Graphs

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1 Definition

A graph G = (V, E) is a pair consisting of a set V (vertices) and a set E (edges). Every element in E is a distinct pair of vertices in V.

2 Degree

The degree of a vertex v, deg(v) is defined as the numbers of edges that are incident on v.

3 Paths

A path is a sequence of vertices connected by edges.

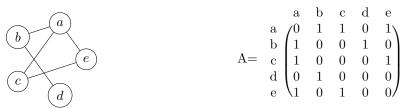
A path is a *cycle* if it starts and ends at the same vertex.

A path is *simple* if every vertex in the path is distinct.

A graph is *connected* if there is at least a path between any pair of vertices.

4 Adjacency Matrices

A finite graph can be represented by a square matrix $n \times n$ where n is the number of vertices.



Every row and column represents a vertice. 1 means that the two vertices are adjacent, 0 otherwise. The diagonal of this matrix will always e 0s since no vertice is adjacent to itself and $A = A^t$