
Switched-capacitor filters

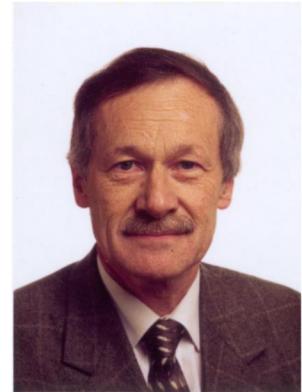


Willy Sansen

KULeuven, ESAT-MICAS

Leuven, Belgium

willy.sansen@esat.kuleuven.be



Willy Sansen 10-05 N171

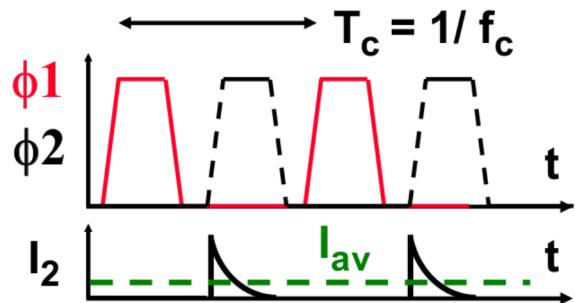
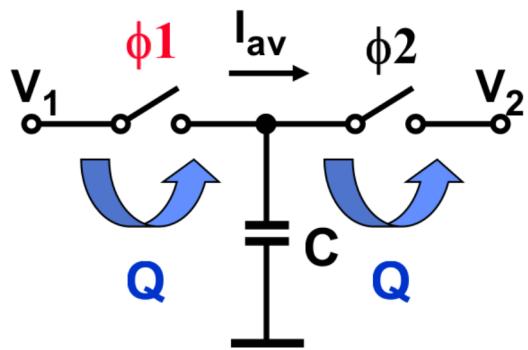
Switched-Capacitor Filters

- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - MOST switches
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Willy Sansen 10-05 N172

Principle



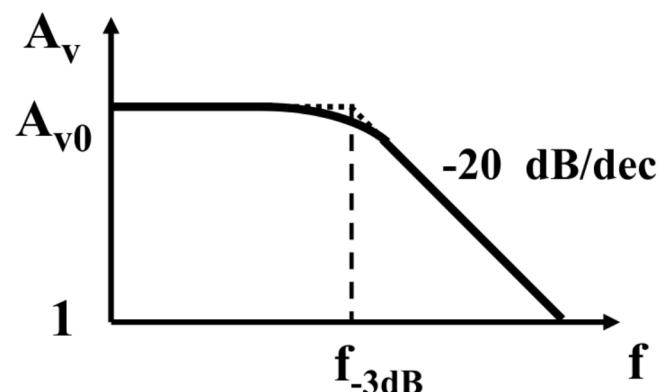
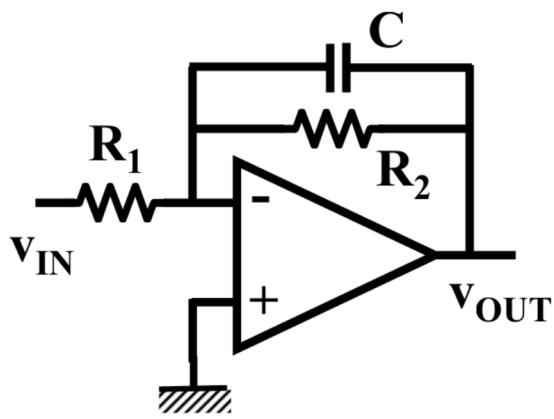
$$I_{av} = \frac{Q_{av}}{T_c} = \frac{C(V_1 - V_2)}{T_c}$$

$$I_{av} = \frac{(V_1 - V_2)}{R}$$

- Non overlapping clocks
 - Switches are MOSTs
- $$R = \frac{T_c}{C} = \frac{1}{f_c C}$$

For $C = 1 \text{ pF}$ & $f_c = 100 \text{ kHz}$ $R = 10 \text{ M}\Omega$

Low-Pass Filter with R's and C



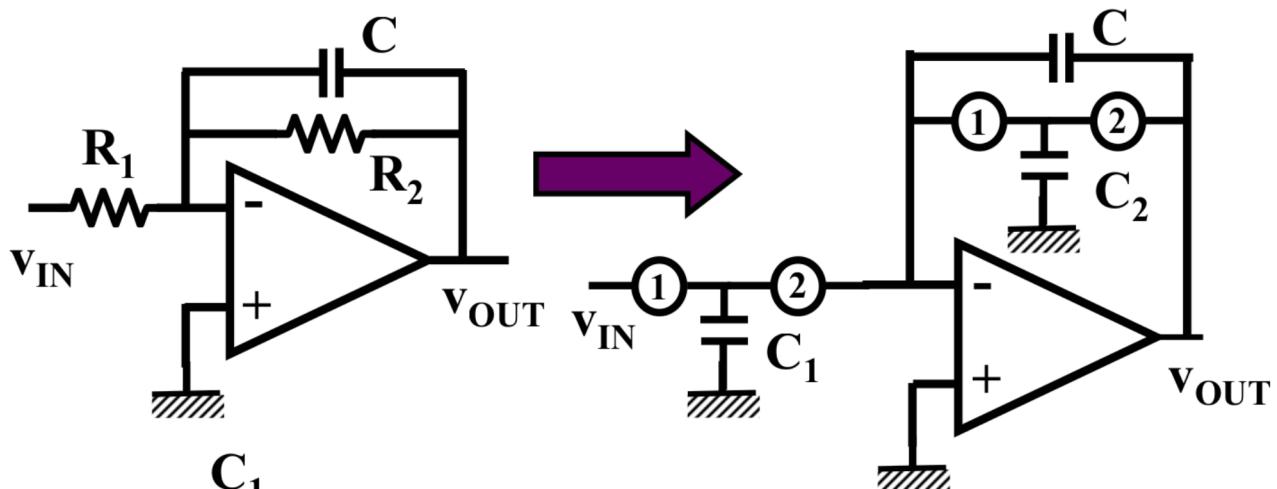
$$A_{v0} = \frac{R_2}{R_1}$$

Ratio's of R: 0.5% accuracy

$$f_{-3db} = \frac{1}{2\pi R_2 C}$$

Absolute value of RC : 20 % accuracy

Low-Pass Filter with switched C's



$$A_{v0} = \frac{C_1}{C_2}$$

$$f_{-3\text{db}} = \frac{f_c}{2\pi} \frac{C_2}{C}$$

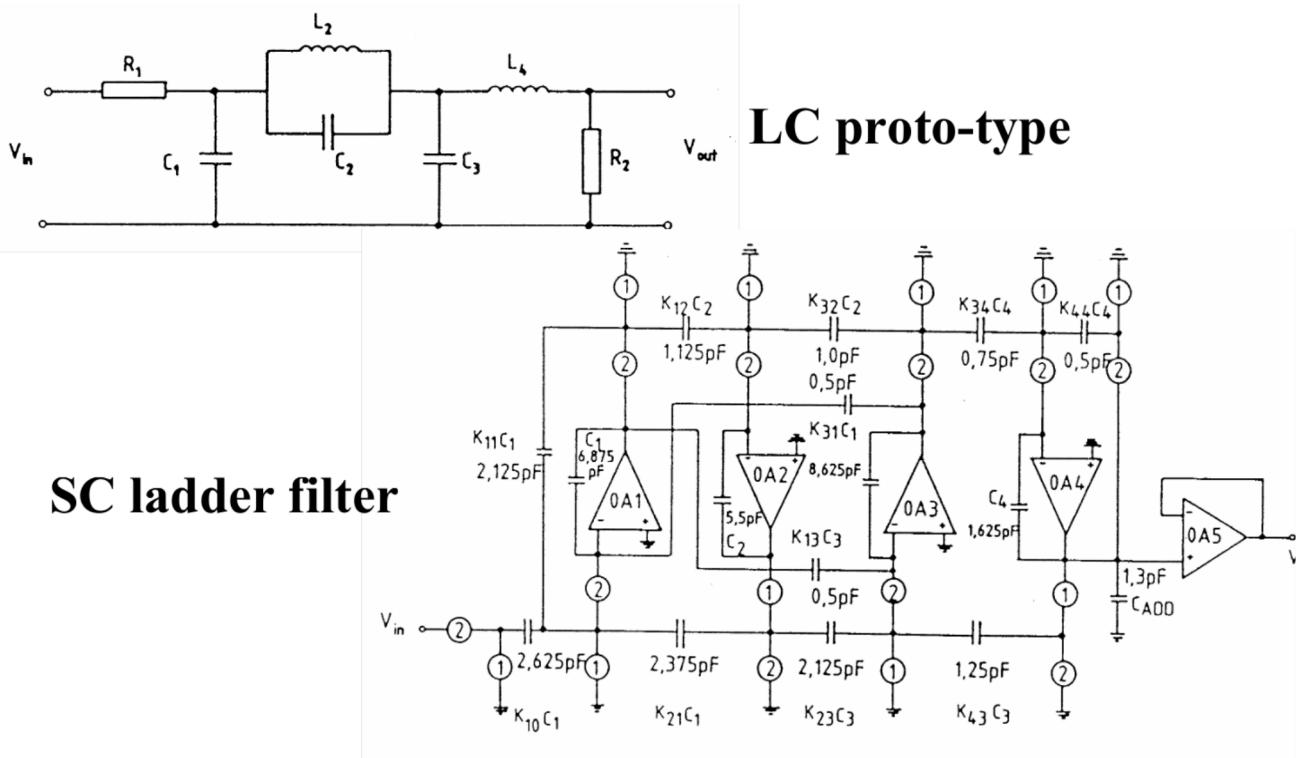
High accuracy: only ratio's of C: 0.2%

Only capacitors to drive : low power !

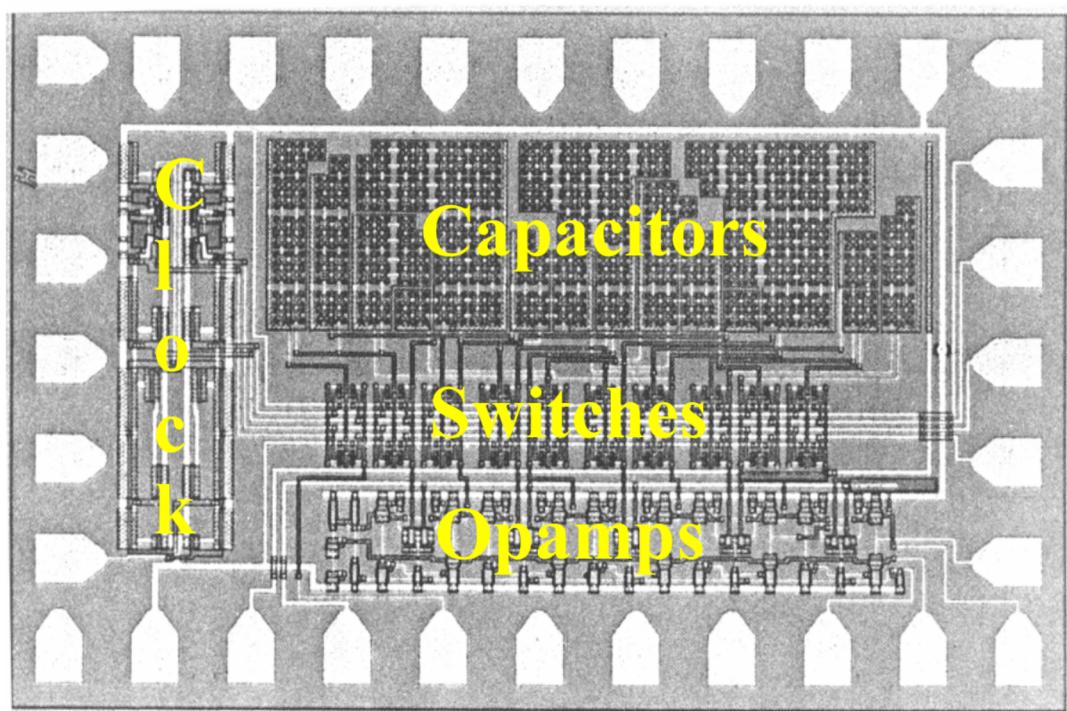
Tunable & easy to integrate !

But : only for frequencies << f_c

Example of 4th-Order SC Low-Pass filter



4th-Order SC Low-Pass filter

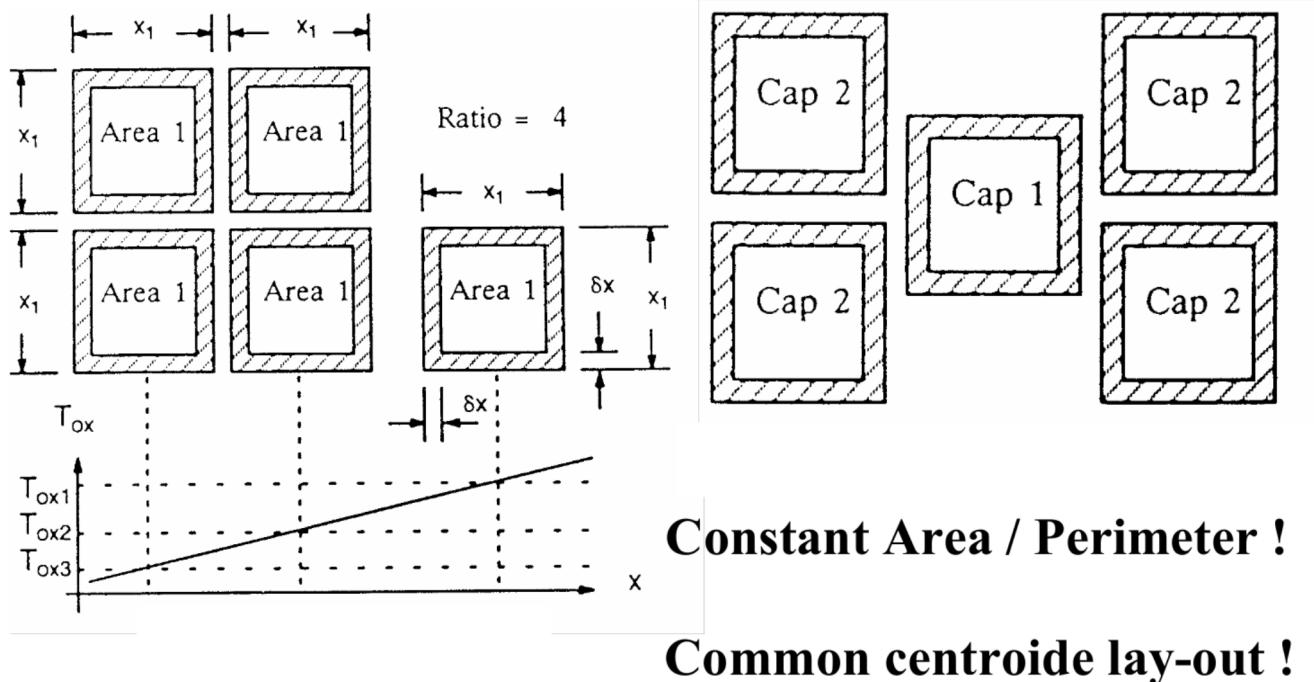


Switched-Capacitor Filters

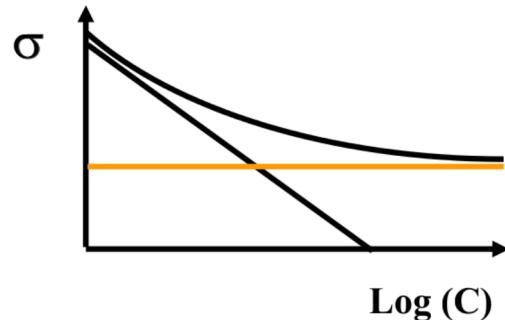
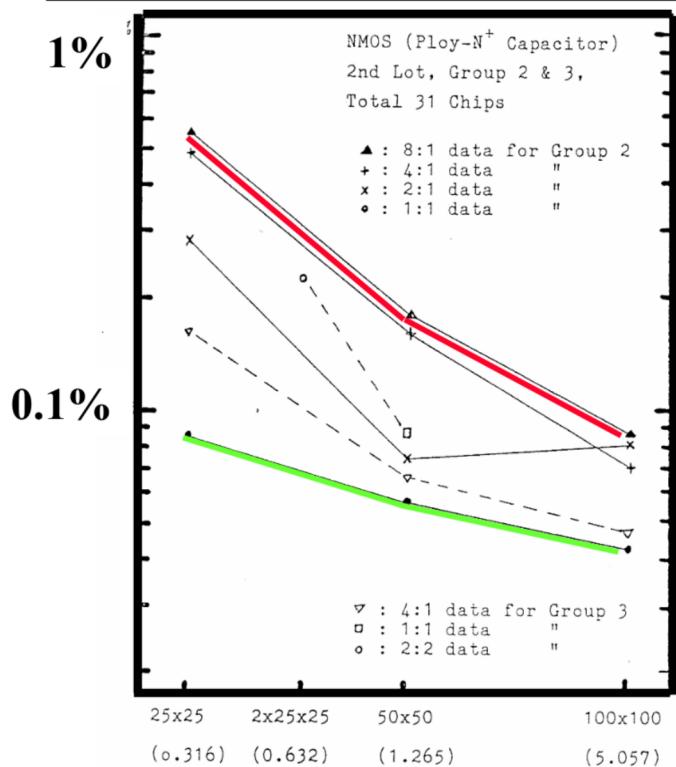
- Introduction : principle
- Technology:
 - MOS capacitors
 - MOST switches
- SC Integrator
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- SC Filters : LC ladder / bi-quadratic section
- Opamp requirements
 - Charge transfer accuracy
 - Noise
- Switched-current filters

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Capacitor Matching

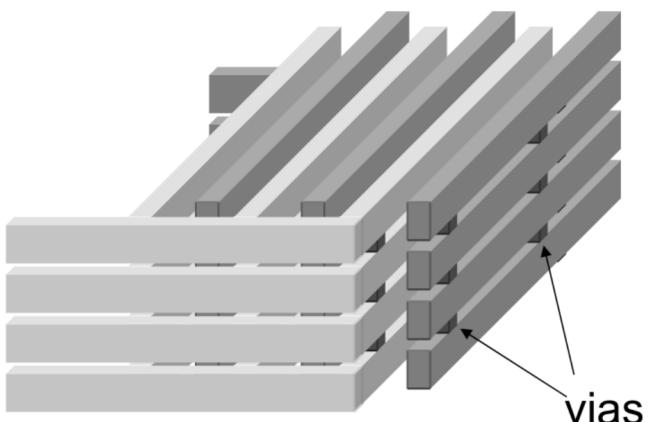
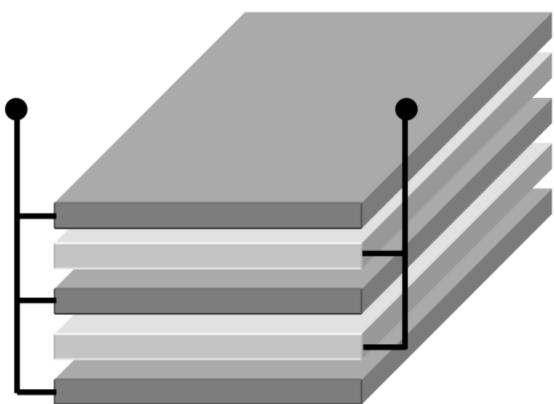


Random Error (σ)



local vs **global** t_{ox} effects

Capacitances in nanometer CMOS



- **MIM capacitors**
- **5 metal layers, $0.35 \text{ fF}/\mu\text{m}^2$**
- **Excellent matching**
- **Digital technology, no MIM cap.**
- **lateral metal-metal capacitance**
- **8 metal layers, $1.7 \text{ fF}/\mu\text{m}^2$**
- **Good matching**

Aparicio, JSSC March 02, 384-393

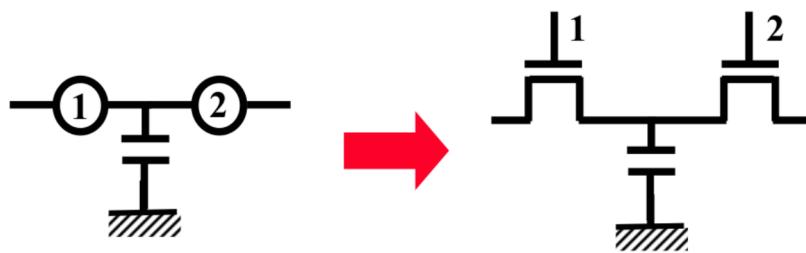
Willy Sansen 10-05 N1712

Switched-Capacitor Filters

- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - **MOST switches**
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

A MOST as a switch



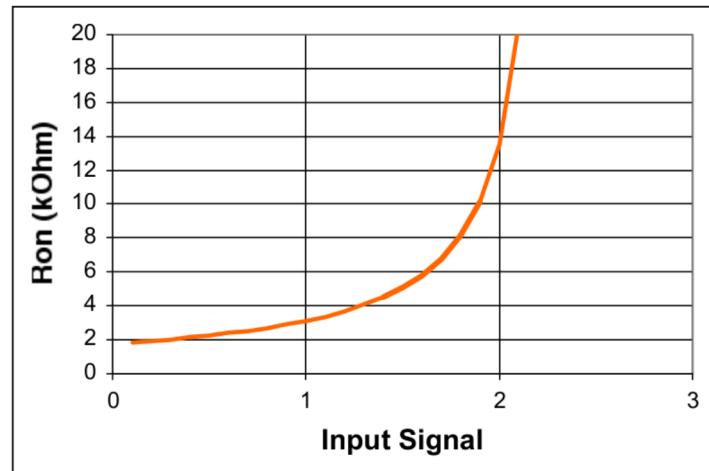
$$R_{on} = \frac{1}{K_P n \frac{W}{L} (V_h - V_T - V_{sign})}$$

$W = 2 \mu\text{m}$ $L = 0.7 \mu\text{m}$

$K_P n = 80 \mu\text{A/V}^2$

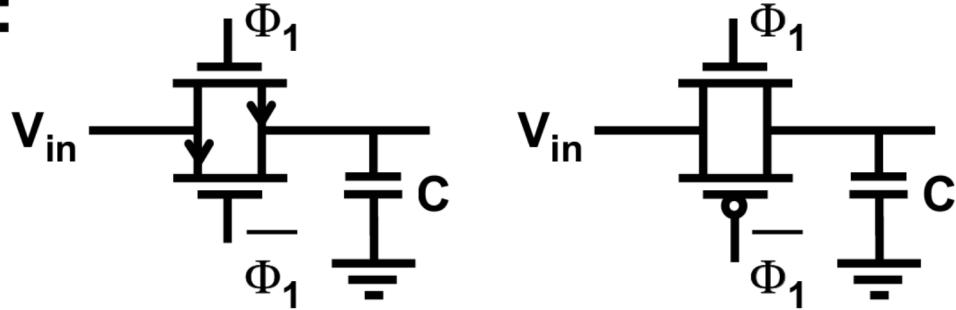
$V_T = 0.7 \text{ V}$

$V_h = 3 \text{ V}$



Double Switch or transmission gate

Switch:

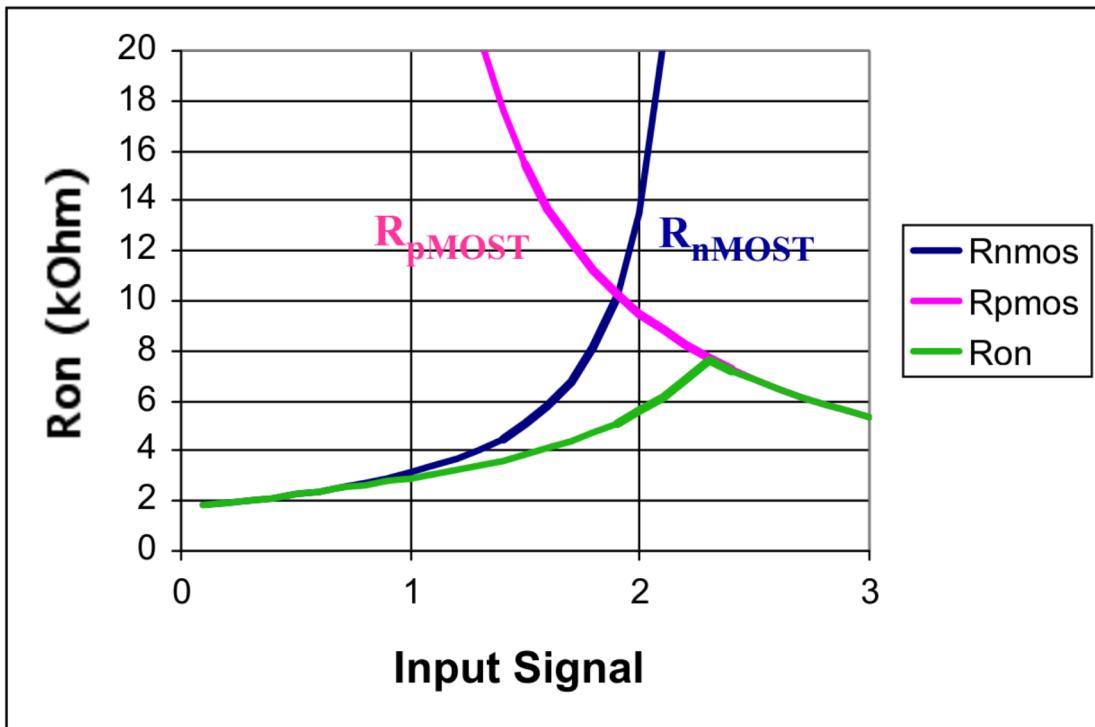


nMOS: $V_{in} < V_{DD} - V_{GS,n} \approx V_{DD} - 0.7 \text{ V}$

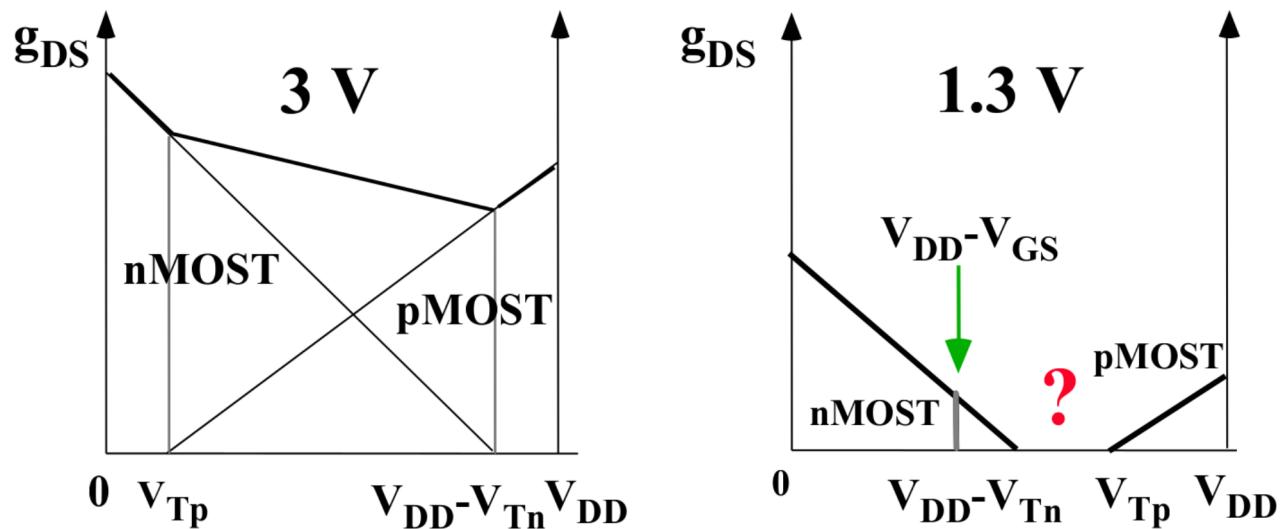
pMOS: $V_{in} > V_{GS,p} \approx 0.7 \text{ V}$

Minimum $V_h = V_{DD}$: $V_{DD} - V_{GS,n} = V_{GS,p} \Rightarrow V_{DD} > 1.4 \text{ V}$

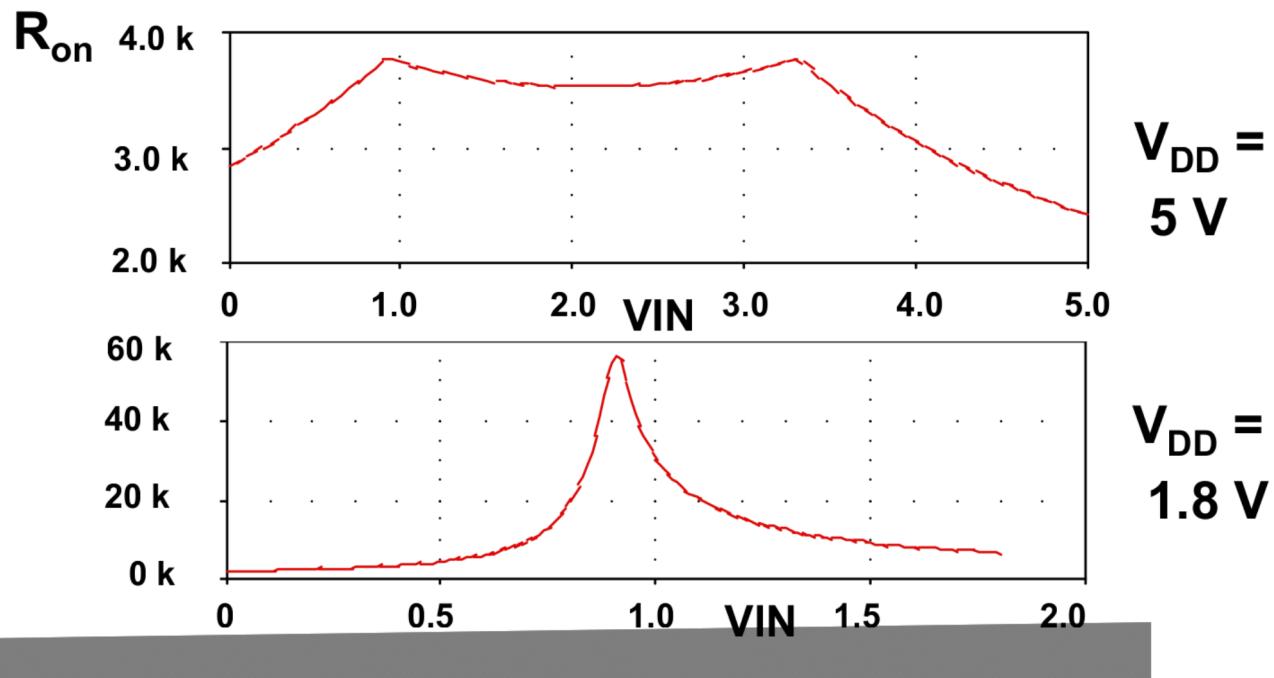
Double Switch



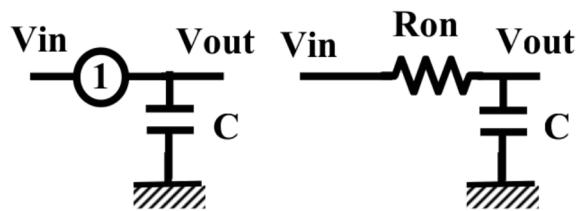
Low Voltage SC : MOST-Switch



Low Voltage SC : MOST-Switch



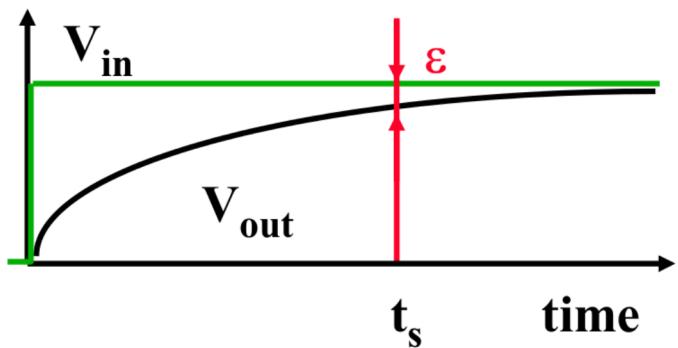
Time constant of Ron



$$V_{\text{out}} = V_{\text{in}} \left(1 - \exp\left(-\frac{t}{RC}\right)\right)$$

$$t_s = RC \ln(1/\varepsilon)$$

$$t_s \approx 7 RC \text{ for } \varepsilon = 0.1 \%$$



Speed ↓ if
large C (low noise)
large R (small switch)

Maximum frequency of operation

For $W/L = 2$ and $V_{GS} - V_T \approx 1 \text{ V}$

$R_{on} \approx 10 \text{ k}\Omega$

For $C \approx 1 \text{ pF}$

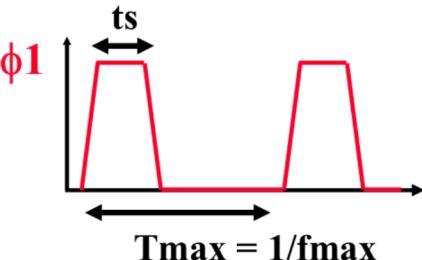
For $\varepsilon \approx 0.1\%$

$t_s = 7 \text{ RC} \approx 70 \text{ ns}$

$T_c = 140 \text{ ns} \Rightarrow f_{max} \approx 7 \text{ MHz}$

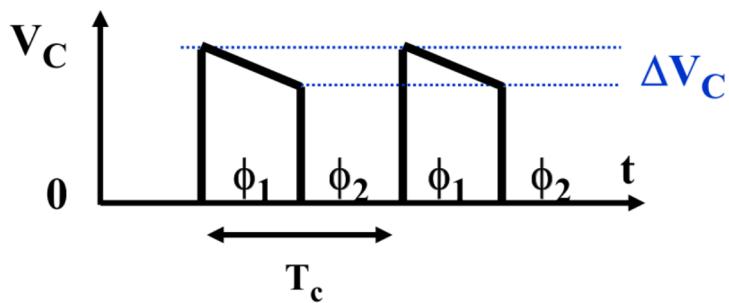
Due to only one switch

\Rightarrow practical $f_{max} : 1-10 \text{ MHz}$



$L \downarrow \Rightarrow R_{on} \downarrow$

Minimum frequency of operation



$$\text{Leakage } i = C \frac{dV_C}{dt}$$

i is 10 nA/cm^2 at 25°
is $10 \mu\text{A/cm}^2$ at 125°

For $C_{\min} \approx 0.25 \text{ pF}$ (mismatch)

$\Delta V_C = 1\%$ of 0.1 V or $\Delta V_C = 1 \text{ mV}$

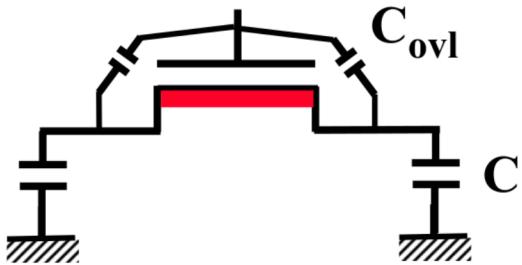
For $10 \times 1 \mu\text{m}$: 2 fA (25°)
or 2 pA (125°)

$$dt = T_c/2 \text{ with } T_c = 1/f_{c\min}$$

$$f_{c\min} = \frac{i}{2 C_{\min} \Delta V_C} = 4 \text{ Hz or } 4 \text{ kHz } (125^\circ)$$

Clock Feed-Through

Overlap Capacitors



$$C_{ovl} \approx W C_{ovlo}$$

$W \uparrow \Rightarrow R \downarrow$ but $C_{ovl} \uparrow$

Example : $W = 3\mu m$ $L = 0.7\mu m$

$$C_{ovlo} = 0.5 \text{ fF}/\mu m$$

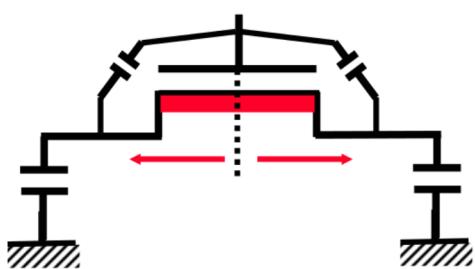
$$\Rightarrow C_{ovl} \approx 1 \text{ fF}$$

$$\Delta V: Q = C_{ovl} (V_h - V_l) \approx 1 \text{ fF} \cdot 3 \text{ V} \approx 3 \text{ fC}$$

$$\Rightarrow \Delta V \approx \frac{Q}{C} \approx 3 \text{ fC}/1 \text{ pF} \approx 3 \text{ mV}$$

Charge redistribution

Inversion layer charge



$$Q_m \approx C_{ox} WL(V_h - V_{sign} - V_T)$$

$$\text{Ex. } W = 3\mu\text{m } L = 0.7\mu\text{m}$$

$$C_{ox} = 1.6 \text{ fF}/\mu\text{m}^2$$

$$V_T = 0.7\text{V } V_{sign} = 1.5\text{V}$$

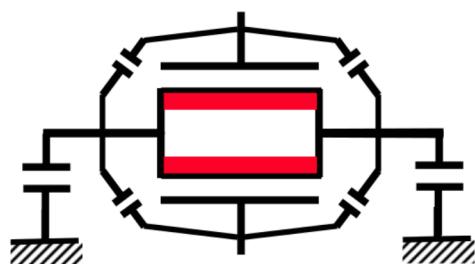
$$\Rightarrow Q \approx 6 \text{ fC}$$

ΔV : Half is stored in each cap

$$\Rightarrow \Delta V \approx Q/2C \approx 3 \text{ fC}/1\text{pF} \approx 3 \text{ mV}$$

Total: $\Delta V \approx 10 \text{ mV/pF}$ $C \uparrow \Rightarrow CD \downarrow \text{ Speed} \downarrow \text{ Power} \uparrow$

Clock injection & Charge redistribution

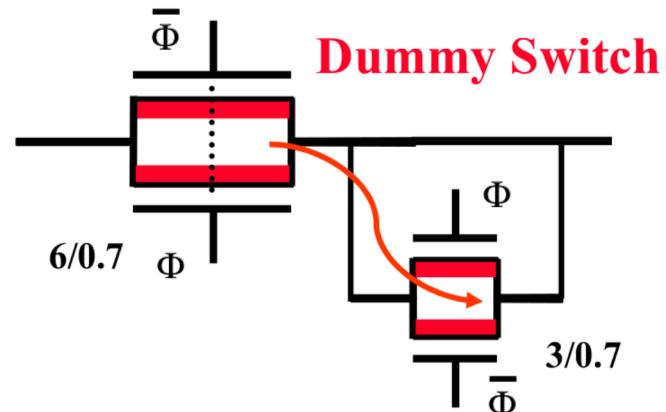


If

$$C_{ovl,n} = C_{ovl,p}$$

No Clock FT !

Problems: matching
 $W_n = W_p$?

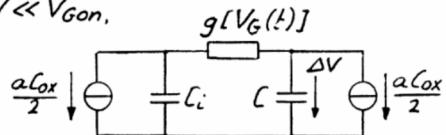


OK if Q is split equal 1/2

Problems: clock skew
rise/fall time
impedance

Quantitative Charge Redistribution

If $\Delta V \ll V_{Gon}$,
then:



$$\beta = \mu_{Cox} \cdot W/L$$

$$a = dV/dt$$

V_{Te} = effective V_T
(with bulk effect)

$$C_i/C$$

$C_i \ll C, B \gg 1$

$$\Delta Q \rightarrow Q$$

\Rightarrow Dummy

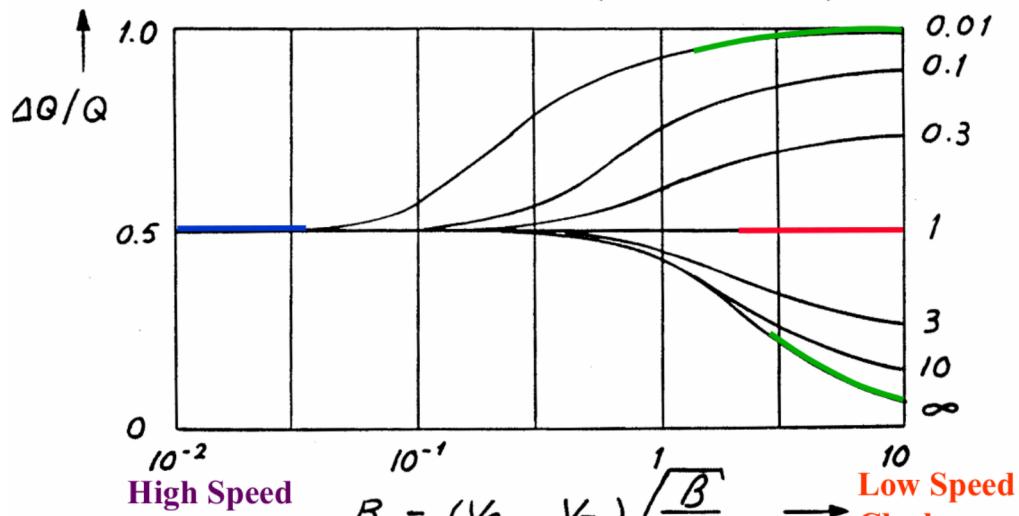
$C_i = C: \Delta Q = Q/2$

\Rightarrow Dummy

$C_i \gg C, B \gg 1$

$$\Delta Q \rightarrow 0$$

NO dummy

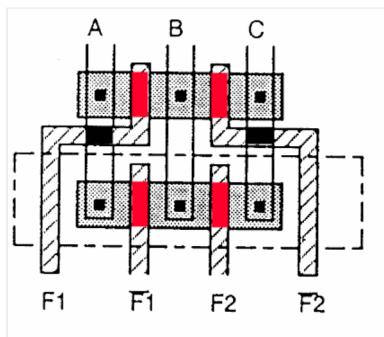


$$B = (V_{Gon} - V_{Te}) \sqrt{\frac{\beta}{\alpha C}}$$

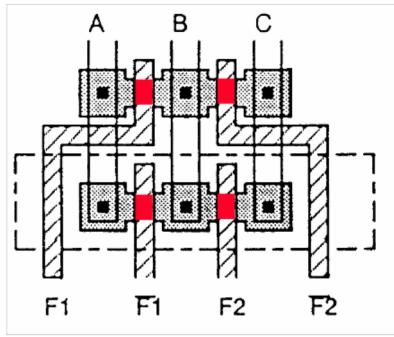
$B \ll 1 : \Delta Q = Q/2 \Rightarrow$ Dummy

Ref. Wegmann, Vittoz,
JSSC Dec.87, 1091-1097

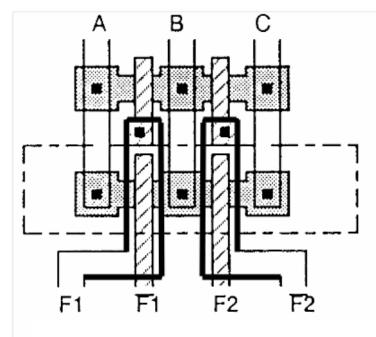
Layout considerations



Parasitic C
↓
CFT



Reduce C_{ox} area



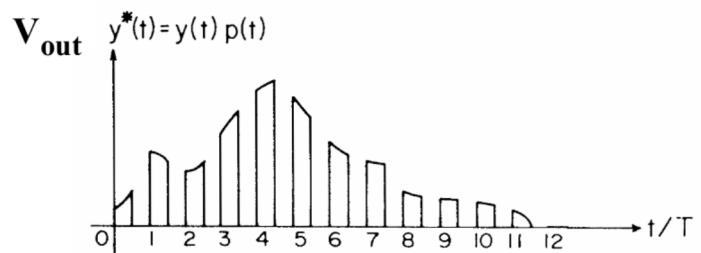
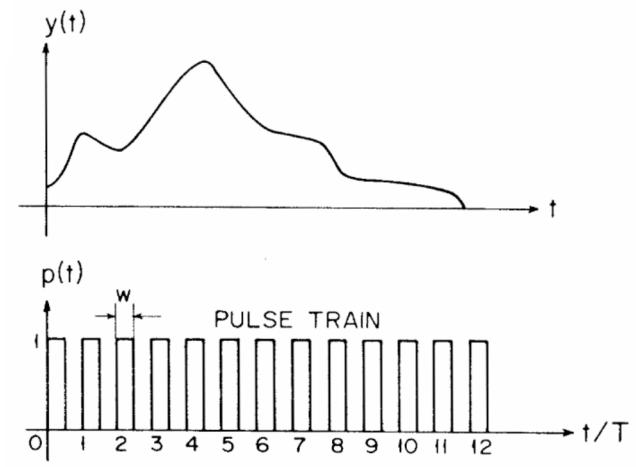
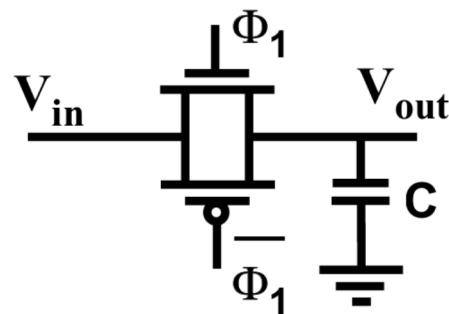
Use metal to
‘shield’
clock lines

Switched-Capacitor Filters

- Introduction : principle
- Technology:
 - MOS capacitors
 - MOST switches
- SC Integrator
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- SC Filters : LC ladder / bi-quadratic section
- Opamp requirements
 - Charge transfer accuracy
 - Noise
- Switched-current filters

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Sampling analog signals

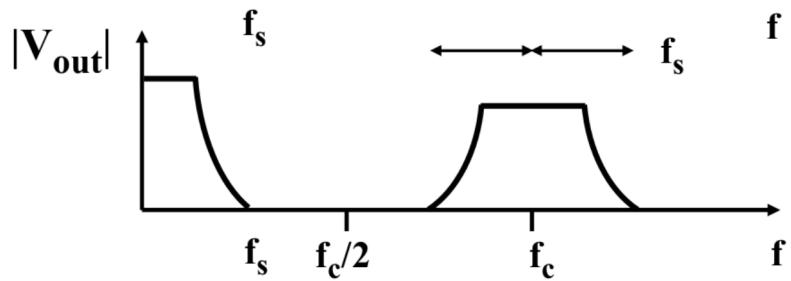


Spectra

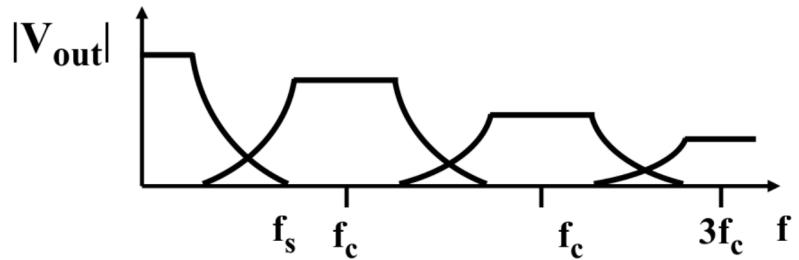
Input signal v_{in}



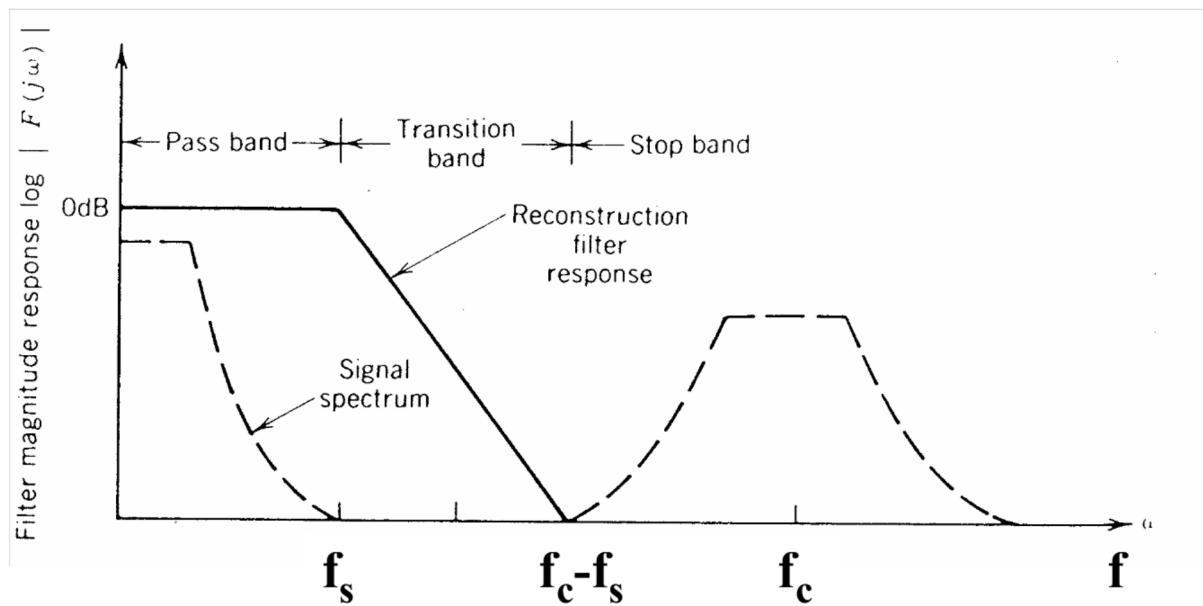
Sampled signal
 $f_c/2 \gg f_{signal}$



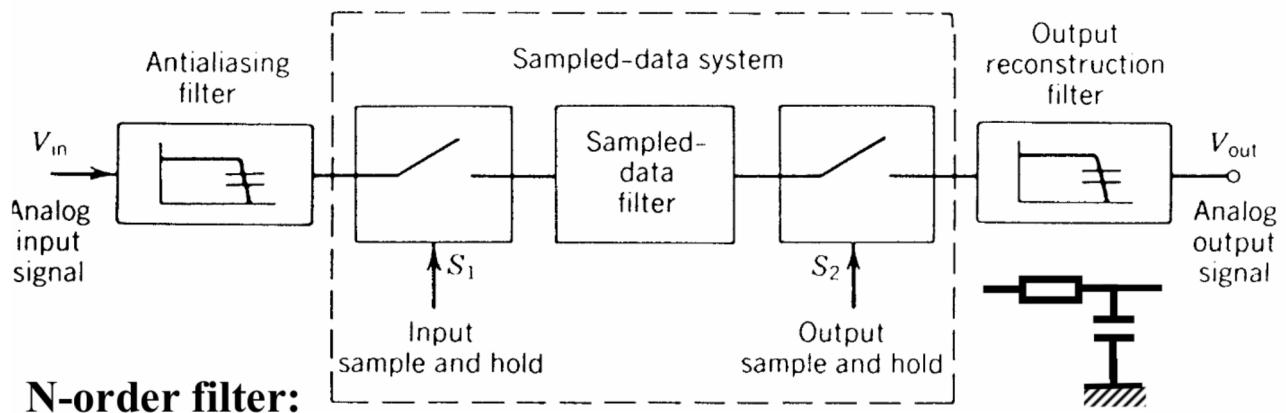
Sampled signal
 $f_c/2 < f_{signal}$
Nyquist !



Anti-Aliasing filter



Anti-aliasing / Reconstruction



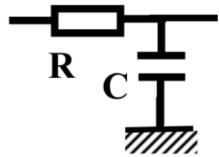
N-order filter:

$$\left[\frac{f_s}{f_c - f_s} \right]^N = 10^{\frac{-\text{Attenuation}}{20}} \quad f_c = f_s \cdot 10^{\frac{\text{Attenuation}}{20 \cdot N}}$$

Ex. Attenuation = 40 dB; $f_s = 10$ kHz ; $N = 1 \Rightarrow f_c = 1$ MHz

Sampled Data Basics : z-transform

Analog System: $s = j\omega$



$$\frac{V_{out}}{V_{in}} = \frac{1}{1 + sRC}$$

| z-TRANSFORM | SEQUENCE |
|-----------------------|-----------------|
| $a X(z) + b V(z)$ | $ax(n) + bv(n)$ |
| $z^{-n_1} Y(z)$ | $y(n - n_1)$ |
| $Y(z/b)$ | $b^n y(n)$ |
| $-z \frac{dY(z)}{dz}$ | $n y(n)$ |
| $Y(z^{-1})$ | $y(-n)$ |
| $X(z) V(z)$ | $x(n) * v(n)$ |

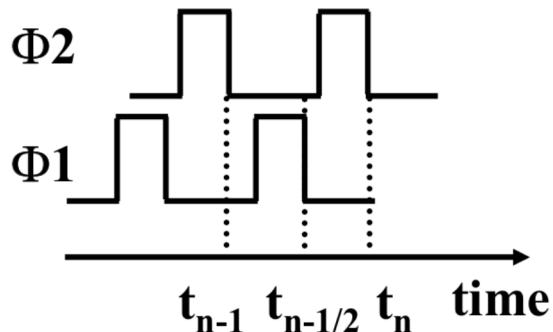
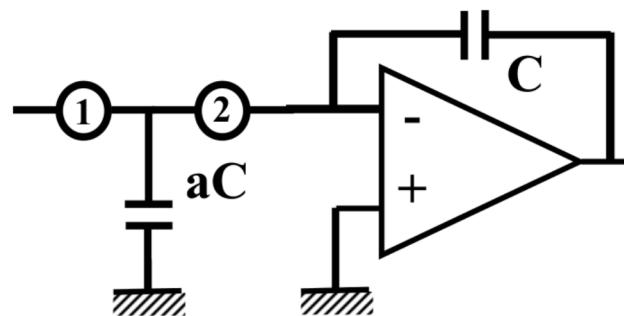
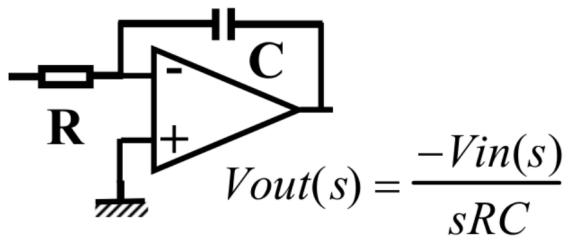
Sampled data: z-transforms

1 delay is z^{-1}

$$z = e^{j\omega T_c} = e^{j \frac{2\pi f}{f_c}}$$

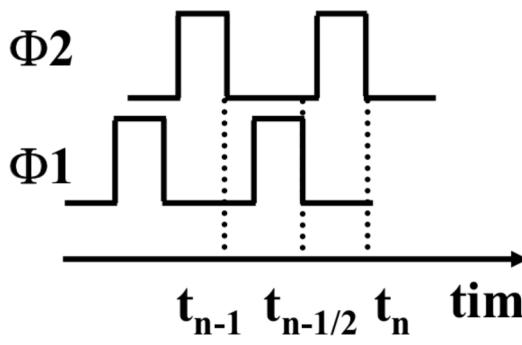
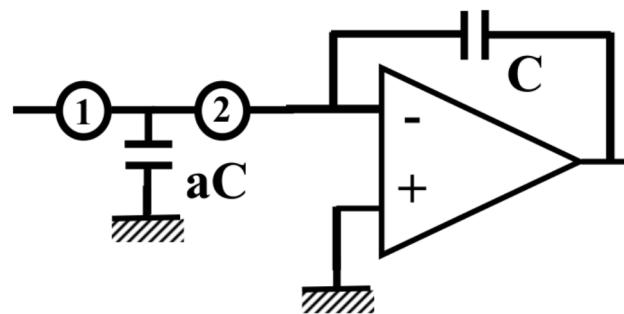
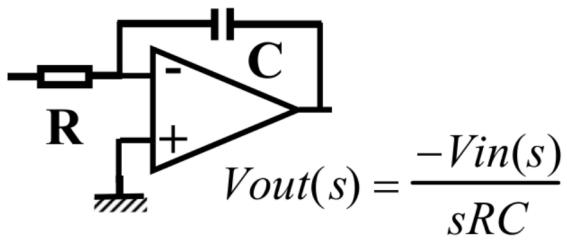
$$e^{j\omega T_c} = 1 + j\omega T_c + \frac{(j\omega T_c)^2}{2} + \dots \quad \text{if } \omega T_c \ll 1$$

SC-Integrator in phase 1



Φ_1 $Q_{aC1} = aC V_{in}(n-1/2)$
 $Q_{C1} = - C V_{out}(n-1)$
 $V_{out}(n-1/2) = V_{out}(n-1)$

SC-Integrator in phase 2 : charge conservation



$$\begin{aligned} \Phi_2 \quad & Q_{aC2} = 0 \\ & Q_{C2} = -C V_{out}(n) \\ & Q_{aC2} + Q_{C2} = Q_{aC1} + Q_{C1} \\ -C V_{out}(n) &= aC V_{in}(n-1/2) \\ & -C V_{out}(n-1) \end{aligned}$$

SC-Integrator : approximate transfer function

$$- C V_{\text{out}}(n) = aC V_{\text{in}}(n-1/2) - C V_{\text{out}}(n-1)$$

$$V_{\text{out}}(n-1) = z^{-1} V_{\text{out}}$$

$$\Rightarrow C \cdot V_{\text{out}} = z^{-1} C V_{\text{out}} - z^{-1/2} a C V_{\text{in}}$$

$$\frac{V_{\text{out}}}{V_{\text{in}}} = -a \frac{z^{-1/2}}{1 - z^{-1}} \quad z^{-1} = e^{-j\omega T_c} \approx 1 - j\omega T_c$$

$$\Rightarrow \frac{V_{\text{out}}}{V_{\text{in}}} \approx -\frac{a(1 - j\cancel{\omega T_c}/2)}{j\omega T_c} \approx -\frac{a}{j\omega T_c}$$

Integrator
 $RC = \frac{T_c}{a}$

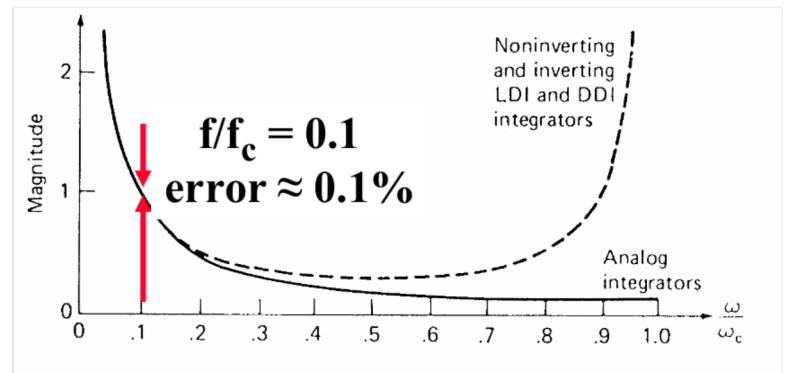
Exact Transfer function

$$H(z) = -\frac{az^{-1/2}}{1 - z^{-1}}$$

$$H(e^{j\omega T_c}) = -\frac{ae^{-j\omega T_c/2}}{1 - e^{-j\omega T_c}}$$

$$H(e^{j\omega T_c}) = -\frac{a}{e^{j\omega T_c/2} - e^{-j\omega T_c/2}}$$

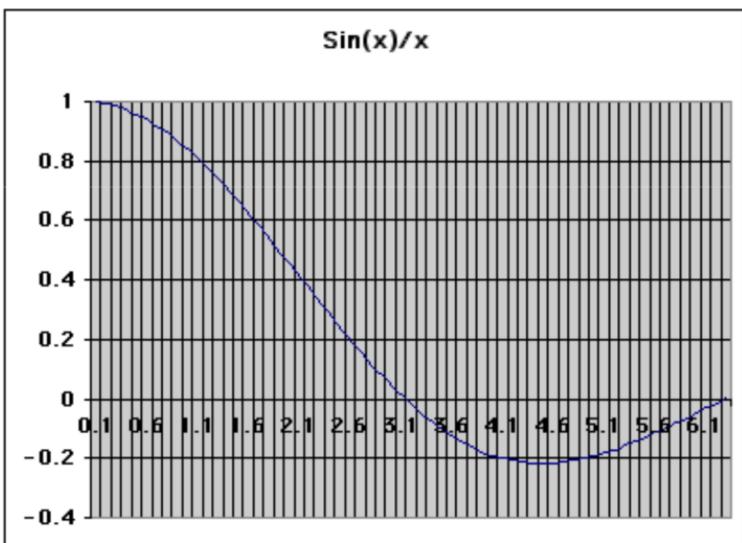
$$H(e^{j\omega T_c}) = -\frac{a}{j\omega T_c} \frac{\omega T_c/2}{\sin(\omega T_c/2)}$$



Euler's relationship:

$$\sin(x) = \frac{e^{+jx} - e^{-jx}}{2j}$$

The $\sin(x)/x$ function



$$\sin(x) \approx x - \frac{x^3}{3} + ..$$

$$\frac{\sin(x)}{x} \approx 1 - \frac{x^2}{3} + ..$$

For $x = 0.1$

$$\sin(x)/x \approx 1 - 0.003$$

For $x = 0.05$

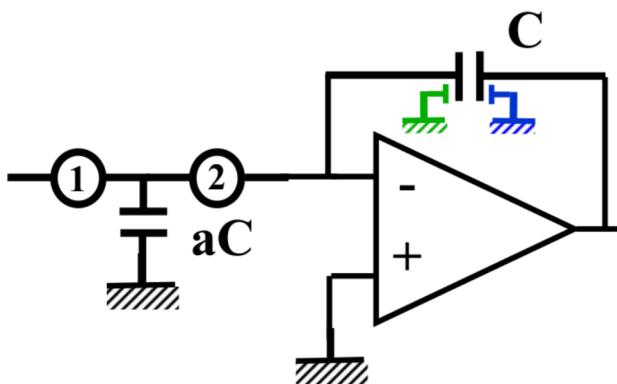
$$\begin{aligned}\sin(x)/x &\approx 1 - 0.0008 \\ &\approx 1 - 0.001\end{aligned}$$

Switched-Capacitor Filters

- Introduction : principle
- Technology:
 - MOS capacitors
 - MOST switches
- SC Integrator
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- SC Filters : LC ladder / bi-quadratic section
- Opamp requirements
 - Charge transfer accuracy
 - Noise
- Switched-current filters

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Stray Capacitances



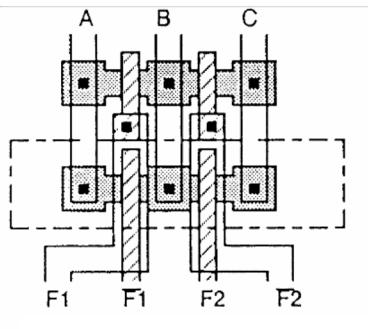
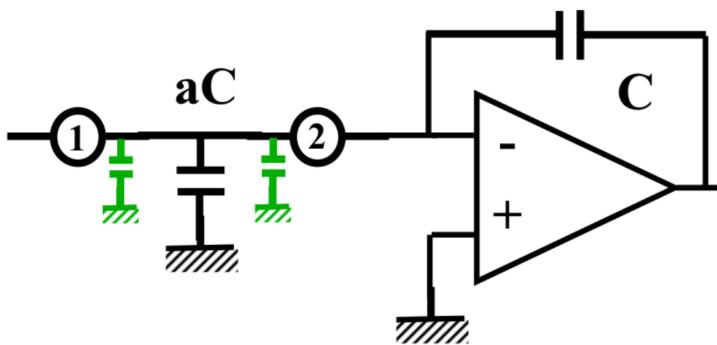
Stray Cap at input:

Substrate coupling
Continuous time
PSRR very bad

Stray Cap at output:

**C_p is extra load
for opamp**

Stray Capacitances

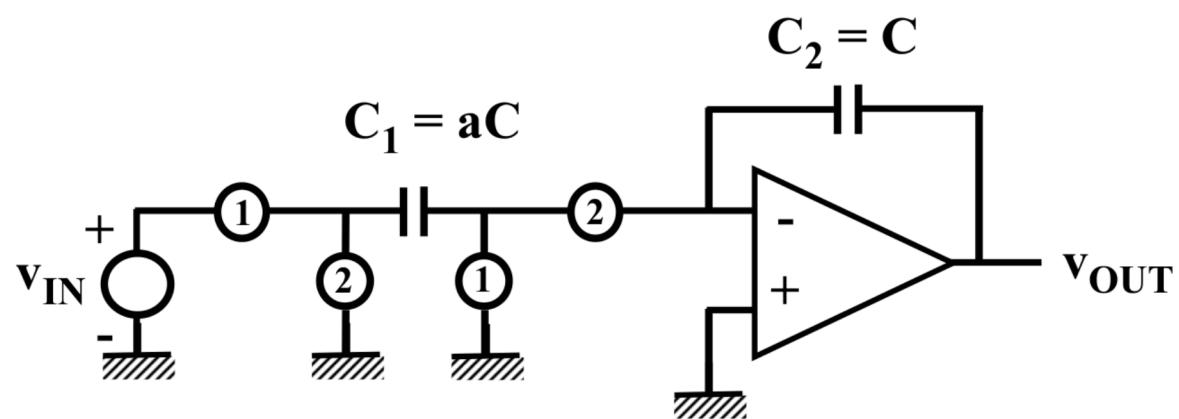


$$C_p \approx 2 \cdot C_{js} \cdot \text{Area} \approx 20 \text{ fF}$$

$$\text{Gain} = \frac{aC + 2C_p}{C}$$

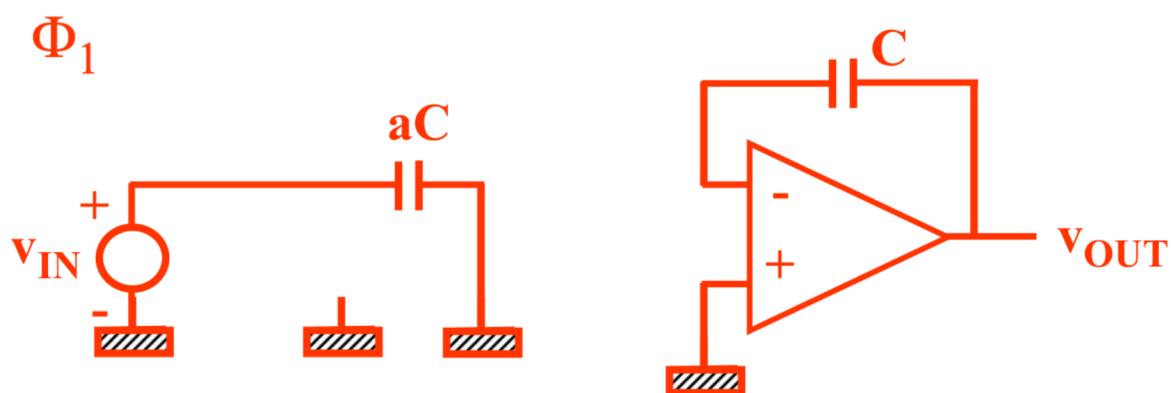
$$\text{error} \approx \frac{2C_p}{aC} \approx 5 - 10\%$$

Stray Insensitive SC integrator



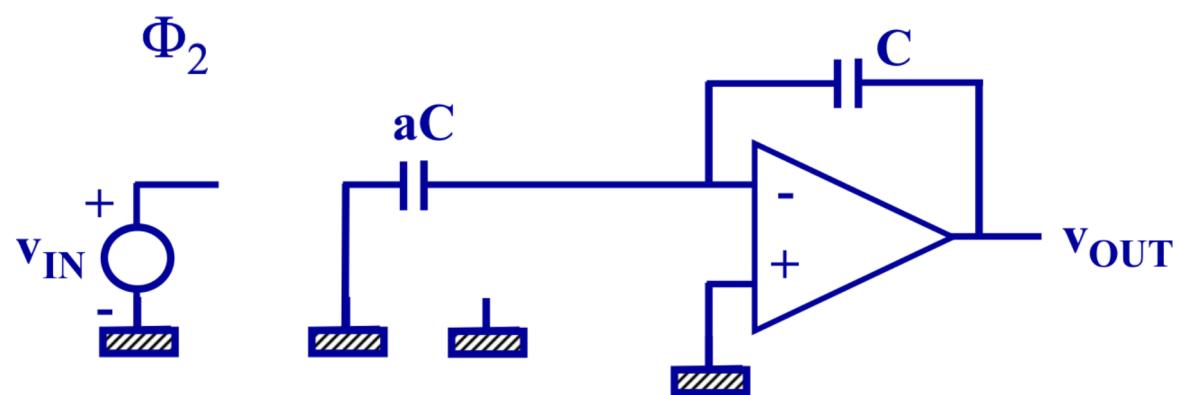
$$A_v = \frac{C_1}{C_2} = a$$

Stray Insensitive SC integrator



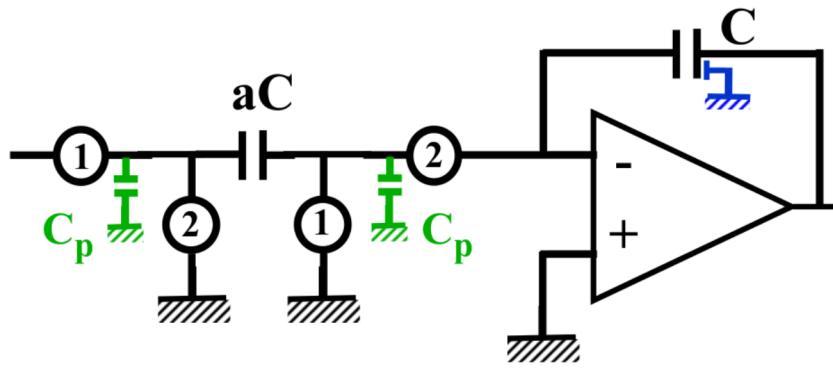
$$A_v = \frac{C_1}{C_2} = a$$

Stray Insensitive SC integrator

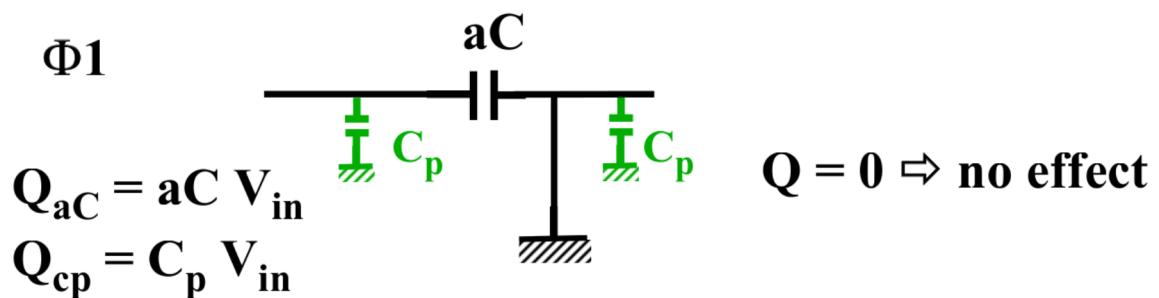


$$A_v = \frac{C_1}{C_2} = a$$

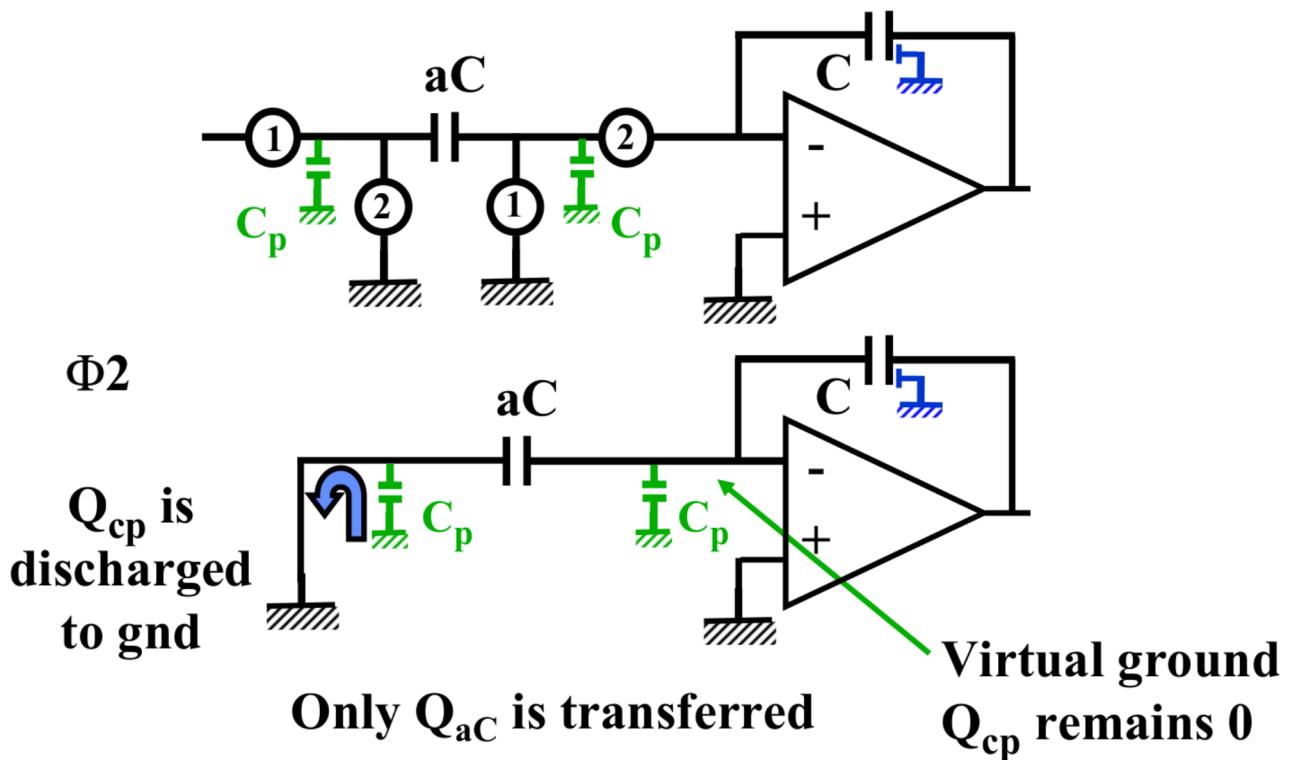
Stray Insensitive Integrator during phase 1



$$A_v = \frac{C_1}{C_2} = a$$
$$\tau = \frac{1}{af_c}$$



Stray Insensitive Integrator during phase 2

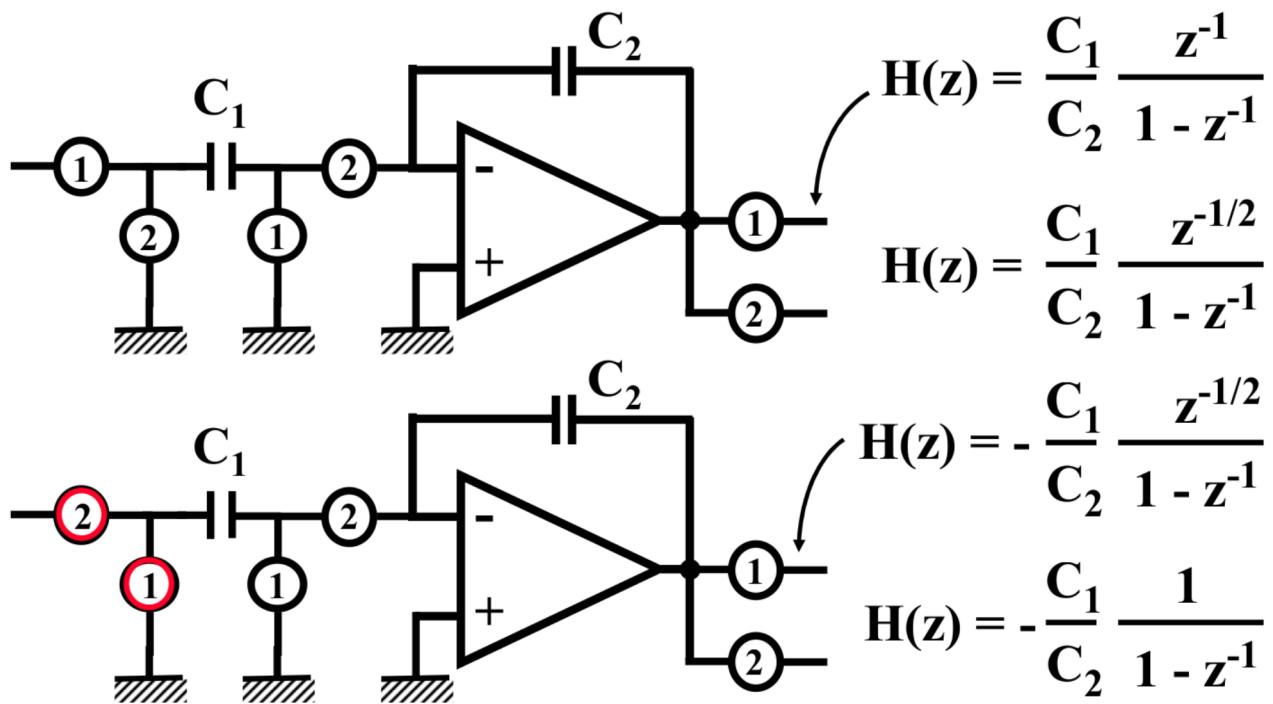


Switched-Capacitor Filters

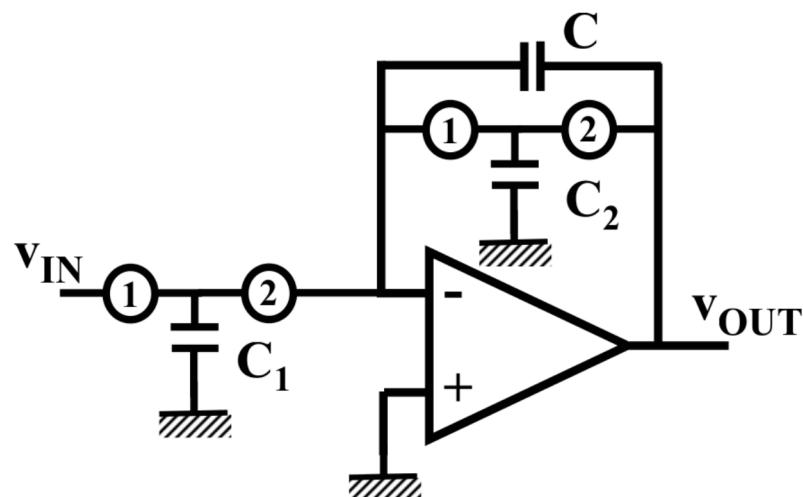
- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - MOST switches
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - **Basic SC-integrator building blocks**
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Loss-less Integrators



Low-pass filter of 1st order

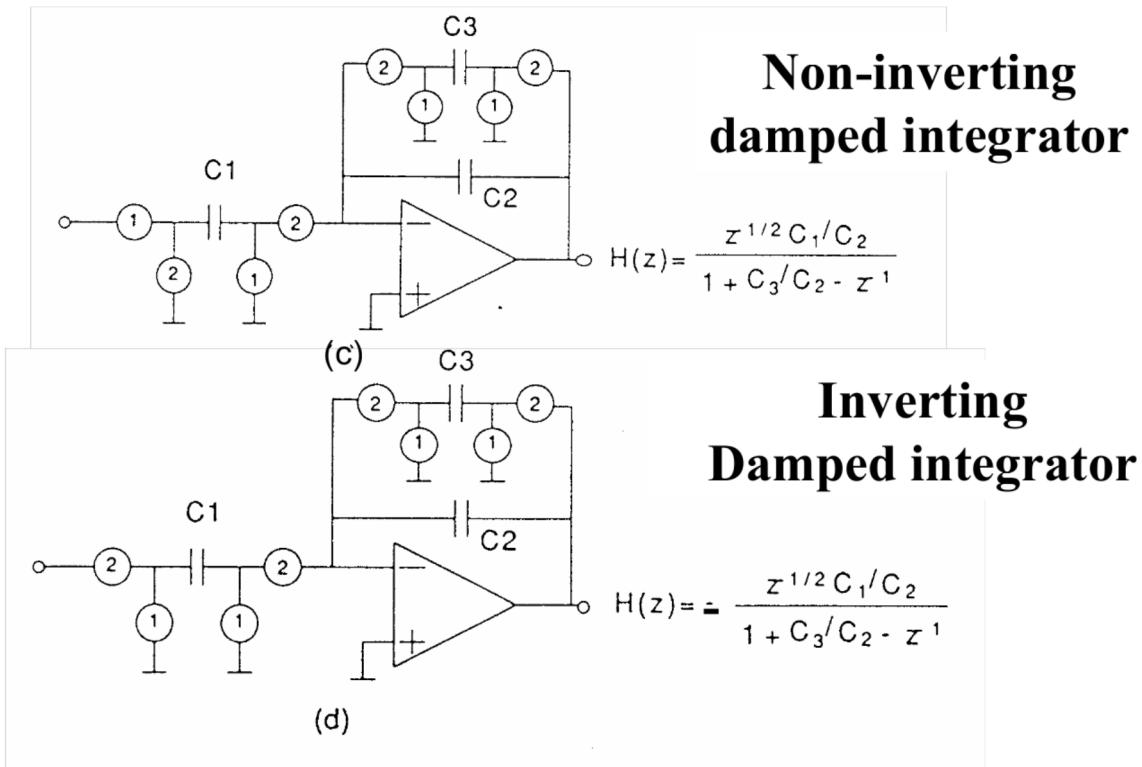


$$A_v = \frac{C_1}{C_2}$$

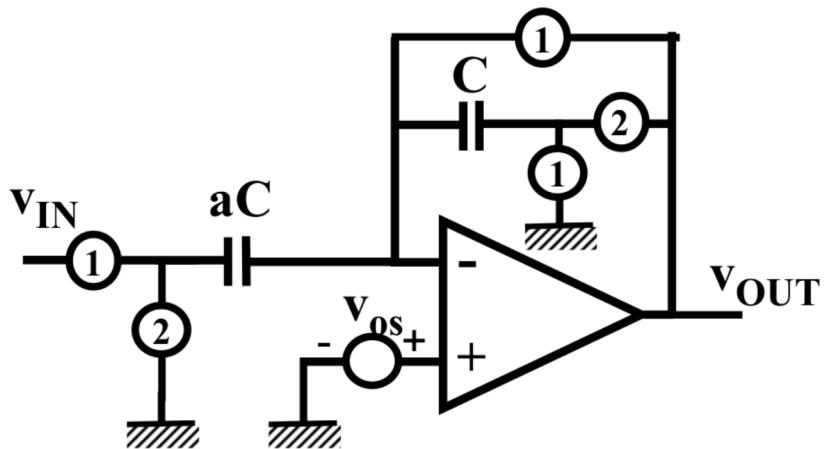
$$BW = \frac{f_c}{2\pi} \frac{C_2}{C}$$

Damped because of R/C !

Damped integrators



Offset compensation



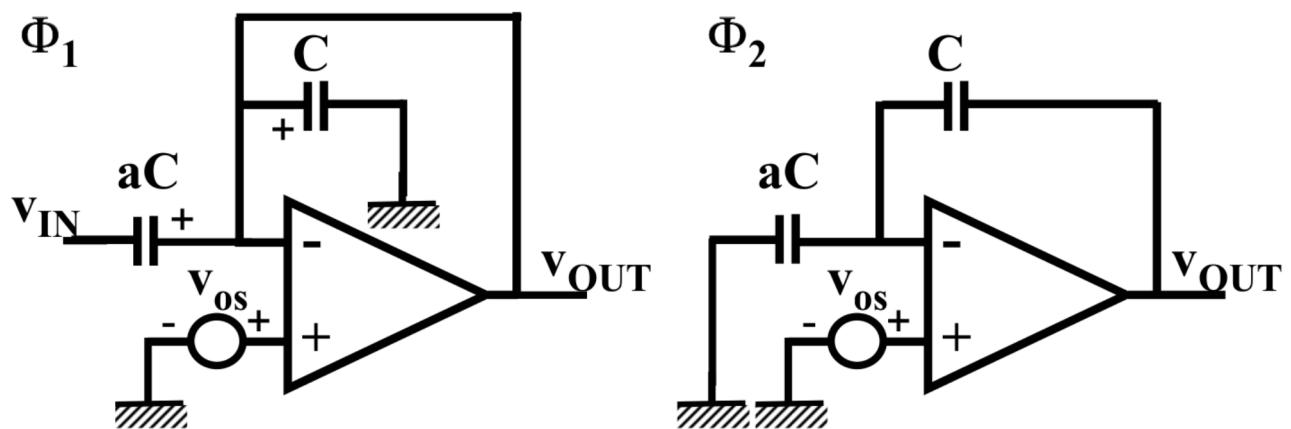
$$A_v = a z^{-1/2}$$

independent of v_{os}

Gregorian, IEEE Proc. Aug 83, 941-986

Willy Sansen 10-05 N1750

Offset compensation



$$Q_{aC1} = aC (v_{os} - v_{IN}(n-1/2))$$

$$Q_{C1} = C v_{os}$$

$$Q_{aC2} = aC v_{os}$$

$$Q_{C2} = C (v_{os} - v_{OUT}(n))$$

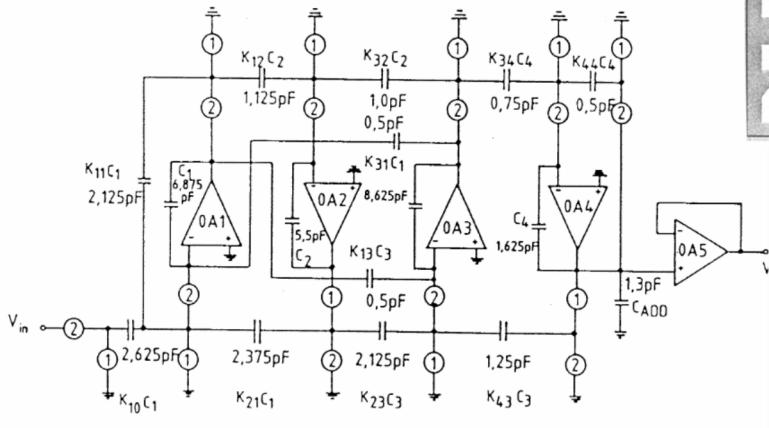
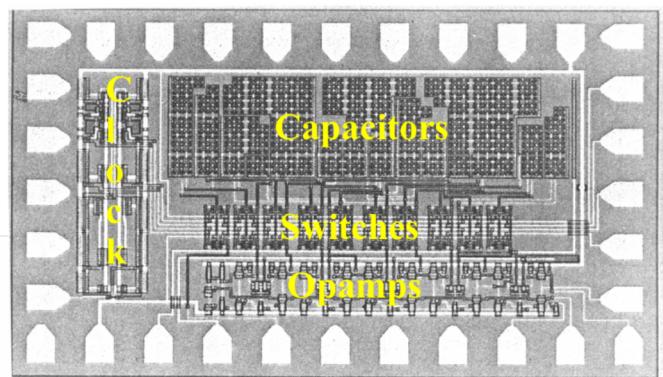
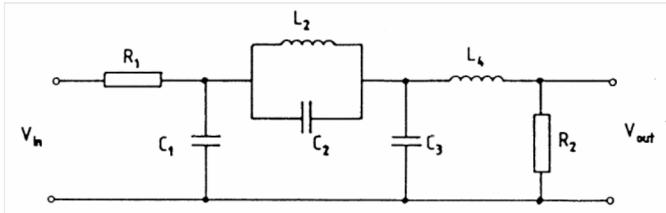
$$Q_{aC1} + Q_{C1} = Q_{aC2} + Q_{C2} \quad \Rightarrow \quad A_v = a z^{-1/2}$$

Switched-Capacitor Filters

- **Introduction : principle**
 - **Technology:**
 - MOS capacitors
 - MOST switches
 - **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
 - **SC Filters : LC ladder / bi-quadratic section**
 - **Opamp requirements**
 - Charge transfer accuracy
 - Noise
 - **Switched-current filters**
-

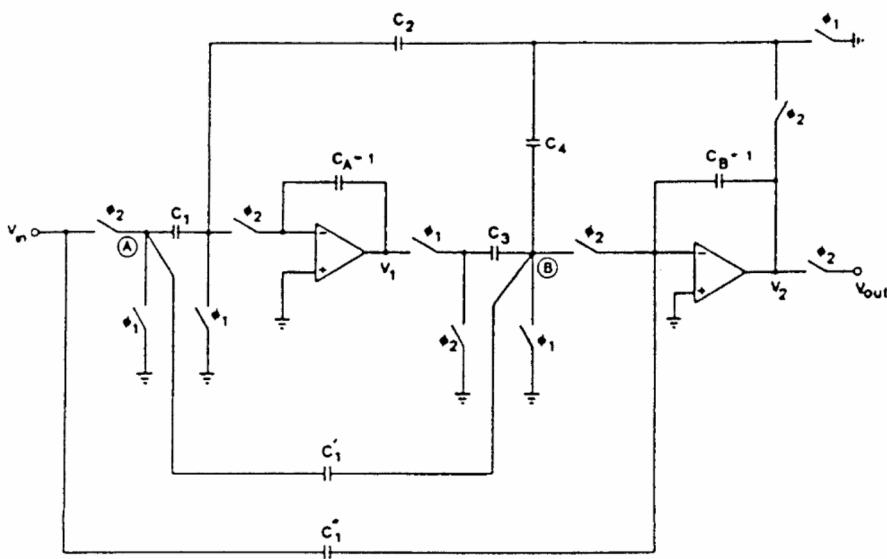
Gregorian, Temes, Analog MOS Integrated Circuits for Signal Processing, Wiley, 1986
Laker, Sansen, Design of Analog Integrated Circuits and Systems, McGrawHill, 1994
Johns, Martin, Analog Integrated Circuit Design, Wiley 1997

4th Order SC low-pass ladder filter



| | |
|--------------------|--------------------------------------|
| Clock freq | 100 kHz |
| Cut-off | 5 kHz |
| Pass ripple | 0.25dB |
| Stop reject | >45 dB |
| Power | 190µW ($\pm 2.5V$) |
| S/N | 75 dB |
| Harm dist | 0.25% |
| Area | 0.9 mm² |

Biquadratic filter



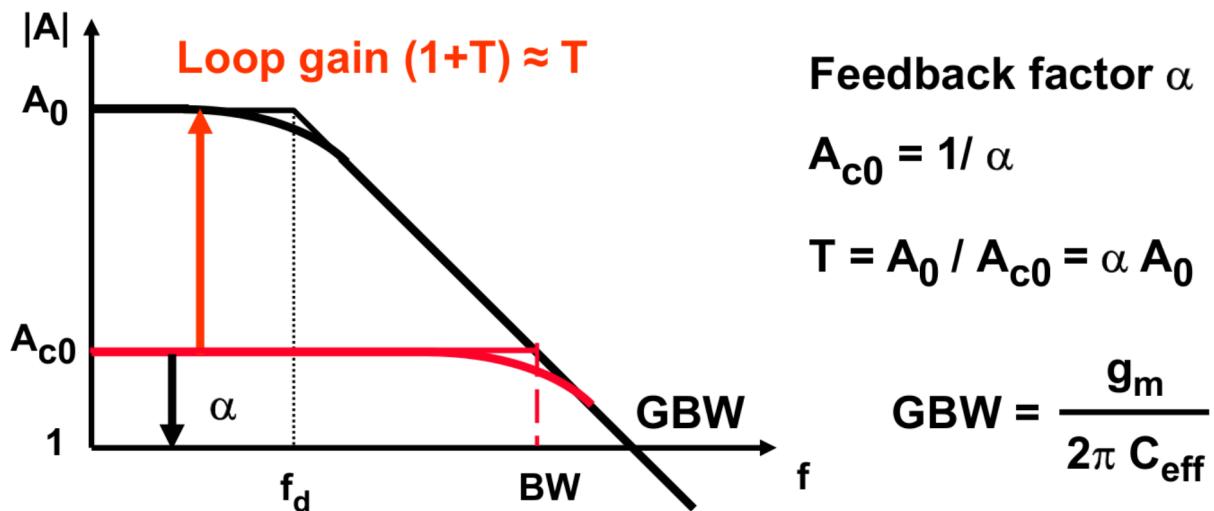
$$H(z) = -\frac{a_2 z^2 + a_1 z + a_0}{b_2 z^2 + b_1 z + b_0} = -\frac{(C_1' + C_1'')z^2 + (C_1 C_3 - C_1' - 2C_1'')z + C_1''}{(1 + C_4)z^2 + (C_2 C_3 - C_4 - 2)z + 1}$$

Switched-Capacitor Filters

- Introduction : principle
- Technology:
 - MOS capacitors
 - MOST switches
- SC Integrator
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- SC Filters : LC ladder / bi-quadratic section
- Opamp requirements
 - Charge transfer accuracy
 - Noise
- Switched-current filters

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Opamp parameters



$$BW = \alpha GBW$$

Static error

$$V_{out, t = \infty} = -\frac{Ao \cdot V_{step}}{1 + \alpha \cdot Ao}$$

$$\varepsilon_s = \frac{V_{step}/\alpha - V_{out}}{V_{step}/\alpha} = 1 - \frac{Ao}{1 + Ao \cdot \alpha} \approx \frac{1}{\alpha \cdot Ao}$$

Minimum Gain

$$Ao > \frac{1}{\alpha \cdot \varepsilon_s}$$

$\varepsilon = 0.05\%$
↓
 $A_0 \approx 1-10k$
 $\approx 60-80 \text{ dB}$

Dynamic error

$$\mathcal{E}_D = EXP\left(-\frac{\alpha \cdot gm \cdot ts}{C_{L,ef}}\right)$$

$$GBW = \frac{gm}{2\pi C_{L,ef}}$$

$$\mathcal{E}_D = EXP(-\alpha \cdot 2\pi \cdot GBW \cdot ts)$$

$$ts = \frac{1}{2f_c}$$

$$GBW = \frac{1}{\alpha \cdot 2\pi \cdot ts} \ln\left(\frac{1}{\mathcal{E}_D}\right) = \frac{2f_c}{2\pi\alpha} \ln\left(\frac{1}{\mathcal{E}_D}\right)$$

Minimum GBW:
$$GBW > \frac{f_c}{\pi\alpha} \ln\left(\frac{1}{\mathcal{E}_D}\right)$$

$\varepsilon = 0.05\%$
↓
 $GBW \approx 2-3*f_c$

Switched-Capacitor Filters

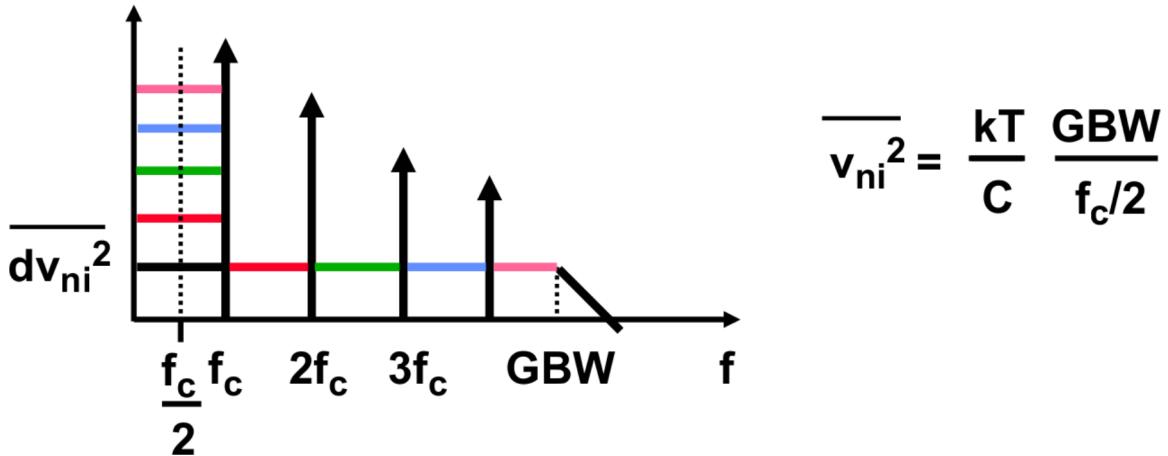
- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - MOST switches
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

kT/C versus kTR noise

Narrow-band noise >> noise density : $\overline{dv_{ni}^2} = 4kT R df$

Wide-band noise >> integrated noise : $\overline{v_{ni}^2} = \frac{kT}{C}$

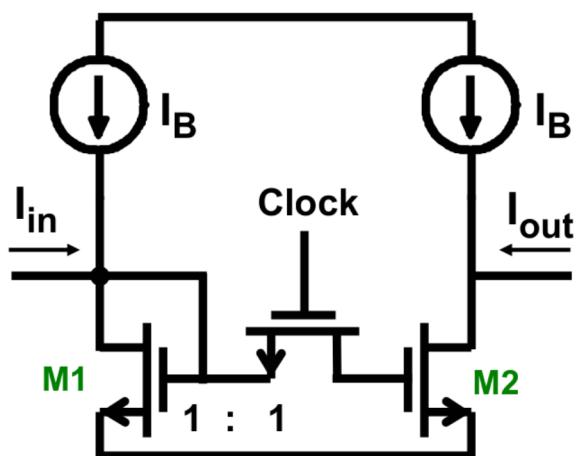


Switched-Capacitor Filters

- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - MOST switches
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986

Switched-current delay block



Switch closed : track V_{GS}

$$I_{out} = I_{in}$$

Switch open : hold V_{GS}

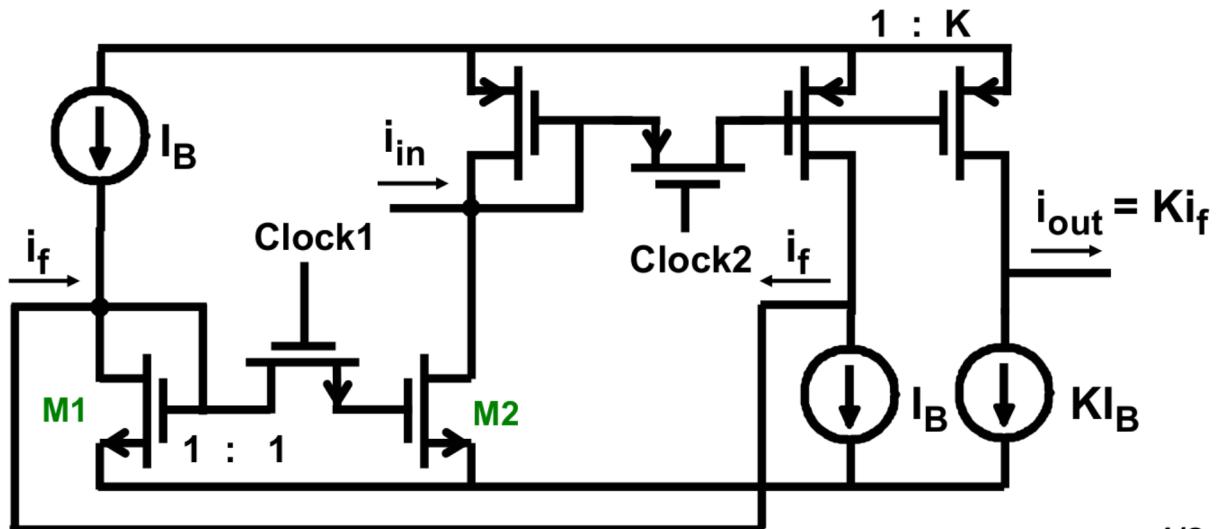
$$I_{out} = I_{in} (\Delta T_c)$$

$$I_{out} = I_{in} z^{-1/2}$$

Ref. Zele JSSC Feb. 96, 157- 168

Willy Sansen 10-05 N1762

Switched-current low-pass filter

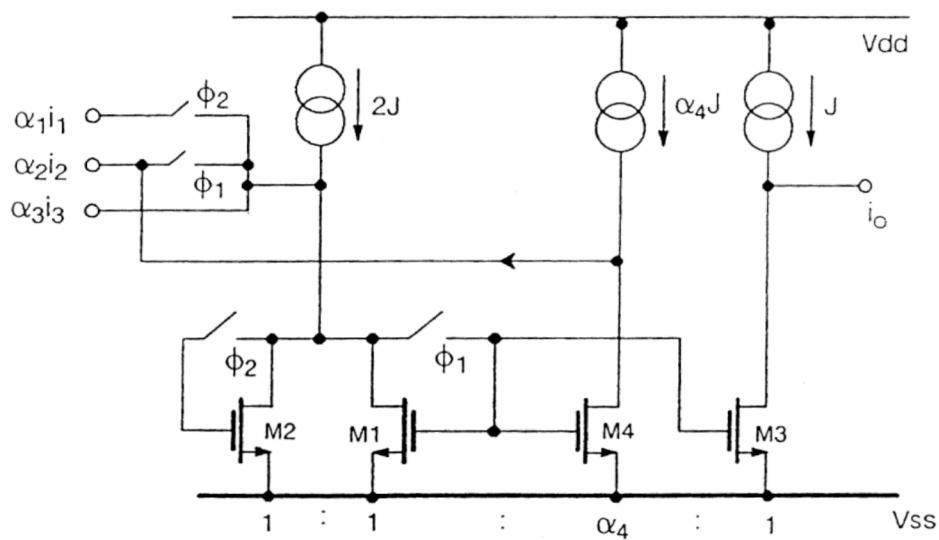


$$i_f = i_f z^{-1} - i_{in} z^{-1/2}$$
$$\frac{i_{out}}{i_{in}} = \frac{K z^{-1/2}}{1 - z^{-1}}$$

Ref. Zele JSSC Feb. 96, 157- 168

Willy Sansen 10-05 N1763

2nd-generation switched-current filter



$$A_1 = \frac{\alpha_1}{1 + \alpha_4}$$

$$A_2 = \frac{\alpha_2}{1 + \alpha_4}$$

$$A_3 = \frac{\alpha_3}{1 + \alpha_4}$$

$$B = \frac{1}{1 + \alpha_4}$$

$$i_o(z) = \frac{A_1 z^{-1}}{1 - Bz^{-1}} i_1(z) - \frac{A_2 z^{-1}}{1 - Bz^{-1}} i_2(z) - \frac{A_3 (1-z^{-1})}{1 - Bz^{-1}} i_3(z)$$

Comparison SC - SI

SC

Signal : Voltage

Charge on linear C

$$Q = C V$$

Accuracy : Capacitor ratio

0.2 %

Amps : Opamps

S/N+D 70 dB

SI

Current

Charge on MOST C_{GS}

$$Q = I t$$

MOST area ratio

2 %

Current mirrors

50 dB

Switched-Capacitor Filters

- **Introduction : principle**
- **Technology:**
 - MOS capacitors
 - MOST switches
- **SC Integrator**
 - SC integrator : Exact transfer function
 - Stray insensitive integrator
 - Basic SC-integrator building blocks
- **SC Filters : LC ladder / bi-quadratic section**
- **Opamp requirements**
 - Charge transfer accuracy
 - Noise
- **Switched-current filters**

McCreary, JSSC Dec 75, 371-379
Gregorian, IEEE Proc. Aug 83, 941-986