Fundamentals of Quantum Physics

Paolo Bettelini

${\bf Contents}$

1 The Probabilistic Nature of Qubits

 $\mathbf{2}$

1 The Probabilistic Nature of Qubits

A qubit is comprable to a bit in the "classical" world, but it exists on a sub-atomic level.

When a qubit is measured, its state will either be a "1" or a "0".

The crucial aspect is that before the measurement, a qubit is in a superposition of both states.

For example, a given qubit $|\Psi\rangle$ can be represented as

$$|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

which means a linear combination of the two states $|0\rangle$ and $|1\rangle$.

The coefficients α and β represent the probability of the qubit collapsing into one of the two states when measured. The probability of the qubit collapsing into $|0\rangle$ is α^2 , while the probability of collapsing into $|1\rangle$ is β^2 .

Since there is 100% chance of the qubits collapsing into one of the two states, α and β must satisfy the following requirement:

$$\alpha^2 + \beta^2 = 1$$

A uniform superposition of the two states looks like this:

$$|\Psi\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

which means that we have 50% probability of the state collapsing into a $|0\rangle$ or $|1\rangle$ since $\left(\frac{1}{\sqrt{2}}\right)^2 = \frac{1}{2}$.

When the qubit is measured, the superposition is destroyed, leaving it in a "classical" binary state.