



Master's Thesis Nr. 510

Systems Group, Department of Computer Science, ETH Zurich in collaboration with CERN

A Very Cool Master Thesis

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DINFK

${\bf Acknowledgements}$

Abstract

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Introduction

Background

- 2.1 CERN
- 2.1.1 ATLAS Experiment
- 2.1.2 Liquid Argon Calorimeter
- 2.2 High Level Synthesis

2.2.1 Catapult CCOREs

When designing blocks, Catapult offers the possibility to set them as CCORE. This directives should be used for elementary blocks used many times throughout the design. CCOREs are synthesized and optimized as a single block once and then reused where needed. This can save synthesis run time and area on the FPGA.

Two types of CCORE are offered by Catapult: sequential or combinational. The former should be used when registers are required for sequential steps, like counters, while the latter should be used for combinational logic, such as routing. Throughout the thesis, the CCOREs played an important role, and setting them correctly was crucial for the optimization process.

Latome Hardware Design

3.1 Specifications

3.1.1 The Liquid Argon Calorimeter Data Path

The LAr Calorimeter is made of 180,000 cells which are then summed up to form 34,048 supercells. The 12-bit readings of 8 supercells are serialized into one packet and sent through one optic fiber. The 116 LATOME boards are each connected to 48 optic fibers, thus receiving data from $48 \times 8 = 384$ supercells. These boards are responsible for transforming the ADC levels into energy levels, reorganizing the data and summing some energies for LATOMEs covering specific regions of the detector and distributing the data to the Feature Extraction (FEX) system. The FEX system is responsible for processing the data and sending it to the Level 1 Trigger system.

The FEX system is made of 3 groups: the Global Feature Extractor (gFEX), the Jet Feature Extractor (jFEX) and the Electron Feature Extractor (eFEX). Within these groups, gFEX only contains one board which gets summed data from all LATOMEs, thus showing the lowest granularity but with one board covering the whole detector. Then the jFEX is made of 6 boards, each receiving data from 19 LATOMEs, and finally the eFEX, with the highest granularity, is made of 24 boards, each receiving data from 4 LATOMEs.

3.1.2 The LATOME Specifications

The part of the LATOME firmware responsible for the conversion of ADC levels into energy levels is referred to as *User Code* in the LAr group. This code is not owned by the LATOME HLS team. However, the team is responsible for the different data organization steps, also called mapping or remapping, and the summing of energies for LATOMEs in specific regions of the detector. Additionally, since the output energies are only encoded on 10 bits, it is necessary to compress the data from 12 to 10 bits via a Multi Linear Encoder (MLE).

Initially, the whole LATOME firmware was written in VHDL. The implementation of all the functionalities took over 8 years and still had timing violations.

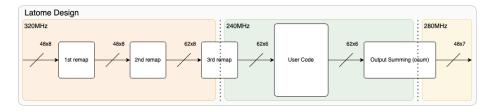


Figure 3.1: Original VHDL Design

Because in the next runs of the LHC, the amount of energy and collision is expected to increase, the LATOME design should be optimized to leave space for other functionalities, and sustain the increase in data.

3.2 Current LATOME Firmware

The original design is characterized by more clock domain crossings than the current one.

Because bunch crossings (BC) happen at a frequency of 40MHz, it is necessary to run the different blocks of the design at multiples of this frequency. The figure 4.2 shows three different frequencies being used. At the first remap stage, since the frames are made of 8 words, it is necessary to run the blocks at 320MHz. Then the frames become 6 words long, corresponding to a frequency of 240MHz. Finally, the FEX systems expect 7 32 bits words, thus the frequency is 280MHz.

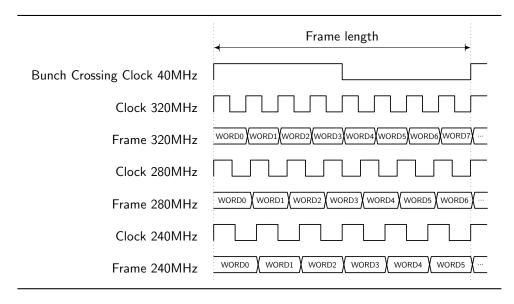


Figure 3.2: Different clocks used in the design

These clock domain crossings made the original implementation very complex...

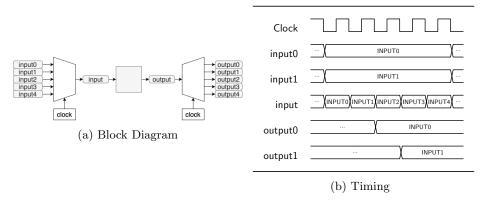


Figure 3.3: Space Division Multiplexing

3.3 Leveraging Time vs Space Division Multiplexing

When a chunk of data is available at a given time for processing, it can all be processed at the same time, or pieces after pieces. Processing simultaneously all the data offers the advantage of a reduced latency, but requires creating copies of the processing blocks for each piece. A sequential processing gives the possibility of having just one processing block treating the data step by step at a price of latency.

3.3.1 Time Division Multiplexing

The time division multiplexing approach consists in sharing the resources, or processing blocks, by routing each piece of data depending on time t. Choosing this implementation can be intuitive as computers usually process data using frames of 32 to 64 bits. It has the advantage of reusing design blocks hence possibly reducing area usage, but performs poorly in case of data dependencies. If the word from time t=0 of the frame needs to be available at the same time as the one of t=4, the logic becomes very complex thus canceling the positive area impact unlocked by resource sharing.

This sequential processing approach requires counters used by multiplexers to latch the input data at the right moments. This approach is represented in figure 3.3.

3.3.2 Space Division Multiplexing

Another way of treating the data is to make it all available at the same time, as parallel inputs of the processing block. This approach is more natural as it is closer to what humans experience; we see, hear, feel, taste at the same time, not one after the other. It is represented in figure 3.4. Space Division Multiplexing generally offers small latencies, as every block runs in parallel and reduces the use of sequential logic which would be required in TDM. In fact, using a parallel

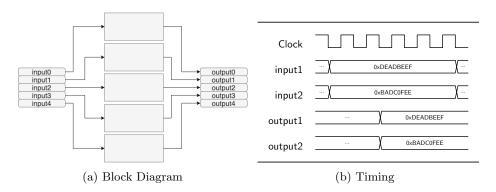


Figure 3.4: Space Division Multiplexing

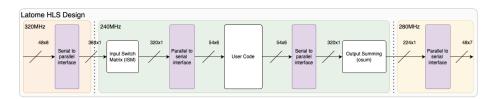


Figure 3.5: Current HLS Design

logic, some processing blocks can become purely combinational ones.

3.3.3 Tradeoffs

Whether one approach is better than the other is impossible to determine prior to having a deep understanding of the data processing blocks. The most common tradeoff is the one of latency at the price of area. But the Maximal Operating Frequency (F_{max}) can also be traded to improve other metrics.

Having access to all variables at the same time makes the code development easier.

3.4 New HLS Design

When developing the new firmware from the specifications in HLS, very interesting insights from Dr. Marcos Oliveira emphasizing benefits of space division multiplexing were taken into account. By using parallel full frames, the frequency of the design blocks is not locked anymore depending on the frame size. This allows to reduce the logic dedicated only to synchronization and time-division multiplexing which can become very complex when there are dependencies between the words of the frame.

The figure 3.5 shows that all the remapping and processing blocks except for the User Code are being processed using parallel data. This is possible thanks to the serial-to-parallel and parallel-to-serial data transformation blocks. This approach drastically simplifies the design and showed very promising results in terms of area reduction, reduced latency.

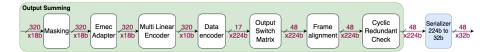


Figure 3.6: Output Summing Block Diagram

The Output Summing was completely redesigned and broken down in different blocks which are represented in figure 3.6. It is made of the following blocks:

- Masking: responsible for disabling some inputs depending on the detector region that a specific LATOME treats
- Emec Adapter: this block performs additional summing for the LATOME responsible for the EMEC region of the detector
- Multi Linear Encoder (MLE): Since the ADC readings are 12 bits long but the FEX systems requires 10 bits long energy levels, this block encodes the ADC readings on 10 bits
- Data Encoder: Once the encoded energy levels are ready, this block creates 17 frames of 224 bits representing the whole data
- Output Switch Matrix (OSM): This switch matrix routes the 17 224 bits frames to the different FEX systems that the LATOME is connected too
- Frame Alignment: Each couple of BC, the LATOME does not send any data but instead it sends an alignment frame built by this block
- CRC9: This final block appends to the last 9 bits of each frame a CRC9 value which it computes

Implementation

4.1 Different Spaces of Design Exploration

The optimization of the LATOME firmware can be done by leveraging different division multiplexing approaches, HLS directives or design implementations. These are three different spaces of design exploration that were explored to improve the firmware. This chapter will present the different explorations that were conducted in the context of this thesis in a first section. Next, the second section will focus on the results obtained after testing these different options.

4.2 Methodology

This section presents the methodology followed to perform the Design Space Explorations. The only design changes involving new code are those concerning the TDM exploration. The HLS directives and the unrolling inside or outside the CCORE are only changes in the HLS synthesis options.

To perform a fair comparison of both the v6 firmware and the new one, characterized by the changes introduced by TDM, a DSE was also conducted for the v6 firmware, to make sure two optimized firmware versions are compared.

4.2.1 Time Division Multiplexing

The v5 of the LATOME firmware only uses the TDM approach. The data frames are broken down in different words which are processed sequentially. On the other hand, the v6 firmware leverages almost only the SDM approach with parallel interfaces for the ISM and OSUM blocks, using describing and serializer.

As the base code for this thesis is the v6 HLS firmware, the TDM design space can be explored by moving up or down the serializer currently placed at the output of the OSUM. The figure 4.1 shows the different possible positions for the serializer.

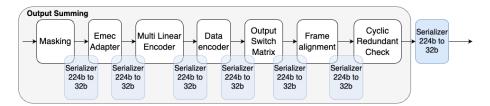


Figure 4.1: Current and potential positions of the serializer

The serializer at the output of the OSUM breaks down frames of 224 bits into 7 words of 32 bits. The main intuition behind this design exploration is that using smaller data words could reduce the size of some design blocks. Meanwhile, the latency of the design remains unchanged, as the serializer is only moving up in the design.

During this thesis, the serializer was moved up to two main different positions. The first one was before the Output Switch Matrix, and the second one was before the Data Encoder. In both cases, the OSM, Frame Alignment and CRC9 blocks were modified to handle the new data format.

An important aspect to check is the data dependencies, since these could have a critical impact when using TDM. The OSM block is a routing block which does not change any data in the frames. The Frame Alignment only overwrites the data that it gets as input if the current BC index is an alignment one, hence it does not show data dependencies. Finally the Cyclic Redundant Check can be both computed in a parallel or serial fashion equivalently and only depends on the CRC temporary result from time t=-1. Having no data dependencies, the TDM approach can be used without any issue.

The new design of these blocks required little code changes but introduced new sequential logic, like counters, to keep track of the current word being processed. Additionally, the operating frequency becomes $7 \times 40 = 280 \mathrm{MHz}$, as the serializer must process 7 words of 32 bits in 7 clock cycles and the OSUM must maintain a throughput of 7 clock cycles to never miss new data from the detector.

Output Switch Matrix

The different LATOME boards must route the data differently to the FEX systems depending on the detector region they are connected to. To tackle this problem, either each LATOME has a different version of the firmware, or some code must be added to allow an online configuration procedure defining the routing. The second possibility was chosen in the LAr group, and the solution proposed by Marcos for the v6 firmware was to add an Output Switch Matrix.

The OSM uses multiplexers to route the 17 inputs to the 48 outputs and takes its selection bits from registers configured online via an ipbus. The HLS implementation is very simple, involving a 2D array with 48 rows made of a subgroup of the 17 possible inputs.

Without looking at the different LATOME routings, it appears that, there should be 48 multiplexers of input size $224 \times 17 = 3808$ bits. However when

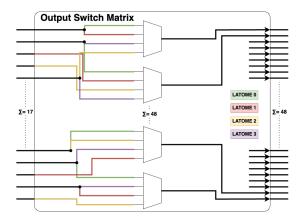


Figure 4.2: Output Switch Matrix Simplified Diagram

considering the data paths and optimizing for them, the biggest multiplexers turn out to have at most 4 input frames, meaning that each row from the HLS 2D array has only 4 entries. In other words, the Output Switch Matrix is a sparse matrix. By moving the serializer before the OSM, the biggest multiplexers have an input size of 4×32 instead of 4×224 .

Frame Encoder

The frame encoder block is responsible for creating the 17 frames of 224 bits representing the whole data. When using parallel data, the block is very simple and only needs to concatenate and order the different data words. Serializing before the Frame Encoder, makes the building of 224 bits frames unnecessary.

The Frame Encoder takes as input the 320 MLE results, the control bits and the BCID and assembles them. To create the 32 bit words, a counter is used to keep track of the current word being processed. A switch statement is used to handle the different cases.

Impact on the Following Blocks

The seven sequential cycles needed to process the serial words making up one frame are created using a simple for loop without catapult unroll directives. The frame alignment and CRC9 blocks use a counter to keep track of the current word being processed. In the case of the CRC9, since the code is appended on the 9 last bits of the frames, the block must first compute 6 32-bit word followed by one 23-bit word. The overhead of having two specialized blocks is considered to be very small as each of them only contain a limited number of XOR gates.

The frame alignment block reads the current BC index and if it matches the alignment index, it overwrites the data with the new data, otherwise it simply forwards it. The introduction of a simple counter indicating which of the 7 words is currently being processed together with a switch statement taking care of the different cases is enough to get a TDM version of this block. Additionally, this block sends a 4 bit control character indicating for each byte if it is a data

byte or a control byte. Before the serialization, the block sent the complete 28-bit control word, now it sends 4 bits at a time.

4.2.2 Leveraging HLS Directives

The second space of design exploration is the HLS directives, specifically, the CCORE related ones. Each processing block of the Output Summing is declared as a CCORE one. This makes Catapult optimize the design inside of the CCORE once to reuse it for all the instances. The two options offered by Catapult (sequential or combinational) were tested for each block.

Additionally, Catapult gives the possibility to set the design goal for the optimization to be either latency or area. Setting this goal to either one will have an important impact on the final result.

Overall, there are six different blocks with each two options for the CCORE and two options for the optimization goal. This gives a total of 128 different possible combinations. The table 4.1 shows the different possible combinations. The CRC9 block is not included as it is, by essence, a sequential block, and cannot be set as combinational.

	Option	Value		
	Masking	Sequential / Combinational		
	Emec Adapter	Sequential / Combinational		
CCORE	MLE	Sequential / Combinational		
CCORE	Data Encoder	Sequential / Combinational		
	OSM	Sequential / Combinational		
	Frame Alignment	Sequential / Combinational		
Optimization Goal		Latency / Area		

Table 4.1: Possible values for each HLS option

In the OSUM, many "for" loops are used to create the different instances of the blocks. A full unroll means that the for loop creates as many parallel instances as there are iterations. In some cases, a partial unroll can be used to create a fixed number of instances which are reused to process all the data. For example a for loop of 320 iterations can have an "unroll 4" directive to create 4 instances that will process 80 iterations each. This can lead to very high area reduction at the price of latency. The choice of full or partial unroll can be done manually, or left to Catapult to decide. For this design exploration, we have given Catapult the freedom to choose the best unroll factor, within the following constraints:

- The initiation interval (throughput) must be 7 clock cycles.
- The maximum latency is 26 clock cycles.

The first value is a direct consequence of the 280MHz operating frequency, while the second value is the latency of the v5 design, which should not be exceeded.

To create all the different combinations, a tcl script looping through each of them and launching the Catapult synthesis was used. The results were then

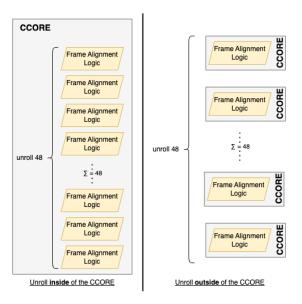


Figure 4.3: Unrolling inside vs outside the CCORE

analyzed to find the best combination of options. A follow-up Quartus compilation analysis was done to get more precise and meaningful results. Overall, the HLS synthesis run time for all the combination lasted around 9 hours, while the Quartus compilation for all the combinations lasted 3 days.

4.2.3 Unrolling Inside or Outside the CCORE

When developing the HLS code for these design blocks, two options can be considered using CCOREs in for loops, as illustrated in figure 4.3. The first one is to set the OSM, Frame Alignment or CRC9 as an elementary block processing only one frame at a time, and to create as many copies as there are frames to process. The second option is to make the design block process all the frames, and to set it as a CCORE. Using the HLS jargon, the first option refers to unrolling "outside" of the CCORE, while the second refers to unrolling "inside" of the CCORE.

For this DSE, the Frame Alignment and CRC9 blocks were considered. The study was performed by either using the creating the unrolled for loop in the CCORE or outside of it. The results were then compared to see which option was the best, both in the v6 firmware and in the new one.

4.3 Design Space Explorations Results

To get results from a specific optimization, one can compile only the block being studied, the block within its parents block, or the whole firmware. In the LATOME HLS team, four levels of compilation exist and can be considered in this thesis: the block alone, within the OSUM, with the ISM and finally the whole firmware. Improvements on one level does not necessarily translate to the next as Quartus may or may not be able to perform further optimizations. However, at each level, the results can be compared to the original design to get a sense of the impact of the optimization. Additionally, the smaller compilation times of the lower levels can be used to quickly test different options.

4.3.1 Time Division Multiplexing

Serializing Before the OSM

The expected results at the block level are an increase of the maximum operating frequency, as less signals must be synchronized, as well as an area reduction of a factor of 7.

Version	Area (ALMs)	F_{max} (MHz)
Original OSM	3621.5	310.17
Serialized OSM	476.8	524.38
Improvement	-86.8%	+69.1%

Table 4.2: Results From the OSM Optimization

The table 4.2 shows an actual area reduction of a factor of 7.6 and an increase of the maximum operating frequency of 69%. The area reduction is slightly higher than the expected factor of 7, which can be explained by the overhead that the signal synchronization logic had on the original design.

Serializing Before Frame Encoder

4.3.2 HLS Directives

Once the results were obtained, they were extracted in an Excel file to be analyzed. A python script created the different figures presented in this section.

The first figure, figure 4.4, shows the overall results for all the combinations, each represented by a point. The color of the points indicate the latency for this solution. Finally, the blue horizontal line shows the operating frequency of the OSUM block, 280MHz. This figure shows that the solutions with the highest latencies are the ones with the worst F_{max} . This is explained by the fact that when Catapult implements resource sharing, with partial unrolling, the latency increases, but the resource sharing logic has a negative impact on the F_{max} .

In figure 4.5, the points are "+" when the goal for the solution is latency and "o" when it is area. Each line connects two solutions with all the same options except for the optimization goal. The line colorization depends on the latency. For instance, the points on the left of the figure all have lines going from bottom left to top right, with a color gradient from red to yellow. Additionally, the points at the bottom left are all area optimized solutions, while the ones at the top right are latency optimized solutions. This indicates that using the latency optimization goal will lead to a higher F_{max} , lower latency at a small area cost, since the lines have a very big slope. Two clusters can be clearly distinguished, the one on the left showing a clear tendency and the one on the right showing a more scattered distribution.

Figures 4.6, 4.7, 4.9, show no clear tendency when varying the CCORE type for the Masking, EMEC Adapter and Data Encoder blocks. These blocks are more secondary ones for the optimizations and are very dependent on the more important ones. Hence they should be used for adjustments once the main blocks are optimized.

The figures 4.8, 4.10, 4.11 show the results when varying the CCORE type for the MLE, OSM and Frame Select blocks. The MLE block shows a clear tendency: all the points on the right are combinational ones, while the ones on the left are sequential, the lines have a very small slope, and points are far from each other. This means that setting the MLE CCORE as sequential instead of combinational has a small impact on the F_{max} , but reduces the area drastically. The OSM has almost no impact on the area, since the lines are vertical, but has one on the F_{max} , which is very dependant on the other blocks' settings. Finally, most of the lines for the Frame Select block are going from the bottom right where the combinational points are to the sequential ones on the top left, indicating that the sequential setting has a positive impact both on the F_{max} and the area.

Another interesting aspect rising from this DSE is the discrepancy between the results given by Catapult and the ones from Quartus. In the table below, the results are ordered by the area given by Catapult. The columns "Goal" to "crc9" contain the different CCORE options. "mask." refers to the Masking block and is also called "ena mux", "emec" refers to the EMEC Adapter, "mle" to the Multi Linear Encoder, "frame" to the Frame Encoder, "osm" to the Output Switch Matrix "align." to the Frame Alignment and "crc9" to the Cyclic Redundant Check. Additionally, "lat." refers to the latency. These abbreviations are used to fit the table in the page.

The colorization of the area values ranges from green when it is the lowest to red when it is the highest. The Quartus area values gradient follows the one from Catapult in average but for some groups of solutions Catapult seems to be too optimistic and for others too pessimistic. In the Catapult result, one can also see the slack column which indicates, in nanosecond, the time left for the design to meet the timing constraints. In most cases, Catapult is too optimistic, as the slack is positive but the F_{max} is under 280 MHz.

								С	atapult		Qua	rtus
Goal	mask.	emec	mle	frame	osm	align.	crc9	Area	Slack	Lat.	Area	Fmax
area	comb	seq	seq	comb	comb	seq	seq	27218	0,08	26	18405,1	253,68
area	comb	seq	seq	comb	seq	seq	seq	27219	0,08	26	18314,6	255,36
area	comb	comb	seq	comb	comb	seq	seq	28792	0,22	26	18223,6	272,63
area	comb	comb	seq	comb	seq	seq	seq	28793	0,22	26	17988,1	255,75
area	seq	seq	seq	comb	seq	seq	seq	29913	0,38	21	18421,3	265,89
area	seq	seq	seq	comb	comb	seq	seq	29914	0,38	21	18495,9	269,18
area	comb	seq	seq	seq	seq	seq	seq	30075	0,22	21	18752,1	268,82
area	comb	seq	seq	seq	comb	seq	seq	30076	0,22	21	18835,5	260,69
area	comb	comb	seq	seq	seq	seq	seq	30393	0,22	21	18385,4	253,61
area	comb	comb	seq	seq	comb	seq	seq	30394	0,22	21	18335,1	260,69
area	seq	comb	seq	comb	seq	seq	seq	30614	0,48	21	18189,2	265,04
area	seq	comb	seq	comb	comb	seq	seq	30614	0,48	21	18324,8	263,23
area	seq	seq	seq	seq	seq	seq	seq	31047	0,38	22	19378,5	257
area	seq	seq	seq	seq	comb	seq	seq	31048	0,38	22	19539	277,32
area	seq	comb	seq	seq	seq	seq	seq	31748	0,48	22	19147,2	261,78
area	seq	comb	seq	seq	comb	seq	seq	31749	0,48	22	19202,9	262,95
lat.	comb	seq	seq	comb	seq	seq	seq	38403	0,5	16	20173,8	288,43
lat.	comb	seq	seq	comb	comb	seq	seq	38403	0,5	16	20303,2	294,55
lat.	seq	seq	seq	comb	seq	seq	seq	38639	0,64	17	20225,9	292,4
lat.	seq	seq	seq	comb	comb	seq	seq	38639	0,64	17	20374	295,25
lat.	seq	seq	seq	seq	seq	seq	seq	38975	0,5	18	20857,7	291,8
lat.	seq	seq	seq	seq	comb	seq	seq	38975	0,5	18	20978	293,94
lat.	seq	comb	seq	comb	seq	seq	seq	39018	0,65	17	20374,6	300,93
lat.	seq	comb	seq	comb	comb	seq	seq	39018	0,65	17	20449,1	294,29
lat.	comb	comb	seq	comb	seq	seq	seq	39055	0,5	16	20153,5	286,86
lat.	comb	comb	seq	comb	comb	seq	seq	39055	0,5	16	20276,4	282,41
lat.	comb	seq	seq	seq	seq	seq	seq	39141	0,64	17	21060,5	284,66
lat.	comb	seq	seq	seq	comb	seq	seq	39141	0,64	17	21200,5	290,87
lat.	seq	comb	seq	seq	seq	seq	seq	39361	0,5	18	20992,7	283,61
lat.	seq	comb	seq	seq	comb	seq	seq	39361	0,5	18	21057,5	293,17
lat.	comb	comb	seq	seq	seq	seq	seq	39793	0,5	17	20894,2	293,6
lat.	comb	comb	seq	seq	comb	seq	seq	39793	0,5	17	20994	295,95
area	comb	seq	seq	comb	comb	comb	seq	48301	0,08	25	20414,3	253,61
area	comb	seq	seq	comb	seq	comb	seq	48305	0,08	26	20455	256,67
area	comb	seq	seq	seq	comb	comb	seq	49151	0,08	26	21161,7	251,95
lat.	comb	comb	comb	seq	comb	seq	seq	49247	0,12	14	26515,1	280,35
lat.	comb	comb	comb	seq	seq	seq	seq	49248	0,12	14	26374,7	267,09
lat.	seq	comb	comb	seq	seq	seq	seq	49282	0,12	15	24850	274,57
lat.	seq	comb	comb	seq	comb	seq	seq	49282	0,12	15	24924,4	285,47
area	seq	seq	seq	comb	comb	comb	seq	49553	0,18	26	21241,8	259,88
area	comb	comb	seq	comb	comb	comb	seq	49877	0,18	25	20109,3	259,2
area	comb	comb	seq	comb	seq	comb	seq	49906	0,18	26	20100,8	254,84

Table 4.3: Compilation of the Design Space Exploration results

area	seq	comb	seq	comb	comb	comb	seq	50054	0,18	26	21108,1	244,68
area	comb	comb	seq	seq	comb	comb	seq	50750	0,18	26	20878,4	249,75
area	seq	seq	seq	comb	seq	comb	seq	50997	0,18	21	20875	261,64
area	comb	seq	seq	seq	seq	comb	seq	51158	0,18	21	21072,9	260,69
area	comb	comb	seq	seq	seq	comb	seq	51480	0,18	21	20786,4	263,78
area	seq	comb	seq	comb	seq	comb	seq	51699	0,18	21	20509,9	254,71
area	seq	seq	seq	seq	comb	comb	seq	52105	0,18	21	21739,3	259,74
area	seq	seq	seq	seq	seq	comb	seq	52131	0,18	22	21432,1	263,78
area	seq	comb	seq	seq	comb	comb	seq	52807	0,18	21	21493	261,44
area	seq	comb	seq	seq	seq	comb	seq	52832	0,18	22	21302,6	261,3
area	comb	seq	comb	comb	seq	seq	seq	53101	0,08	25	29865,5	273,07
area	comb	seq	comb	comb	comb	seq	seq	53101	0,08	25	30070,6	268,89
area	seq	seq	comb	comb	seq	seq	seq	53331	0,38	26	30721	269,61
area	seq	seq	comb	comb	comb	seq	seq	53333	0,38	26	31060,1	259,47
area	comb	seq	comb	seq	seq	seq	seq	53547	-0,42	25	28933	258,26
area	comb	seq	comb	seq	comb	seq	seq	53547	-0,42	25	29252,6	266,45
area	comb	comb	comb	comb	seq	seq	seq	53761	0,22	24	29991,7	252,33
area	comb	comb	comb	comb	comb	seq	seq	53761	0,22	24	30469,2	262,88
area	seq	comb	comb	comb	seq	seq	seq	53918	0,38	25	30480,6	262,47
area	seq	comb	comb	comb	comb	seq	seq	53918	0,38	25	31023,5	266,1
area	seq	seq	comb	seq	comb	seq	seq	53948	-0,42	26	30255,5	248,39
	seq	seq	comb	seq	seq	seq	seq	53974	-0,42	26	30034	243,19
	comb	comb	comb	seq	seq	seq	seq	54005	-0,42	24	29244,6	244,44
area	comb	comb	comb	seq	comb	seq	seq	54005	-0,42	24	29440,9	262,81
	seq	comb	comb	seq	seq	seq	seq	54183	-0,42	25	30728,2	261,3
	seq	comb	comb	seq	comb	seq	seq	54183	-0,52	25	30827,4	262,81
lat.	comb	comb	comb	comb	comb	seq	seq	55038	0,38	14	27948,7	286,86
lat.	comb	comb	comb	comb	seq	seq	seq	55039	0,38	14	27729,6	288,1
	seq	comb	comb	comb	seq	seq	seq	55073	0,38	15	27081	292,06
	seq	comb		comb	comb	seq	seq	55073	0,38	15	27239,3	297,18
	comb	seq	comb	comb	seq	seq	seq	55180	0,38	15	30072,8	283,93
lat.	comb	seq	comb	comb	comb	seq	seq	55180	0,38	15	30343,7	285,71
lat.	comb	seq	comb	seq	seq	seq	seq	55684	-0,02	15	29833,3	294,72
lat.	comb	seq	comb	seq	comb	seq	seq	55684	-0,02	15	29947,5	280,35
lat.	seq	seq	comb	comb	seq	seq	seq	55876	0,38	16	28477,7	293,6
lat.	seq	seq	comb		comb	sea	seq	55876	0,38	16		290,87
lat.	seq	seq		seq	seq	seq	seq	56379	-0,02	16	28465,5	279,1
lat.	seq	seq	comb	seq	comb	seq	seq	56379	-0,02	16	28608,3	288,27
lat.	comb	seq	seq	comb	seq	comb	seq	59488	0,18	16	22539,1	271,81
	seq	seq	seq	comb	comb	comb	seq	59490	0,18	16	22395,4	293,6
lat.	comb	seq	seq	comb	comb	comb	seq	59499	0,18	15	22218,4	272,78
	seq	seq	seq	comb	seq	comb	seq	59648	0,18	17	22374,9	277,47
lat.	seq	comb	seq	comb	comb	comb	seq	59884	0,18	16	22428,4	273
			•				seq	59923	0,18	18	22904,1	286,62
ıaı.	seq	seq	seq	seq	seq	COIID	seq	33323	0,10	10	22504,1	200,02

Table 4.4: Compilation of the Design Space Exploration results

lat. seq comb seq comb seq 60028 0,18 17 23329,4 288,8 lat. seq seq seq comb comb seq 60063 0,18 17 23041,2 273,6 lat. comb comb seq seq comb seq 60141 0,18 17 23291,9 291,3 lat. comb seq seq seq comb seq 60152 0,18 15 22179,2 289,3 lat. seq comb seq comb comb seq 60152 0,18 15 22179,2 289,2 lat. comb seq seq comb comb seq 60650 0,18 17 23138,4 287,7 lat. comb comb seq comb comb seq comb seq comb seq seq comb seq ded,92 274,23 <td< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th><th></th></td<>													
lat. seq seq seq comb comb seq 60063 0,18 17 23041,2 273,6 lat. comb comb seq comb seq comb seq 60141 0,18 16 22354,7 276,7 lat. comb seq seq comb comb seq 60149 0,18 17 23291,9 291,31 lat. comb comb seq comb comb seq 60149 0,18 15 22179,2 289,2 lat. comb comb seq comb comb 60650 0,18 16 23118,4 287,7 lat. comb comb seq comb comb seq comb seq comb seq 274,4 lat. comb comb seq comb comb seq 17333 0,12 14 26694,2 257,5 14 lat. <td< td=""><td>lat.</td><td>comb</td><td>seq</td><td>seq</td><td>seq</td><td>comb</td><td>comb</td><td>seq</td><td>59997</td><td>0,18</td><td>16</td><td>23382,1</td><td>279,1</td></td<>	lat.	comb	seq	seq	seq	comb	comb	seq	59997	0,18	16	23382,1	279,1
lat. comb comb seq comb seq 60141 0,18 16 22354,7 276,74 lat. comb seq seq seq comb comb seq 60149 0,18 17 23291,9 291,31 lat. comb comb seq comb comb seq 60152 0,18 18 23738,3 288,2* lat. seq comb seq comb comb seq 60444 0,18 17 23996,5 284,0* lat. comb comb seq comb comb seq 60650 0,18 16 23115,7 274,2 lat. comb comb seq comb comb seq 60650 0,18 16 23115,7 274,2 lat. comb comb seq comb comb seq 60802 0,18 17 23138,4 287,7* 278,7* lat.	lat.	seq	comb	seq	comb	seq	comb	seq	60028	0,18	17	23329,4	288,85
lat. comb seq seq seq comb comb seq comb seq comb seq comb seq comb seq comb seq comb comb seq comb seq comb comb seq comb seq comb comb seq seq comb seq seq comb seq seq seq comb seq seq comb seq <t< td=""><td>lat.</td><td>seq</td><td>seq</td><td>seq</td><td>seq</td><td>comb</td><td>comb</td><td>seq</td><td>60063</td><td>0,18</td><td>17</td><td>23041,2</td><td>273,67</td></t<>	lat.	seq	seq	seq	seq	comb	comb	seq	60063	0,18	17	23041,2	273,67
lat. comb comb seq comb comb comb seq 60152 0,18 15 22179,2 289,1 lat. seq comb seq seq comb seq comb seq comb seq comb seq comb seq comb seq seq comb seq seq <td>lat.</td> <td>comb</td> <td>comb</td> <td>seq</td> <td>comb</td> <td>seq</td> <td>comb</td> <td>seq</td> <td>60141</td> <td>0,18</td> <td>16</td> <td>22354,7</td> <td>276,78</td>	lat.	comb	comb	seq	comb	seq	comb	seq	60141	0,18	16	22354,7	276,78
lat. seq comb seq seq comb seq comb seq 288,2 lat. seq comb seq comb comb seq comb seq 284,0 lat. comb comb seq comb comb seq 60600 0,18 16 23115,7 274,4 lat. comb comb comb comb comb seq comb seq 60802 0,18 17 23138,4 287,7 lat. comb comb comb comb comb seq comb 66802 0,18 17 23138,4 287,7 lat. comb comb comb seq comb seq comb seq 2694,2 257,5 lat. seq comb comb seq comb seq 2608,2 264,3 261,3 lat. seq comb comb seq comb se	lat.	comb	seq	seq	seq	seq	comb	seq	60149	0,18	17	23291,9	291,38
tat. seq comb seq seq comb comb seq 60444 0,18 17 23696,5 284,09 tat. comb comb seq seq comb comb seq 60650 0,18 16 23115,7 274,18 tat. comb comb seq seq seq comb seq 60802 0,18 17 23138,4 287,77 tat. comb comb comb seq seq comb seq 60802 0,18 17 23138,4 287,77 tat. comb comb comb seq seq comb seq 60802 0,18 17 23138,4 287,77 tat. comb comb comb seq seq comb seq 70333 0,12 14 27482,8 2864,99 tat. seq comb comb seq comb seq 70334 0,12 14 27482,8 2864,99 tat. seq comb comb seq comb seq comb seq 70334 0,12 14 2683,8 260,8 tat. seq comb comb seq comb seq comb seq 70334 0,12 15 26479,7 278,77 area comb seq comb comb seq comb seq 70336 0,12 15 26479,7 278,77 area comb seq comb comb seq comb seq 70366 0,12 15 26479,7 278,77 area seq seq comb comb seq comb seq 74046 0,08 25 31674 261,5 area seq seq comb comb comb seq comb seq 74412 0,18 26 32932,7 259,67 area seq seq comb comb comb comb seq 74412 0,18 26 32932,7 259,67 area comb seq comb seq comb seq comb seq 74430 0,18 25 32895,5 253,67 area comb seq comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,4 area seq comb comb comb comb seq comb seq 74638 0,18 23 32382 263,00 area comb comb comb comb seq comb seq 74638 0,18 23 32382 263,00 area comb comb comb comb seq comb seq 74670 0,18 25 32401 252,77 area comb comb comb comb seq comb seq 74879 -0,42 24 32398,4 253,17 area comb comb comb seq comb seq 74879 -0,42 24 32398,4 253,17 area seq comb comb comb comb seq seq comb seq 75013 -0,42 24 32398,4 253,17 area seq seq comb comb seq seq comb seq 75013 -0,42 24 32398,4 253,17 area seq seq comb comb seq seq comb seq 75014 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb comb comb seq 75043 -0,42 25 32153,6 259,4 area seq co	lat.	comb	comb	seq	comb	comb	comb	seq	60152	0,18	15	22179,2	289,1
tat. comb comb seq seq comb comb seq 60650 0,18 16 23115,7 274,8 tat. comb comb seq seq seq comb seq 60802 0,18 17 23138,4 287,7 tat. comb comb comb seq seq comb seq 67516 0,12 13 26694,2 257,5; tat. comb comb comb seq seq comb seq 70333 0,12 14 27482,8 264,9; tat. seq comb comb seq seq comb seq 70334 0,12 14 26583,8 260,8; tat. seq comb comb seq comb comb seq 70334 0,12 14 26583,8 260,8; tat. seq comb seq comb seq comb seq 70336 0,12 15 26479,7 278,7; area comb seq comb comb seq comb seq 74046 0,08 25 31674 261,5; area comb seq comb comb seq comb seq 74412 0,18 26 32932,7 259,6; area seq seq comb comb seq comb seq 74430 0,18 25 32895,5 253,6; area comb seq comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,4 area comb seq comb comb comb seq 74626 -0,42 24 3151,7 242,9; area comb comb comb comb seq comb seq 74674 0,18 25 32895,5 253,6; area comb comb comb comb seq comb seq 74674 0,22 24 3151,7 242,9; area comb comb comb comb seq comb seq 74674 0,22 24 3151,7 242,9; area comb comb comb comb seq comb seq 74674 0,22 24 3151,7 242,9; area comb comb comb comb seq comb seq 74674 0,22 24 32394, 253,1; area seq comb comb comb seq comb seq 74879 0,42 23 3070,6 258,8; area seq comb comb comb comb seq comb seq 74879 0,42 25 3213,6 259,4 area seq comb comb comb seq comb seq 75000 0,18 24 30607,5 254,9; area seq seq comb seq seq comb seq 75000 0,18 24 30607,5 254,9; area seq seq comb seq seq comb seq 75043 0,42 25 32294,9 255,7; tat. seq comb comb comb comb seq comb seq 75043 0,42 25 32294,9 255,7; tat. seq comb comb comb seq comb seq 76125 0,18 14 30618,1 275,4; tat. seq comb comb comb seq comb seq 76125 0,18 14 30618,1 275,4; tat. seq comb comb comb seq comb seq 76630 0,18 15 30586,5 285,2; tat. comb seq comb comb seq comb seq 76670 0,02 15 31298,8 272,9; tat. comb seq comb comb comb seq comb seq 76696 0,18 15 31963,9 272,2; tat. comb seq comb comb comb seq comb seq 76965 0,18 15 31963,9 272,2; tat. comb comb comb comb comb seq comb seq 76965 0,18 15 31963,9 272,2; tat. comb comb comb comb	lat.	seq	comb	seq	seq	seq	comb	seq	60312	0,18	18	23738,3	288,27
lat. comb comb seq seq comb seq 60802 0,18 17 23138,4 287,7 lat. comb comb comb seq comb comb seq 7516 0,12 13 26694,2 257,5; lat. seq comb comb seq comb seq 70333 0,12 14 27482,8 264,9; lat. seq comb comb seq comb seq comb seq 70334 0,12 14 26683,8 260,8; lat. seq comb seq comb seq comb seq 70466 0,08 24 32092,6 280,8; area comb seq comb comb seq comb seq 3293,7 259,6 area seq comb comb comb comb seq 44412 0,18 25 31210,3 268,8	lat.	seq	comb	seq	seq	comb	comb	seq	60444	0,18	17	23696,5	284,09
tat. comb comb comb seq comb comb seq 67516	lat.	comb	comb	seq	seq	comb	comb	seq	60650	0,18	16	23115,7	274,2
lat. comb comb seq seq comb seq 70333 0,12 14 27482,8 264,9 lat. seq comb comb seq comb seq 70334 0,12 14 26583,8 260,83 lat. seq comb seq comb seq comb seq 70366 0,12 15 26479,7 278,73 area comb seq comb comb seq comb seq 74046 0,08 25 31674 261,53 area seq comb comb comb seq comb seq 74233 0,08 24 32092,6 280,83 area seq comb comb comb comb comb comb seq comb seq 32323,7 259,6 area comb seq comb comb seq comb seq 74494 -0,42 23	lat.	comb	comb	seq	seq	seq	comb	seq	60802	0,18	17	23138,4	287,77
lat. seq comb comb seq sed	lat.	comb	comb	comb	seq	comb	comb	seq	67516	0,12	13	26694,2	257,53
tat. seq comb comb seq seq comb seq 70366 0,12 15 26479,7 278,7 area comb seq comb comb seq comb seq comb seq 74046 0,08 25 31674 261,55 area comb seq comb comb comb seq 74046 0,08 25 31674 261,55 area seq seq comb comb comb seq 74412 0,18 26 32932,7 259,65 area seq seq comb comb comb seq 74412 0,18 26 32932,7 259,65 area seq seq comb seq comb seq 74412 0,18 26 32932,7 259,65 area seq seq comb seq comb seq 74410 0,18 25 32895,5 253,65 area comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,4 area comb comb comb comb comb seq 74626 -0,42 24 31517,7 242,95 area comb comb comb comb seq comb seq 74671 0,22 24 32398,4 253,14 area seq comb comb comb seq comb seq 74876 0,18 25 32401 252,75 area comb comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,85 area seq comb comb comb comb comb seq 74879 -0,42 23 30700,6 258,85 area seq comb comb comb comb seq comb seq 75000 0,18 24 33269,9 260,44 area comb comb comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75004 -0,42 25 321315 254,43 area seq comb comb seq seq comb seq 75043 -0,42 25 321315 254,43 area seq comb comb seq seq comb seq 75026 -0,42 26 32317 254,43 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq comb comb comb seq comb seq 75026 -0,42 25 32193,9 258,3 area seq	lat.	comb	comb	comb	seq	seq	comb	seq	70333	0,12	14	27482,8	264,97
area comb seq comb comb seq comb seq 74046 0,08 25 31674 261,55 area comb seq comb comb comb seq 74233 0,08 24 32092,6 280,83 area seq seq comb comb seq comb seq 74412 0,18 26 32932,7 259,65 area seq seq comb seq comb seq 74412 0,18 26 32932,7 259,65 area seq seq comb seq comb seq 74410 0,18 25 32895,5 253,65 area comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,6 area comb seq comb seq comb seq comb seq 74626 -0,42 24 31517,7 242,95 area comb comb comb comb seq comb seq 74671 0,22 24 32398,4 253,14 area seq comb comb comb seq comb seq 74876 0,18 25 32401 252,74 area comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,85 area seq comb comb comb seq comb seq 75000 0,18 24 33269,9 260,44 area comb comb comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75002 0,42 25 321317 254,43 area seq seq comb seq seq comb seq 75026 -0,42 26 32317 254,43 area seq seq comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb comb seq comb seq 75026 -0,42 25 321293,9 259,44 area seq comb	lat.	seq	comb	comb	seq	comb	comb	seq	70334	0,12	14	26583,8	260,82
area comb seq comb comb comb comb seq 74233 0,08 24 32092,6 280,81 area seq seq comb comb seq comb seq 74412 0,18 26 32932,7 259,61 area seq seq comb comb comb comb seq 74430 0,18 25 32895,5 253,61 area comb seq 74494 -0,42 25 31210,3 268,64 area comb comb comb comb comb comb seq 74626 -0,42 24 31517,7 242,99 area comb comb comb comb seq comb seq 74638 0,18 23 32382 263,01 area comb comb comb comb seq comb seq 74876 0,18 25 32401 252,74 area seq comb comb comb seq comb seq 74876 0,18 25 32401 252,74 area seq comb comb comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,81 area seq comb comb comb comb comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area seq seq comb seq seq comb seq 75013 -0,42 24 30607,5 254,91 area seq seq comb seq seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb comb seq comb seq 76125 0,18 14 30618,1 275,43 area seq comb comb comb comb seq comb seq 76125 0,18 14 30618,1 275,43 area seq comb comb comb comb seq comb seq 76263 0,18 15 30586,5 285,23 area seq comb comb comb seq comb seq 76263 0,18 15 31298,8 272,93 area seq comb seq comb seq comb seq 76676 -0,02 15 31298,8 272,93 area seq comb comb comb comb seq comb seq 76665 0,18 15 31963,9 272,24 area seq comb comb comb comb seq comb seq 76965 0,18 15 31963,9 272,24 area seq comb comb comb comb comb seq 76965 0,18 15 31963,9 272,24 area seq comb comb comb comb comb seq 77307 0,18 13 29073 262,66 area seq comb comb seq comb seq 77307 0,18 13 29073 262,66 area seq comb seq comb seq comb seq 77307 0,18 13 29073 262,66 area comb seq comb seq comb seq comb seq 77307 0,18 13 29073 262,66 area	lat.	seq	comb	comb	seq	seq	comb	seq	70366	0,12	15	26479,7	278,71
area seq comb comb seq comb seq 74412 0,18 26 32932,7 259,6° area seq seq comb comb comb seq 74430 0,18 25 32895,5 253,6° area comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,6° area comb seq comb comb comb seq 74626 -0,42 24 31517,7 242,9° area comb comb comb comb comb comb comb seq 74638 0,18 23 32382 263,0° area comb comb comb comb comb seq comb seq 74771 0,22 24 32398,4 253,1° area seq comb comb comb comb comb comb comb seq 74879 <td>area</td> <td>comb</td> <td>seq</td> <td>comb</td> <td>comb</td> <td>seq</td> <td>comb</td> <td>seq</td> <td>74046</td> <td>0,08</td> <td>25</td> <td>31674</td> <td>261,51</td>	area	comb	seq	comb	comb	seq	comb	seq	74046	0,08	25	31674	261,51
area seq comb comb comb seq 74430 0,18 25 32895,5 253,6 area comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,6 area comb seq comb comb comb seq comb seq 74626 -0,42 24 31517,7 242,93 area comb comb comb comb comb seq	area	comb	seq	comb	comb	comb	comb	seq	74233	0,08	24	32092,6	280,82
area comb seq comb seq comb seq comb seq 74494 -0,42 25 31210,3 268,6 area comb seq comb seq comb comb seq 74626 -0,42 24 31517,7 242,99 area comb comb comb comb seq comb seq 74638 0,18 23 32382 263,00 area comb comb comb comb seq comb seq 74771 0,22 24 32398,4 253,10 area seq comb comb comb seq comb seq 74876 0,18 25 32401 252,70 area comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,80 area seq comb comb comb comb seq comb seq 75000 0,18 24 33269,9 260,40 area comb comb comb seq seq comb seq 75000 0,18 24 33269,9 260,40 area seq seq comb seq seq comb seq 75013 -0,42 24 30607,5 254,90 area seq seq comb seq comb seq 75043 -0,42 25 32153,6 259,40 area seq seq comb seq comb seq romb s	area	seq	seq	comb	comb	seq	comb	seq	74412	0,18	26	32932,7	259,67
area comb seq comb seq comb seq 74626 -0,42 24 31517,7 242,93 area comb comb comb comb seq 74638 0,18 23 32382 263,03 area comb comb comb seq comb seq 74771 0,22 24 32398,4 253,10 area seq comb comb seq comb seq 74876 0,18 25 32401 252,73 area seq comb comb seq comb seq 74879 -0,42 23 30700,6 258,83 area seq comb comb comb comb seq 75000 0,18 24 33269,9 260,44 area comb comb seq seq comb seq 75000 0,18 24 33269,9 260,44 area comb comb seq seq comb seq 75013 -0,42 24 30607,5 254,93 area seq seq comb seq seq comb seq 75026 -0,42 26 32317 254,44 area seq seq comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq seq comb seq 75141 -0,42 25 32294,9 258,2 area seq comb comb comb seq comb seq 75262 -0,42 24 32597,2 255,73 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,24 lat. seq comb comb comb seq comb seq 76125 0,18 14 30618,1 275,44 lat. seq comb comb comb seq comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76677 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76965 0,18 15 31963,9 272,261 lat. seq seq comb comb comb seq romb seq 76965 0,18 15 31963,9 272,261 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,261 lat. comb comb comb comb comb seq 76965 0,18 15 31963,9 272,261 lat. comb comb comb comb comb seq 76965 0,18 15 31963,9 272,261 lat. comb comb comb comb comb seq 77466 -0,02 16 30713,4 269,81	area	seq	seq	comb	comb	comb	comb	seq	74430	0,18	25	32895,5	253,61
area comb comb comb comb comb seq 74638 0,18 23 32382 263,00 area comb comb comb seq comb seq 74771 0,22 24 32398,4 253,14 area seq comb comb seq comb seq 74876 0,18 25 32401 252,78 area comb comb comb seq comb seq 74876 0,18 25 32401 252,78 area seq comb comb comb comb seq 74879 -0,42 23 30700,6 258,83 area seq comb comb comb comb seq 75000 0,18 24 33269,9 260,48 area comb comb comb seq seq comb seq 75013 -0,42 24 30607,5 254,93 area seq seq comb seq seq comb seq 75026 -0,42 26 32317 254,48 area seq seq comb seq comb comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq romb seq 76125 0,18 14 30618,1 275,43 lat. comb seq comb comb comb seq comb seq 76232 0,18 14 30247,9 278,33 lat. comb seq comb comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq romb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq seq comb seq 76663 0,18 15 32068,8 273,53 lat. seq seq comb comb seq comb seq 76663 0,18 16 31573,3 282,03 lat. seq seq comb comb comb seq romb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb seq romb seq 76965 0,18 15 31963,9 272,26 lat. seq seq comb comb comb comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb comb comb comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb comb comb comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb comb comb comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6 lat. seq seq comb seq seq comb seq 77007 0,18 13 29073 262,6	area	comb	seq	comb	seq	seq	comb	seq	74494	-0,42	25	31210,3	268,6
area comb comb comb comb seq comb seq 74771 0,22 24 32398,4 253,16 area seq comb comb comb seq comb seq 74876 0,18 25 32401 252,78 area comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,83 area seq comb comb comb comb comb seq 75000 0,18 24 33269,9 260,48 area comb comb comb seq comb seq 75013 -0,42 24 30607,5 254,93 area seq seq comb seq seq comb seq 75013 -0,42 24 30607,5 254,93 area seq seq comb seq comb comb seq 75026 -0,42 26 32317 254,48 area seq seq comb seq comb comb seq 75043 -0,42 25 32153,6 259,43 area seq comb comb seq comb seq 75043 -0,42 25 32153,6 259,43 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,23 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,23 area seq comb comb comb seq comb seq 75124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq comb seq 76125 0,18 14 30618,1 275,43 lat. seq comb comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb seq comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq 76630 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq roma se	area	comb	seq	comb	seq	comb	comb	seq	74626	-0,42	24	31517,7	242,95
area seq comb comb seq comb seq 74876 0,18 25 32401 252,78 area comb comb comb seq comb seq 74879 -0,42 23 30700,6 258,83 area seq comb comb comb comb seq 75000 0,18 24 33269,9 260,48 area seq comb comb seq seq comb seq 75000 0,18 24 33269,9 260,48 area seq seq comb seq seq comb seq 75013 -0,42 24 30607,5 254,9 area seq seq comb seq comb seq 75026 -0,42 26 32317 254,44 area seq seq comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,2 area seq comb comb seq comb seq 75262 -0,42 24 32597,2 255,78 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq comb seq 76125 0,18 14 30618,1 275,43 lat. seq comb comb comb seq comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76663 0,18 15 32068,8 273,53 lat. seq seq comb seq comb seq 76663 0,18 15 31963,9 272,26 lat. seq seq comb comb comb seq romb seq 76965 0,18 15 31963,9 272,26 lat. seq seq comb comb comb seq romb seq 76307 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq romb seq 76365 0,18 15 31963,9 272,26 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 76307 0,18 13 29073 262,66 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,66 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,8 lat.	area	comb	comb	comb	comb	comb	comb	seq	74638	0,18	23	32382	263,02
area comb comb seq comb comb seq 74879 -0,42 23 30700,6 258,8 area seq comb comb comb comb seq 75000 0,18 24 33269,9 260,48 area comb comb comb seq seq comb seq 75013 -0,42 24 30607,5 254,9 area seq seq comb seq comb seq 75026 -0,42 26 32317 254,48 area seq seq comb seq comb comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb seq 75262 -0,42 24 32597,2 255,78 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb comb seq comb seq 76232 0,18 14 32247,9 278,35 lat. comb seq comb seq comb seq comb seq 76263 0,18 15 32068,8 273,55 lat. comb seq comb seq comb seq comb seq 766767 -0,02 14 31655,4 287,23 lat. seq seq comb seq comb seq comb seq 76963 0,18 16 31573,3 282,08 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. seq seq comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83 lat.	area	comb	comb	comb	comb	seq	comb	seq	74771	0,22	24	32398,4	253,16
area seq comb comb comb comb seq 75000 0,18 24 33269,9 260,49 area comb comb seq seq comb seq 75013 -0,42 24 30607,5 254,99 area seq seq comb seq seq comb seq 75026 -0,42 26 32317 254,49 area seq seq comb seq comb comb seq 75043 -0,42 25 32153,6 259,40 area seq comb comb seq seq comb seq 75043 -0,42 25 32153,6 259,40 area seq comb comb seq seq comb seq 75141 -0,42 25 32294,9 258,20 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,20 area seq comb comb comb seq comb seq 76124 0,18 14 29932,2 260,20 area seq comb comb comb comb seq romb seq 76125 0,18 14 30618,1 275,40 area seq comb comb comb seq comb seq 76157 0,18 15 30586,5 285,20 area seq comb seq comb seq comb seq 76232 0,18 14 32247,9 278,30 area seq comb seq comb seq comb seq romb seq	area	seq	comb	comb	comb	seq	comb	seq	74876	0,18	25	32401	252,78
area comb comb comb seq seq comb seq 75013 -0,42 24 30607,5 254,99 area seq seq comb seq comb seq 75026 -0,42 26 32317 254,44 area seq seq comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,2 area seq comb comb seq comb seq 75141 -0,42 25 32294,9 258,2 area seq comb comb comb seq comb seq 75262 -0,42 24 32597,2 255,74 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq romb seq 76125 0,18 14 30618,1 275,44 lat. seq comb comb comb comb seq romb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb comb seq romb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq romb seq	area	comb	comb	comb	seq	comb	comb	seq	74879	-0,42	23	30700,6	258,87
area seq seq seq comb seq 75026 -0,42 26 32317 254,44 area seq comb seq comb comb seq 75043 -0,42 25 32153,6 259,4 area seq comb seq comb seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb seq 75262 -0,42 24 32597,2 255,75 lat. comb comb comb seq comb seq 76124 0,18 14 29932,2 260,26 lat. seq comb comb seq comb seq 76124 0,18 14 30618,1 275,4 lat. seq comb comb seq comb seq 76125 0,18 15 30586,5 285,23 lat. comb	area	seq	comb	comb	comb	comb	comb	seq	75000	0,18	24	33269,9	260,48
area seq seq comb seq comb seq comb seq 75043 -0,42 25 32153,6 259,4 area seq comb comb seq seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb comb seq 75262 -0,42 24 32597,2 255,78 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq 76125 0,18 14 30618,1 275,43 lat. seq comb comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb seq comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,23 lat. comb seq comb seq seq comb seq 76663 0,18 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. seq seq comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat.	area	comb	comb	comb	seq	seq	comb	seq	75013	-0,42	24	30607,5	254,97
area seq comb comb seq seq comb seq 75141 -0,42 25 32294,9 258,3 area seq comb comb seq comb comb seq 75262 -0,42 24 32597,2 255,73 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq romb seq 76125 0,18 14 30618,1 275,43 lat. seq comb comb comb comb seq romb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb comb seq romb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq romb seq	area	seq	seq	comb	seq	seq	comb	seq	75026	-0,42	26	32317	254,45
area seq comb comb seq comb comb seq 75262 -0,42 24 32597,2 255,73 lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq 76125 0,18 14 30618,1 275,43 lat. seq comb comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,23 lat. comb seq comb seq seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb comb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	area	seq	seq	comb	seq	comb	comb	seq	75043	-0,42	25	32153,6	259,4
lat. comb comb comb comb seq comb seq 76124 0,18 14 29932,2 260,28 lat. seq comb comb comb comb seq 76125 0,18 14 30618,1 275,49 lat. seq comb comb comb comb seq 76157 0,18 15 30586,5 285,28 lat. comb seq comb comb comb seq 76232 0,18 14 32247,9 278,39 lat. comb seq comb comb seq comb seq 76232 0,18 14 32247,9 278,39 lat. comb seq comb seq comb seq 76263 0,18 15 32068,8 273,59 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,29 lat. comb seq comb seq seq comb seq 76767 -0,02 15 31298,8 272,99 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,09 lat. seq seq comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,69 lat. seq seq comb seq seq comb seq 77307 0,18 13 29073 262,69 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,89 lat.	area	seq	comb	comb	seq	seq	comb	seq	75141	-0,42	25	32294,9	258,2
lat. seq comb comb comb seq 76125 0,18 14 30618,1 275,4 lat. seq comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,23 lat. comb seq comb seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb seq comb seq 76963 0,18 16 31573,3 282,03 lat. seq comb	area	seq	comb	comb	seq	comb	comb	seq	75262	-0,42	24	32597,2	255,75
lat. seq comb comb comb seq comb seq 76157 0,18 15 30586,5 285,23 lat. comb seq comb comb seq comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,23 lat. comb seq comb seq comb seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,08 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	comb	comb	comb	seq	comb	seq	76124	0,18	14	29932,2	260,28
lat. comb seq comb comb comb seq 76232 0,18 14 32247,9 278,33 lat. comb seq comb seq comb seq comb seq 76263 0,18 15 32068,8 273,53 lat. comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,23 lat. comb seq comb seq comb seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	seq	comb	comb	comb	comb	comb	seq	76125	0,18	14	30618,1	275,41
lat. comb seq comb comb seq comb seq 76263 0,18 15 32068,8 273,52 lat. comb seq comb seq comb seq comb seq 76736 -0,02 14 31655,4 287,22 lat. comb seq comb seq seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,20 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	seq	comb	comb	comb	seq	comb	seq	76157	0,18	15	30586,5	285,23
lat. comb seq comb seq comb comb seq 76736 -0,02 14 31655,4 287,27 lat. comb seq comb seq seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,03 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	seq	comb	comb	comb	comb	seq	76232	0,18	14	32247,9	278,32
lat. comb seq comb seq comb seq comb seq 76767 -0,02 15 31298,8 272,93 lat. seq seq comb comb seq 76963 0,18 16 31573,3 282,09 lat. seq seq comb comb comb seq 76965 0,18 15 31963,9 272,26 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	seq	comb	comb	seq	comb	seq	76263	0,18	15	32068,8	273,52
lat. seq seq comb comb seq comb seq 76963 0,18 16 31573,3 282,09 lat. seq seq comb comb comb comb seq 76965 0,18 15 31963,9 272,20 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,69 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	seq	comb	seq	comb	comb	seq	76736	-0,02	14	31655,4	287,27
lat. seq seq comb comb comb seq 76965 0,18 15 31963,9 272,20 lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	seq	comb	seq	seq	comb	seq	76767	-0,02	15	31298,8	272,93
lat. comb comb comb comb comb seq 77307 0,18 13 29073 262,63 lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	seq	seq	comb	comb	seq	comb	seq	76963	0,18	16	31573,3	282,09
lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	seq	seq	comb		comb	comb	seq	76965	0,18	15	31963,9	272,26
lat. seq seq comb seq seq comb seq 77466 -0,02 16 30713,4 269,83	lat.	comb	comb	comb	comb	comb	comb	seq	77307	0,18	13	29073	262,61
	lat.	seq	seq	comb	seq	seq	comb	seq	77466	-0,02	16	30713,4	269,83
tati 004 004 001110 001110 001110 004 77400 0,02 10 00400,0 2/1,44	lat.	seq	seq	comb	seq	comb		seq	77468	-0,02	15	30488,5	271,44

Table 4.5: Compilation of the Design Space Exploration results

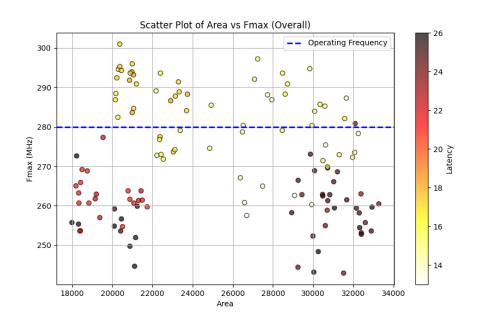


Figure 4.4: Overall Results

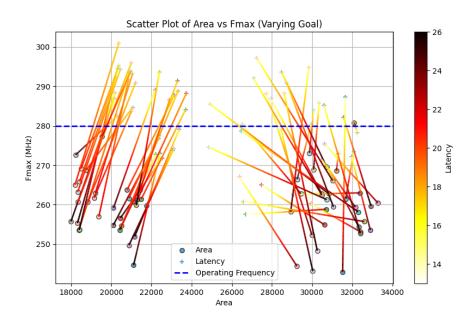


Figure 4.5: Results when varying the design goal

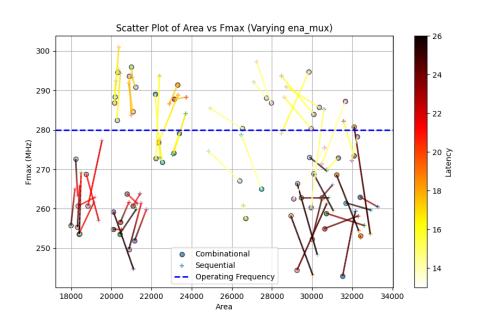


Figure 4.6: Results when varying the CCORE type for the Masking

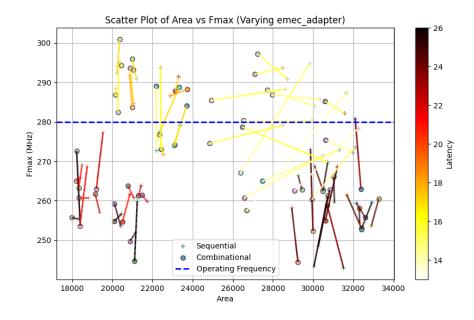


Figure 4.7: Results when varying the CCORE type for the EMEC Adapter

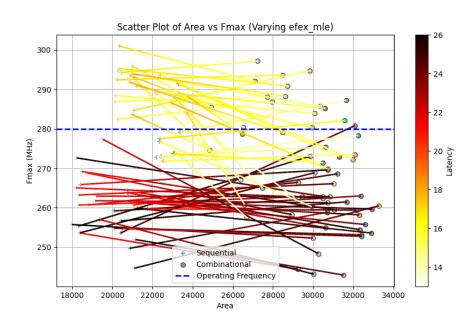


Figure 4.8: Results when varying the CCORE type for the MLE

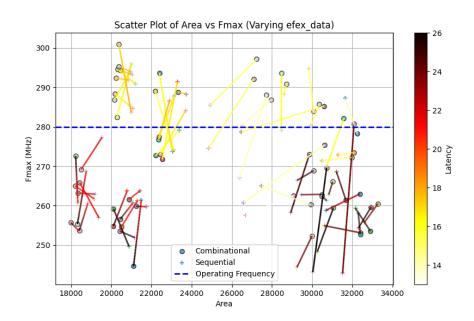


Figure 4.9: Results when varying the CCORE type for the Data Encoder

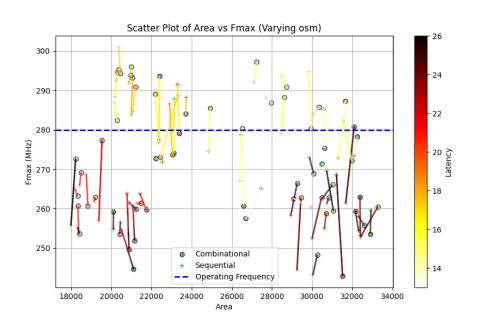


Figure 4.10: Results when varying the CCORE type for the OSM $\,$

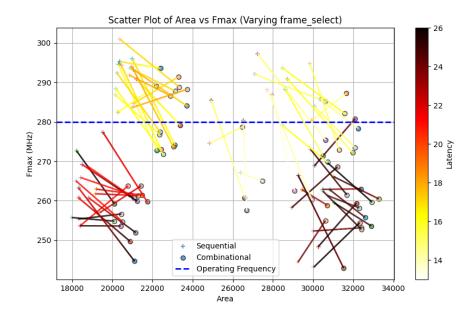


Figure 4.11: Results when varying the CCORE type for the Frame Select

4.3.3 Unrolling inside or outside the CCORE

Frame Alignment

For the Frame Alignment, the v6 firmware unrolls outside of the CCORE. One frame alignment CCORE uses very little area, and because it uses only combinational logic, unrolling inside does not have any significant impact on the area. In table 4.6, we see that the first option yields a Frame Alignment of 21 ALMs. To compare it with the second option, we can multiply it by the number of instances that will be created: 48, for the 48 frames. This gives a total area of 1008, very similar to the 1087 of the second option. The F_{max} parameter, on the other hand, decreases by 98MHz, but this should be disregarded as the "unrolling inside" version of the CCORE contains the logic to synchronize the different instances, which the other one does not.

To have an idea of the true impact that the two implementations could have on the full firmware, the table 4.6 also shows the area and F_{max} of the OSUM parent block. The low impact on the area is confirmed by our results, but the F_{max} gets a decrease of 3.6%, reducing the margin of the design.

unroll outside							
Block	Area (ALMs)	F_{max} (MHz)					
Frame Alignment	$\underline{21} (21 \times 48 = 1008)$	371.4					
OSUM	30449	274.5					
	unroll inside						
Block	Area (ALMs)	F_{max} (MHz)					
Frame Alignment	1087 (1087/48 = 22.6)	272.6					
OSUM	30512	264.6					

Table 4.6: Frame Alignment design exploration using the v6 firmware

In fact, unrolling outside can be useful when some sequential logic can be shared among all the CCOREs. The serialized Frame Alignment is a good example where unrolling outside has a positive impact, as it can be seen in the table 4.7. In this specific case, Catapult is able to optimize the design inside of the CCORE by sharing some logic between the different parallel instances. As a result, unrolling inside of the CCORE will create redundant logic and the total area of the CCORE instances is almost the double of the "unrolling inside" version. Additionally, this negative impact gets amplified on the OSUM block, with an area increase of 15% and new timing violations with the "unroll outside" option.

CRC9

In the v6 firmware, similarly to the Frame Alignment, the CRC9 block is unrolled outside of the CCORE. The block alone represents 68 ALMs for an F_{max} of 395.6 MHz. When unrolling inside of the CCORE, the whole block gives an area of 3332 ALMs and an operating frequency of 357.1 MHz. Unrolling inside of the CCORE makes the block 49 times bigger, which matches the number of frames to process, and has a negative impact on the F_{max} which must be double

unroll outside							
Block	Area (ALMs)	F_{max} (MHz)					
Frame Alignment	$36 (36 \times 48 = 1728)$	388.8					
OSUM	18669	274.7 < 280					
	unroll inside						
Block	Area (ALMs)	F_{max} (MHz)					
Frame Alignment	940 (940/48 = 19.6)	345.1					
OSUM	15875	291.1					

Table 4.7: Frame Alignment design exploration using the new firmware

checked in the OSUM block.

	unroll outside	
Block	Area (ALMs)	F_{max} (MHz)
CRC9	$\underline{68} \ (68 \times 48 = 3264)$	395.5
OSUM	30534	271.89
	unroll inside	
Block	Area (ALMs)	F_{max} (MHz)
CRC9	3332 (3332/48 = 69.4)	357.1
OSUM	30507	262.6

Table 4.8: CRC9 design exploration using the v6 firmware

Table 4.9 shows the impact of both approaches on the OSUM block. While the area difference is negligeable, the F_{max} is reduced by 10 MHz when unrolling inside of the CCORE.

4.3.4 Overall Improvement

With the knowledge from the different design space explorations, the new firmware could be optimized to yield the best results.

The TDE exploration showed that serializing before the OSM was the best option, as the area reduction at the block level translated to the higher levels. Moreover, the higher F_{max} value allows the circuit to operate at 280 MHz without any timing violations.

The blocks with the biggest impacts concerning the HLS CCORE type are the MLE and the Frame Select. Those two must be set to sequential in order to unlock resource sharing and reduce the area. When setting the design goal to area, the F_{max} value unfortunately does not match the 280 MHz requirement. However this is not a major problem, as the best area with the design goal set to area is 10% smaller than the best area with the design goal set to latency.

Finally, the unrolling inside or outside of the CCORE was tested for the Frame Alignment and CRC9 blocks and compared both for the v6 firmware and the new one.

	unroll outside	
Block	Area (ALMs)	F_{max} (MHz)
CRC9	$\underline{68} \ (68 \times 48 = 3264)$	395.5
OSUM	30534	271.89
	unroll inside	
Block	Area (ALMs)	F_{max} (MHz)
CRC9	3332 (3332/48 = 69.4)	357.1
OSUM	30507	262.6

Table 4.9: CRC9 design exploration using the v6 firmware

Evaluation

5.1 Software Simulation

In the LATOME HLS team, the software simulation stack is made of 4 layers:

- The layer 0 (l0) tests are written in C++, without timing information, and use both a C++ only and RTL simulation. They are close to unit tests and are used to validate the blocks individually.
- The layer 1 (l1) is written in Python using the cocotb library. It is used to test the integration of the blocks with timing information and monitoring. The Layer 1 tests both the ISM and OSUM blocks, without the clock domain transfers and actual User Code.
- The layer 2 (l2) implements the l1 but takes into account the clock domain transfers and serial-to-parallel and parallel-to-serial conversions VHDL blocks.
- The layer 3 (13) is the final layer and tests the whole system with the User Code, and the different Software configuration programs.

Each layer can catch different types of bug, and the higher the layer, the more time it takes to run and the more complex it becomes. The new firmware developed for this thesis has passed successfully each of these layers.

5.1.1 Layer 0

The layer 0 are divided in two types of tests: the C++ only tests and the RTL tests. The C++ only tests are used to validate the C++ logic used in the HLS blocks. For instance, it can test that an adder function is actually adding two numbers and giving the correct result.

With the same code, also called "test bench" the generated RTL files can be tested using Questa simulation. This is very helpful as the test bench code can directly use the C++ HLS types, such as ac_int or ac_channel. However, the layer 0 has no access to the different clocks and individual signals of the design.

For the different blocks, the test bench generates random inputs which are processed with C++ code and compared with the output of the HLS design.

5.1.2 Firmware Aware and Agnostic Models

The layers 1, 2 and 3 use a LATOME software model to compare against the RTL outputs. Two models are used to reduce the risk of bugs: the firmware aware model and the firmware agnostic model. The former replicates each blocks of the firmware in Python and gives access to the results at each steps, while the latter is only based on the specifications of the firmware and only gives access to the final outputs.

5.1.3 Layer 1

To only test the HLS code, corresponding to the ISM and the OSUM, the layer 1 uses Python and the cocotb library, together with Questa simulation. The User Code which connects the ISM and OSUM is a simple bypass at this level. With cocotb, the test bench can access the different signals of the design, and monitor them. Layers 1, 2 and 3 are used to validate the integration of the blocks, and the timing information.

- 5.1.4 Layer 2
- 5.1.5 Layer 3
- 5.2 Hardware testing

Conclusion