

Fundamental Interaction Language

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Chapter 1

Foundations and Semantic Constants

1.1 The Information–Observation–Language (I–O–L) Triad

Modern knowledge systems reveal a recurring motif: comprehension requires only the *differences* between two bodies of knowledge, not their entirety. We formalise this with the **Information–Observation–Language triad**

$$(\mathcal{I}, \mathcal{O}, \mathcal{L}) = (\mathcal{I}, \mathcal{O}, \mathcal{L}), \quad (1.1)$$

where \mathcal{I} denotes possible information states, \mathcal{O} the set of admissible observations, and \mathcal{L} the symbolic language capable of encoding both. Minimal "bridges" between domains are implemented by Local Language Constructors (LLCs), treated in Chapter ??.

1.2 Foundational Postulates

Postulate F1 (Semantic locality). Any act of communication factors through a finite sub-language $B \subseteq \mathcal{L}$ such that $E \otimes B \cong \mathcal{L}$, with E the receiver's existing language fragment.

Postulate F2 (Minimal bridges). Among all such B , natural communication selects one that minimises $|B|$.

Postulate F3 (Hierarchical union). Languages compose by hierarchical union and the semantic density ρ is non-decreasing under this union.

1.3 Semantic Constants

We introduce two universal constants:

c_s the *semantic light-speed*, bounding information propagation in a knowledge graph:

$$d_G(v_1, v_2) \leq c_s \Delta t. \quad (1.2)$$

\hbar_s the *semantic Planck constant*, appearing in an uncertainty relation between discovery and invention operators:

$$\Delta D \Delta I \geq 12 \hbar_s. \quad (1.3)$$

Convenient units set $c_s = \hbar_s = 1$; deviations measure complexity.

1.4 Road-map

This chapter establishes notation for the remainder of the book. Chapter ?? develops the geometric view (c_s as cone slope), Chapter ?? derives global limits from Eq. eq:sem-uncertainty, Chapter ?? treats drift and masks, and Chapter ?? links the constants to physical information bounds.

Take-away. The triad $(\mathcal{I}, \mathcal{O}, \mathcal{L})$ and constants (c_s, \hbar_s) provide an irreducible substrate on which all higher FIL structures are built.

Chapter 2

Semantic Geometry

2.1 Semantic Light-Cones

In a knowledge graph $G = (V, E)$ we define the *semantic distance* $d_G(v_1, v_2)$ as the minimal edge-weighted path length between two concept vertices. Postulate F1 implies that information flow is bounded by the constant c_s introduced in Chapter ??:

$$d_G(v_1, v_2) \leq c_s \Delta t. \quad (2.1)$$

Points satisfying equality trace **semantic light-cones**. They encode the frontier beyond which two agents cannot reach mutual comprehension within Δt .

Propagation kernel. Let $K_t(v)$ denote the reachable set from v in time t . A discrete propagator is $P_t = 1_{d_G \leq c_s t}$.

2.2 Informational Curvature

Light-cone slope alone does not capture *semantic gravitation*—the tendency of dense subgraphs to attract interpretive trajectories. We introduce an *informational curvature tensor* \mathcal{K} via the deviation of geodesics in G :

$$\delta^2 d_G = -\mathcal{K}(\gamma, \dot{\gamma}) d\sigma^2. \quad (2.2)$$

Positive curvature corresponds to semantic "mass" and appears near high mutual-information clusters. See [?](§2) for the full derivation.

Example – category junction

Two dense languages L_1, L_2 joined by a minimal LLC bridge B create negative curvature in the bridge (saddle) and positive curvature inside each language core.

2.3 Computational Spacetime Correspondence

Mapping Eq. eq:semantic-cone onto a Turing tape with physical delays τ , we recover the computational light-speed bound $c_s \approx 1/\tau$ [?]. Informational curvature then corresponds to non-uniform memory access latencies—regions of high semantic mass behave as RAM “black holes”.

2.4 Meta-Law and Quantisation

FL_Field Meta-Law postulates a universal action principle in information space. Quantising small oscillations of d_G about a ground state yields a discrete spectrum analogous to normal modes in Riemannian geometry. This motivates the uncertainty relation derived in Eq. (??).

Take-away. The geometry of semantic light-cones and informational curvature generalises relativistic causality to knowledge systems, setting the stage for global bounds (Chapter ??) and dynamical drift analysis (Chapter ??).