Statistical Analysis of EEG-experiment data

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1 Introduction

```
knitr::opts_chunk$set(echo = TRUE)
```

1.1 The data

(Fictitious data)

ERP experiment

- 20 Subjects,
- 6 Channels: O1, O2, PO7, PO8, P7, P8
- Stimuli: pictures. Conditions:
 - 1 (f): fear (face)
 - 2 (h): happiness (face)
 - 3 (d): disgust (face)
 - 4 (n): neutral (face)
 - 5 (o): object (face)
- Measure: Area around the component P170

Setting parameters, importing the data:

```
rm(list=ls())
load("./dataset/datiEEG.Rdata")

# dati2 is the same as dati, only selecting:
# ( Chan = "01" ) & ( Condition = "f" or "n" )
load("./dataset/dati2EEG.Rdata")

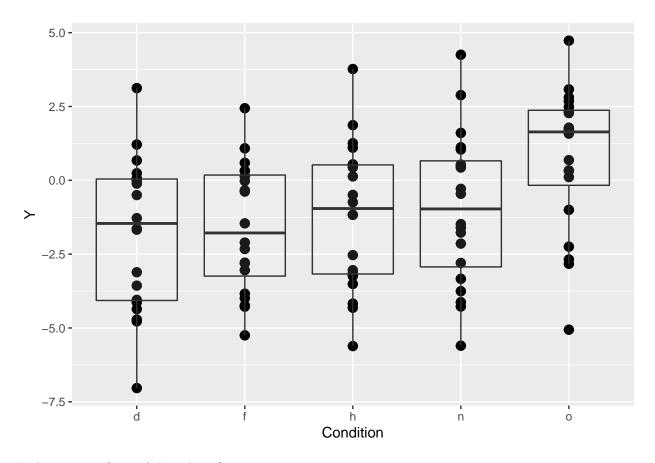
# VERY IMPORTANT:
contrasts(dati$Chan) <- contr.sum(6)
contrasts(dati$Condition) <- contr.sum(5)
contrasts(dati$Subj) <- contr.sum(nlevels(dati$Subj))

contrasts(dati2$Condition) <- contr.sum(2)
contrasts(dati2$Subj) <- contr.sum(nlevels(dati2$Subj))</pre>
```

1.2 Motivation (EDA)

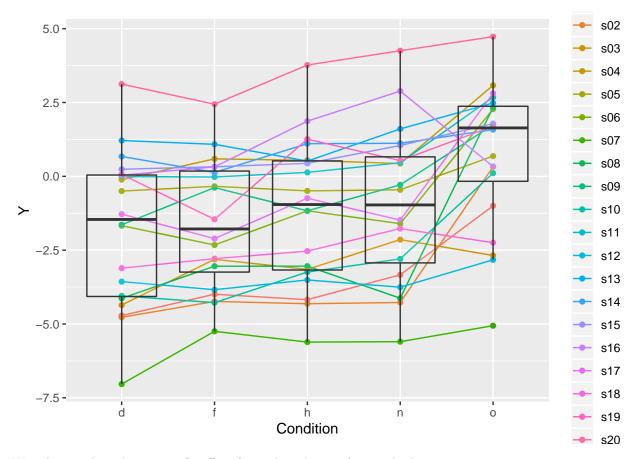
For Channel 01:

```
library(ggplot2)
p <- ggplot(subset(dati,Chan=="01"),aes(Condition,Y))
p+geom_point(size = 3) +geom_boxplot(alpha=.1)</pre>
```



Is there a specificity of the subject?

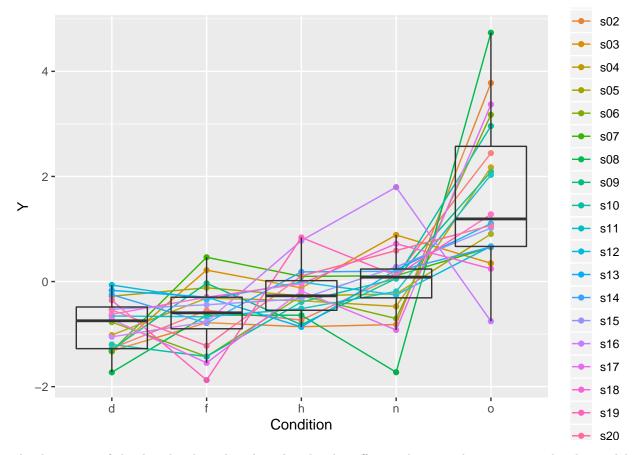
```
dati01=subset(dati,Chan=="01")
library(ggplot2)
p <- ggplot(dati01,aes(Condition,Y))
p+geom_point(aes(group = Subj, colour = Subj))+
  geom_line(aes(group = Subj, colour = Subj))+
  geom_boxplot(alpha=.1)</pre>
```



We subtract the subject-specific effect (i.e. subject's mean) to each observation.

```
dati01=subset(dati,Chan=="01")
Y=scale(matrix(dati01$Y,5),scale=FALSE)
dati01$Y=as.vector(Y)

library(ggplot2)
p <- ggplot(dati01,aes(Condition,Y))
p+geom_point(aes(group = Subj, colour = Subj))+
    geom_line(aes(group = Subj, colour = Subj))+
    geom_boxplot(alpha=.1)</pre>
```



The dispersion of the data has been largely reduced. This effect is the one taken in account by the models for repeated measures.

2 Repeated Mesures ANOVA

2.1 Introduction

wiki reference: https://en.wikipedia.org/wiki/Repeated_measures_design

A nice explanation can be found (in particular see 7.9 and 7.10):

Jonathan Baron (2011) Notes on the use of R for psychology experiments and questionnaires https://www.sas.upenn.edu/~baron/from_cattell/rpsych/rpsych.html

and in the Course materal of

ST 732, Applied Longitudinal Data Analysis, NC State University by Marie Davidian https://www.stat.ncsu.edu/people/davidian/courses/st732/notes/chap5.pdf from https://www.stat.ncsu.edu/people/davidian/courses/st732/

2.2 2 conditions, matched observations

Let consider the reduced problem: channel Chan=="01" and Condition=="n" or Condition=="f".

How to compare the two conditions? First try:

```
t.test(dati2$Y[dati2$Condition=="n"],
       dati2$Y[dati2$Condition=="f"])
##
   Welch Two Sample t-test
##
##
## data: dati2$Y[dati2$Condition == "n"] and dati2$Y[dati2$Condition == "f"]
## t = 0.8449, df = 36.861, p-value = 0.4036
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.8868791 2.1552491
## sample estimates:
## mean of x mean of y
## -0.964530 -1.598715
Is it ok?
NO! We don't take in account the fact that measures are taken on the same subject!
t.test(dati2$Y[dati2$Condition=="n"],
       dati2$Y[dati2$Condition=="f"],paired=TRUE)
##
##
   Paired t-test
##
## data: dati2$Y[dati2$Condition == "n"] and dati2$Y[dati2$Condition == "f"]
## t = 3.287, df = 19, p-value = 0.003877
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.2303616 1.0380084
## sample estimates:
## mean of the differences
##
                  0.634185
## equivalent to
t.test(dati2$Y[dati2$Condition=="n"]-
         dati2$Y[dati2$Condition=="f"])
##
##
   One Sample t-test
## data: dati2$Y[dati2$Condition == "n"] - dati2$Y[dati2$Condition ==
                                                                             "f"]
## t = 3.287, df = 19, p-value = 0.003877
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 0.2303616 1.0380084
## sample estimates:
## mean of x
## 0.634185
```

```
mod2=lm(Y~ Condition+Subj,data=dati2)
anova (mod2)
## Analysis of Variance Table
##
## Response: Y
##
            Df
               Sum Sq Mean Sq F value
                                         Pr(>F)
## Condition 1
               4.022 4.0219 10.804 0.003877 **
            19 207.022 10.8959 29.270 3.118e-10 ***
## Residuals 19
                 7.073 0.3722
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Compare the results. (Different or the same?)

2.3 Linear models with repeated measures

Let's consider (and fit) a linear model with Chan*Condition:

```
modlmf=lm(Y~ Chan*Condition,data=dati)
anova(modlmf)
```

```
## Analysis of Variance Table
##
## Response: Y
                  Df Sum Sq Mean Sq F value Pr(>F)
                  5 871.9 174.376 25.4499 <2e-16 ***
## Chan
                  4 1022.9 255.714 37.3209 <2e-16 ***
## Condition
                             3.328 0.4857 0.9719
## Chan:Condition 20 66.6
                 570 3905.5
                             6.852
## Residuals
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

We don't take in account the fact that measures are taken on the same subject!

Can we just add the Subj term?

```
modlmf=lm(Y~ Chan*Condition+Subj,data=dati)
anova(modlmf)
```

```
## Analysis of Variance Table
##
## Response: Y
##
                  Df Sum Sq Mean Sq F value Pr(>F)
## Chan
                   5 871.88 174.376 68.0714 <2e-16 ***
                  4 1022.86 255.714 99.8233 <2e-16 ***
## Condition
                  19 2494.02 131.264 51.2418 <2e-16 ***
## Subj
## Chan:Condition 20 66.56
                               3.328 1.2992 0.1724
## Residuals
                               2.562
                 551 1411.48
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Answer: yes and no.

The estimates are ok, but we need to take care of the residuals SS in the testing phase.

All the SS that we need can be found in the saturated linear model. We compute them now and we use them later.

```
modlmf=lm(Y~ Chan*Condition*Subj,data=dati)
anova(modlmf)
## Warning in anova.lm(modlmf): ANOVA F-tests on an essentially perfect fit
## are unreliable
## Analysis of Variance Table
##
## Response: Y
                       Df Sum Sq Mean Sq F value Pr(>F)
                        5 871.88 174.376
## Chan
## Condition
                        4 1022.86 255.714
                       19 2494.02 131.264
## Subj
## Chan:Condition
                       20 66.56
                                    3.328
## Chan:Subj
                       95 1017.54 10.711
## Condition:Subj
                       76 246.95
                                    3.249
## Chan:Condition:Subj 380 146.99
                                    0.387
## Residuals
                        0
                             0.00
```

2.4 Repeated measures

```
# The standard way
mod=aov(Y~ Chan*Condition+Subj + Error(Subj/(Chan*Condition)),data=dati)
summary(mod)
```

```
##
## Error: Subj
       Df Sum Sq Mean Sq
## Subj 19
            2494
                   131.3
##
## Error: Subj:Chan
            Df Sum Sq Mean Sq F value
                                      Pr(>F)
             5 871.9 174.38
                                16.28 1.42e-11 ***
## Residuals 95 1017.5
                        10.71
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Error: Subj:Condition
            Df Sum Sq Mean Sq F value Pr(>F)
## Condition 4 1022.9 255.71
                                 78.7 <2e-16 ***
## Residuals 76 246.9
                         3.25
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Error: Subj:Chan:Condition
```

```
##
                   Df Sum Sq Mean Sq F value Pr(>F)
## Chan: Condition 20 66.56
                                3.328
                                        8.604 <2e-16 ***
## Residuals
                  380 146.99
                                0.387
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
A better output and slightly more compleate analysis (Sphericity Corrections):
library(ez)
## Registered S3 methods overwritten by 'lme4':
##
     method
                                      from
##
     cooks.distance.influence.merMod car
##
     influence.merMod
##
     dfbeta.influence.merMod
                                      car
     dfbetas.influence.merMod
##
                                      car
mod=ezANOVA(dv=Y, wid=Subj, within=.(Chan,Condition),data=dati,type=3)
## Warning in log(det(U)): NaNs produced
print(mod)
## $ANOVA
##
             Effect DFn DFd
                                     F
                                                  p p<.05
                                                                  ges
## 2
                         95 16.280163 1.422895e-11
                                                        * 0.18250183
## 3
          Condition
                      4 76 78.697466 2.998429e-26
                                                        * 0.20754506
## 4 Chan: Condition 20 380 8.604227 5.232560e-21
                                                        * 0.01675807
## $`Mauchly's Test for Sphericity`
##
        Effect
                        W
                                      p p<.05
## 2
          Chan 0.03433646 3.910057e-07
## 3 Condition 0.06754172 4.802965e-07
##
## $`Sphericity Corrections`
                                     p[GG] p[GG]<.05
##
             Effect
                          GGe
                                                            HFe
               Chan 0.4368229 3.441213e-06
                                                    * 0.4957490 9.287363e-07
          Condition 0.4114825 4.226482e-12
                                                    * 0.4454085 6.399344e-13
## 4 Chan:Condition 0.1134660 4.452748e-04
                                                    * 0.1296611 2.121437e-04
##
     p[HF]<.05
## 2
## 3
## 4
```

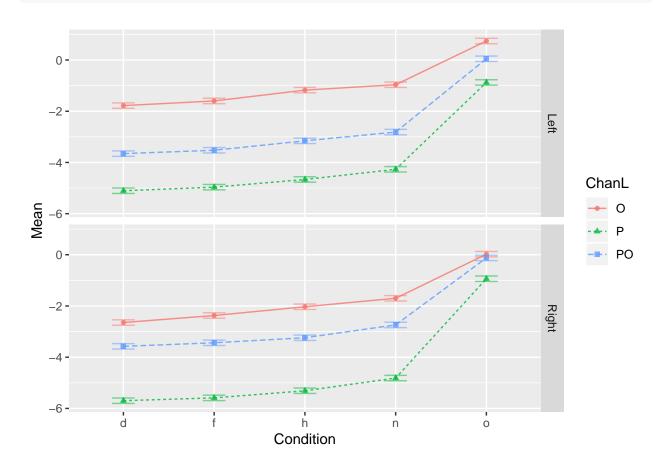
To see the relation between repeated measures and linear model, again, the Baron material is a good start. Specially see section "7.9.3 The Appropriate Error Terms"

2.5 Spend your DF in a different way!

Same number of DF, but spent in a different way

```
dati$Lateral=dati$Chan
levels(dati$Lateral)
## [1] "01" "02" "P7" "P8" "P07" "P08"
levels(dati$Lateral)[c(1,3,5)]="Left"
levels(dati$Lateral)[-1]="Right"
levels(dati$Lateral)
## [1] "Left" "Right"
contrasts(dati$Lateral) <- contr.sum(2)</pre>
dati$ChanL=dati$Chan
# https://en.wikipedia.org/wiki/Regular_expression
# Digits: \d
levels(dati$ChanL)=gsub("\\d","",levels(dati$ChanL))
contrasts(dati$ChanL) <- contr.sum(3)</pre>
# The standard way
# mod=aov(Y~ ChanL*Lateral*Condition+Subj + Error(Subj/(ChanL*Lateral*Condition)), data=dati)
# summary(mod)
#
library(ez)
mod=ezANOVA(dv=Y, wid=Subj, within=.(Condition, Lateral, ChanL), data=dati, type=3)
print(mod)
## $ANOVA
                      Effect DFn DFd
##
                                              F
                                                           p p<.05
## 2
                   Condition 4 76 78.6974657 2.998429e-26
                     Lateral 1 19 0.8340652 3.725436e-01
## 3
                       ChanL 2 38 56.1729241 4.478690e-12
## 4
## 5
         Condition:Lateral 4 76 0.1443064 9.649821e-01
           Condition: ChanL 8 152 35.1954651 5.609013e-31
## 6
              Lateral:ChanL 2 38 2.8073524 7.292266e-02
## 7
## 8 Condition:Lateral:ChanL 8 152 2.6449974 9.620701e-03
## 2 0.2075450604
## 3 0.0070380089
## 4 0.1749978790
## 5 0.0001853800
## 6 0.0159782333
## 7 0.0040220980
## 8 0.0006202045
## $`Mauchly's Test for Sphericity`
##
                     Effect
                                                     p p<.05
                                        W
## 2
                   Condition 6.754172e-02 4.802965e-07
## 4
                       ChanL 6.299144e-01 1.561471e-02
          Condition:Lateral 9.051612e-03 1.045354e-13
## 5
```

```
## 6
             Condition: ChanL 1.397323e-05 7.887294e-21
               Lateral:ChanL 8.087935e-01 1.480945e-01
## 7
## 8 Condition:Lateral:ChanL 3.462436e-05 2.626994e-18
##
## $`Sphericity Corrections`
##
                      Effect
                                    GGe
                                               p[GG] p[GG]<.05
                                                                      HFe
## 2
                   Condition 0.4114825 4.226482e-12
                                                              * 0.4454085
                       ChanL 0.7298814 2.181290e-09
                                                              * 0.7752249
## 4
## 5
           Condition:Lateral 0.3235149 7.714124e-01
                                                                0.3371918
             Condition: ChanL 0.2488273 2.427683e-09
## 6
                                                              * 0.2778788
## 7
               Lateral:ChanL 0.8394850 8.359370e-02
                                                                0.9115913
## 8 Condition:Lateral:ChanL 0.2410174 8.634269e-02
                                                                0.2677123
            p[HF] p[HF]<.05
##
## 2 6.399344e-13
## 4 7.702179e-10
## 5 7.811776e-01
## 6 3.463383e-10
## 7 7.863060e-02
## 8 7.969075e-02
```

2.6 Sphericity

The sphericity assumption is an assumption about the structure of the covariance matrix in a repeated measures design. Before we describe it lets consider a simpler (but stricter) condition.

Compound symmetry

Compound symmetry is met if all the covariances (the off-diagonal elements of the covariance matrix) are equal and all the variances are equal in the populations being sampled. Provided the observed covariances are roughly equal in our samples (and the variances are OK too) we can be pretty confident that compound symmetry is not violated.

If compound symmetry is met, then sphericity is also met.

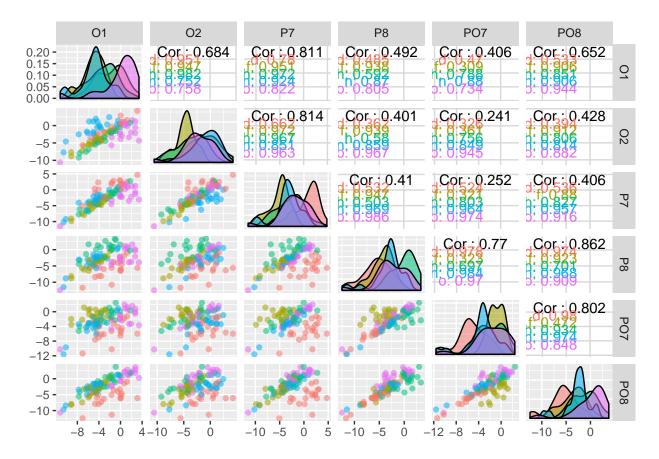
compound symmetry is met when the correlation between Condition f and Condition h is equal to the correlation between Condition f and Condition o or Condition h and Condition n, etc (same for any other factor within subject, such as Chan). But a more direct way to think about compound symmetry is to say that it requires that all subjects in each group change in the same way over trials. In other words the slopes of the lines regressing the dependent variable on time are the same for all subjects. Put that way it is easy to see that compound symmetry can really be an unrealistic assumption.

Is compound symmetry met in our data?

```
# install.packages("GGally")
library(GGally)

## Registered S3 method overwritten by 'GGally':
## method from
## +.gg ggplot2

Y=matrix(dati$Y,byrow = TRUE,nrow = 20*5)
Y=data.frame(Y)
names(Y)=levels(dati$Chan)
ggpairs(Y,aes(colour = dati$Condition[1:100], alpha = 0.4))
```



Not really! (correlations often differ)

Sphericity

The sphericity assumption is that the all the variances of the differences are equal (in the population sampled). In practice, we'd expect the observed sample variances of the differences to be similar if the sphericity assumption was met.

We can check sphericity assumption using the covariance matrix, but it turns out to be fairly laborious. Remember that variance of differences can be computed as:

$$S_x^2 - S_y^2 = S_x^2 + S_y^2 - 2S_{xy}$$

Further reading: http://homepages.gold.ac.uk/aphome/spheric.html

This is often an unrealistic assumption in EEG data (spatial location of channel relates to correlation between measures)

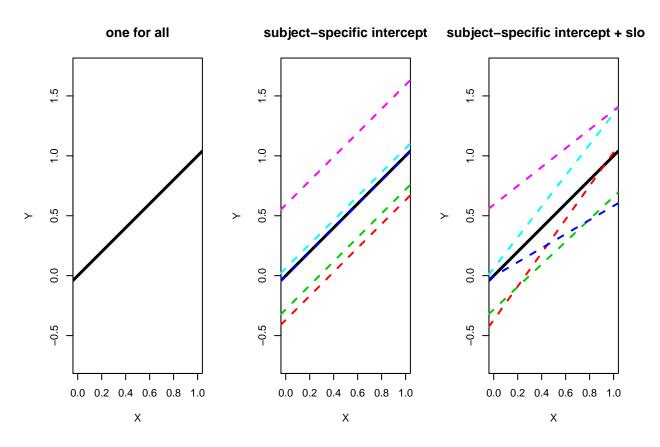
2.7 (Further) Limitations

- (Design and) Data must be balanced
- Repeated Measures Anova doesn't allow for missing data (e.g. subjects/condiction/channel cells)
- It only handle factors, no quantitative variables

Mixed model is a more flexible approach.

3 Mixed models

3.1 Motivation/Introduction



Mixed models allow for more flexible modelization.

I assume you are expert on mixed models, if not https://en.wikipedia.org/wiki/Mixed_model and much more on: http://webcom.upmf-grenoble.fr/LIP/Perso/DMuller/M2R/R_et_Mixed/documents/Bates-book.pdf

and

https://cran.r-project.org/web/packages/lme4/vignettes/lmer.pdf

3.2 The model

Models with random effects can be defined as:

$$Y_{n\times 1} = X_{n\times p}B_{p\times 1} + Z_{n\times q}b_{q\times 1} + \varepsilon_{n\times 1}$$

where

$$\varepsilon \sim \mathcal{N}(0, \sigma^2 I_n)$$

In the models we will consider, the random effects are modeled as a multivariate normal random variable:

$$b \sim \mathcal{N}(0, \Sigma_{a \times a}),$$

In a linear mixed model the conditional distribution $(Y|\mathcal{B}=b)$ is a spherical multivariate Gaussian.

In our case $n = \#Subjects \times \#Conditions \times \#Channels = 20 \times 5 \times 6 = 600$. X is the matrix of (dummified) predictors. Z can take many dimensions and values. Examples follow.

Random effect for Subject (Random Intercept)

Z is the matrix of dummy variables of the column dati\$Subj.

```
library(lmeTest)
# library(lme4)
# contrasts(dati$Lateral)=contr.sum
# contrasts(dati$ChanL)=contr.sum
# contrasts(dati$Condition)=contr.sum
mod=lmer(Y~ Condition*Lateral*ChanL +(1|Subj),data=dati)
car::Anova(mod)
```

```
## Analysis of Deviance Table (Type II Wald chisquare tests)
## Response: Y
##
                             Chisq Df Pr(>Chisq)
                          399.2932 4 < 2.2e-16 ***
## Condition
## Lateral
                          10.8062 1
                                       0.001012 **
## ChanL
                          323.3939 2 < 2.2e-16 ***
## Condition:Lateral
                            0.2827 4
                                       0.990905
## Condition:ChanL
                           24.7559 8
                                      0.001710 **
## Lateral:ChanL
                            6.1568 2
                                       0.046032 *
## Condition:Lateral:ChanL
                            0.9461 8
                                        0.998566
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Random effect for Subject and Channel

Actually, instead of Channel, we use the combination of ChanL*Lateral. Same prediction ability (6 channels in Channel and 3X2 combination of ChanL and Lateral), just a different point of view.

Z is the matrix of dummy variables of the column dati\$Subj.

```
mod2=lmer(Y~ 0+Lateral*ChanL*Condition +(0+Lateral*ChanL|Subj),data=dati)
## boundary (singular) fit: see ?isSingular
summary(mod2)
```

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## ImerModLmerTest]
## Formula: Y ~ 0 + Lateral * ChanL * Condition + (0 + Lateral * ChanL |
## Subj)
## Data: dati
##
## REML criterion at convergence: 1935.8
##
## Scaled residuals:
## Min 1Q Median 3Q Max
## -4.1900 -0.4578 -0.0039 0.5129 3.5464
```

```
##
## Random effects:
                             Variance Std.Dev. Corr
   Groups
             Name
                             3.8594
                                       1.9645
##
   Subj
             LateralLeft
##
             LateralRight
                             6.9792
                                       2.6418
                                                 0.63
##
                                      0.8233
                                                 0.20 0.24
             ChanL1
                             0.6778
##
             ChanL2
                                                -0.47 -0.45 -0.87
                             0.4653
                                       0.6821
                                                -0.07 0.18 -0.18 0.02
##
             Lateral1:ChanL1 0.1852
                                       0.4304
##
             Lateral1:ChanL2 0.1643
                                       0.4054
                                                -0.28 -0.14 0.29 -0.16 -0.82
##
   Residual
                             0.8518
                                       0.9229
  Number of obs: 600, groups: Subj, 20
##
## Fixed effects:
                                Estimate Std. Error
##
                                                             df t value
## LateralLeft
                               -2.516722
                                            0.442503
                                                     18.975804 -5.687
## LateralRight
                               -2.946310
                                            0.593125
                                                      19.053346
                                                                 -4.967
## ChanL1
                                1.381018
                                            0.191654
                                                      19.024146
                                                                  7.206
## ChanL2
                               -1.490922
                                            0.161564
                                                     19.015837
                                                                 -9.228
                               -1.011749
## Condition1
                                            0.075358 474.981472 -13.426
## Condition2
                               -0.849248
                                            0.075358 474.981472 -11.269
## Condition3
                               -0.531396
                                            0.075358 474.981472 -7.052
## Condition4
                               -0.151912
                                            0.075358 474.981472 -2.016
## Lateral1:ChanL1
                                            0.110006 19.164989
                                0.180370
                                                                  1.640
## Lateral1:ChanL2
                                            0.105142 19.226322
                                0.032409
                                                                   0.308
## Lateral1:Condition1
                                0.015606
                                            0.075358 474.981472
                                                                  0.207
## Lateral1:Condition2
                                0.004035
                                            0.075358 474.981472
                                                                  0.054
## Lateral1:Condition3
                                            0.075358 474.981472
                                0.049614
                                                                   0.658
## Lateral1:Condition4
                               -0.013239
                                            0.075358 474.981472
                                                                 -0.176
## ChanL1:Condition1
                                            0.106573 474.981472
                                0.149200
                                                                  1.400
## ChanL2:Condition1
                               -0.167232
                                            0.106573 474.981472
                                                                 -1.569
## ChanL1:Condition2
                                0.213801
                                            0.106573 474.981472
                                                                   2.006
## ChanL2:Condition2
                               -0.204413
                                            0.106573 474.981472 -1.918
## ChanL1:Condition3
                                0.278675
                                            0.106573 474.981472
                                                                   2.615
## ChanL2:Condition3
                               -0.233478
                                            0.106573 474.981472
                                                                 -2.191
## ChanL1:Condition4
                                0.169969
                                            0.106573 474.981472
                                                                  1.595
## ChanL2:Condition4
                                            0.106573 474.981472
                               -0.166870
                                                                 -1.566
## Lateral1:ChanL1:Condition1
                                0.022442
                                            0.106573 474.981472
                                                                  0.211
## Lateral1:ChanL2:Condition1
                                0.034156
                                            0.106573 474.981472
                                                                  0.320
## Lateral1:ChanL1:Condition2 -0.011970
                                            0.106573 474.981472
                                                                 -0.112
## Lateral1:ChanL2:Condition2
                                0.060872
                                            0.106573 474.981472
                                                                   0.571
## Lateral1:ChanL1:Condition3
                               -0.017273
                                            0.106573 474.981472
                                                                -0.162
## Lateral1:ChanL2:Condition3
                                0.026281
                                            0.106573 474.981472
                                                                  0.247
## Lateral1:ChanL1:Condition4
                               -0.014015
                                            0.106573 474.981472 -0.132
## Lateral1:ChanL2:Condition4
                                0.039652
                                            0.106573 474.981472
                                                                  0.372
##
                              Pr(>|t|)
## LateralLeft
                              1.76e-05 ***
## LateralRight
                              8.48e-05 ***
## ChanL1
                              7.58e-07 ***
## ChanL2
                              1.88e-08 ***
## Condition1
                               < 2e-16 ***
                               < 2e-16 ***
## Condition2
## Condition3
                              6.28e-12 ***
## Condition4
                               0.04438 *
## Lateral1:ChanL1
                               0.11739
```

```
## Lateral1:ChanL2
                              0.76122
## Lateral1:Condition1
                              0.83602
## Lateral1:Condition2
                              0.95732
## Lateral1:Condition3
                              0.51062
## Lateral1:Condition4
                              0.86061
## ChanL1:Condition1
                             0.16217
## ChanL2:Condition1
                             0.11727
## ChanL1:Condition2
                             0.04541 *
## ChanL2:Condition2
                              0.05570 .
## ChanL1:Condition3
                             0.00921 **
## ChanL2:Condition3
                             0.02895 *
## ChanL1:Condition4
                              0.11141
## ChanL2:Condition4
                              0.11807
## Lateral1:ChanL1:Condition1 0.83330
## Lateral1:ChanL2:Condition1 0.74873
## Lateral1:ChanL1:Condition2 0.91062
## Lateral1:ChanL2:Condition2 0.56815
## Lateral1:ChanL1:Condition3 0.87132
## Lateral1:ChanL2:Condition3 0.80532
## Lateral1:ChanL1:Condition4 0.89543
## Lateral1:ChanL2:Condition4 0.71001
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 30 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
#alternative:
# mod=lmer(Y~ Condition*Lateral*ChanL +(1+ChanL|Subj), data=dati)
  +(1+Chan|Subj) (equivalent to +(Chan|Subj)) is a linear combination of +(0+Chan|Subj). I better lik
car::Anova(mod2)
## Analysis of Deviance Table (Type II Wald chisquare tests)
## Response: Y
                              Chisq Df Pr(>Chisq)
##
## Lateral
                            31.7679 2 1.264e-07 ***
## ChanL
                            81.2828 2 < 2.2e-16 ***
                          1200.7713 4 < 2.2e-16 ***
## Condition
## Lateral:ChanL
                             7.7581 2
                                          0.02067 *
## Lateral:Condition
                                          0.93161
                             0.8501 4
                            74.4469 8 6.365e-13 ***
## ChanL:Condition
## Lateral:ChanL:Condition
                           2.8453 8
                                          0.94369
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

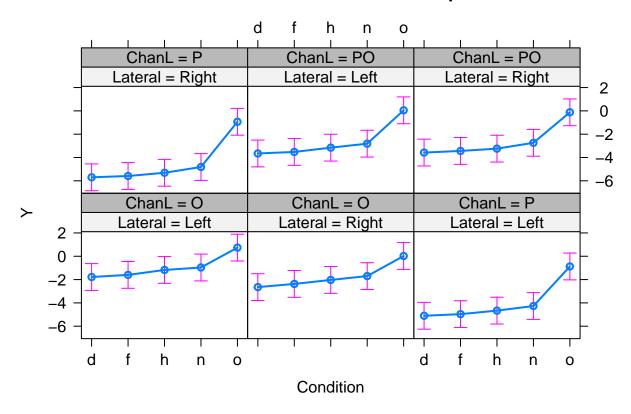
```
 \begin{tabular}{ll} \# \ \textit{More flexible, but hard to fit:} \\ \# \ \textit{mod3=lmer(Y$^\sim$ Condition*ChanL+Lateral + (0+Lateral|Subj) + (0+Condition|Subj) + (0+ChanL|Subj), data=dati)} \\ \# \ \begin{tabular}{ll} \# \ \begin{tabul
```

3.3 Plotting tools

for the first model:

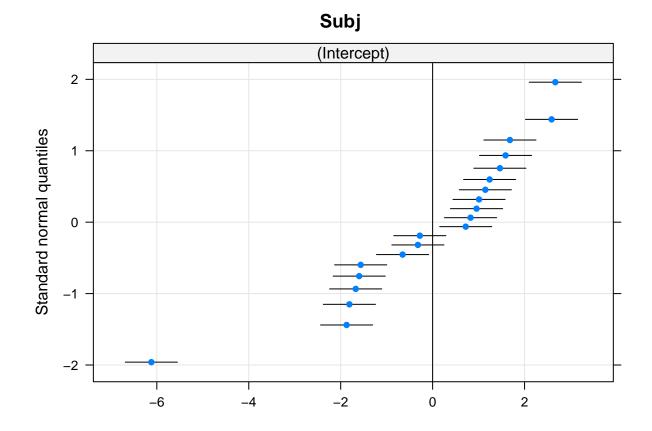
```
library(effects)
plot(allEffects(mod))
```

Condition*Lateral*ChanL effect plot



```
#plot random effects:
require(lattice)
qqmath(ranef(mod, condVar=TRUE))
```

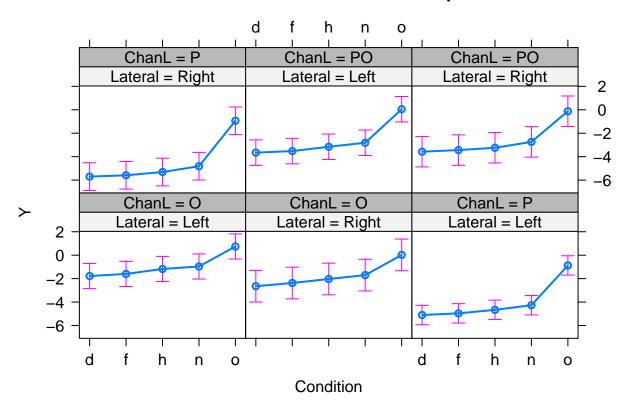
\$Subj



The second model:

```
library(effects)
plot(allEffects(mod2))
```

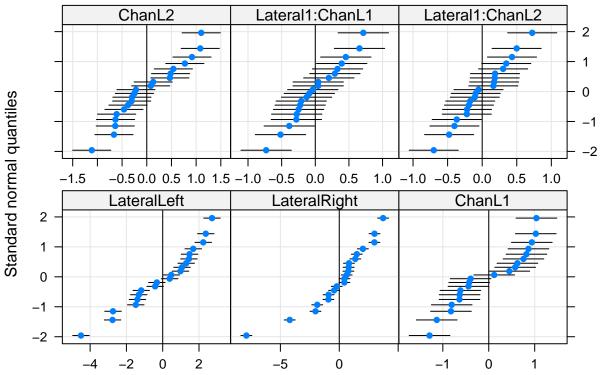
Lateral*ChanL*Condition effect plot



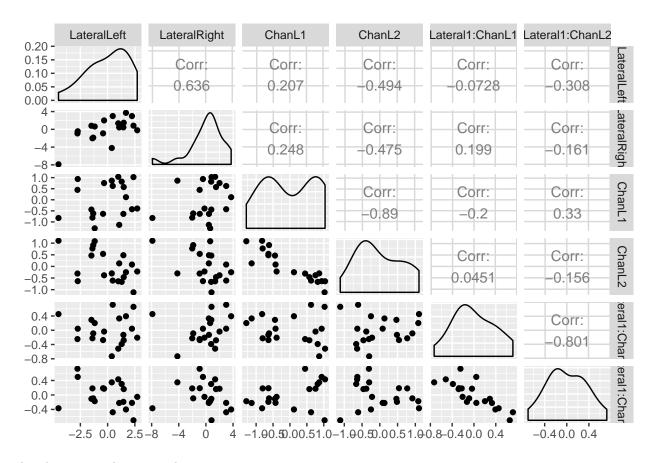
```
#plot random effects:
require(lattice)
qqmath(ranef(mod2, condVar=TRUE))
```

\$Subj





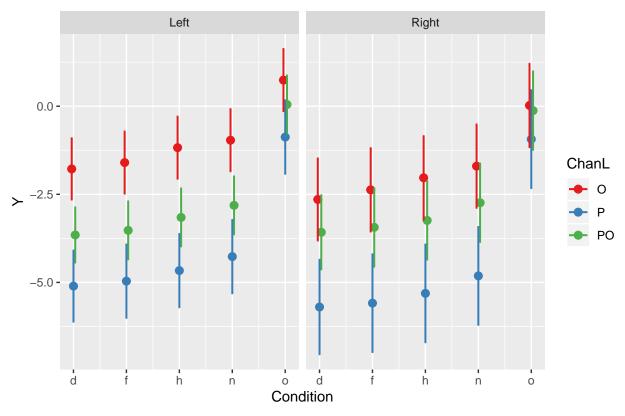
scatter plot
ggpairs(ranef(mod2, condVar=TRUE)[[1]])



An alternative plotting tool:

```
library(sjPlot)
library(ggplot2)
plot_model(mod2, type = "pred", terms = c("Condition", "ChanL", "Lateral"))
```

Predicted values of Y

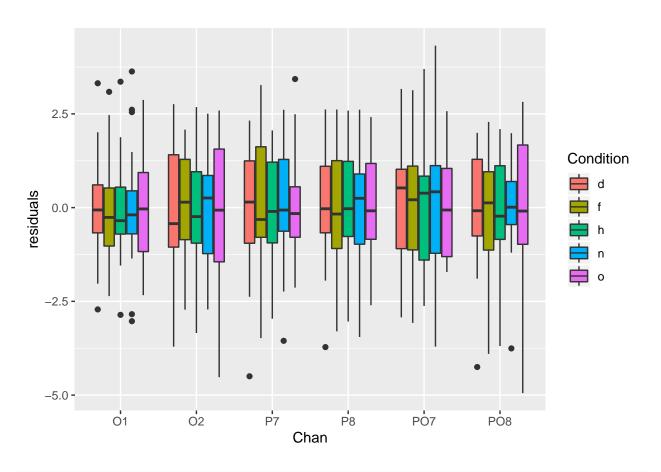


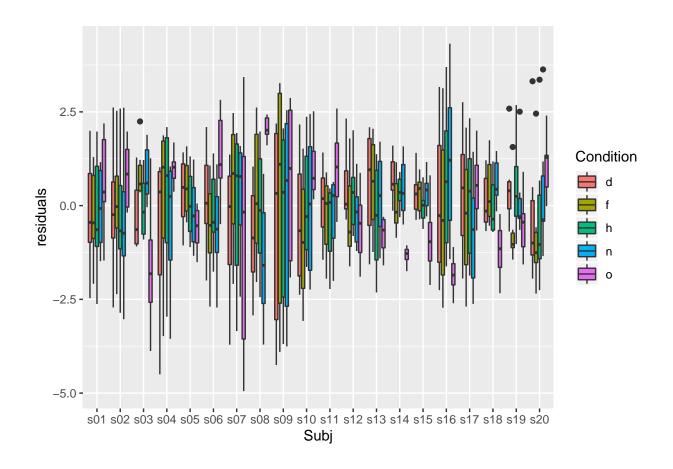
3.4 Validity of the assumptions

- Independence of the residuals?
- Normality of the residuals?
- Homoscedasticity of the residuals (i.e. same variance between subject/channel/condition?
- \bullet outliers?
- Leaverage? (influential observations)

Please, do not test for normality, for homoscedasticity, sphericity etc.

Use Exploratory data Analysis, instead!





3.5 Contrasts and post-hoc

3.5.1 Post-hoc

```
library(multcomp)

## Loading required package: mvtnorm

## Loading required package: survival

## Loading required package: TH.data

## Loading required package: MASS

## ## Attaching package: 'TH.data'

## The following object is masked from 'package:MASS':

## ## geyser
```

```
summary(glht(mod2, linfct = mcp(Condition = "Tukey")))
## Warning in mcp2matrix(model, linfct = linfct): covariate interactions found
## -- default contrast might be inappropriate
##
##
    Simultaneous Tests for General Linear Hypotheses
##
## Multiple Comparisons of Means: Tukey Contrasts
##
##
## Fit: lmer(formula = Y ~ 0 + Lateral * ChanL * Condition + (0 + Lateral *
      ChanL | Subj), data = dati)
##
## Linear Hypotheses:
##
             Estimate Std. Error z value Pr(>|z|)
## f - d == 0
              0.1625
                        0.1192 1.364
                                         0.6509
## h - d == 0
              0.4804
                          0.1192 4.031
                                         <0.001 ***
## n - d == 0
              0.8598
                          0.1192
                                 7.216
                                         <0.001 ***
## o - d == 0
                          0.1192 29.845
              3.5561
                                         <0.001 ***
## h - f == 0
              0.3179
                          0.1192 2.668
                                          0.0589 .
## n - f == 0
              0.6973
                                  5.852
                                         <0.001 ***
                          0.1192
## o - f == 0
              3.3936
                          0.1192 28.481
                                          <0.001 ***
## n - h == 0
              0.3795
                          0.1192 3.185
                                         0.0127 *
## o - h == 0
              3.0757
                          0.1192 25.813
                                          <0.001 ***
## o - n == 0
                          0.1192 22.628
                                          <0.001 ***
              2.6962
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- single-step method)
```

3.5.2 Custom contrasts

An example:

- neutral vs object in O1 (left)
- disgust vs neutral in O1 (left)
- fear vs neutral in O1 (left)
- happy vs neutral in O1 (left)

```
##
## Simultaneous Tests for General Linear Hypotheses
##
```

```
## Fit: lmer(formula = Y ~ 0 + Lateral * ChanL * Condition + (0 + Lateral *
      ChanL | Subj), data = dati)
##
##
## Linear Hypotheses:
##
             Estimate Std. Error z value Pr(>|z|)
## d - n == 0 0.53140
                        0.07536
                                7.052 1.77e-12 ***
## f - n == 0 -0.48035
                        0.11915 -4.031 5.54e-05 ***
## h - n == 0 -0.31785
                        0.11915 -2.668 0.00764 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- none method)
# with multiple comparisons
summary(compa)
##
##
    Simultaneous Tests for General Linear Hypotheses
##
## Fit: lmer(formula = Y ~ 0 + Lateral * ChanL * Condition + (0 + Lateral *
##
      ChanL | Subj), data = dati)
##
## Linear Hypotheses:
##
             Estimate Std. Error z value Pr(>|z|)
## n - o == 0 -0.37948
                        0.11915 -3.185 0.00494 **
## d - n == 0 0.53140
                        0.07536
                                 7.052
                                       < 0.001 ***
## f - n == 0 - 0.48035
                        0.11915
                                -4.031
                                        < 0.001 ***
## h - n == 0 -0.31785
                        0.11915 -2.668 0.02320 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Adjusted p values reported -- single-step method)
```

4 Multivariate ANOVA (MANOVA)

4.1 Motivation

ehi, wait a moment... the trials for object condition are much more than any other condition, the variance of its estimated component must be (much?) lower, homoschedastcity doesn't hold!!

Let's use a different approach Reshape the data from long to wide format.

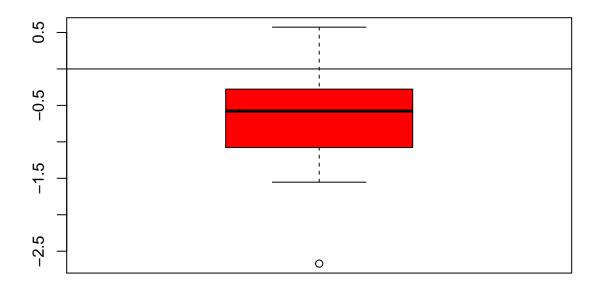
to simplify the example, let's consider the comparison between conditions neutral vs object.

4.2 Reshaping the data

Let' now compute the vectors of contrasts (one vector of reach channel, length equal to number of subjects): Fear vs Neutral

```
Y=matrix(dati$Y,byrow = TRUE,nrow = 20)
colnames(Y)=paste(dati$Condition,dati$ChanL,dati$Lateral,sep = "_")[1:30]
```

```
colnames(Y)
  [1] "f_P_Left"
##
                    "h_P_Left"
                                 "d_P_Left"
                                              "n_P_Left"
                                                           "o_P_Left"
## [6] "f_PO_Left" "h_PO_Left" "d_PO_Left" "n_PO_Left" "o_PO_Left"
## [11] "f_O_Left"
                    "h_O_Left"
                                 "d_O_Left"
                                              "n_O_Left"
                                                           "o_O_Left"
## [16] "f_P_Right" "h_P_Right" "d_P_Right" "n_P_Right" "o_P_Right"
## [21] "f_PO_Right" "h_PO_Right" "d_PO_Right" "n_PO_Right" "o_PO_Right"
## [26] "f_O_Right" "h_O_Right"
                                 "d_O_Right"
                                              "n_O_Right"
                                                           "o_O_Right"
contr=matrix(0,30,6)
contr[c(1,4),1]=c(1,-1)
contr[c(1,4)+5,2]=c(1,-1)
contr[c(1,4)+10,3]=c(1,-1)
contr[c(1,4)+15,4]=c(1,-1)
contr[c(1,4)+20,5]=c(1,-1)
contr[c(1,4)+25,6]=c(1,-1)
dim(contr)
## [1] 30 6
head(contr)
        [,1] [,2] [,3] [,4] [,5] [,6]
##
## [1,]
          1
               0
                    0
                         0
                              0
                                   0
## [2,]
                                   0
          0
                    0
                         0
                              0
## [3,]
                         0
                              0
                                   0
          0
               0
                    0
## [4,]
         -1
               0
                    0
                         0
                              0
                                   0
## [5,]
        0
                    0
                         0
                              0
                                   0
               0
## [6,]
                                   0
Yfn=Y%*%contr
colnames(Yfn) = levels(dati$Chan)
dim(Yfn)
## [1] 20 6
What we see in O1?
boxplot(Yfn[,1],col=2)
abline(0,0)
```



Same test as above, but under a different model

t.test(Yfn[,1])

```
##
## One Sample t-test
##
## data: Yfn[, 1]
## t = -4.3327, df = 19, p-value = 0.0003587
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0327953 -0.3599747
## sample estimates:
## mean of x
## -0.696385
```

We can run the analysis over all channels

(uni_t=apply(Yfn,2,t.test))

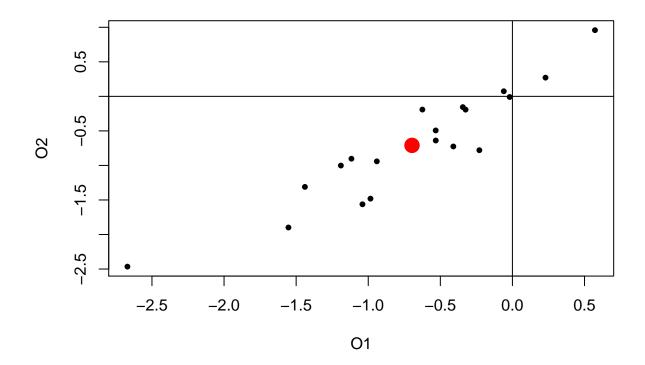
```
## $01
##
## One Sample t-test
##
## data: newX[, i]
```

```
## t = -4.3327, df = 19, p-value = 0.0003587
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0327953 -0.3599747
## sample estimates:
## mean of x
## -0.696385
##
##
## $02
##
   One Sample t-test
##
##
## data: newX[, i]
## t = -3.9761, df = 19, p-value = 0.0008092
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0831578 -0.3360722
## sample estimates:
## mean of x
## -0.709615
##
##
## $P7
##
##
   One Sample t-test
##
## data: newX[, i]
## t = -3.287, df = 19, p-value = 0.003877
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0380084 -0.2303616
## sample estimates:
## mean of x
## -0.634185
##
##
## $P8
##
  One Sample t-test
##
## data: newX[, i]
## t = -5.1301, df = 19, p-value = 5.95e-05
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0889013 -0.4578487
## sample estimates:
## mean of x
## -0.773375
##
##
## $P07
##
## One Sample t-test
```

```
##
## data: newX[, i]
## t = -3.8837, df = 19, p-value = 0.0009992
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.0736034 -0.3216666
## sample estimates:
## mean of x
## -0.697635
##
##
## $P08
##
## One Sample t-test
##
## data: newX[, i]
## t = -3.1978, df = 19, p-value = 0.004737
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -1.1131969 -0.2324531
## sample estimates:
## mean of x
## -0.672825
```

4.3 Manova

```
plot(Yfn[,1:2],pch=20)
abline(v=0)
abline(h=0)
points(mean(Yfn[,1]),mean(Yfn[,2]),cex=3,col=2,pch=20)
```

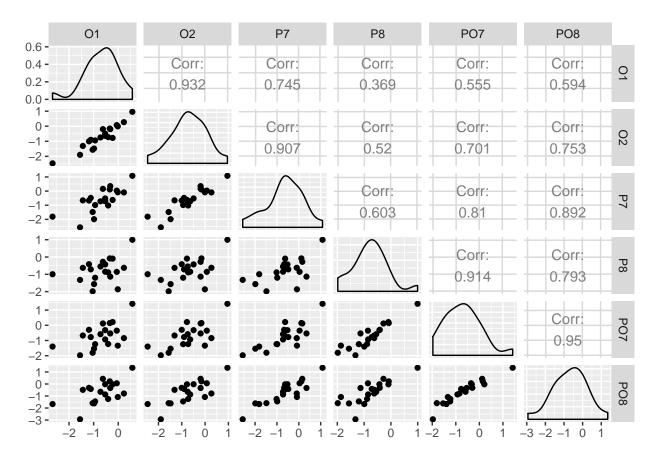


Manova test, overall among all channels:

 H_0 neutral=object in ANY of the channels. https://en.wikipedia.org/wiki/Multivariate_analysis_of_variance https://en.wikipedia.org/wiki/Hotelling%27s_T-squared_distribution

Assumptions: multivariate normality

```
subj=dati$Subj[(1:20)*30]
ggpairs(data.frame(Yfn))
```

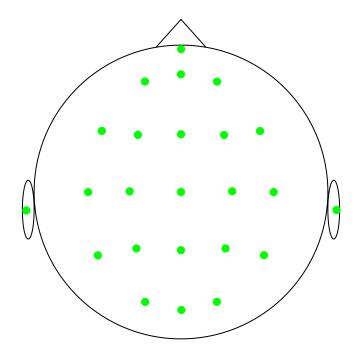


Not so bad, actually.

5 Mapping results on a scalp

```
# install.packages("eegkit")
library(eegkit)

# plot 2d cap without labels
eegcap("10-20", plotlabels = FALSE)
```

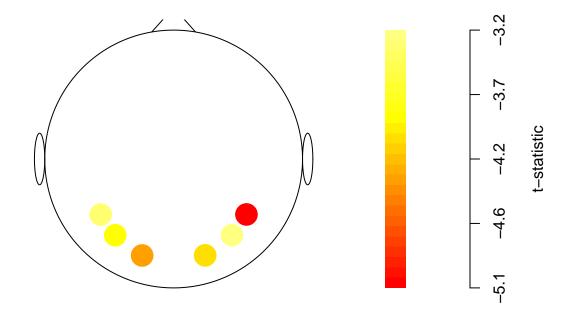


```
# get the t-statistic for each channel:
t_chan=sapply(uni_t,function(chan)chan$statistic)
names(t_chan)=gsub("\\.t","",names(t_chan))

# match to eeg coordinates
data(eegcoord)
cidx <- match(names(t_chan),rownames(eegcoord))

# # plot t-stat in 3d
# open3d()
# eegspace(eegcoord[cidx,1:3],t_chan)

# plot t-stat in 2d
eegspace(eegcoord[cidx,4:5],t_chan,cex.point = 3,colorlab="t-statistic",mycolors=heat.colors(4))</pre>
```



If you like to play with library ggplot2 this may help: http://www.mattcraddock.com/blog/2017/02/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-topographical-scalp-maps-part-1/2012/25/erp-visualization-creating-creating-creating-creating-creating-creat

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and Course materal of

ST 732, Applied Longitudinal Data Analysis, NC State University by Marie Davidian https://www.stat.ncsu.edu/people/davidian/courses/st732/notes/chap5.pdf from https://www.stat.ncsu.edu/people/davidian/courses/st732/

About Mixed models:

 $http://webcom.upmf-grenoble.fr/LIP/Perso/DMuller/M2R/R_et_Mixed/documents/Bates-book.pdf and$

https://cran.r-project.org/web/packages/lme4/vignettes/lmer.pdf