

# 微电子器件物理 PN结的电流特性

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# PN结的连续性方程

$$\nabla \bullet E = q(p - n + N_D^+ - N_A^-) \quad \text{能带图}$$

$$\frac{\partial n}{\partial t} = \frac{1}{q} \nabla \bullet \mathbf{J}_N - r_N + g_N$$

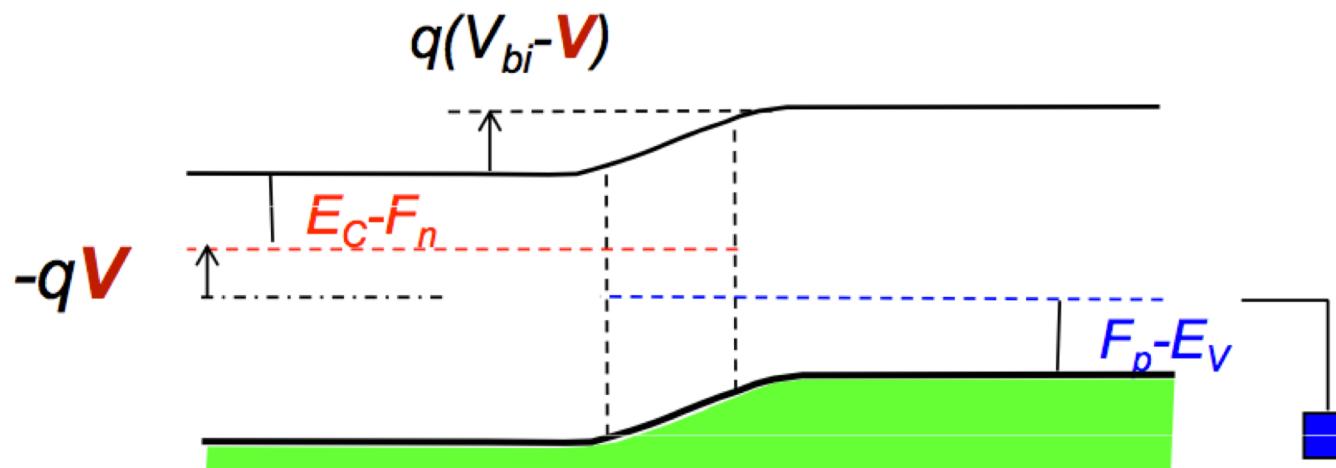
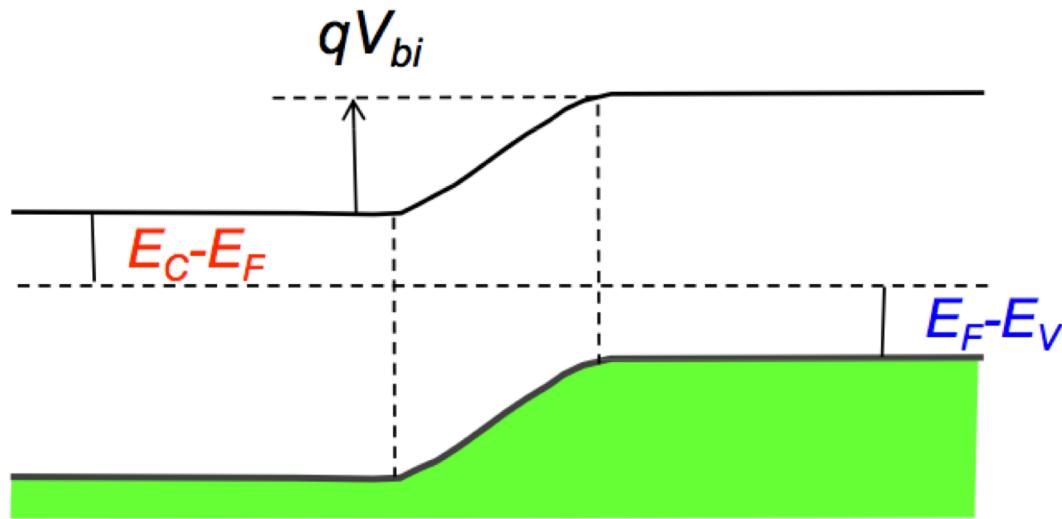
$$\mathbf{J}_N = qn\mu_N E + qD_N \nabla n$$

$$\frac{\partial p}{\partial t} = \frac{1}{q} \nabla \bullet \mathbf{J}_P - r_P + g_P$$

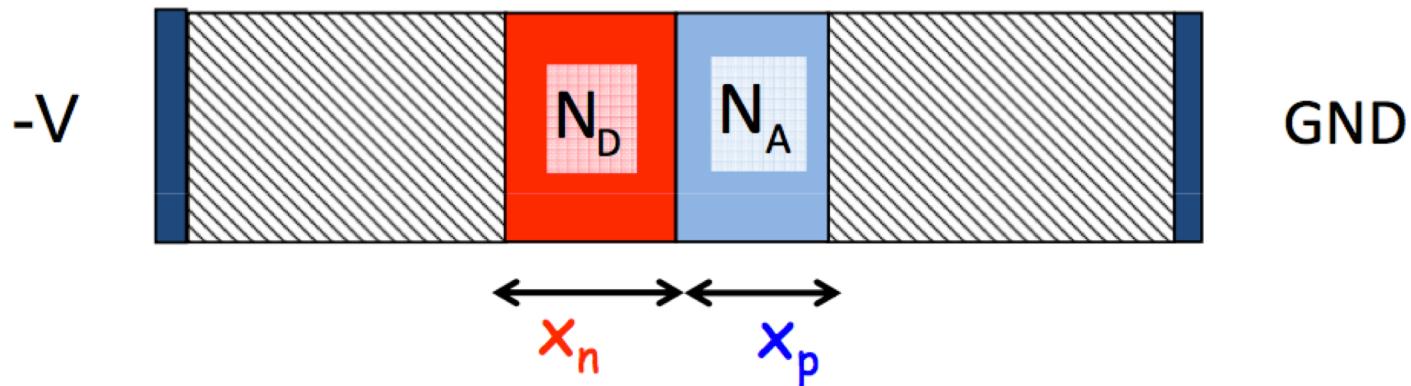
$$\mathbf{J}_P = qp\mu_P E - qD_P \nabla p$$

正向电流和反向电流

# PN结的正向偏置

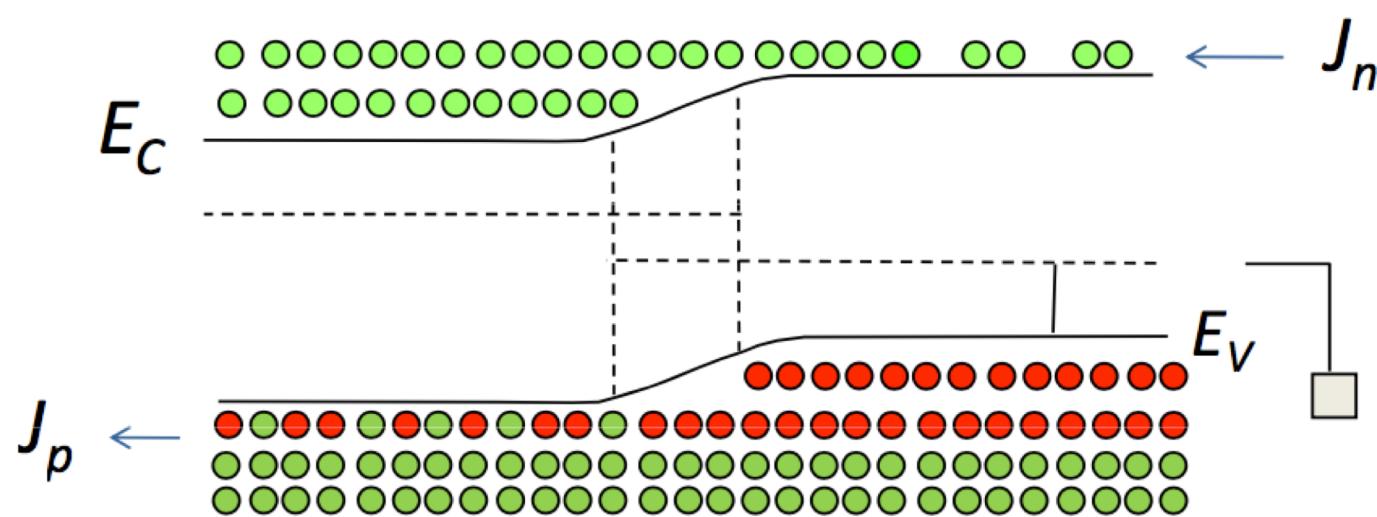
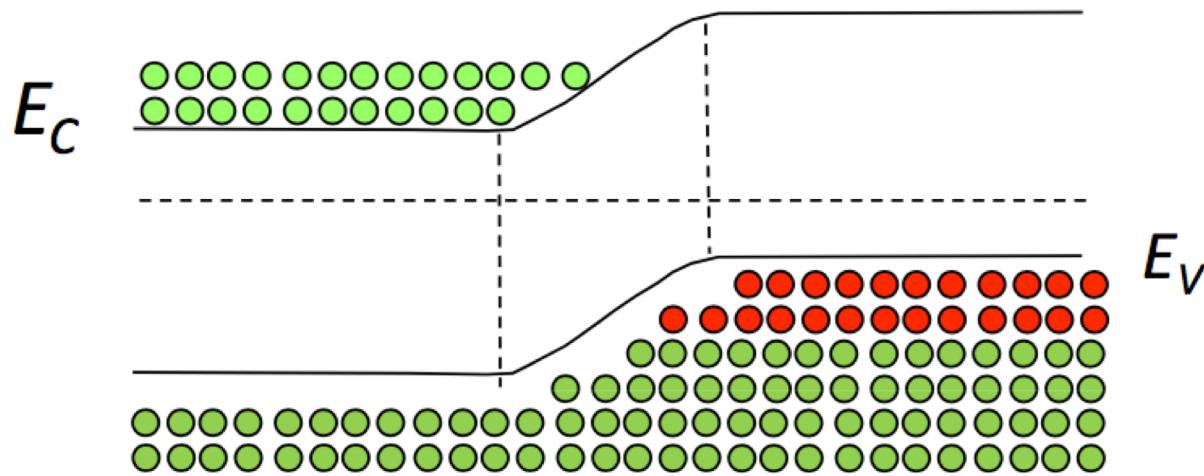


# 耗尽区宽度



$$\left. \begin{aligned} N_D x_n &= N_A x_p \\ q(V_{bi} - V) &= \frac{qN_D x_n^2}{2k_s \epsilon_0} + \frac{qN_A x_p^2}{2k_s \epsilon_0} \end{aligned} \right\}$$
$$x_n = \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_A}{N_D(N_A + N_D)} (V_{bi} - V)}$$
$$x_p = \sqrt{\frac{2k_s \epsilon_0}{q} \frac{N_D}{N_A(N_A + N_D)} (V_{bi} - V)}$$

# 准费米能级



# 边界条件

$$\Delta n(0^+) = n(0^+)_{V_G} - n(0^+)_{V_G=0}$$

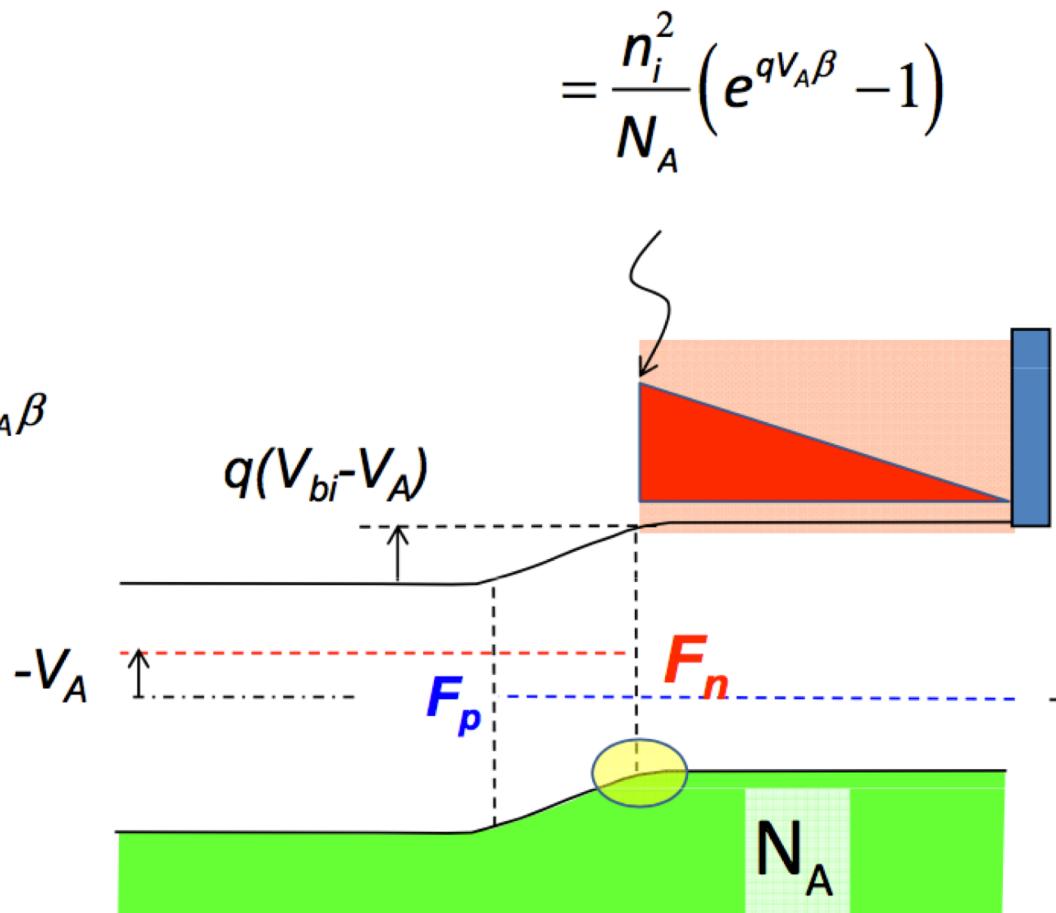
$$n(x=0^+) = n_i e^{(F_n - E_i)\beta}$$

$$p(x=0^+) = n_i e^{-(F_p - E_i)\beta}$$

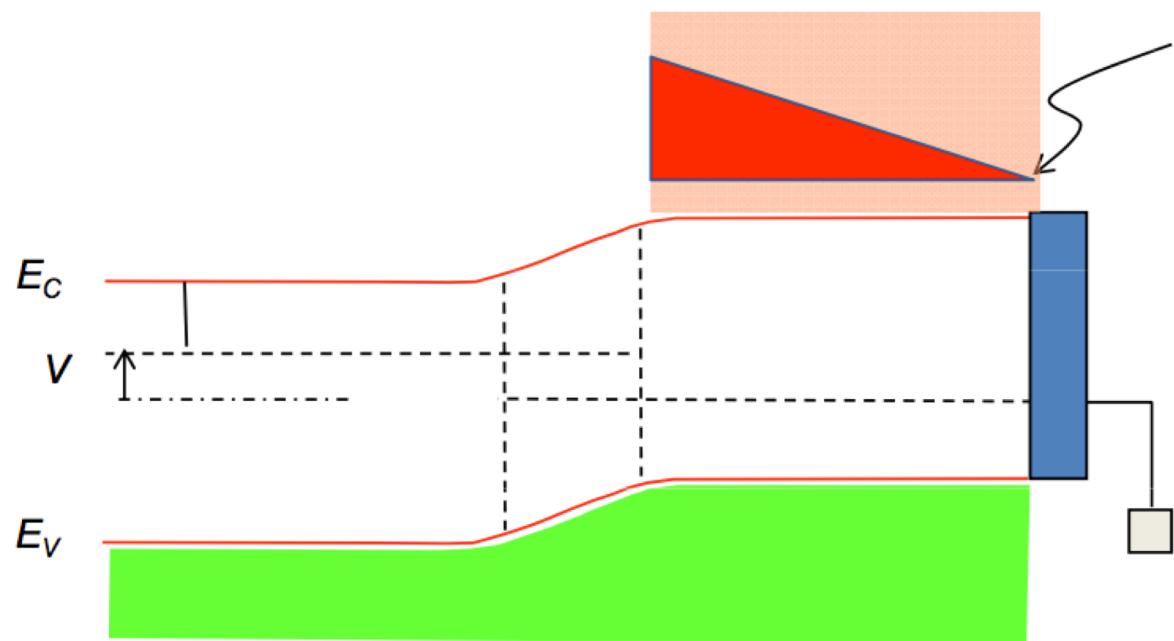
$$np = n_i^2 e^{(F_n - F_p)\beta} = n_i^2 e^{qV_A\beta}$$

$$p(0^+) = N_A$$

$$n(0^+) = \frac{n_i^2}{N_A} e^{qV_A\beta}$$



# 边界条件

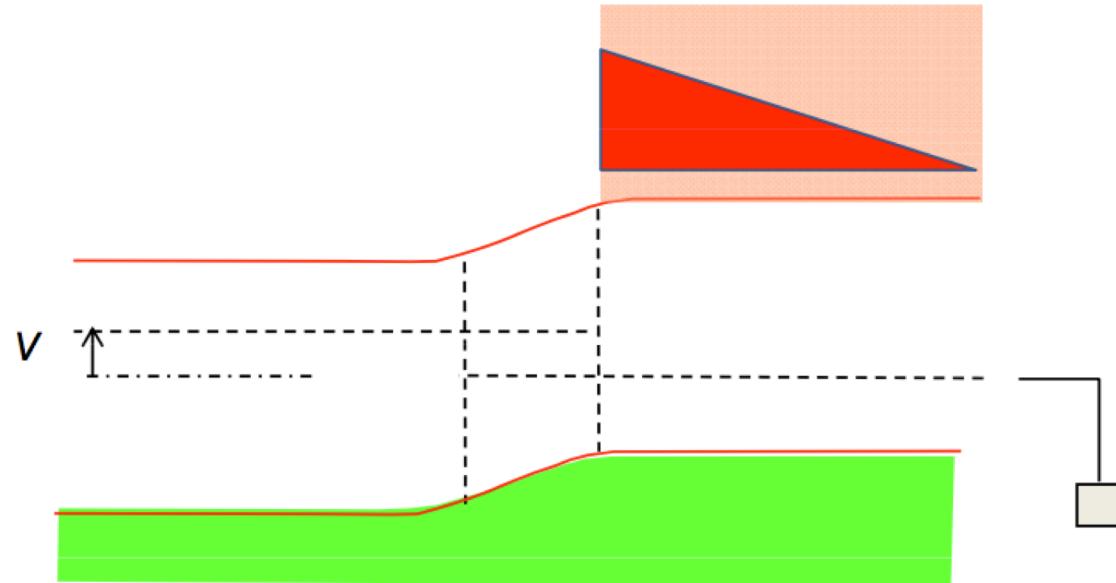


$$n(x = W_p) \approx \frac{n_i^2}{N_A}$$
$$\Delta n(x = W_p) = 0$$

# 边界条件

$$D_N \frac{d^2 n}{dx^2} = 0$$

$$\Delta n(x, t) = C + Dx$$



$$x = W_p, \quad \Delta n(x = W_p) = 0 \Rightarrow C = -DW_p$$

$$x = 0', \quad \Delta n(x = 0) = \frac{n_i^2}{N_A} \left( e^{qV_A \beta} - 1 \right) = C$$

$$\Delta n(x, t) = \frac{n_i^2}{N_A} \left( e^{qV_A \beta} - 1 \right) \left( 1 - \frac{x}{W_p} \right)$$

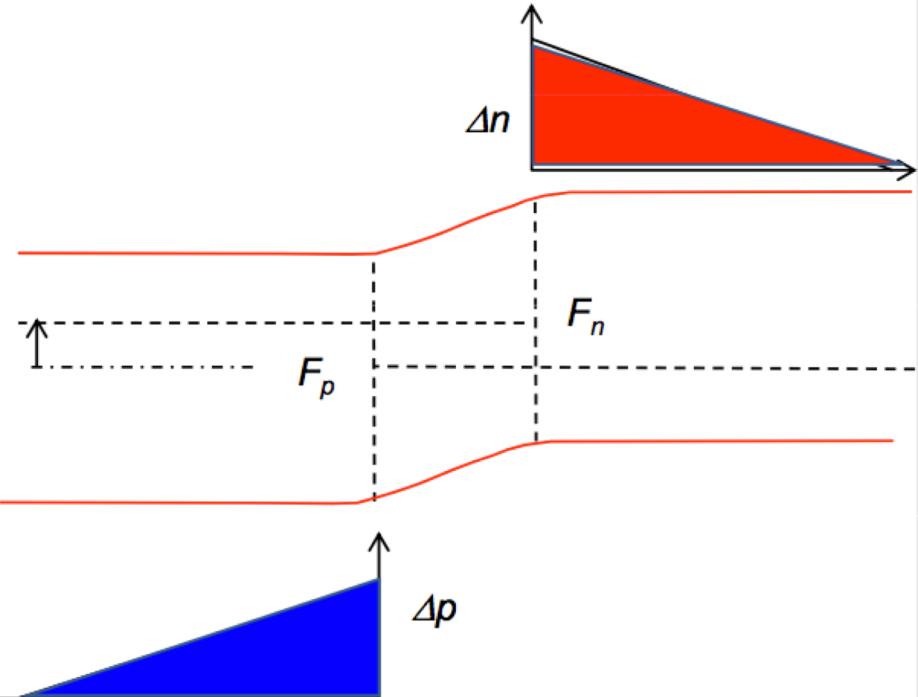
# 电子电流和空穴电流

$$\Delta n(x) = \frac{n_i^2}{N_A} \left( e^{qV_A\beta} - 1 \right) \left( 1 - \frac{x}{W_p} \right)$$

$$\mathbf{J}_N = qn\mu_N \mathcal{E} + qD_N \nabla n$$

$$J_n = qD_n \frac{dn}{dx} \Big|_{x=0} = -\frac{qD_n}{W_p} \frac{n_i^2}{N_A} \left( e^{qV_A\beta} - 1 \right)$$

$$J_p = -qD_p \frac{dp}{dx} \Big|_{x=0} = -\frac{qD_p}{W_n} \frac{n_i^2}{N_D} \left( e^{qV_A\beta} - 1 \right)$$



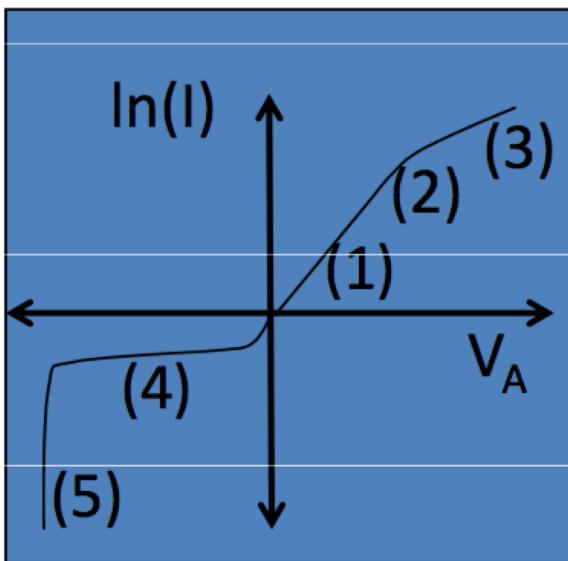
# 总电流

正向偏置

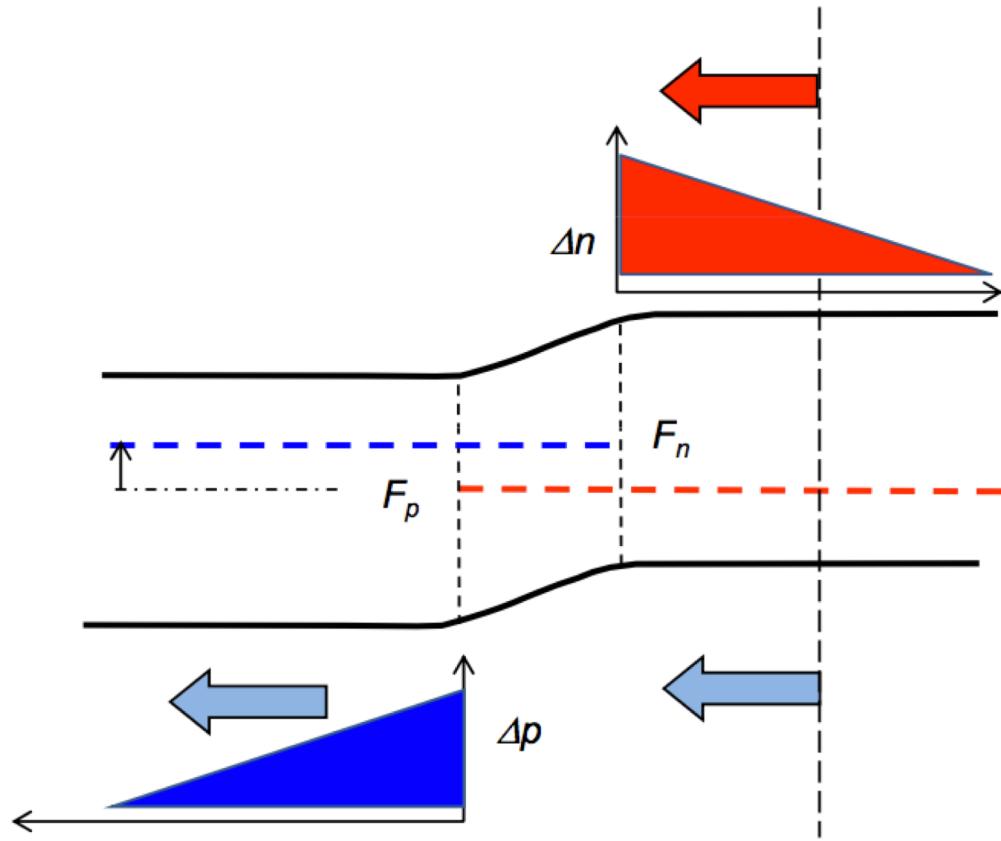
$$\ln J_T \approx qV_A/k_B T + \ln(\text{const.})$$

反向偏置

$$J_T \approx \text{const.}$$



$$J_T = -q \left[ \frac{D_n}{W_p} \frac{n_i^2}{N_A} + \frac{D_p}{W_n} \frac{n_i^2}{N_D} \right] (e^{qV_A\beta} - 1)$$



**Thanks!**  
**Q&A**