# Fundamentals of Quantum Physics

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### 1 The Probabilistic Nature of Qubits

A qubit is comprable to a bit in the "classical" world, but it exists on a sub-atomic level.

When a qubit is measured, its state will either be a "1" or a "0".

The crucial aspect is that before the measurement, a qubit is in a *superposition* of both states.

For example, a given qubit  $|\Psi\rangle$  can be represented as

$$|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

which means a linear combination of the two states  $|0\rangle$  and  $|1\rangle$ .

The coefficients  $\alpha$  and  $\beta$  represent the probability of the qubit collapsing into one of the two states when measured. The probability of the qubit collapsing into  $|0\rangle$  is  $|\alpha|^2$ , while the probability of collapsing into  $|1\rangle$  is  $|\beta|^2$ .

Since there is 100% chance of the qubits collapsing into one of the two states,  $\alpha$  and  $\beta$  must satisfy the following requirement:

$$|\alpha|^2 + |\beta|^2 = 1$$

A uniform superposition of the two states looks like this:

$$|\Psi\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

which means that we have 50% probability of the state collapsing into a  $|0\rangle$  or  $|1\rangle$  since  $\left(\frac{1}{\sqrt{2}}\right)^2 = \frac{1}{2}$ .

When the qubit is measured, the superposition is destroyed, leaving it in a "classical" binary state.

You mght have noticed that I used the absolute value in  $|\alpha|^2$  or  $|\beta|^2$ , which doesn't usually make sense since squaring the value is already going to give us a positive result.

This is because the coefficients  $\alpha$  and  $\beta$  can also be complex numbers. The absolute value of a complex number is defined as its distance from the origin.

## 2 Types of Algorithms

#### 2.1 Deterministic

Example: the quantum circuit is run and we measure the output.

#### 2.2 Probabilistic

Example: The more we run the circuit, the higher the chance of getting the right or a more precise result.