## 公式表

物理常量:	$\hbar = 1.055 \times 10^{-34}$ [J-s] $m_0 = 9.109 \times 10^{-31}$ [kg]	
	$k_B = 1.380 \times 10^{-23} $ [J/K]	
	$q = 1.602 \times 10^{-19}$ [C] $\varepsilon_0 = 8.854 \times 10^{-12}$ [F/m]	
	$N_C = 3.23 \times 10^{19} \text{ cm}^{-3}$	
材料"硅"相关参数:	$N_c = 3.23 \times 10^{-10} \text{ cm}^{-3}$	
	$n_i = 1 \times 10^{10} \text{ cm}^{-3}$	
	$K_{s} = 11.8$	
两平面之间的夹角:	$\cos\theta = \frac{h_1 h_2 + k_1 k_2 + l_1 l_2}{\sqrt{h_1^2 + k_1^2 + l_1^2} \sqrt{h_2^2 + k_2^2 + l_2^2}}$	
两平面之间的距离:	$d = \frac{1}{ \vec{N} } = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$	
DOS: $g_C(E) = \frac{(m_n^*)^{3/2} \sqrt{2(E - E_C)}}{\pi^2 \hbar^3}$ FF: $f(E) = \frac{1}{1 + e^{(E - E_F)/k_B T}}$ $n_i = \sqrt{N_C N_V} e^{-E_G/2k_B T}$		
平衡载流子浓度:	$n_0 = N_C e^{(E_F - E_C)/k_B T}  \text{m}^{-3}  N_C = \frac{1}{4} \left( \frac{2m_n^* k_B T}{\pi \hbar^2} \right)^{3/2} \text{m}^{-3}  n_0 = n_i e^{(E_F - E_i)/k_B T}$	
	$p_0 = N_V e^{(E_V - E_F)/k_B T}  \text{m}^{-3}  N_V = \frac{1}{4} \left( \frac{2m_p^* k_B T}{\pi \hbar^2} \right)^{3/2} \text{m}^{-3}  p_0 = n_i e^{(E_i - E_F)/k_B T}$	
电中性关系:	$p - n + N_D^+ - N_A^- = 0   n_0 p_0 = n_i^2$	
电导和电阻率:	$\sigma = (\sigma_n + \sigma_p) = q(n\mu_n + p\mu_p) = 1/\rho$	
电流公式:	$J_{n} = n\mu_{n} \frac{dF_{n}}{dx} \qquad J_{n} = nq\mu_{n} \mathcal{E}_{x} + qD_{n} \frac{dn}{dx} \qquad D_{n}/\mu_{n} = k_{B}T/q$	
	$J_{p} = p\mu_{p} \frac{dF_{p}}{dx} \qquad J_{p} = pq\mu_{p} \mathcal{E}_{x} - qD_{p} \frac{dp}{dx} \qquad D_{p}/\mu_{p} = k_{B}T/q$	
SRH 复合:	$R = \Delta n/\tau_n \text{ m}^{-3}\text{s}^{-1} \text{ or } R = \Delta p/\tau_p \text{ m}^{-3}\text{s}^{-1}$	
半导体公式:	$\frac{\partial n}{\partial t} = -\nabla \cdot \left(\frac{\vec{J}_n}{-q}\right) + G_n - R_n$	
	$\frac{\partial p}{\partial t} = -\nabla \cdot \left(\frac{\vec{J}_p}{q}\right) + G_p - R_p$	
	$0 = -\nabla \cdot \left(\varepsilon \vec{\mathcal{E}}\right) + \rho$	

少数载流子扩散密度:	$\frac{\partial \Delta p}{\partial t} = D_p \frac{\partial^2 \Delta p}{\partial x^2} - \frac{\Delta p}{\tau_p} + G_L$
	$L_p = \sqrt{D_p \tau_p}$
载流子密度和 QFL's:	$n = N_C e^{(F_n - E_C)/k_B T} $ $n = n_i e^{(F_n - E_i)/k_B T}$
	$p = N_V e^{(E_V - F_p)/k_B T} $ $p = n_i e^{(E_i - F_p)/k_B T}$
非平衡关系:	$E_F \to F_n(x), F_p(x)$ $n_0 p_0 = n_i^2 \to np = n_i^2 e^{(F_n - F_p)/k_B T}$
	$n_0 = N_C e^{(E_F - E_C)/k_B T} \rightarrow n = N_C e^{(F_n - E_C)/k_B T}$
	$p_0 = N_{\nu} e^{(E_{\nu} - E_F)/k_B T} \to p = N_{\nu} e^{(E_{\nu} - F_p)/k_B T}$
PN 结静电关系:	$V_{bi} = rac{k_B T}{q} \ln \left( rac{N_D N_A}{n_i^2}  ight) \qquad rac{d\mathcal{E}}{dx} = rac{ ho(x)}{K_S arepsilon_0}$
	$W = \begin{bmatrix} 2K_S \varepsilon_0 \\ q \end{bmatrix} \begin{pmatrix} N_A + N_D \\ N_D N_A \end{pmatrix} V_{bi} \end{bmatrix}^{1/2} \qquad x_n = \frac{N_A}{N_A + N_D} W  x_p = \frac{N_D}{N_A + N_D} W$
	$\mathcal{E}\left(0\right) = \sqrt{\frac{2qV_{bi}}{K_{s}\varepsilon_{0}} \left(\frac{N_{D}N_{A}}{N_{A} + N_{D}}\right)}$
二极管电流:	$\Delta n(0) = \frac{n_i^2}{N_A} \left( e^{qV_A/k_B T} - 1 \right) \qquad \Delta p(0) = \frac{n_i^2}{N_D} \left( e^{qV_A/k_B T} - 1 \right)$
	$I_D = I_0 \left( e^{qV_A/k_B T} - 1 \right)$
	$I_0 = qA \left( \frac{D_n}{L_n} \frac{n_i^2}{N_A} + \frac{D_p}{L_p} \frac{n_i^2}{N_D} \right) \text{ (long)}  I_0 = qA \left( \frac{D_n}{W_p} \frac{n_i^2}{N_A} + \frac{D_p}{W_n} \frac{n_i^2}{N_D} \right) \text{ (short)}$
	$\text{non-ideal } I_D = I_0 \left( e^{q(V - IR_S)/nk_BT} - 1 \right)  I_{gen} = -qA \frac{n_i}{2\tau_0} W$
小信号:	$G_{d} = \frac{I_{D} + I_{0}}{k_{B}T/q} \qquad C_{J}(V_{R}) = \frac{K_{S}\varepsilon_{0}A}{\left[\frac{2K_{S}\varepsilon_{0}}{qN_{A}}(V_{bi} - V_{A})\right]^{1/2}} \qquad C_{D} = G_{d} \tau_{n}$
MS 二极管:	$qV_{bi} =  \Phi_{M} - \Phi_{S}  \qquad \Phi_{BP} = \chi + E_{G} - \Phi_{M} \qquad \Phi_{BN} = \Phi_{M} - \chi$ $J = J_{0} \left( e^{qV_{A}/k_{B}T} - 1 \right) \qquad J_{0} = A^{*}T^{2}e^{-\Phi_{B}/k_{B}T} \qquad A^{*} = \frac{4\pi q m^{*}k_{B}^{2}}{h^{3}}$
	$J = J_0 \left( e^{qV_A/k_B T} - 1 \right) \qquad J_0 = A^* T^2 e^{-\Phi_B/k_B T} \qquad A^* = \frac{4\pi q m^* k_B^2}{h^3}$
MOS 电容:	$W = \sqrt{\frac{2K_s \varepsilon_0 \phi_s}{q N_A}} \text{ cm } \mathcal{E}_s = \sqrt{\frac{2q N_A \phi_s}{K_s \varepsilon_0}} \text{ V/cm}$
	$Q_B = -qN_AW(\phi_S) = -\sqrt{2qK_S\varepsilon_0N_A\phi_S} \text{ C/cm}^2$
	$Q_{B} = -qN_{A}W(\phi_{S}) = -\sqrt{2q} K_{S} \varepsilon_{0} N_{A} \phi_{S} \text{ C/cm}^{2}$ $V_{G} = V_{FB} + \phi_{S} + \Delta \phi_{ox} = V_{FB} + \phi_{S} - \frac{Q_{S}(\phi_{S})}{C_{ox}}$ $C_{ox} = K_{O} \varepsilon_{0} / x_{o}$
	$V_{FB} = \Phi_{ms}/q - Q_F/C_{ox}$

	$C = \frac{C_{ox}}{1 + \frac{K_o W(\phi_S)}{K_S x_o}} \qquad V_T = -\frac{Q_B(2\phi_F)}{C_{ox}} + 2\phi_F \qquad Q_n = -C_{ox}(V_G - V_T)$
MOSFETs:	$\begin{split} I_D &= -WQ_n \big( y = 0 \big) \big\langle \upsilon_y \big( y = 0 \big) \big\rangle \\ I_D &= \frac{W}{I} \mu_n C_{ox} \big( V_{GS} - V_T \big) V_{DS} \qquad I_D = W C_{ox} \upsilon_{sat} \big( V_{GS} - V_T \big) \\ \text{平方律原理:} \\ I_D &= \frac{W}{L} \mu_n C_{ox} \Big[ \big( V_{GS} - V_T \big) V_{DS} - V_{DS}^2 \big/ 2 \Big]  \begin{pmatrix} 0 \leq V_{DS} \leq V_{GS} - V_T \\ V_{GS} \geq V_T \end{pmatrix} \\ I_D &= \frac{W}{2L} \mu_n C_{ox} \big( V_{GS} - V_T \big)^2  \begin{pmatrix} V_{DS} > V_{GS} - V_T \\ V_{GS} \geq V_T \end{pmatrix} \end{split}$
双极型晶体管: (NPN,短发射极, 基极和集电极)	Ebers-Moll equations: $I_{C}(V_{BE}, V_{BC}) = \alpha_{F}I_{F0}\left(e^{qV_{BE}/k_{B}T} - 1\right) - I_{R0}\left(e^{qV_{BC}/k_{B}T} - 1\right)$ $I_{E}(V_{BE}, V_{BC}) = I_{F0}\left(e^{qV_{BE}/k_{B}T} - 1\right) - \alpha_{R}I_{R0}\left(e^{qV_{BC}/k_{B}T} - 1\right)$ $I_{F0} = qA\left(\frac{D_{nB}}{W_{B}}\frac{n_{i}^{2}}{N_{AB}} + \frac{D_{pE}}{W_{E}}\frac{n_{i}^{2}}{N_{DE}}\right)$ $I_{R0} = qA\left(\frac{D_{nB}}{W_{B}}\frac{n_{i}^{2}}{N_{AB}} + \frac{D_{pC}}{W_{C}}\frac{n_{i}^{2}}{N_{DC}}\right)$ $\alpha_{F} = \gamma_{F}\alpha_{T}$ $\alpha_{R} = \gamma_{R}\alpha_{T}$ $\alpha_{F}I_{F0} = \alpha_{R}I_{R0}$ $\gamma_{F} = \frac{I_{En}}{I_{En} + I_{Ep}} = \frac{1}{1 + \frac{D_{pE}}{D_{nB}}\frac{W_{B}}{W_{E}}\frac{N_{AB}}{N_{DE}}}$ $\alpha_{T} = \frac{I_{Cn}}{I_{En}} = \frac{1}{1 + \frac{1}{2}\left(\frac{W_{B}}{L_{nB}}\right)^{2}}$ $\beta_{F} = \frac{\alpha_{F}}{1 - \alpha_{F}}$ $\alpha_{F} = \frac{\beta_{F}}{1 + \beta_{F}}$