

# Module: Information Acceleration and Observational Hierarchies

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## 1 Introduction

This module extends our prior discussions by introducing acceleration in directed graphs as a model for information propagation. We examine the accumulation of information in a manner similar to viral spread, introduce a moving observation window mechanism, and relate hierarchical observations to training in neural networks.

## 2 Information Spread as Viral Propagation

Let  $G = (V, E)$  be a directed graph representing an information network, where  $V$  denotes nodes (information states) and  $E$  denotes directed edges (information transfer). Define the strength of information at a node  $v_i$  as a function  $S(v_i)$  based on incoming information:

$$S(v_i) = \sum_{v_j \in \text{in-neighbors}(v_i)} w_{ji} S(v_j) \quad (1)$$

where  $w_{ji}$  is a weight function representing the influence of node  $v_j$  on  $v_i$ .

Consider a layered propagation model where the depth of nodes from an initial node  $v_0$  is defined as levels  $L_k$ . The probability of information reaching level  $L_n$  is proportional to the aggregated strength along paths:

$$P(L_n) \propto \sum_{p \in \mathcal{P}_{0 \rightarrow n}} \prod_{(v_i, v_j) \in p} w_{ij} \quad (2)$$

where  $\mathcal{P}_{0 \rightarrow n}$  represents all paths from  $v_0$  to level  $L_n$ .

## 3 Moving Window Encoding and Memory Optimization

Define a moving observation window  $W_t$  over an information trajectory. Let  $W_t$  maintain a record of recent nodes and encode previous states with a compression

function  $C$ . The update rule follows:

$$W_{t+1} = \begin{cases} \{v_{t+1}\} \cup W_t, & \text{if } |W_t| < k \\ \{v_{t+1}\} \cup C(W_t), & \text{otherwise} \end{cases} \quad (3)$$

where  $k$  is the memory threshold, and  $C(W_t)$  compresses past nodes based on redundancy and relevance.

A mathematical rule for dropping information is defined using an entropy threshold  $H_T$ :

$$H(W_t) = - \sum_{v_i \in W_t} P(v_i) \log P(v_i) \quad (4)$$

where  $P(v_i)$  is the frequency-based probability of encountering  $v_i$ . If  $H(W_t) < H_T$ , older nodes are removed.

## 4 Acceleration in Information Race

Define the acceleration of information propagation between levels as:

$$a_n = \frac{S(L_n) - S(L_{n-1})}{\Delta t} \quad (5)$$

where  $S(L_n)$  is the cumulative information strength at level  $L_n$  and  $\Delta t$  is the time step. The most influential paths maximize acceleration, defining an optimal information trajectory.

## 5 Observation as Training

Observations are defined as changes in system state due to incoming signals. Define an observation function  $O$  as:

$$O : X \times I \rightarrow X' \quad (6)$$

where  $X$  is the state space,  $I$  is an input signal, and  $X'$  is the updated state. Hierarchical observations align with layers in neural networks, where each layer  $L_k$  abstracts features from the previous layer:

$$L_k = f_k(L_{k-1}) \quad (7)$$

where  $f_k$  represents a transformation function.

## 6 Conclusion

This module formalizes information acceleration, hierarchical observations, and moving window optimization in information networks. These principles will be integrated into the next iteration of our main research document.