

# Fundamental Interaction Language

Paolo Pignatelli

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# Chapter 1

## Foundations and Semantic Constants

### 1.1 The Information–Observation–Language (I–O–L) Triad

Modern knowledge systems reveal a recurring motif: comprehension requires only the *differences* between two bodies of knowledge, not their entirety. We formalise this with the **Information–Observation–Language triad**

$$(\mathcal{I}, \mathcal{O}, \mathcal{L}) = (\mathcal{I}, \mathcal{O}, \mathcal{L}), \quad (1.1)$$

where  $\mathcal{I}$  denotes possible information states,  $\mathcal{O}$  the set of admissible observations, and  $\mathcal{L}$  the symbolic language capable of encoding both. Minimal "bridges" between domains are implemented by Local Language Constructors (LLCs), treated in Chapter ??.

### 1.2 Foundational Postulates

**Postulate F1 (Semantic locality).** Any act of communication factors through a finite sub-language  $B \subseteq \mathcal{L}$  such that  $E \otimes B \cong \mathcal{L}$ , with  $E$  the receiver's existing language fragment.

**Postulate F2 (Minimal bridges).** Among all such  $B$ , natural communication selects one that minimises  $|B|$ .

**Postulate F3 (Hierarchical union).** Languages compose by hierarchical union and the semantic density  $\rho$  is non-decreasing under this union.

### 1.3 Semantic Constants

We introduce two universal constants:

$c_s$  the *semantic light-speed*, bounding information propagation in a knowledge graph:

$$d_G(v_1, v_2) \leq c_s \Delta t. \quad (1.2)$$

$\hbar_s$  the *semantic Planck constant*, appearing in an uncertainty relation between discovery and invention operators:

$$\Delta D \Delta I \geq 12 \hbar_s. \quad (1.3)$$

Convenient units set  $c_s = \hbar_s = 1$ ; deviations measure complexity.

## 1.4 Road-map

This chapter establishes notation for the remainder of the book. Chapter ?? develops the geometric view ( $c_s$  as cone slope), Chapter ?? derives global limits from Eq. eq:sem-uncertainty, Chapter ?? treats drift and masks, and Chapter ?? links the constants to physical information bounds.

**Take-away.** The triad  $(\mathcal{I}, \mathcal{O}, \mathcal{L})$  and constants  $(c_s, \hbar_s)$  provide an irreducible substrate on which all higher FIL structures are built.

## Chapter 2

# Semantic Geometry

### 2.1 Semantic Light-Cones

In a knowledge graph  $G = (V, E)$  we define the *semantic distance*  $d_G(v_1, v_2)$  as the minimal edge-weighted path length between two concept vertices. Postulate F1 implies that information flow is bounded by the constant  $c_s$  introduced in Chapter ??:

$$d_G(v_1, v_2) \leq c_s \Delta t. \quad (2.1)$$

Points satisfying equality trace **semantic light-cones**. They encode the frontier beyond which two agents cannot reach mutual comprehension within  $\Delta t$ .

**Propagation kernel.** Let  $K_t(v)$  denote the reachable set from  $v$  in time  $t$ . A discrete propagator is  $P_t = 1_{d_G \leq c_s t}$ .

### 2.2 Informational Curvature

Light-cone slope alone does not capture *semantic gravitation*—the tendency of dense subgraphs to attract interpretive trajectories. We introduce an *informational curvature tensor*  $\mathcal{K}$  via the deviation of geodesics in  $G$ :

$$\delta^2 d_G = -\mathcal{K}(\gamma, \dot{\gamma}) d\sigma^2. \quad (2.2)$$

Positive curvature corresponds to semantic "mass" and appears near high mutual-information clusters. See [?](§2) for the full derivation.

#### Example – category junction

Two dense languages  $L_1, L_2$  joined by a minimal LLC bridge  $B$  create negative curvature in the bridge (saddle) and positive curvature inside each language core.

### 2.3 Computational Spacetime Correspondence

Mapping Eq. eq:semantic-cone onto a Turing tape with physical delays  $\tau$ , we recover the computational light-speed bound  $c_s \approx 1/\tau$  [?]. Informational curvature then corresponds to non-uniform memory access latencies—regions of high semantic mass behave as RAM “black holes”.

### 2.4 Meta-Law and Quantisation

FL\_Field Meta-Law postulates a universal action principle in information space. Quantising small oscillations of  $d_G$  about a ground state yields a discrete spectrum analogous to normal modes in Riemannian geometry. This motivates the uncertainty relation derived in Eq. (??).

**Take-away.** The geometry of semantic light-cones and informational curvature generalises relativistic causality to knowledge systems, setting the stage for global bounds (Chapter ??) and dynamical drift analysis (Chapter ??).

## Chapter 3

# Informational Bounds

### 3.1 Bekenstein-like Entropy Limit for Language

The classical Bekenstein bound [?] constrains the maximum entropy  $S$  of physical matter in a region of radius  $R$  and energy  $E$  by  $S \leq 2\pi kER/\hbar c$ . In the FIL setting, tokens carry informational mass and the analogue becomes

$$H(\mathcal{L}) \leq 2\pi k_s E_{\mathcal{L}} R_{\mathcal{L}} / \hbar_s, \quad (3.1)$$

where  $E_{\mathcal{L}}$  is the cumulative energetic cost of storing the language fragment and  $R_{\mathcal{L}}$  its semantic diameter.

**Interpretation.** If  $H$  exceeds this limit, further compression (via LLC bridges) or hierarchical segmentation is required.

### 3.2 Finite Knowledge Bounds

Let  $G = (V, E)$  be a directed knowledge graph with path entropy  $H_P$  and symbol complexity  $C_s$ . finiteknowledgebounds2025 derive upper and lower compression bounds

$$\frac{|V|}{\log C_s} \leq H_P \leq |E| \log C_s. \quad (3.2)$$

We adopt the lower bound as the *finite knowledge bound* (FKB) for any segment.

#### 3.2.1 Prime-Encoding Lower Bound

Prime-encoding of edge labels achieves the lower bound asymptotically; see Appendix ??.

### 3.2.2 Voronoi Capacity Upper Bound

Semantic Voronoi cells give a geometric ceiling; we revisit this in Chapter ?? when studying drift fields.

## 3.3 Acceleration Constraint

acceleration2025 show that rapid semantic updates imply an *acceleration cost*

$$a_{\mathcal{L}} \equiv \frac{d^2 H}{dt^2} \leq c_s^2 / \ell_{\min}, \quad (3.3)$$

with  $\ell_{\min}$  the minimum edge length. This links light-cone slope ( $c_s$ ) to second-order dynamics.

## 3.4 Big Bang as Information Phase Transition

The cosmological Big Bang is recast as a phase transition where  $H \rightarrow 0$  while  $dH/dt \rightarrow \infty$ . Under FKB this corresponds to the creation of the minimal language fragment required for any subsequent evolution.

## 3.5 Road-map

Informational limits set the stage for Chapter ??, where drift and masks operate within these bounds, and Chapter ??, which ties them to particle-level information exchange.



## Chapter 4

# Dynamics, Drift, and Mask-Based Stabilisation

### 4.1 Diagnosing Semantic Drift

Let  $\delta_k(n)$  denote the *drift magnitude* of concept  $k$  after  $n$  network layers. Following SSR<sub>Draft3</sub>, we define  $\delta_k(n) = \frac{\|P_k^n - P_k^0\|}{\|P_k^0\|}$ , (4.1) where  $P_k^n$  is the perturbation field of concept  $k$  at depth  $n$ . The *shadow depth*  $\Delta_k^n$  is the first layer  $m > n$  such that  $\delta_k(m) < \varepsilon$ . A rising sequence  $\Delta_k^n$  indicates unstable semantics.

### 4.2 Mask Evolution Operator

Dynamic masks  $M_k^n$  are injected at layer  $n$  to probe drift. The **Mask Evolution Operator** (MEO) propagates masks across depth:

$$T_1^n : M_k^1 \mapsto M_k^n, \quad T_1^n = T_{n-1}^n \circ \dots \circ T_1^2. \quad (4.2)$$

The *error tensor*

$$E_k^n = M_k^n - T_1^n(M_k^1) \quad (4.3)$$

serves as a drift-diagnostic:  $\|E_k^n\| \rightarrow 0$  implies layer stability.

### 4.3 Gaussian-Mixture View of Observation

Observation tokens are embedded as weighted Gaussian mixtures  $GMM(w_i, \mu_i, \Sigma_i)$ . Overlap of components predicts hallucination regions. The mixture distance introduces a probabilistic refinement of the drift metric:

$$d_{GMM}(p, q) = 1 - \sum_i \sqrt{w_i^{(p)} w_i^{(q)}} e^{-12 \Delta \mu_i^\top \Sigma_i^{-1} \Delta \mu_i}. \quad (4.4)$$

## 4.4 Perturbation Cellular Automata

Discrete propagation of truth-wavefronts may be simulated by a perturbation cellular automaton (PCA) on the concept graph  $G = (V, E)$ . Each cell updates via

$$s_{t+1}(v) = f(s_t(v), (s_t(u))_{u \in N(v)}), \quad (4.5)$$

where  $f$  conserves a local *semantic energy* to satisfy the bound  $d_G \leq c_s \Delta t$ .

## 4.5 The Nibbler Algorithm

1. Initialise discovery state  $D_0$  and pattern set  $P_0$ .
2. (Discovery)  $D_{t+1} \leftarrow D_t + \text{NibblerStep}(D_t)$ .
3. (Pattern)  $P_{t+1} \leftarrow \text{MetaPattern}(P_t, D_{t+1})$ .
4. Repeat until  $\Delta D$  and  $\Delta P$  fall below thresholds.

The interface kernel

$$k_{NI}(x, y) = \alpha k_D(x, y) + (1 - \alpha) k_P(x, y) \quad (4.6)$$

controls the discovery–pattern balance.

## 4.6 Integration with the UIL Framework

Integration<sub>UIL</sub> extends the graph model to include confidence  $c(\omega)$  and security  $\lambda(\omega)$ . The drift-aware propagation rule becomes

$$\Delta(v_i, v_{i+1}) = \min(\text{infochange} \mid \lambda(v_{i+1}) \geq \lambda_{\min}, c(\omega) \geq c_{\min}). \quad (4.7)$$

## 4.7 Outlook

This chapter introduced dynamical machinery that preserves the semantic constants while allowing adaptive evolution. Chapter ?? maps these operators to physical processes—e.g. interferometric stabilisation in the InterferoShell.

**Take-away.** Mask evolution, GMM observation, and Nibbler search conspire to keep drift bounded without violating the informational limits of Chapter ??.

## Chapter 5

# Physical and Computational Correspondence

### 5.1 Particles as Information Events

Each fundamental interaction instantiates new information[?]. Let  $S(t) = \{p_i, E_{ij}\}$  denote the quantum state at time  $t$ . A collision  $T : S(t) \rightarrow S(t+1)$  increases the descriptive complexity

$$\Delta I = I(S(t+1)) - I(S(t)) \leq kE. \quad (5.1)$$

This yields a conservation-of-information principle analogous to energy conservation in QFT.

### 5.2 Computational Relativity Analogy

#### 5.2.1 Complexity *vs.* Time-Dilation

Landauer–Bremermann bounds suggest that executing  $N$  logical operations on mass  $m$  requires a minimum proper time  $\Delta\tau \geq N\hbar/(mc^2)$ . Interpreting complexity as curvature we obtain a metric on algorithmic spacetime:

$$ds^2 = -\left(1 - 2G C c^2 r\right) c^2 dt^2 + \left(1 - 2G C c^2 r\right)^{-1} dr^2 + r^2 d\Omega^2, \quad (5.2)$$

with  $C$  the local Kolmogorov-complexity density.

#### 5.2.2 Physical Foundations of Computational Light-Speed

Chapter 3 of [?] derives a physical upper speed of algorithmic propagation that matches the semantic constant  $c_s$  from Chapter ??.

### 5.3 Computational Spacetime Geometry

Information flow defines a causal set  $\mathcal{C}$  whose Hasse diagram embeds into the knowledge graph  $G$ . Curvature of  $\mathcal{C}$  matches informational curvature  $\kappa$  of Section ??, closing the semantic-physical loop.

### 5.4 Prime Path Encoding for Graph Compression

Path-encoding maps concept trajectories to unique prime products  $\pi(P) = \prod p_i^{n_i}$ . The path length satisfies

$$|P| \leq O(\log \pi(P)), \quad (5.3)$$

providing asymptotically optimal storage[?].

### 5.5 Discussion and Future Work

Links between semantic and physical bounds suggest experimental tests:

1. Measure algorithmic time-dilation effects in high-complexity quantum circuits.
2. Investigate Hawking-like emission at semantic black-hole horizons where  $\rho \rightarrow \infty$ .
3. Extend computational-relativity metrics to non-commutative graph geometries.

**Take-away.** Physical interaction, algorithmic complexity, and semantic structure obey the same limiting principles, unifying FIL with foundational physics.