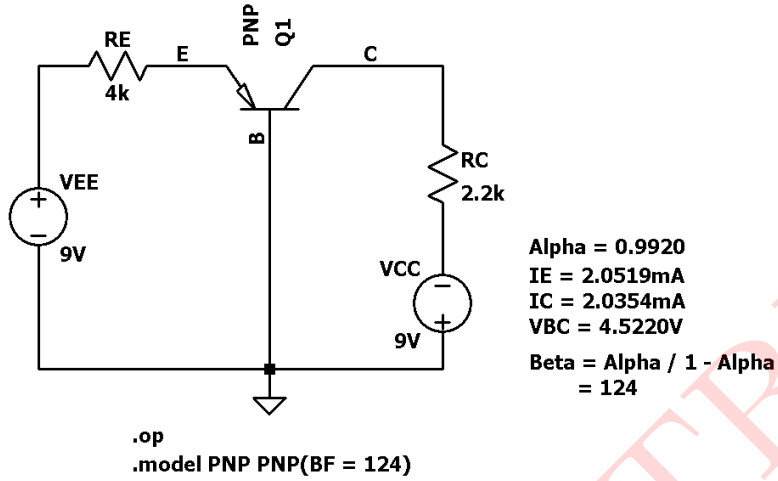


Figure 15: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
I_E	2.0519mA	2.075mA
I_C	2.0354mA	2.0584mA
V_{BC}	4.5220V	4.4715V

Table 7: Numerical 8

9. Find I_C, I_B, I_E, V_{CE} for the following shown in below circuit with given parameters
 $\beta = 150, R_E = 1.5k\Omega, R_C = 1.5k\Omega, V_{EE} = -12V, V_{CC} = 12V$

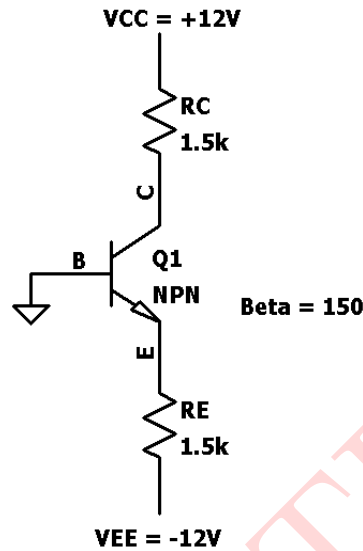


Figure 16: Circuit 9

Solution:

From circuit 9

$$-V_{EE} - V_{BE} - I_E R_E = 0$$

$$I_E = I_B + I_C$$

$$I_C = \beta I_B$$

$$I_E - (1 + \beta)I_B - V_{EE} - V_{BE} - (1 + \beta)I_B R_E = 0$$

$$I_B = \frac{-V_{EE} - V_{BE}}{(1 + \beta)R_E}$$

$$I_B = \frac{12 - 0.7}{1.5 \times 10^3 \times 151}$$

$$I_B = \mathbf{49.889 \mu A}$$

$$I_C = \beta I_B$$

$$I_C = \mathbf{7.4834 mA}$$

$$I_E = I_B + I_C$$

$$I_E = \mathbf{7.533 mA}$$

For circuit 9 applying KVL to output loop

$$V_{CE} = +V_{CC} - I_C R_C - I_C R_C - V_{EE}$$

$$V_{CE} = 12 - (7.4834 \times 1.5) - (7.533 \times 1.5) + 12$$

$$V_{CE} = 1.4754V$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

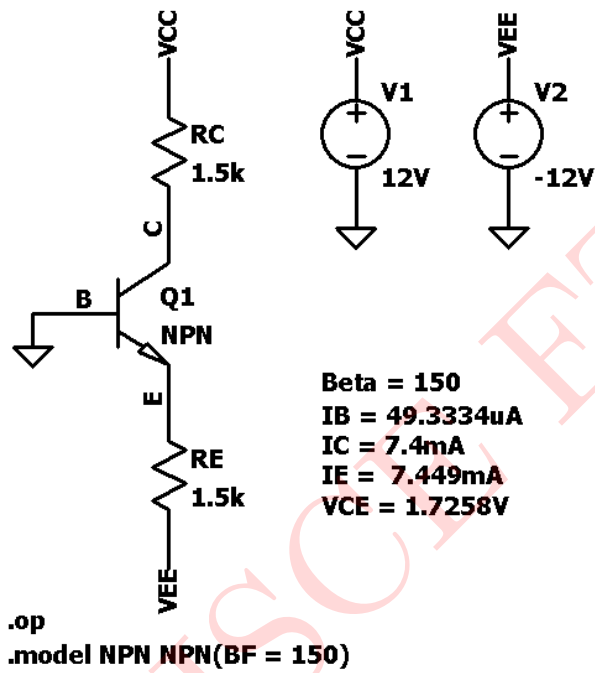


Figure 17: Circuit Schematic: Results

Comparison between observed and theoretical values :

Parameters	Observed	Theoretical
I_B	$49.3334\mu A$	$49.889\mu A$
I_C	$7.4mA$	$7.4834mA$
I_E	$7.449mA$	$7.533mA$
V_{CE}	$1.7258V$	$1.4754V$

Table 8: Numerical 9

10. Find I_C, I_B, V_{CE} for the following shown in circuit 10 with given parameters
 $\beta = 100, R_B = 400\text{k}\Omega, R_C = 3.3\text{k}\Omega, V_{CC} = 12\text{V}, R_E = 1.5\text{k}\Omega$

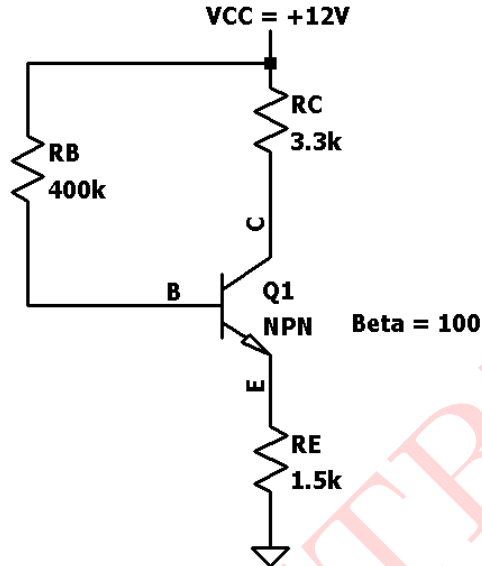


Figure 18: Circuit 10

Solution:

Applying KVL to the input loop of the above circuit

$$V_{CC} - I_B R_B - V_{BE} - I_E R_E = 0$$

$$I_C = \beta I_B$$

$$I_E = I_C + I_B$$

$$I_E = (1 + \beta) I_B$$

$$V_{CC} - I_B R_B - V_{BE} - (1 + \beta) I_B R_E = 0$$

$$I_B = \frac{V_{CC} - V_{BE}}{R_B + (1 + \beta) R_E}$$

$$I_B = \frac{12 - 0.7}{400 \times 10^3 + 101 \times 1.5 \times 10^3}$$

$$I_B = \mathbf{20.4895 \mu A}$$

$$I_C = \beta I_B$$

$$I_C = \mathbf{2.0489 \text{ mA}}$$

Applying KVL to the output loop of the above circuit

$$V_{CC} - V_{CE} - I_C R_C - I_E R_E$$

$$V_{CE} = V_{CC} - I_C R_C - (I_C + I_B) R_E$$

$$V_{CE} = 12 - (2.0489 \times 3.3) - (10 \times 20.4895 \times 10^{-6} \times 1.5 \times 10^3)$$

$$V_{CE} = \mathbf{2.1344V}$$

SIMULATED RESULTS:

Above circuit is simulated in LTspice and results are as follows

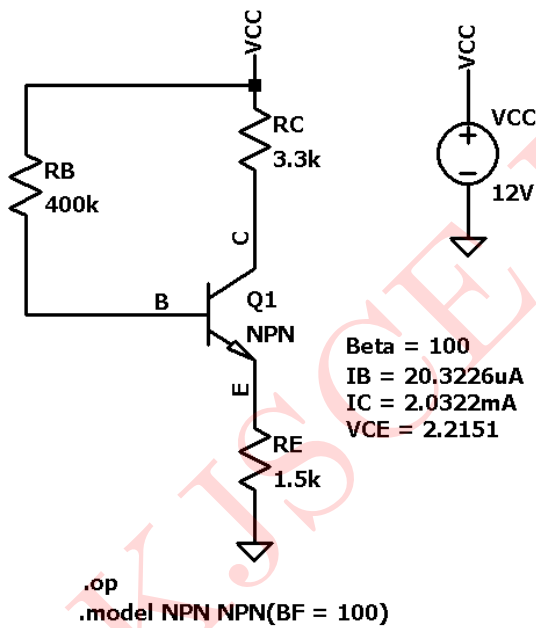


Figure 19: Circuit Schematic: Results

Comparsion between observed and theoretical values :

Parameters	Observed	Theoretical
I_B	$20.3226\mu A$	$20.4895\mu A$
I_C	$2.0322mA$	$2.0489mA$
V_{CE}	$2.2151V$	$2.1344V$

Table 9: Numerical 10
