

# Category Theory

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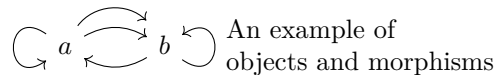
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# 1 Category

A category consists of *objects* and *morphism* or *arrows*.

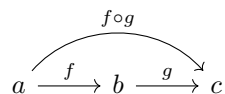
An arrow has a beginning and an ending, and it goes from one object to another.

Objects serve the purpose of marking the beginning and ending of a morphism.



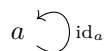
## 1.1 Composition

Composition is a property that says that if there is an arrow from  $a$  to  $b$ , and an arrow from  $b$  to  $c$ , there must exist an arrow from  $a$  to  $c$ .

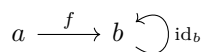


## 1.2 Identity

For every object there is an identity arrow.



The composition of an arrow with an identity is the arrow itself



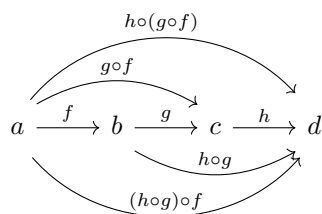
$$f \circ \text{id}_b = f$$

and also vice versa

$$\text{id}_b \circ f = f$$

## 1.3 Associativity

Compositions have the associative property



$$h \circ (g \circ f) = (h \circ g) \circ f$$