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DEPARTMENT OF ELECTRONICS ENGINEERING
ELECTRONIC CIRCUITS
Cascode Amplifier

Numerical 1:

For the cascode amplifier circuit shown in figure 1, calculate the voltage gain A_V and output voltage V_o . Given $\beta_1 = 200$ & $\beta_2 = 200$

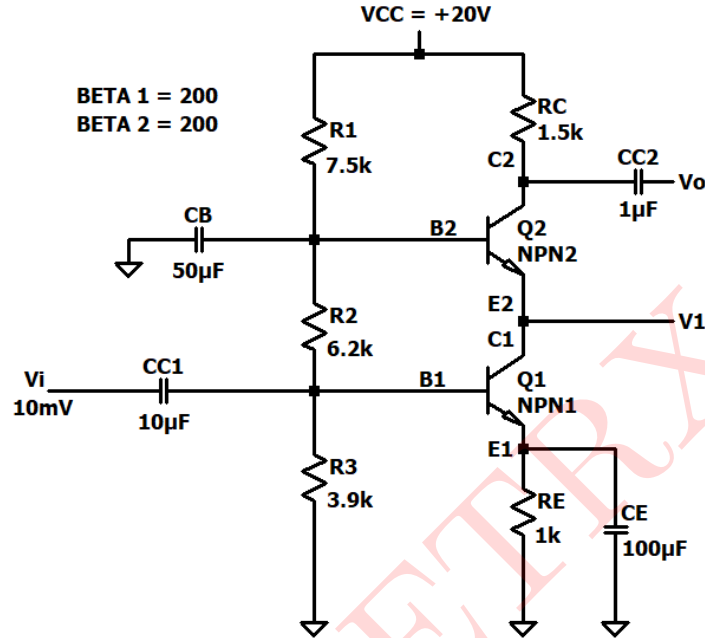


Figure 1: Circuit 1

Solution:

DC Analysis:

We open circuit all the capacitors as the frequency is $0Hz$,

$$\therefore X_C = \frac{1}{2\pi f_C} = \infty$$

Thus the circuit becomes as shown in figure 2,

$$\beta_1 = \beta_2 = 200; I_{C1} = I_{C2} = I_{E1} = I_{E2}$$

Assuming $I_{B1} = I_{B2}$ are very small,

$$\begin{aligned} V_{B1} &= \frac{R_3}{R_1 + R_2 + R_3} \times V_{CC} && [\text{Considering } I_{B2} \cong 0] \\ &= \frac{3.9k\Omega}{7.5k\Omega + 6.2k\Omega + 3.9k\Omega} \times 20V \\ &= \mathbf{4.4318V} \end{aligned}$$

$$\begin{aligned} V_{B2} &= \frac{R_3 + R_2}{R_1 + R_2 + R_3} \times V_{CC} && [\text{Considering } I_{B1} \cong 0] \\ &= \frac{3.9k\Omega + 6.2k\Omega}{7.5k\Omega + 6.2k\Omega + 3.9k\Omega} \times 20V = \mathbf{11.477V} \end{aligned}$$

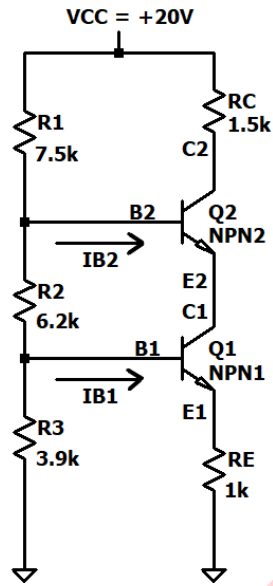


Figure 2: DC Equivalent Circuit

$$\begin{aligned}
 V_{E_1} &= V_{B_1} - V_{BE_1} \\
 &= 4.4318 - 0.7 \\
 &= \mathbf{3.7318V}
 \end{aligned}$$

$$[V_{BE_1} = V_{B_1} - V_{E_1}]$$

$$\begin{aligned}
 V_{E_1} &= I_{E_1} R_E \\
 I_{E_1} &= \frac{V_{E_1}}{R_E} = \frac{3.7318V}{1k\Omega} = \mathbf{3.7318mA}
 \end{aligned}$$

$$I_{C_1} = I_{C_2} = I_{E_1} = I_{E_2} = 3.7318mA$$

$$\begin{aligned}
 V_{C_2} &= V_{CC} - I_{C_2} R_C \\
 &= 20 - (3.7138mA \times 1.5k\Omega) \\
 &= \mathbf{14.4023V}
 \end{aligned}$$

$$\begin{aligned}
 V_{E_2} &= V_{B_2} - V_{BE_2} \\
 &= 11.477V - 0.7V \\
 &= \mathbf{10.777V}
 \end{aligned}$$

$$\begin{aligned}
 V_{CE_1} &= V_{C_1} - V_{E_1} \\
 &= 10.477 - 3.7318 \\
 &= \mathbf{7.045V}
 \end{aligned}$$

$$\begin{aligned}
 V_{CE_2} &= V_{C_2} - V_{E_2} \\
 &= 14.4023 - 10.777 \\
 &= \mathbf{3.625V}
 \end{aligned}$$

Small Signal Parameters:

$$\beta_1 = \beta_2 = \beta = 200, I_{CQ_1} = I_{CQ_2} = 3.7318mA$$

$$r_{\pi_1} = r_{\pi_2} = \frac{\beta V_T}{I_{CQ}} = \frac{200 \times 0.026V}{3.7318mA} = 1.393k\Omega$$

$$g_{m_1} = g_{m_2} = \frac{I_{CQ}}{V_T} = \frac{3.7318mA}{0.026V} = 143.53mA/V$$

Mid Frequency AC Equivalent Circuit:

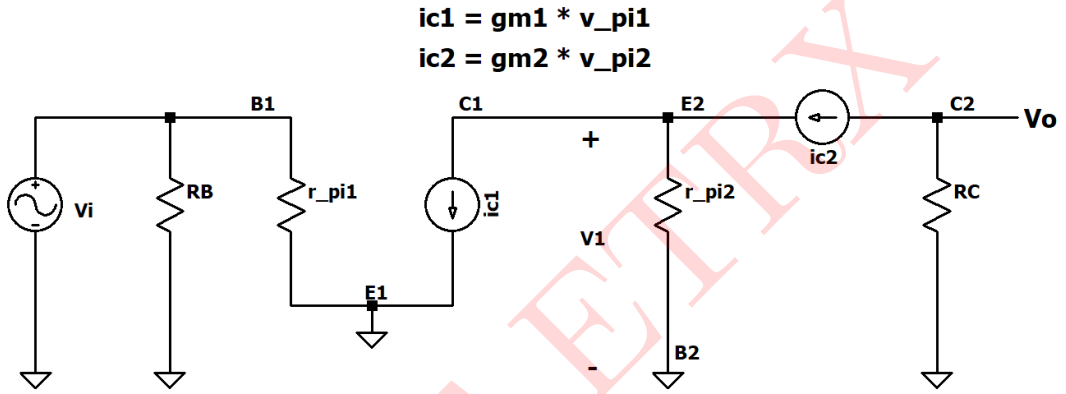


Figure 3: Small Signal Equivalent Circuit

$$\begin{aligned} R_B &= R_2 \parallel R_3 \\ &= 3.9k\Omega \parallel 6.2k\Omega \\ &= 2.394k\Omega \end{aligned}$$

Input Impedance of 1st stage (Z_i):

$$\begin{aligned} Z_i &= R_B \parallel r_{\pi_1} \\ &= 2.394k\Omega \parallel 1.393k\Omega \\ &= 880.6\Omega \end{aligned}$$

Output Impedance of 2nd stage (Z_o):

$$\begin{aligned} Z_o &= R_C = 1.5k\Omega \\ Z_o &= 1.5k\Omega \end{aligned}$$

Gain of CB stage : $Av_2 = \frac{V_o}{V_1}$

$$\begin{aligned} Av_2 &= g_m(R_C) \\ &= (143.53mA/V)(1.5k\Omega) \\ &= 215.295 \end{aligned}$$

Gain of CE stage : $Av_1 = \frac{V_1}{V_i}$

$$\begin{aligned} Av_i &= -g_m \left(\frac{r_\pi}{1 + \beta} \right) \\ &= -(143.53mA/V) \left(\frac{1.393k\Omega}{1 + 200} \right) \\ &= \mathbf{-0.9947} \end{aligned}$$

Overall Voltage Gain (A_{V_T}):

$$A_{V_T} = \frac{V_o}{V_i} = \frac{V_1}{V_i} \times \frac{V_o}{V_1}$$

$$\begin{aligned} A_{V_T} &= Av_1 \times Av_2 \\ &= (-0.9947) \times (215.295) \\ &= \mathbf{-214.1539} \end{aligned}$$

$$\begin{aligned} A_{V_T} \text{ in dB} &= 20 \log_{10} (|A_{V_T}|) \\ &= 20 \log_{10} (214.1539) \\ &= \mathbf{46.614dB} \end{aligned}$$

Output Voltage (V_o):

Input Voltage: $V_i = 10mV$ [peak to peak]

$$A_{V_T} = \frac{V_o}{V_i} \implies V_o = A_{V_T} \times V_i$$

$$\begin{aligned} \therefore V_o &= A_{V_T} \times V_i \\ &= -214.1539 \times 10mV \\ &= \mathbf{-2.14V} \text{ [peak to peak]} \end{aligned}$$

SIMULATED RESULTS

The above circuit is simulated in LTspice and results are presented below:

Results:

$$Av1 = V1/Vi = -9.76\text{mV}/10\text{mV} = -0.976$$

$$Av2 = Vo/V1 = -2\text{V}/-9.76\text{mV} = 204.918$$

$$Avt = Av1 * Av2 = 199.99$$

$$Avt(\text{dB}) = 46.02\text{dB}$$

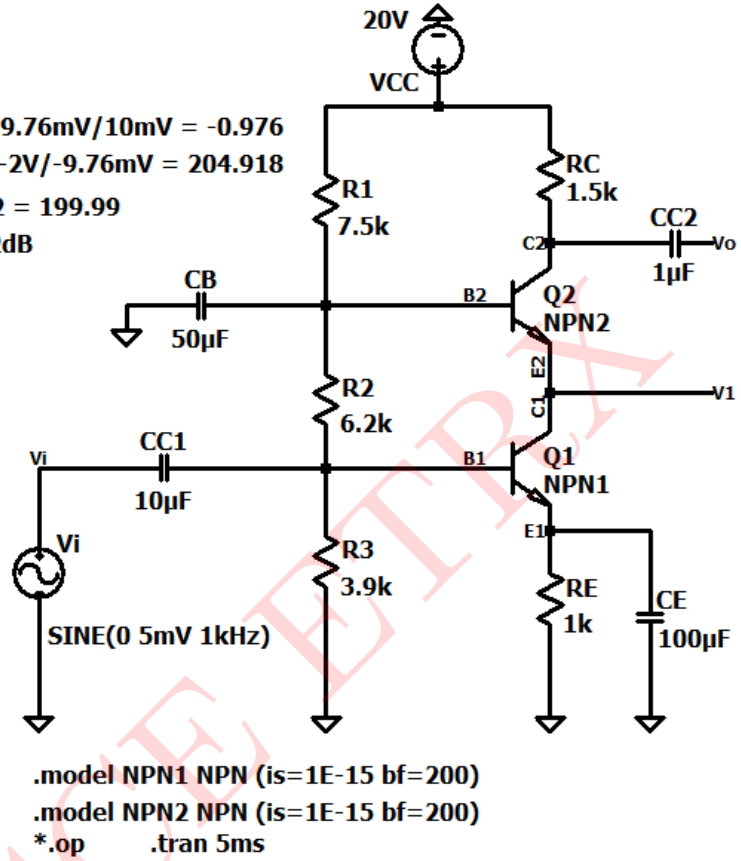


Figure 4: Circuit Schematic

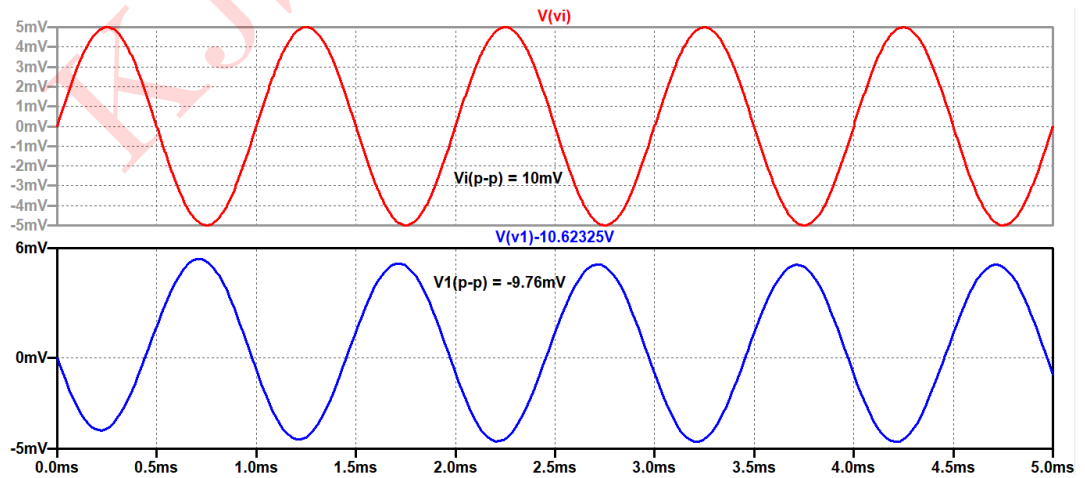


Figure 5: Input Output waveforms of 1st stage

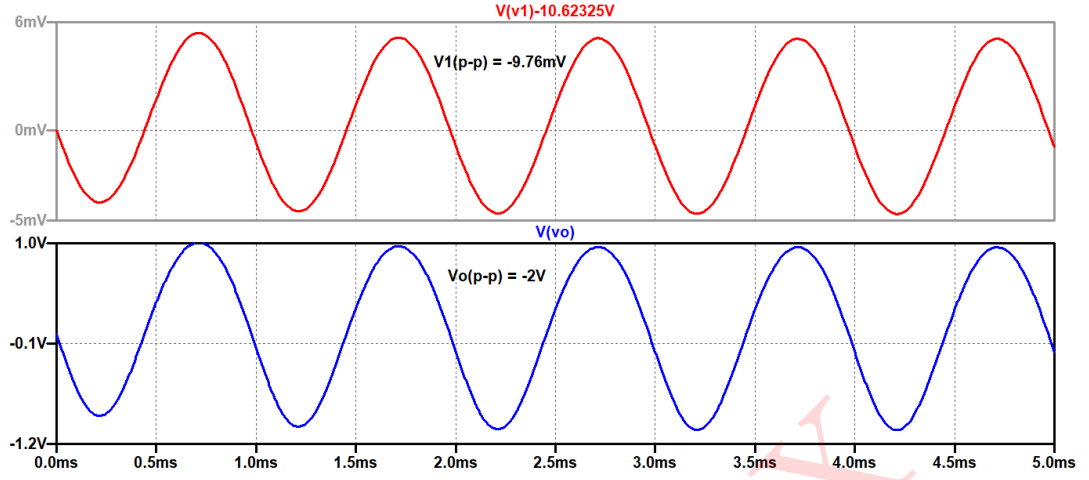


Figure 6: Input Output waveforms of 2nd stage

Comparison of Theoretical and Simulated results:

Parameters	Theoretical	Simulated
V_{B1}	4.4318V	4.34782V
V_{C1}	10.777V	10.6233V
V_{E1}	3.7318V	3.60015V
I_{C1}	3.7318mA	3.582mA
I_{B1}	18.659 μ A	17.9112 μ A
I_{E1}	3.7318mA	3.60015mA
V_{B2}	11.4777V	11.3708V
V_{C2}	14.4023V	14.6534V
V_{E2}	10.777V	10.6233V
I_{C2}	3.7318mA	3.56441mA
I_{B2}	18.659 μ A	17.822 μ A
I_{E2}	3.7318mA	3.58224mA
Voltage gain of 1 st stage: Av_1	-0.9947	-0.976
Voltage gain of 2 nd stage: Av_2	215.295	204.918
Overall Voltage gain: Av_T in dB	46.614dB	46.02dB
Input Impedance of 1 st stage: Z_i	880.6 Ω	—
Output Impedance of 2 nd stage: Z_o	1.5k Ω	—
Output Voltage: V_o	-2.14V	-2V

Table 1: Numerical 1

Numerical 2:

Determine the small signal voltage gain of the cascode circuit shown in figure 7. The transistors parameters are: $k_{n1} = k_{n2} = 0.8\text{mA/V}^2$, $V_{TN1} = V_{TN2} = 1.2\text{V}$ and $\lambda_1 = \lambda_2 = 0$

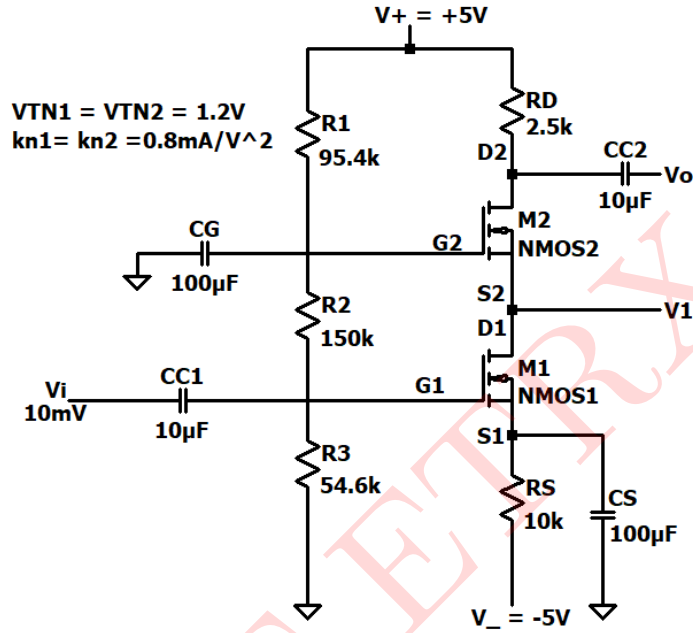


Figure 7: Circuit 2

Solution:

DC Analysis:

We open circuit all the capacitors as the frequency is 0Hz ,

$$\therefore X_C = \frac{1}{2\pi f_C} = \infty$$

Thus the circuit becomes as shown in figure 8,

Since $I_{G1} = I_{G2} = 0\text{A}$

$\therefore R_1, R_2$ & R_3 are in series

$$\begin{aligned} R_T &= R_1 + R_2 + R_3 \\ &= 95.4\text{k}\Omega + 150\text{k}\Omega + 54.6\text{k}\Omega \\ &= \mathbf{300\text{k}\Omega} \end{aligned}$$

$$\begin{aligned} V_{G1} &= \frac{R_3}{R_T} \times V_+ \\ &= \frac{54.6\text{k}\Omega}{300\text{k}\Omega} \times 5 \\ &= \mathbf{0.91\text{V}} \end{aligned}$$

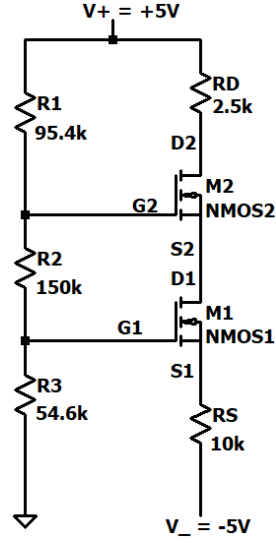


Figure 8: DC Equivalent Circuit

$$\begin{aligned}
 V_{G_2} &= \frac{R_2 + R_3}{R_T} \times V_+ \\
 &= \frac{54.6k\Omega + 150k\Omega}{300k\Omega} \times 5 \\
 &= \mathbf{3.41V}
 \end{aligned}$$

We know,

$$\begin{aligned}
 V_{GS_1} &= V_{G_1} - V_{S_1} \\
 &= 0.91 - V_{S_1}
 \end{aligned}$$

Applying KVL at the Source terminal of M_1 ,

$$\begin{aligned}
 V_{S_1} - I_{D_1} R_S &= V_- \\
 V_{S_1} &= I_{D_1} R_S + V_- = (10k)I_{D_1} - 5
 \end{aligned}$$

$$\begin{aligned}
 V_{GS_1} &= 0.91 - (10k)I_{D_1} + 5 \\
 &= 5.91 - (10k)I_{D_1}
 \end{aligned}$$

.....(1)

Also,

$$\begin{aligned}
 I_{D_1} &= k_{n_1}(V_{GS_1} - V_{TN_1})^2 \\
 &= (0.8mA/V^2)(V_{GS_1} - 1.2)^2
 \end{aligned}$$

.....(2)

Substitute equation (2) in equation (1),

$$\begin{aligned}
 V_{GS_1} &= 5.91 - 8(V_{GS_1}^2 - 2.4V_{GS_1} + 1.44) \\
 &= 5.91 - 8V_{GS_1}^2 + 19.2V_{GS_1} - 11.52
 \end{aligned}$$

$$8V_{GS_1}^2 - 18.2V_{GS_1} + 5.61 = 0$$

$$\therefore V_{GS_1} = 1.9V, 0.36V$$

$$\because V_{GS} > V_{TP}, \therefore V_{GS_1} = \mathbf{1.9V}$$

Thus, $I_{D_1} = k_n(V_{GS_1} - V_{TN_1})^2$

$$I_{D_1} = (0.8mA/V^2)(1.9V - 1.2V)^2 = 0.4mA$$

$$I_{D_1} = I_{D_2} = \mathbf{0.4mA}$$

$$\begin{aligned} V_{D_2} &= V_+ - I_{D_2}R_D \\ &= 5 - (0.4mA)(2.5k\Omega) \\ &= \mathbf{4V} \end{aligned}$$

$$\begin{aligned} V_{S_1} &= I_{D_1}R_S + V_- \\ &= (0.4mA)(10k\Omega) - 5 \\ &= \mathbf{-1V} \end{aligned}$$

$$\begin{aligned} V_{GS_1} &= V_{GS_2} = \mathbf{1.9V} \\ V_{GS_2} &= V_{G_2} - V_{S_2} \\ 1.9V &= 3.14V - V_{S_2} \\ V_{S_2} &= \mathbf{1.51V} \end{aligned}$$

$$\begin{aligned} V_{DS_2} &= V_{D_2} - V_{S_2} \\ &= 4V - 1.51V \\ &= \mathbf{2.49V} \end{aligned}$$

$$V_{D_1} = V_{S_2} = \mathbf{1.51V}$$

$$\begin{aligned} V_{DS_1} &= V_{D_1} - V_{S_1} \\ &= 1.51V - (-1) \\ &= \mathbf{2.51V} \end{aligned}$$

Small Signal Parameters:

$$k_n = k_{n_1} = k_{n_2} = 0.8mA/V^2, V_{GS} = V_{GS_1} = V_{GS_2} = 1.9V, V_{TN} = V_{TN_1} = V_{TN_2} = 1.2V$$

$$g_{m_1} = g_{m_2} = 2k_n(V_{GS} - V_{TN}) = 2(0.8mA/V^2)(1.9 - 1.2) = \mathbf{1.12mA/V}$$

AC (Mid Frequency) Equivalent Circuit:

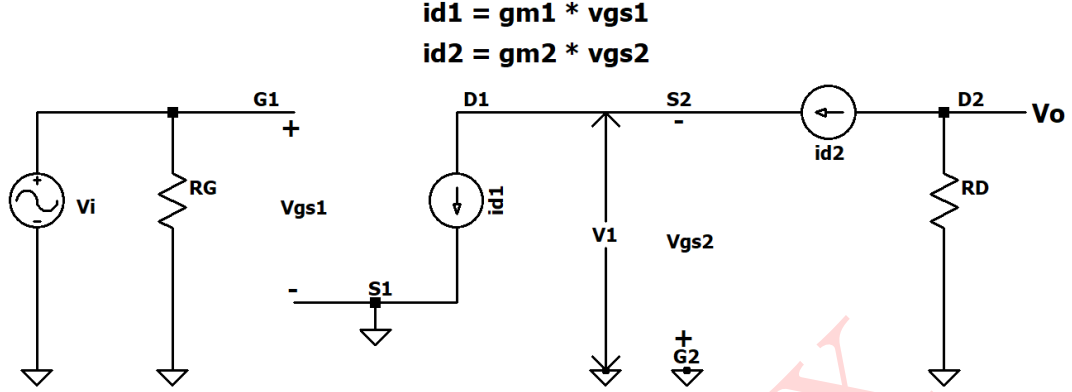


Figure 9: Small Signal Equivalent Circuit

$$\because V_{gs1} = V_{gs2} \quad \& \quad g_{m1} = g_{m2}$$

$$g_{m1} V_{gs1} = g_{m2} V_{gs2}$$

$$R_G = R_2 \parallel R_3$$

$$Z_i = R_G = R_2 \parallel R_3 = 150k\Omega \parallel 54.6k\Omega = 40k\Omega$$

$$Z_o = R_D = 2.5k\Omega$$

Voltage Gain of second stage : $Av_2 = \frac{V_o}{V_1}$

$$\begin{aligned} Av_2 &= \frac{-g_{m2} V_{gs2} R_D}{-V_{gs2}} \\ &= g_{m2} R_D \\ &= (1.12mA/V)(2.5k\Omega) \\ &= 2.8 \end{aligned}$$

Voltage Gain of first stage : $Av_1 = \frac{V_1}{V_i}$

$$\begin{aligned} Av_1 &= \frac{V_1}{V_i} = \frac{-V_{gs2}}{V_{gs1}} = \frac{-V_{gs1}}{V_{gs1}} = -1 \\ Av_1 &= -1 \end{aligned}$$

Overall Voltage Gain (A_{V_T}):

$$A_{V_T} = \frac{V_o}{V_s}$$

$$A_{V_T} = Av_1 \times Av_2 = -2.8$$

$$\begin{aligned}
A_{V_T} \text{ in dB} &= 20 \log_{10} (|A_{V_T}|) \\
&= 20 \log_{10} (2.8) \\
&= \mathbf{8.943\text{dB}}
\end{aligned}$$

Output Voltage (V_o):

$$A_{V_T} = \frac{V_o}{V_i} \implies V_o = A_{V_T} \times V_i$$

Input Voltage: $V_i = 10\text{mV}$ [peak to peak]

$$\begin{aligned}
\therefore V_o &= A_{V_T} \times V_i \\
&= -2.8 \times 10\text{mV} \\
&= \mathbf{-28\text{mV}} \text{ [peak to peak]}
\end{aligned}$$

SIMULATED RESULTS

The above circuit is simulated in LTspice and results are presented below:

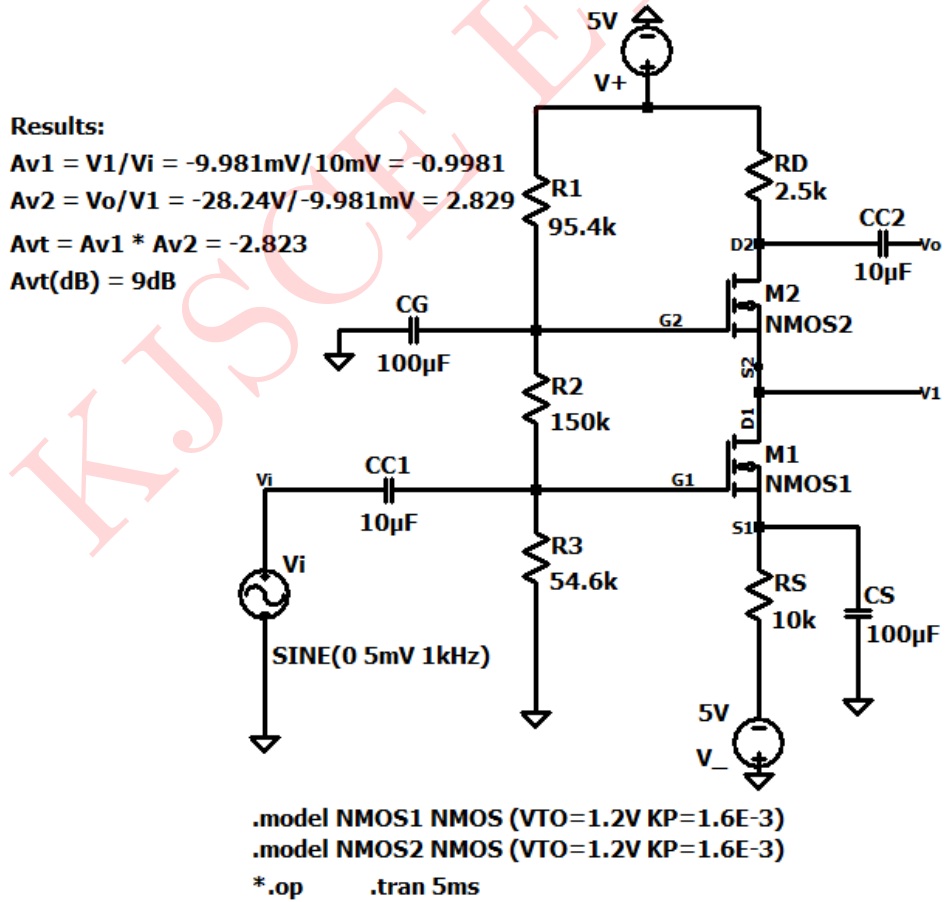


Figure 10: Circuit Schematic

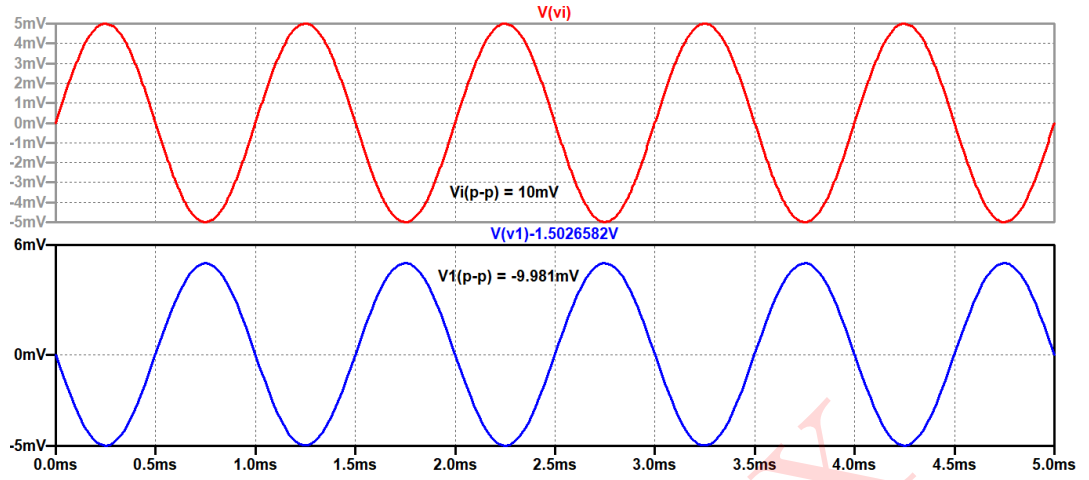


Figure 11: Input Output waveforms of 1st stage

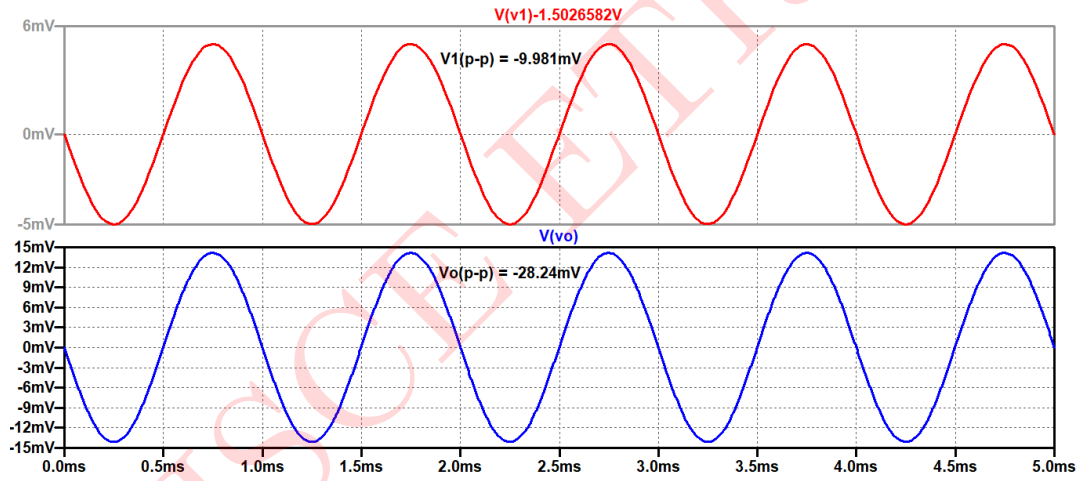


Figure 12: Input Output waveforms of 2nd stage

Comparison of Theoretical and Simulated results:

Parameters	Theoretical	Simulated
V_{G1}, V_{G2}	0.91V, 3.41V	0.91V, 3.41V
V_{D1}, V_{D2}	1.51V, 4V	1.502V, 3.999V
V_{S1}, V_{S2}	-1V, 1.51V	-0.997V, 1.502V
I_{D1}, I_{D2}	0.4mA, 0.4mA	0.4mA, 0.4mA
Voltage gain of 1 st stage: Av_1	-1	-0.9981
Voltage gain of 2 nd stage: Av_2	2.8	2.829
Overall Voltage gain: Av_T in dB	8.934dB	9dB
Input Impedance of 1 st stage: Z_i	40k Ω	—
Output Impedance of 2 nd stage: Z_o	2.5k Ω	—
Output Voltage: V_o	-28mV[peak to peak]	-28.24mV[peak to peak]

Table 2: Numerical 2
