

1、(1) 答案 (5 分): 三角形窗序列 123454321

2、(1) 答案 (5 分): 收敛域 , 不稳定

$$Y(z) = \frac{1}{(1-2z^{-1})} \quad |z| > 2$$

(2) 答案 (10 分): $X(z) = Y(z)/H(z) = \frac{1-0.5z^{-1}}{1-0.9z^{-1}} \quad |z| > 0.9$

$$x(n) = \delta(n) + 0.4 \cdot 0.9^n u(n)$$

4、(1) 答案 (5 分): $H(z) = (1+z^{-1})^2$
 $H(e^{j\omega}) = (1+e^{-j\omega})^2$

(2) 答案 (5 分): $y(n) = H(e^{j\omega})|_{\omega=\frac{\pi}{2}} * e^{j\frac{\pi}{2}n} + H(e^{j\omega})|_{\omega=\pi} * e^{j\pi n}$
 $= (1-j)^2 * j^n$

5、(1) 答案 (5 分):

$$f_1 = \frac{\omega_1}{T} / 2\pi = \frac{\pi}{5 \cdot 0.01} / 2\pi = 10 \text{ Hz}$$

$$f_2 = 20 \text{ Hz}$$

(2) 答案 (5 分): $\omega_0 = \frac{\pi}{5}$

(3) 答案 (10 分):

$$H(e^{j\omega}) = \frac{\sin(5\omega/2)}{\sin(\omega/2)} e^{-j2\omega}$$

$$H(e^{j\omega})|_{\omega=\frac{\pi}{5}} = A e^{j\phi} = \frac{1}{\sin(0.1\pi)} e^{-j\frac{2\pi}{5}}$$

$$H(e^{j\omega})|_{\omega=\frac{2\pi}{5}} = 0$$

$$y[n] = \frac{1}{\sin(0.1\pi)} \sin\left(\frac{\pi}{5}(n-2)\right)$$

$$x(t) = \sin(20\pi t) + \cos(40\pi t)$$

$$x(n) = \sin(20\pi nT) + \cos(40\pi nT)$$

(4) 答案: $w_1 = 20\pi T, w_2 = 40\pi T$

$$\sup: w_1 + 2\pi = w_2$$

$$T = 1/10\pi$$