# LASSO

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# Clear environment
rm(list = ls())

### Loading Data and Exploratory Data Analysis

```
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
# Read in dataset
data = read.csv("https://raw.githubusercontent.com/Panta-Rhei-LZ/MDA_9159_Team_Bits_Project/main/Team_B
# Remove price=0 entries
data = data[data$PRICE != 0, ]
# Remove rows with NA in all columns except 'YR_RMDL'
data = data %>% dplyr::filter(!if_any(-YR_RMDL, is.na))
# Remove not useful columns
data = data %>% dplyr::select(-SSL, -OBJECTID, -GIS_LAST_MOD_DTTM,
                       -QUALIFIED, -SALE_NUM, -BLDG_NUM,
                       -STYLE_D, -STRUCT_D, -GRADE_D,
                       -CNDTN_D, -EXTWALL_D, -ROOF_D,
                       -INTWALL_D, -USECODE, -HEAT_D,
                       -NUM_UNITS, -STRUCT)
head(data)
##
     BATHRM HF_BATHRM HEAT AC ROOMS BEDRM AYB YR_RMDL EYB STORIES
                                        6 1911
## 1
                   1
                         8 Y
                                 12
                                                  2021 1989
                                                               3.75
## 2
                        1 Y
                                        5 1912
                                                  2009 1978
                                                               3.00
         3
                   1
                                 13
## 3
         3
                   1
                        7 Y
                                 6
                                        4 1910
                                                  2022 1993
                                                               3.00
                        7 Y
         3
                                        4 1912
                                                  2000 1978
## 4
                   1
                                 11
                                                               3.00
## 5
                        1 Y
                                 11
                                        5 1912
                                                  2007 1993
                                                               3.00
          4
                    1
## 6
                                        7 1895
                                                               3.00
                   1
                         8 Y
                                 16
                                                  2014 1993
                   SALEDATE PRICE GBA STYLE GRADE CNDTN EXTWALL ROOF INTWALL
## 1 2019/08/19 04:00:00+00 3275000 6765
                                            10
                                                                20
                                                                     11
## 2 1999/08/04 04:00:00+00 550000 2282
                                             7
                                                   6
                                                         4
                                                                14
                                                                      2
                                                                              6
                                             7
## 3 2019/07/22 04:00:00+00 1700000 2016
                                                                      6
                                                                14
                                                                              6
## 4 2021/10/27 04:00:00+00 1500000 2034
                                             7
                                                  6
                                                         4
                                                                14
                                                                      6
                                                                              6
## 5 2023/04/18 04:00:00+00 2232500 2655
                                             7
                                                   6
                                                         5
                                                                14
                                                                      2
                                                                              6
## 6 2013/12/30 05:00:00+00 1320000 2894
                                                                14
                                                                      6
                                                                              6
    KITCHENS FIREPLACES LANDAREA
## 1
           1
                       6
                             2104
## 2
           2
                       3
                              936
           2
                       2
## 3
                              936
## 4
           2
                       2
                              988
## 5
           3
                       4
                             1674
## 6
                             1674
```

### Variable Explanation

We are dealing with housing data in this report, let me go over through the meanings behind each predictor:

- 1. PRICE: response
- 2. BATHRM: # bathrooms
- 3. HF BATHRM: # half bathrooms
- 4. HEAT: heating
- 5. AC: air conditioning
- 6. ROOMS: # rooms
- 7. BEDRM: # bedrooms
- 8. AYB: The earliest time the main portion of the building was built
- 9. YR RMDL: Year structure was remodelled
- 10. EYB: The year an improvement was built
- 11. STORIES: # stories in primary dwelling
- 12. SALEDATE: Date of sale
- 13. GBA: Gross building area in square feet
- 14. STYLE: House style
- 15. GRADE: House grade
- 16. CNDTN: House condition
- 17. EXTWALL: Exterior wall tyle
- 18. ROOF: Roof type
- 19. INTWALL: Interior wall type
- 20. KITCHENS: # kitchens
- 21. FIREPLACES: # fireplaces
- 22. LANDAREA: Land area of property in square feet

#### NA Data

Now let us explore the percentage of missing data for each predictor:

```
missing_data = round(sapply(data, function(x) mean(is.na(x) * 100)), 3)
missing_data
## BATHRM HF_BATHRM HEAT AC ROOMS BEDRM AYB
```

##	BATHRM	HF_BATHRM	HEAT	AC	ROOMS	BEDRM	AYB
##	0.000	0.000	0.000	0.000	0.000	0.000	0.000
##	YR_RMDL	EYB	STORIES	SALEDATE	PRICE	GBA	STYLE
##	36.432	0.000	0.000	0.000	0.000	0.000	0.000
##	GRADE	CNDTN	EXTWALL	ROOF	INTWALL	KITCHENS	FIREPLACES
##	0.000	0.000	0.000	0.000	0.000	0.000	0.000
##	LANDAREA						
##	0.000						

From the R output above, observe that "YR\_RMDL: Year structure was remodeled" has around 36% missing data. A possible explanation for this could be: not all buildings were remodeled.

### Preprocessing

- Converted some predictors to numerical values:
  - AC: "Y" and "N" corresponds to "1" and "0".
  - SALEDATE: Transform calendar format values in SALEDATE to numerical values using as.Date().
- Created dummy variables for categorical predictors:

- These categorical variables include: "AC", HEAT", "STYLE", "GRADE", "CNDTN", "EXTWALL", "ROOF" and "INTWALL".
- Introduced a few new variables:
  - SALE\_YEAR: The year that the house was sold, it is derived from SALEDATE.
  - SALE\_AYB\_DIFF: The difference between the year sold and the year built.
  - SALE\_EYB\_DIFF: The difference between the year sold and the year an improvement was applied.
  - SALE\_RMDL\_DIFF: The difference between the year sold and the year structure was remodeled.'

```
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
library(fastDummies)
# Transform Yes/No for having AC to numerical values
data$AC = ifelse(data$AC == 'Y', 1, 0)
# Add SALEYEAR
data$SALE_YEAR = year(ymd_hms(data$SALEDATE))
# Add SALEYEAR and AYB diff
data$SALE_AYB_DIFF = data$SALE_YEAR - data$AYB
# Add SALEYEAR and EYB diff
data$SALE_EYB_DIFF = data$SALE_YEAR - data$EYB
# Add SALEYEAR and YR_RMDL diff
data$SALE_RMDL_DIFF = data$SALE_YEAR - data$YR_RMDL
# Convert SALEDATE column to numeric values
data$SALEDATE = as.numeric(as.Date(data$SALEDATE))
# Replace NA with column median
data = data.frame(lapply(data, function(column) {
  column_median = median(column, na.rm = TRUE)
  column[is.na(column)] = column_median
  column
}))
set.seed(9159)
# Temporarily storing current data structure for plotting in later steps
temp_data = data[sample(nrow(data), 600),]
# Create dummy variables for categorical predictors
data = dummy_cols(
 data,
 select_columns = c("HEAT", "STYLE", "GRADE", "CNDTN",
                     "EXTWALL", "ROOF", "INTWALL", "AC"),
```

```
remove_selected_columns = TRUE,
  remove_first_dummy = TRUE
)

# Define box-cox and inverse box-cox transformation
powerfun = function(y, lambda) {
  if (lambda == 0) {
    return(log(y))
  } else {
    return((y^lambda - 1) / lambda)
  }
}

inv_powerfun = function(y_transformed, lambda) {
  if (lambda == 0) {
    return(exp(y_transformed))
  } else {
    return((lambda * y_transformed + 1)^(1/lambda))
  }
}
```

### Data for Training and Validating

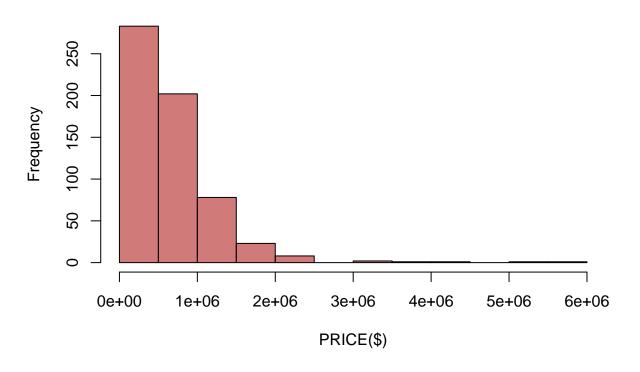
```
set.seed(9159)

# Randomly sample 600 data entries for our project
clean_data = data[sample(nrow(data), 600),]

data_train = clean_data[1:500, ] # First 500 rows for training
data_valid = clean_data[501:600, ] # Last 100 rows for validation
```

### Response Variable Transformation

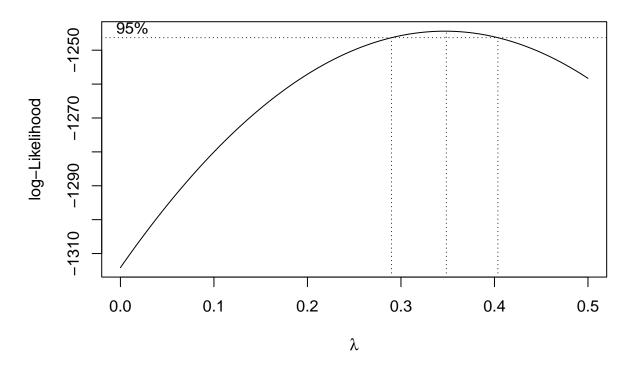
# **Histogram of Untransformed PRICE**



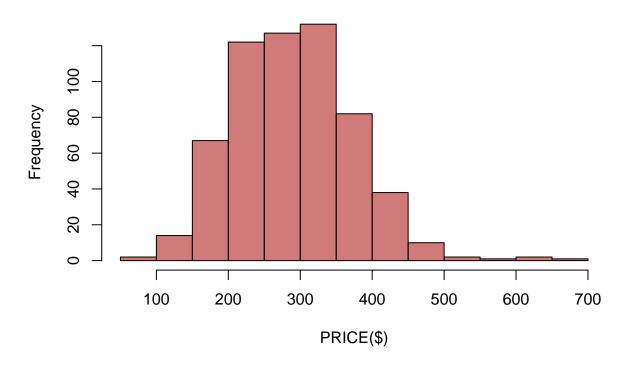
#### shapiro.test(clean\_data\$PRICE)

```
##
## Shapiro-Wilk normality test
##
## data: clean_data$PRICE
## W = 0.76073, p-value < 2.2e-16
library(MASS)

##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
## select
boxcox(lm(PRICE~., data=clean_data),lambda=seq(0,0.5,by=0.05))</pre>
```



# **Histogram of Log-Transformed PRICE**



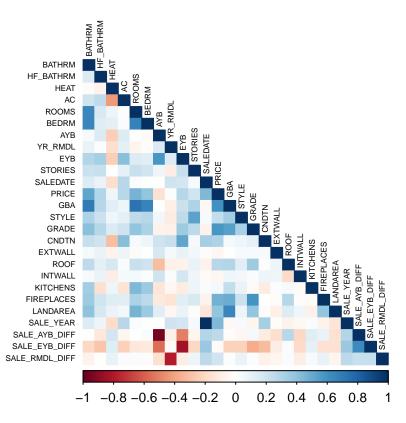
```
shapiro.test(powerfun(clean_data$PRICE, lambda))
```

```
##
## Shapiro-Wilk normality test
##
## data: powerfun(clean_data$PRICE, lambda)
## W = 0.98117, p-value = 5.504e-07
trans_PRICE = powerfun(clean_data$PRICE, lambda)
```

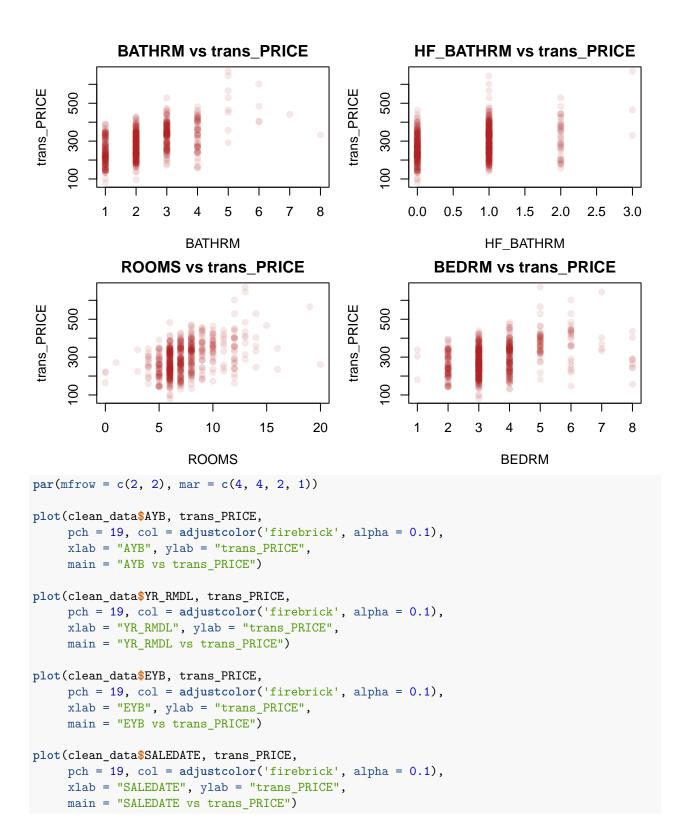
#### Data Visualization

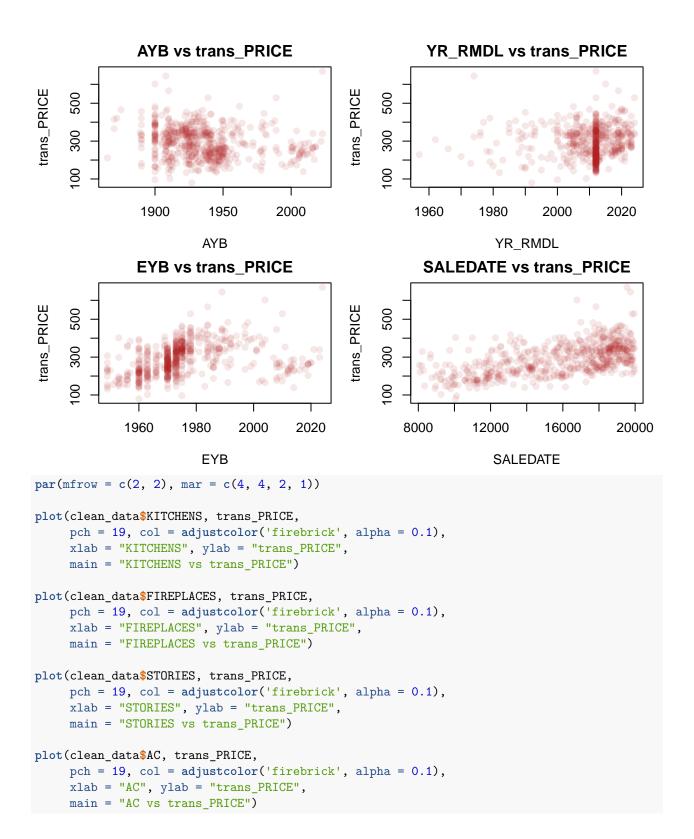
```
## corrplot 0.95 loaded

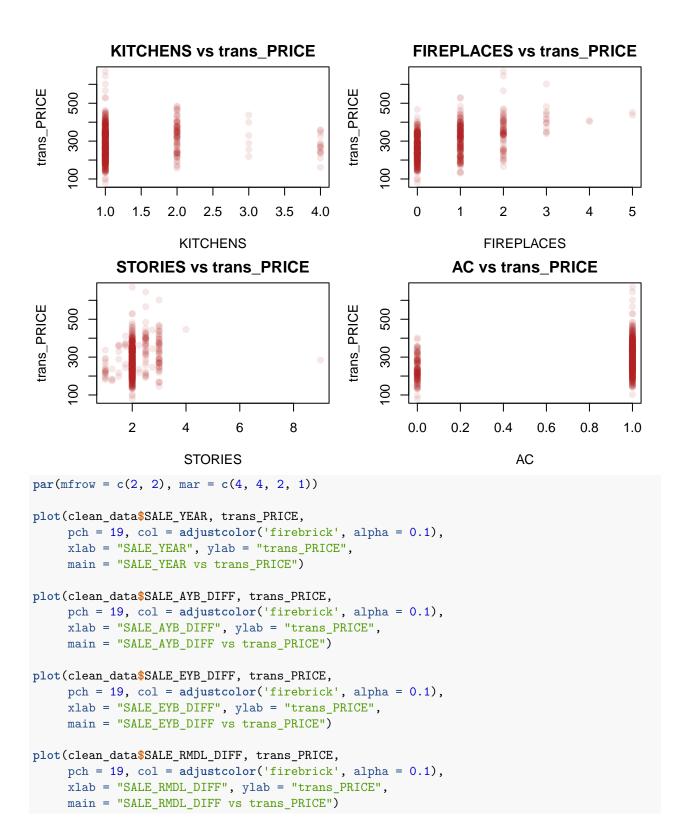
cor_temp_data = cor(temp_data, use='complete.obs', method='pearson')
corrplot(cor_temp_data, method='color', type='lower', tl.col='black', tl.cex=0.5)
```

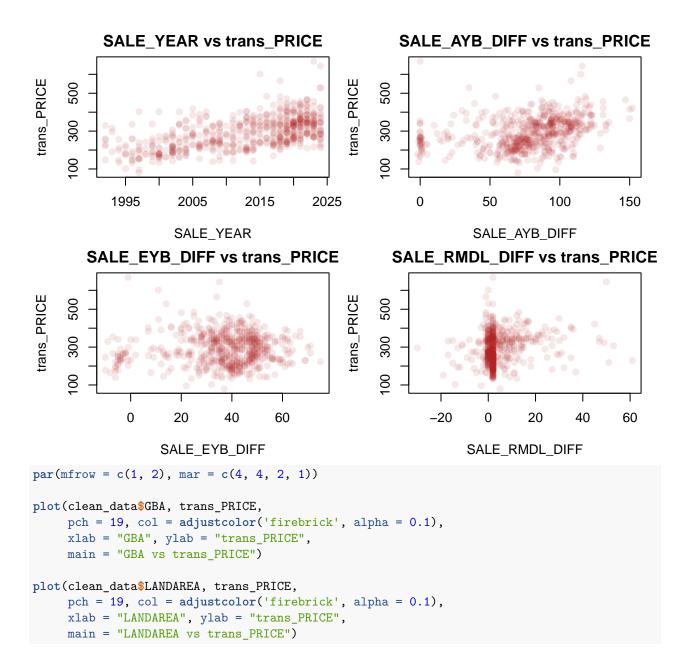


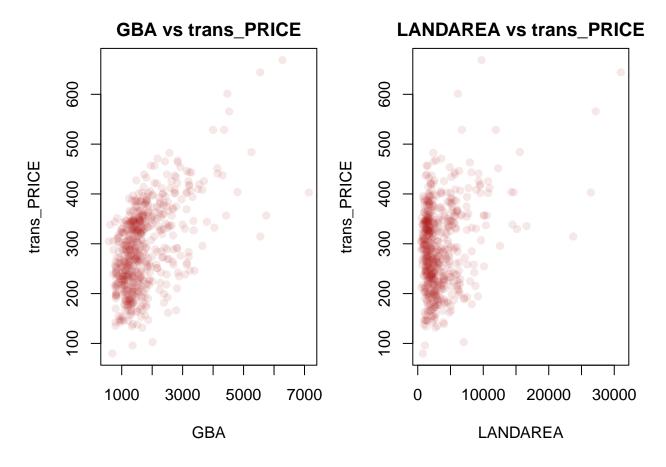
```
par(mfrow = c(2, 2), mar = c(4, 4, 2, 1))
plot(clean_data$BATHRM, trans_PRICE,
     pch = 19, col = adjustcolor('firebrick', alpha = 0.1),
     xlab = "BATHRM", ylab = "trans_PRICE",
     main = "BATHRM vs trans PRICE")
plot(clean_data$HF_BATHRM, trans_PRICE,
     pch = 19, col = adjustcolor('firebrick', alpha = 0.1),
     xlab = "HF_BATHRM", ylab = "trans_PRICE",
     main = "HF_BATHRM vs trans_PRICE")
plot(clean_data$ROOMS, trans_PRICE,
     pch = 19, col = adjustcolor('firebrick', alpha = 0.1),
     xlab = "ROOMS", ylab = "trans_PRICE",
     main = "ROOMS vs trans_PRICE")
plot(clean data$BEDRM, trans PRICE,
     pch = 19, col = adjustcolor('firebrick', alpha = 0.1),
     xlab = "BEDRM", ylab = "trans_PRICE",
     main = "BEDRM vs trans_PRICE")
```











## Model Building and Analysis

### Model Training without Non-Linear Predictors

```
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-8
X_train = model.matrix(powerfun(PRICE, lambda)~., data=data_train)[,-1]
X_test = model.matrix(powerfun(PRICE, lambda)~., data=data_valid)[,-1]
y_train = powerfun(data_train$PRICE, lambda)
y_test = powerfun(data_valid$PRICE, lambda)
cv_lasso = cv.glmnet(X_train, y_train, alpha=1)
best_lasso_lambda = cv_lasso$lambda.min
lasso_model = glmnet(X_train, y_train, alpha=1, lambda=best_lasso_lambda)
# Check non-zero LASSO coefficients
predict(lasso_model, type="coefficients", s=best_lasso_lambda)
## 116 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                  -3.262452e+02
## BATHRM
                   4.588097e+00
```

```
## HF_BATHRM
               3.904705e+00
## ROOMS
                 1.149480e+00
## BEDRM
                 5.370663e-01
## AYB
## YR_RMDL
## EYB
                 1.674562e-01
## STORIES
## SALEDATE
                  1.190030e-02
## GBA
                  1.663851e-02
## KITCHENS
## FIREPLACES
                 1.590030e+01
                  1.705915e-03
## LANDAREA
## SALE_YEAR
## SALE_AYB_DIFF
                   4.573229e-01
## SALE_EYB_DIFF
## SALE_RMDL_DIFF
## HEAT_1
                  -8.221947e+00
## HEAT 2
                  -1.746379e+01
## HEAT_3
## HEAT 4
## HEAT_5
## HEAT 6
## HEAT_7
## HEAT 8
                   2.167639e+01
## HEAT_9
## HEAT_10
## HEAT_11
## HEAT_12
## HEAT_13
                  3.450422e-01
## STYLE_1
                  -6.345856e+00
## STYLE_2
## STYLE_3
## STYLE_4
## STYLE_5
## STYLE 6
## STYLE_7
## STYLE 8
## STYLE_9
## STYLE_10
## STYLE_11
## STYLE 12
## STYLE_13
## STYLE 14
## STYLE_15
## STYLE_94
## STYLE_99
## GRADE_1
## GRADE_2
## GRADE_3
                  -3.041416e+01
## GRADE_4
                  -9.805268e+00
## GRADE_5
## GRADE 6
                 1.983899e+01
## GRADE_7
                 2.371386e+01
## GRADE 8
                 2.054186e+01
```

```
## GRADE 9
             7.057614e+01
## GRADE_10
## GRADE 11
## GRADE_12
## CNDTN_1
## CNDTN 2
               -1.550982e+01
## CNDTN 3
                 -1.415970e+01
## CNDTN_4
                 1.617908e+01
## CNDTN_5
## CNDTN_6
## EXTWALL_1
## EXTWALL_2
## EXTWALL_3
## EXTWALL_4
## EXTWALL_5
                  3.900062e+00
## EXTWALL_6
## EXTWALL_7
## EXTWALL 8
## EXTWALL_10
                 1.681968e+01
## EXTWALL_11
## EXTWALL_12
## EXTWALL_13
## EXTWALL_14
## EXTWALL 15
## EXTWALL_16
## EXTWALL_17
## EXTWALL_18
## EXTWALL_19
                 -1.514672e+01
## EXTWALL_20
                 -1.910498e+01
## EXTWALL_21
                 .
## EXTWALL_22
                 -5.043914e-01
## EXTWALL_23
## EXTWALL_24
## ROOF_1
                 -2.751832e+00
## ROOF_2
## ROOF_3
## ROOF 4
                 -5.339574e+00
## ROOF_5
## ROOF_6
                 8.714045e+00
## ROOF_7
## ROOF 8
## ROOF_9
## ROOF_10
## ROOF_11
## ROOF_12
## ROOF_13
## ROOF_14
## ROOF_15
## INTWALL_1
## INTWALL_2
                 -1.630494e+01
## INTWALL_3
## INTWALL_4
## INTWALL_5
## INTWALL 6
```

```
## INTWALL 7
                 1.874432e+01
## INTWALL 8
## INTWALL 9
## INTWALL_10
## INTWALL 11
                 -1.242621e+00
## AC 1
                  9.564972e+00
# Predicted values on training data
pred_train = predict(lasso_model, newx=X_train, s=best_lasso_lambda)
# Compute training SSE and SST
SSE = sum((y_train - pred_train)^2)
SST = sum((y_train - mean(y_train))^2)
# R-squared
R2 = 1 - SSE / SST
# Adjusted R-squared
n_train = length(y_train)
p_train = sum(coef(lasso_model, s=best_lasso_lambda) != 0)
Adjusted_R2 = 1 - (1 - R2) * (n_train) / (n_train - p_train)
cat("R-squared:", R2, '\n')
## R-squared: 0.8325244
cat("Adjusted R-squared:", Adjusted_R2, '\n')
## Adjusted R-squared: 0.8191409
Compute Loss Metrics
# Predicted values are transformed by powerfun(PRICE, lambda)
valid_pred = predict(lasso_model, s=best_lasso_lambda, newx=X_test)
# Using inv_powerfun to convert back to original scale
inv_valid_pred = inv_powerfun(valid_pred, lambda)
Compute MSE, RMSE and RMSLE
# Compute metrics on validation dataset
mse = mean((data_valid$PRICE - inv_valid_pred)^2)
rmse = sqrt(mse)
rmsle = sqrt(mean((log(data_valid$PRICE) - log(inv_valid_pred))^2))
cat("MSE:", mse, '\n')
## MSE: 145347824793
cat("RMSE:", rmse, '\n')
## RMSE: 381245.1
cat("RMSLE:", rmsle, '\n')
## RMSLE: 0.4067307
```

### Model Training including Non-Linear Predictors

```
X train2 = model.matrix(
 powerfun(PRICE, lambda)~. + poly(BATHRM, 4) +
   poly(HF_BATHRM, 3) + poly(BEDRM, 3) + poly(EYB, 2),
  data=data train
)[,-1]
X_test2 = model.matrix(
  powerfun(PRICE, lambda)~. + poly(BATHRM, 4) +
   poly(HF_BATHRM, 3) + poly(BEDRM, 3) + poly(EYB, 2),
  data=data_valid
)[,-1]
cv_lasso2 = cv.glmnet(X_train2, y_train, alpha=1)
best_lasso_lambda2 = cv_lasso2$lambda.min
lasso_model2 = glmnet(X_train2, y_train, alpha=1, lambda=best_lasso_lambda2)
# Check non-zero LASSO coefficients
predict(lasso_model2, type="coefficients", s=best_lasso_lambda2)
## 128 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                     15.955213972
## BATHRM
                       1.381972647
## HF BATHRM
                      2.346109349
## ROOMS
                      0.740200132
## BEDRM
                      0.174508299
## AYB
## YR_RMDL
                    0.002131434
## EYB
## STORIES
## SALEDATE
                        0.011860373
## GBA
                       0.019429632
## KITCHENS
## FIREPLACES
                     15.367339325
## LANDAREA
                        0.001565030
## SALE_YEAR
## SALE_AYB_DIFF
                        0.384952588
## SALE_EYB_DIFF
## SALE_RMDL_DIFF
                       0.074067132
## HEAT_1
                       -8.582266170
## HEAT 2
                      -20.013982805
## HEAT 3
## HEAT 4
## HEAT 5
## HEAT 6
## HEAT_7
## HEAT 8
                       20.589172254
## HEAT 9
## HEAT_10
## HEAT_11
## HEAT_12
## HEAT_13
## STYLE_1
                       -7.292723097
```

```
## STYLE 2
## STYLE_3
## STYLE 4
## STYLE_5
                      0.069959413
## STYLE 6
## STYLE 7
## STYLE 8
## STYLE_9
## STYLE 10
## STYLE_11
## STYLE_12
## STYLE_13
## STYLE_14
## STYLE_15
## STYLE_94
## STYLE_99
## GRADE_1
## GRADE 2
                     .
-28.247158831
## GRADE_3
## GRADE 4
                      -9.076734247
## GRADE_5
                     18.695135929
## GRADE 6
## GRADE_7
                      26.311045594
                      22.396547342
## GRADE 8
## GRADE_9
                      87.853112053
## GRADE_10
## GRADE_11
## GRADE_12
                    .
-11.263890469
-13.067309907
## CNDTN_1
## CNDTN_2
## CNDTN_3
## CNDTN_4
## CNDTN_5
                      16.768515233
## CNDTN_6
## EXTWALL_1
## EXTWALL_2
## EXTWALL 3
## EXTWALL_4
                    4.059318615
## EXTWALL_5
## EXTWALL_6
## EXTWALL 7
## EXTWALL_8
## EXTWALL_10
                      12.408006368
## EXTWALL_11
## EXTWALL_12
## EXTWALL_13
## EXTWALL_14
## EXTWALL_15
## EXTWALL_16
## EXTWALL_17
## EXTWALL_18
                    -14.083943081
-25.700326516
## EXTWALL 19
## EXTWALL_20
## EXTWALL 21
```

```
## EXTWALL_22
## EXTWALL_23
## EXTWALL 24
## ROOF_1
                       -3.091342746
## ROOF_2
## ROOF 3
## ROOF 4
                       -6.231959891
## ROOF_5
## ROOF_6
                       8.642179087
## ROOF_7
## ROOF_8
## ROOF_9
## ROOF_10
## ROOF_11
## ROOF_12
## ROOF_13
## ROOF_14
## ROOF 15
## INTWALL_1
## INTWALL 2
                     -14.672796892
## INTWALL_3
## INTWALL 4
## INTWALL_5
## INTWALL 6
## INTWALL 7
## INTWALL_8
                      22.005492132
## INTWALL_9
## INTWALL_10
## INTWALL_11
                      -0.762410072
## AC_1
                       6.946199933
                    51.550307002
-63.842247358
## poly(BATHRM, 4)1
## poly(BATHRM, 4)2
## poly(BATHRM, 4)3
## poly(BATHRM, 4)4
## poly(HF_BATHRM, 3)1 14.115285178
## poly(HF_BATHRM, 3)2 .
## poly(HF BATHRM, 3)3 8.445482535
## poly(BEDRM, 3)1
                    13.909364743
## poly(BEDRM, 3)2
                       -52.025933361
## poly(BEDRM, 3)3
## poly(EYB, 2)1
                       36.128865397
## poly(EYB, 2)2
                      -91.500056357
# Predicted values on training data
pred_train = predict(lasso_model2, newx=X_train2, s=best_lasso_lambda2)
# Compute training SSE and SST
SSE = sum((y_train - pred_train)^2)
SST = sum((y_train - mean(y_train))^2)
# R-squared
R2 = 1 - SSE / SST
# Adjusted R-squared
```

```
n_train = length(y_train)
p_train = sum(coef(lasso_model2, s=best_lasso_lambda2) != 0)
Adjusted_R2 = 1 - (1 - R2) * (n_train) / (n_train - p_train)
cat("R-squared:", R2, '\n')
## R-squared: 0.8387716
cat("Adjusted R-squared:", Adjusted_R2, '\n')
## Adjusted R-squared: 0.8228259
Compute Loss Metrics
# Predicted values are transformed by powerfun(PRICE, lambda)
valid_pred = predict(lasso_model2, s=best_lasso_lambda2, newx=X_test2)
# Using inv_powerfun to convert back to original scale
inv_valid_pred = inv_powerfun(valid_pred, lambda)
Compute MSE, RMSE and RMSLE
# Compute metrics on validation dataset
mse = mean((data_valid$PRICE - inv_valid_pred)^2)
rmse = sqrt(mse)
rmsle = sqrt(mean((log(data_valid$PRICE) - log(inv_valid_pred))^2))
cat("MSE:", mse, '\n')
## MSE: 143750464990
cat("RMSE:", rmse, '\n')
```

## RMSLE: 0.4342245

cat("RMSLE:", rmsle, '\n')

## RMSE: 379144.4