

G.C.E.(O.L.) Support Seminar - 2016

Mathematics I

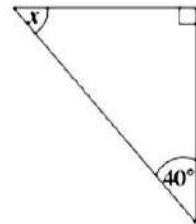
Two hours

Part A

Answer all questions on this paper itself. Each question carries 02 marks.

1. Express $\log_x 64 = 2$ in index form.

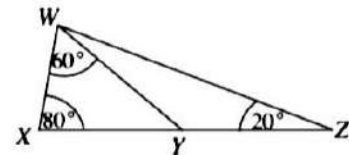
2. Find the value of x based on the information in the figure.



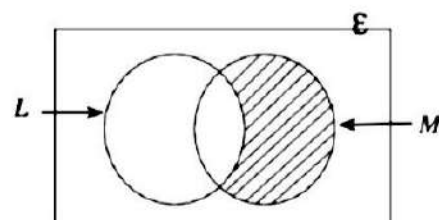
3. Mala gives Rs. 540 000 as a loan at a monthly simple interest rate of 2%. How much interest does Mala receive for 6 months?

4. Factorize : $x^2 + 5x + 4$

5. If XYZ is a straight line, name two sides which are equal, based on the information in the figure.

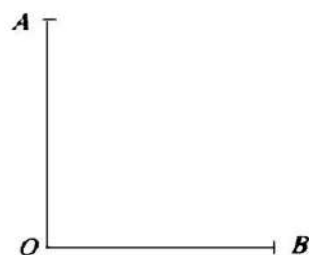


6. Write down the shaded region in the Venn diagram using set notation.



[See page 2

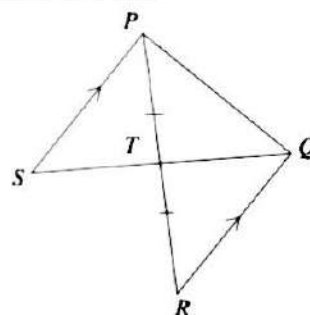
7. O and B in the figure are two points on a horizontal ground and OA is a vertical pillar. The angle of elevation of A when observed from the point B is 60° . What is the magnitude of the angle of depression of B when observed from A ?



8. If S is the sample space of a random experiment with equally likely outcomes and A is an event of it such that $P(A) = \frac{1}{5}$ and $n(A) = 8$, then find $n(S)$.

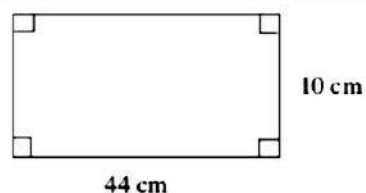
9. Find the inter-quartile range of the group of data 2, 2, 3, 3, 5, 6, 7, 8, 9, 11, 13.

10. Name a pair of congruent triangles in the figure, and write down the condition under which they are congruent.

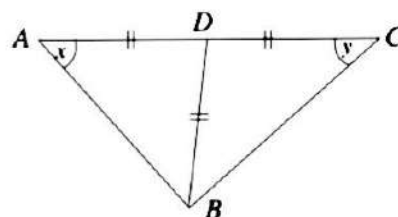


11. Find the least common multiple of $x(x+1)$ and x^2 .

12. The figure shows the rectangular lamina that is obtained when a hollow cylinder of height 10 cm is cut along a line which is perpendicular to its base. Find the radius of the cylinder. (Take $\pi = \frac{22}{7}$)



13. Find the value of $x + y$ based on the information in the given triangle ABC .

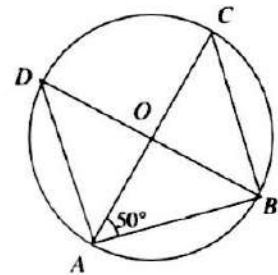


[See page 3]

14. Simplify : $\frac{1}{x} - \frac{1}{3x}$

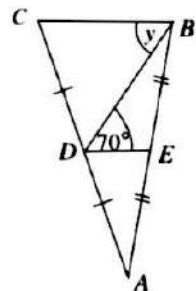
15. The first approximation of the square root of a number is 3.1. What is the perfect square that is closest to this number?

16. In the circle with centre O shown in the figure, $\angle BAC = 50^\circ$. Find the magnitude of $\angle ADB$.

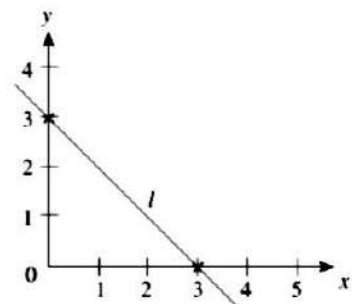


17. $A = \begin{pmatrix} 3 & -2 \\ -1 & 0 \end{pmatrix}_{2 \times 2}$ and $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}_{2 \times 2}$. Find the matrix B such that $2A + B = I$.

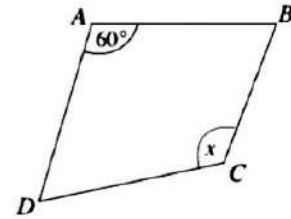
18. Find the value of y based on the information in the figure.



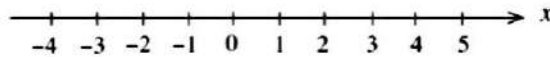
19. Write the equation of the straight line denoted by l in the figure.



20. $ABCD$ in the figure is a cyclic quadrilateral. Find the value of the angle denoted by x .



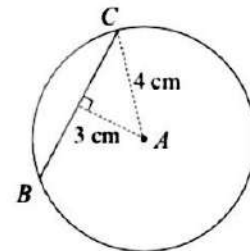
21. Mark the interval of solutions which satisfy both the inequalities $x \geq -2$ and $x < 3$ on the given number line.



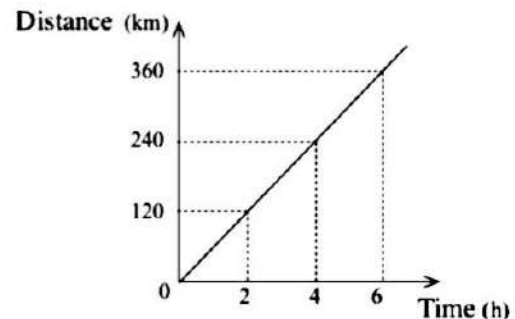
22. Find the common ratio of the geometric progression with first term 3 and fourth term 24.

23. Nine men require 8 days to complete a task. How many days will four men take to complete exactly half this task?

24. Complete the sketch that has been drawn to find the points which are 4 cm from the point A and 6 cm from the line BC and name these points as D and E .



25. The figure shows the distance time graph relevant to the motion of a vehicle travelling with uniform speed. Find the speed of the vehicle.



* *

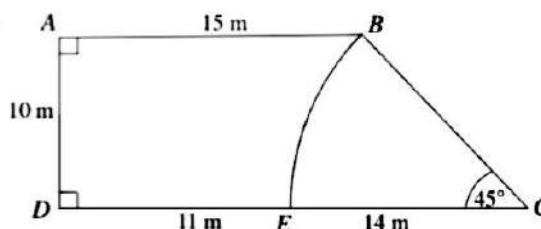
Part B

Answer **all** questions on this question paper itself. Each question carries 10 marks.

1. Of the letters that a post office received on a certain day, $\frac{1}{8}$ were registered letters and $\frac{2}{3}$ were ordinary letters.
 - (i) Find the number of registered letters and ordinary letters that were received as a fraction of the total number of letters that were received by the post office that day.
 - (ii) $\frac{1}{5}$ of the remaining letters were express letters. Find the number of express letters that were received as a fraction of the total number of letters.
 - (iii) If the remaining letters, which were neither registered letters nor ordinary letters nor express letters were all foreign letters, and if this number was 520, then how many registered letters were received that day?
 - (iv) Find the ratio of the ordinary letters to the express letters that were received that day.

2. The figure shows a playground $ABCD$. Sand is spread in the section BCE which is a sector of a circle with central angle 45° . (Take $\pi = \frac{22}{7}$)

- (i) Find the perimeter of the section $ABED$.



- (ii) Find the area of the section in which sand is spread.
- (iii) Find the area of the section apart from that in which sand is spread.
- (iv) It is required to allocate a section within this playground for a milk stall. Its area should be $\frac{1}{6}$ of the area of the section apart from that in which sand is spread and it should take the shape of a right angled triangle with AD as one boundary and another boundary on DC . On the given figure, mark the section that should be allocated for the milk stall, together with the measurements.

3. (a) The annual assessed value of the building in which the business "Sesiri" is conducted is Rs. 75 000. The urban council charges it Rs. 1500 as rates for a quarter.

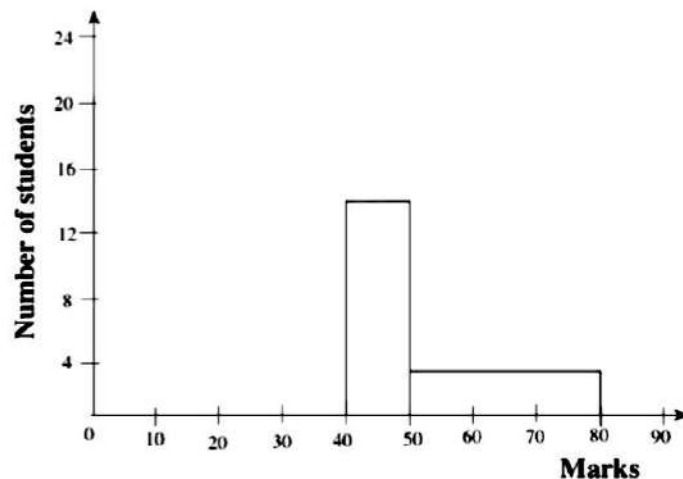
- (i) Find the rates that have to be paid for a year, and calculate the annual rates percentage.
- (ii) A discount of 10% is received if the rates for the whole year is paid before the 31st of January of that year. Find how much the businessman who owns the building saves, if he pays the rates for the whole year before this date.

- (b) Mr. Silva invested Rs. 270 000 to buy shares of a company which pays Rs. 2 per share as dividends, at a time when the market price of a share of this company was Rs. 9.

- (i) Find the dividends income received by Mr. Silva at the end of a year.
- (ii) After receiving the dividends, if Mr. Silva sold all the shares at the current market price of Rs. 10.50 per share, find his capital gain.

4. The incomplete frequency distribution and corresponding incomplete histogram given below have been prepared with the marks obtained by a group of grade 12 students who participated in a project evaluation. (20 – 30 means more than 20 but less than or equal to 30)

Marks	Number of students
0 – 20	4
20 – 30	10
30 – 40	20
40 – 50
50 – 80

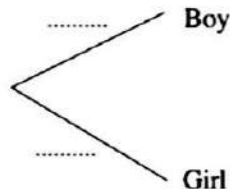


- (i) Complete the frequency distribution using the information in the incomplete histogram.
- (ii) Complete the histogram using the information in the frequency distribution.
- (iii) Draw the frequency polygon on the histogram.
- (iv) It was decided to give a special training to those who have obtained more than 50 marks. Express the number of students who are selected for the training as a percentage of the number of students who participated in the project evaluation.

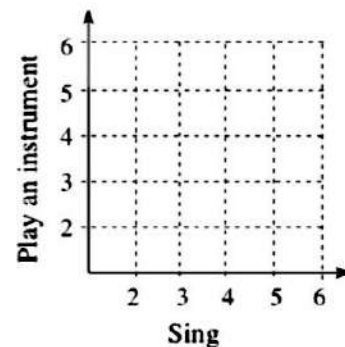
5. Four boys and 2 girls who are able to sing as well as play a musical instrument are to participate in a talent show. The four boys have been given the numbers 1, 2, 3 and 4 while the two girls have been given the numbers 5 and 6, to select the order in which they are to perform. These six numbers are marked on six identical cards such that each card has a different number. A card is picked at random from the box. The child who has the number which is picked has to sing.

(a) (i) Complete the given incomplete tree diagram.

First picking (Sing)



- (ii) The first card picked is replaced in the box and again a card is picked at random. The child with this number has to play an instrument. Extend the given tree diagram in a suitable way, and find the probability of a boy performing on one occasion and a girl on the other occasion.
- (b) Now suppose that the boy who received the number 1 had to withdraw from the show due to another commitment. If the card with the number 1 is removed from the box and children are picked in the same manner as above from the remaining cards, to sing and to play an instrument,
- (i) represent the sample space relevant to picking a child to sing and a child to play an instrument in the given grid.



- (ii) Mark the event of the same child not being picked to sing and play an instrument on the grid and find its probability.

* * *

G.C.E.(O.L.) Support Seminar - 2016

Mathematics II

Three hours

- * Answer **ten** questions, selecting **five** questions from **Part A** and five questions from **Part B**.
- * Each question carries 10 marks.
- * The volume of a right circular cone with base radius r and height h is $\frac{1}{3}\pi r^2 h$.

Part A

Answer only **five** questions.

1. A and B are two financial institutions which provide loans as follows.

Institution A

- Charges interest at an annual interest rate of 18%.
- Interest is calculated on the reducing balance.
- The loan amount and interest have to be paid in equal monthly installments.

Institution B

- Charges interest at an annual interest rate of 10% and the interest is compounded annually.
- The loan amount and the total interest have to be paid together at the end of the loan period.

Samantha needs to obtain a loan of Rs. 300 000. He intends to settle the loan together with the interest by the end of two years. Samantha's friend says that more interest has to be paid if the loan is taken from Institution A. Find the total interest that has to be paid when this loan amount is taken from each of these two institutions, and with reasons explain the truth / falsehood of the friend's statement.

2. The table below gives the y values of the function $y = (x + 1)(x - 3)$ corresponding to several given x values.

x	-1	0	1	2	3	4	5
y	0	-3	-4	-3	0	12

- (a) (i) Find the value of y corresponding to $x = 4$.
(ii) Draw the graph of the above function by selecting a suitable scale.
- (b) By using the graph,
(i) find the minimum value of the function.
(ii) explain the behavior of the graph on the interval $-1 < x < 1$, by indicating whether it is positive or negative and whether it is increasing or decreasing.
- (c) By drawing a suitable straight line graph on the above coordinate plane, obtain a value for $\sqrt{3}$ to the nearest first decimal place.

3. The frequency distribution of the number of trips made during a day by 40 vehicles of the same type transporting soil to the construction site of a expressway is given below.

Class Interval (Number of trips)	4 - 8	9 - 13	14 - 18	19 - 23	24 - 28	29 - 33	34 - 38
Frequency (Number of vehicles)	2	3	5	8	15	5	2

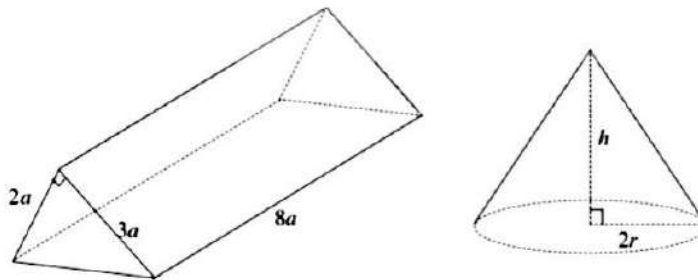
- How many vehicles made more than 33 trips transporting soil?
 - Find the mean number of trips that a vehicle makes during a day transporting soil, to the nearest whole number.
 - Each vehicle can carry 4 cubes of soil per trip. If the price of one cube of soil is Rs. 2000, what is the expected cost of the soil that is transported during a day by one vehicle?
 - The engineer states that since all the above vehicles would have to be used for 2 days to transport the soil required for a length of 100 m of the highway, the cost of the soil for this would exceed 14 million rupees. Give reasons to show that his statement could be true.
4. The government provides aid of Rs. 100 per child and Rs. 150 per adult daily for those sheltering in a certain camp due to being displaced by floods. On a certain day, a group of students brought 31 apples, cut into 6 pieces each, and 29 guavas cut into 4 pieces each to be distributed among the displaced in the camp. When the children were provided with 3 pieces of apple each and the adults with 2 pieces each, and the children were provided with 2 pieces of guava each and the adults with 1 piece each, only 2 pieces of guava were left over. Find the number of children and the number of adults among the displaced in this camp and hence find the total amount of money the government needs to give for a week to the displaced in this camp.
5. The length of the hypotenuse of a right angled triangle is 1 cm less than twice the length of its shortest side.
- If the length of the shortest side is x cm, express the length of the hypotenuse in terms of x .
 - If the remaining side is 3 cm more than the length of the shortest side, using Pythagoras' theorem, write down a relationship between the squares of the lengths of the sides of the triangle.
 - Show that by simplifying the above relationship the equation $x^2 - 5x = 4$ is obtained.
 - Find the length of the hypotenuse by solving the above equation using the method of completing the square or by using the formula. (Take $\sqrt{41} = 6.4$)
6. Starting from the location A, Kamal travels 12 metres to the North and arrives at the location B as shown in the figure. From B he travels 20 metres on a bearing of 040° and arrives at the location C, and from C he travels 25 metres to the East to reach the location D.
-
- Copy the above figure, and mark the given information in it.
 - Find the distance CE to the nearest metre using the trigonometric tables.
 - The distance BE rounded off to the nearest metre is 15 m. Accordingly, calculate \hat{EAD} and the distance AD.

Part B

Answer only five questions.

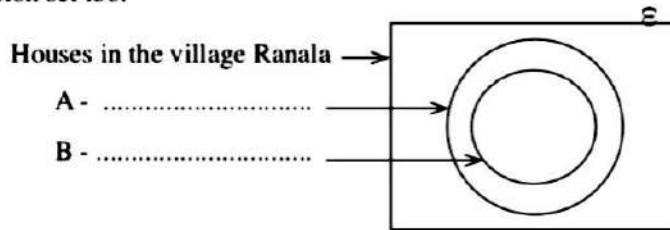
7. A competitor participating in the programme "Wasanavanthaya" organized by a certain television channel, wins by answering 15 questions correctly. The prize money of Rs. 50 for the first question, Rs. 75 for the second question, Rs. 100 for the third question etc., given for the correct answers, are in an arithmetic progression.
- Find the prize money allocated for the 12th question.
 - If Rs. 425 has been allocated as prize money for 2 consecutive questions, which 2 questions are they?
 - A competitor has to leave the program if a wrong answer is given. In this case, the competitor's prize money is half the amount allocated for all the questions he has answered correctly thus far. If a certain competitor had to leave the competition with Rs. 1300 due to not giving the correct answer to a certain question, show that the number of questions he answered is 14.
8. Using only a straight edge with a cm/mm scale and showing the construction lines clearly, do the following constructions.
- Construct a straight line segment PQ of length 8 cm.
 - Mark the point R such that $\hat{QPR} = 45^\circ$ and $PR = QR$, and complete the triangle PQR .
 - Construct the circle that passes through the points P , Q and R and name its centre O .
 - Mark the point S on PR produced such that $PR = RS$.
 - Mark the point T on the circle such that $SQ = ST$ and show that SQ and ST are two tangents to the circle.

9.

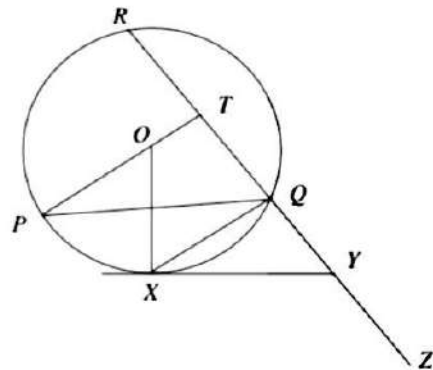


The above figure shows a solid metal right prism with a right triangular cross section, and a solid right circular cone. Their measurements have been given in the figure in the same units. The solid cone with base radius $2r$ and height h is made with the metal that is obtained by melting the prism, such that there is no waste. Show that when the height of the cone is 15 cm, $r^2 = \frac{6a^3}{5\pi}$. By taking $\pi = 3.14$ and using the logarithms table, find the value of r^2 when $a = 4.55$ cm, and hence find the radius of the cone.

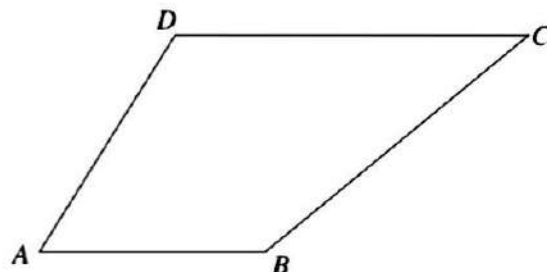
10. There are 120 houses in the village Ranala. 113 of these houses have television sets. Of the houses which have television sets, 78 do not have radios. Every house that has a radio has a television set too.



- Identify the sets A and B and complete the Venn diagram using the given information.
 - How many houses have both a television set and a radio?
 - What is the probability of a house picked at random from the houses in the village Ranala being one which does not have a radio?
 - None of the houses in the village Ranala have computers. A private institution decides to provide computers to 25 selected houses in this village. If they select 4 houses which do not have television sets and 9 houses which have radios to be among the houses which receive the computers, draw the Venn diagram again to represent this information, taking C to be the set of houses which are provided with computers.
 - Now, shade the region in the Venn diagram which denotes the set of houses which do not have radios but have television sets and computers.
11. PQ and QR are two chords of the circle with centre O shown in the figure. PO produced bisects RQ at T . The tangent drawn to the circle at X is XY . The chord RQ has been produced to Z and $\angle POX = 40^\circ$.
- Giving reasons, write the magnitude of $\angle PQX$.
 - Show that $OTYX$ is a cyclic quadrilateral.
 - Find the magnitude of $\angle XYZ$.
 - Name a diameter of the circle passing through the points O , T , Y and X , and write the theorem which is the reason for it.




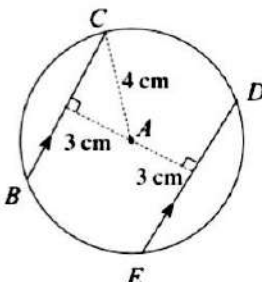
12. In the quadrilateral $ABCD$ shown in the figure, the points E and F lie on the side CD such that $CE = EF = FD$. AF and BE produced meet at G such that $AF = FG$ and $BE = EG$. Sketch a figure with this information marked in it. Show that $BCGF$ and $ABCF$ are parallelograms and that they are equal in area.



* * *

G.C.E. (O.L.) Support Seminar – 2016
Mathematics I (Part A)
Answer Guide

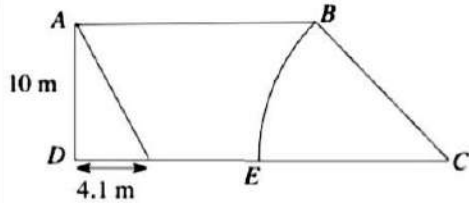


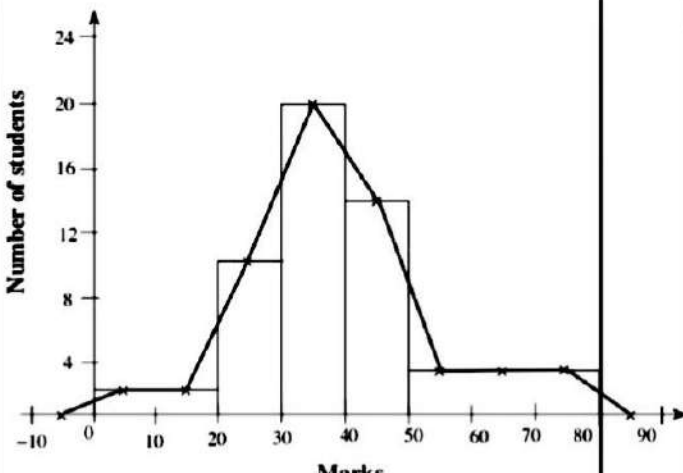
Question Number			Answer	Marks			Other facts
1.			$8^2 = 64$		(2)		
2.			$x = 50^\circ$ $x + 90^\circ + 40^\circ = 180^\circ$ or $x + 40^\circ = 90^\circ$	1	(2)		
3.			Rs. 64 800 Rs. $540\,000 \times \frac{2}{100} \times 6$	1	(2)		
4.			$(x+4)(x+1)$ $x^2 + 4x + x + 4$	1	(2)		
5.			The two equal sides are WY and YZ. $\hat{YWZ} = 20^\circ$	1	(2)		
6.			$L' \cap M$		(2)		
7.			60°		(2)		
8.			40 $\frac{1}{5} = \frac{8}{n(S)}$	1	(2)		
9.			$Q_3 - Q_1 = 6$ $Q_1 = 3, \quad Q_3 = 9$	1	(2)		
10.			ΔPTS and ΔQTR Condition - A.A.S.	1 1	(2)		
11.			$x^2(x+1)$		(2)		
12.			$r = 7 \text{ cm}$ $2 \times \frac{22}{7} \times r = 44$	1	(2)		
13.			$x+y = 90^\circ$ $2x+2y = 180^\circ$	1	(2)		By considering the angle in a semicircle and taking 90°
14.			$\frac{2}{3x}$ $\frac{3}{3x} - \frac{1}{3x}$	1	(2)		

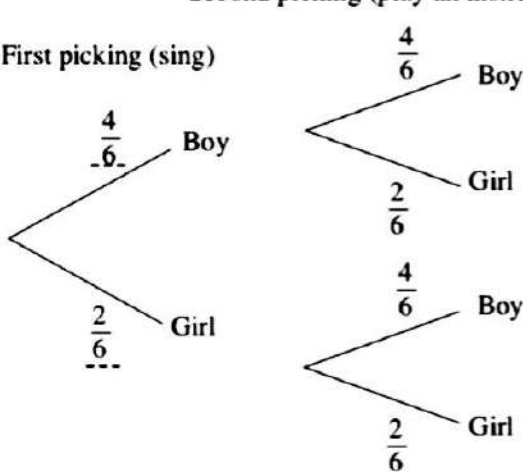
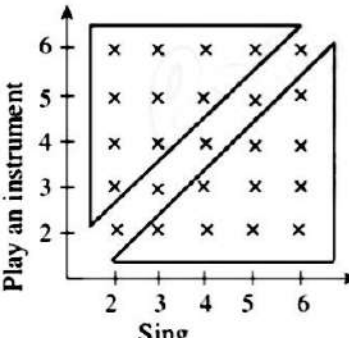
Question Number	Answer	Marks	Other facts
15.	9	(2)	
16.	$\hat{ADB} = 40^\circ$ $\hat{OAD} = 40^\circ$ or $\hat{ACB} = 40^\circ$	1 (2)	
17.	$B = \begin{pmatrix} -5 & 4 \\ 2 & 1 \end{pmatrix}_{2 \times 2}$ $\begin{pmatrix} 6 & -4 \\ -2 & 0 \end{pmatrix}_{2 \times 2} + B = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}_{2 \times 2}$	1 (2)	
18.	$y = 70^\circ$ Observing that $DE \parallel CB$. (Midpoint theorem)	1 (2)	
19.	$y = -x + 3$ $m = -1$ or $c = 3$	1 (2)	
20.	$x = 120^\circ$ $x + 60^\circ = 180^\circ$ (opposite angles of a cyclic quadrilateral are supplementary)	1 (2)	
21.		(2)	
22.	$r = 2$ $24 = 3 \times r^{4-1}$	1 (2)	
23.	9 Number of man days needed for the task = $8 \times 9 = 72$	1 (2)	
24.	 <p>Drawing the line parallel to BC and marking 3cm from A } Marking the points D and E</p>	1 (2)	Marking 6 cm from BC to DE
25.	60 km h^{-1} $\frac{360 \text{ km}}{6 \text{ h}}$ or $\frac{240 \text{ km}}{4 \text{ h}}$ or $\frac{120 \text{ km}}{2 \text{ h}}$	1 (2)	

Mathematics I (Part B)
Answer Guide

Question Number		Answer	Marks				Other facts
1.	(i)	$\frac{1}{8} + \frac{2}{3}$ $= \frac{19}{24}$	1				
			1	(2)			
	(ii)	Remaining letters as a fraction $= \frac{5}{24}$	1				
		Express letters as a fraction $= \frac{5}{24} \times \frac{1}{5}$	1				
		$= \frac{1}{24}$	1	(3)			
	(iii)	Foreign letters as a fraction $= \frac{4}{24}$					
		$\frac{4}{24}$ of the letters $= 520$	1				
		Total number of letters $= \frac{520}{4} \times 24$					
		$= 3120$	1				
		Registered letters $= 3120 \times \frac{1}{8}$					
		$= 390$	1	(3)			
	(iv)	Ordinary letters: Express letters $= \frac{2}{3} : \frac{1}{24}$	1				
		$= 16 : 1$	1	(2)			
						10	The answer can be obtained by finding the number of letters as well
2.	(i)	Length of BE $= \frac{1}{8} \times 2\pi r$					
		$= \frac{1}{8} \times 2 \times \frac{22}{7} \times 14$	1				
		$= 11 \text{ m}$	1				
		Perimeter of $ABED$ $= (11 + 15 + 10 + 11) \text{ m}$					
		$= 47 \text{ m}$	1	(3)			
	(ii)	Area of the section where sand is spread $= \frac{1}{8} \pi r^2$					
		$= \frac{1}{8} \times \frac{22}{7} \times 14 \times 14$	1				
		$= 77 \text{ m}^2$	1	(2)			
	(iii)	Area of the section without sand $= \frac{(25 + 15)}{2} \times 10 - 77$	2				
		$= 200 - 77$					
		$= 123 \text{ m}^2$	1	(3)			

[See page 4

Question Number		Answer	Marks				Other facts				
	(iv)	 <p>Drawing the triangle Marking 4.1 m</p>	1 1	(2)		10					
3.	(a)	(i) Rates for a year = 1500×4 = Rs. 6000 Annual rates percentage = $\frac{6000}{75000} \times 100\%$ = 8%	1 1 1	 (3)							
		(ii) Discount = $6000 \times \frac{10}{100}$ Amount saved = Rs. 600	1 1	 (2)							
	(b)	(i) Number of shares = $\frac{270000}{9}$ = 30 000 Income = Rs. 30 000 \times 2 = Rs. 60 000	1 1 1	 (2)							
		(ii) Gain per share = Rs. 1.50 Capital gain = Rs. 1.50 \times 30 000 = Rs. 45 000	1 1 1	 (3)		10	$(30\,000 \times 10.50) - 270\,000$ $= 315\,000 - 270\,000$ $= 45\,000$				
4.	(i)	<table border="1" data-bbox="323 1184 588 1263"><tr><td>40 - 50</td><td>14</td></tr><tr><td>50 - 80</td><td>12</td></tr></table>	40 - 50	14	50 - 80	12	1 1	(2)			
40 - 50	14										
50 - 80	12										
	(ii)	 <p>Completing the histogram Marking the endpoints of the frequency polygon Marking the midpoints Completing the frequency polygon</p>	2 1 1 1	(2) (3)							
	(iv)	Percentage = $\frac{12}{60} \times 100\%$ = 20%	2 1	 (3)		10					

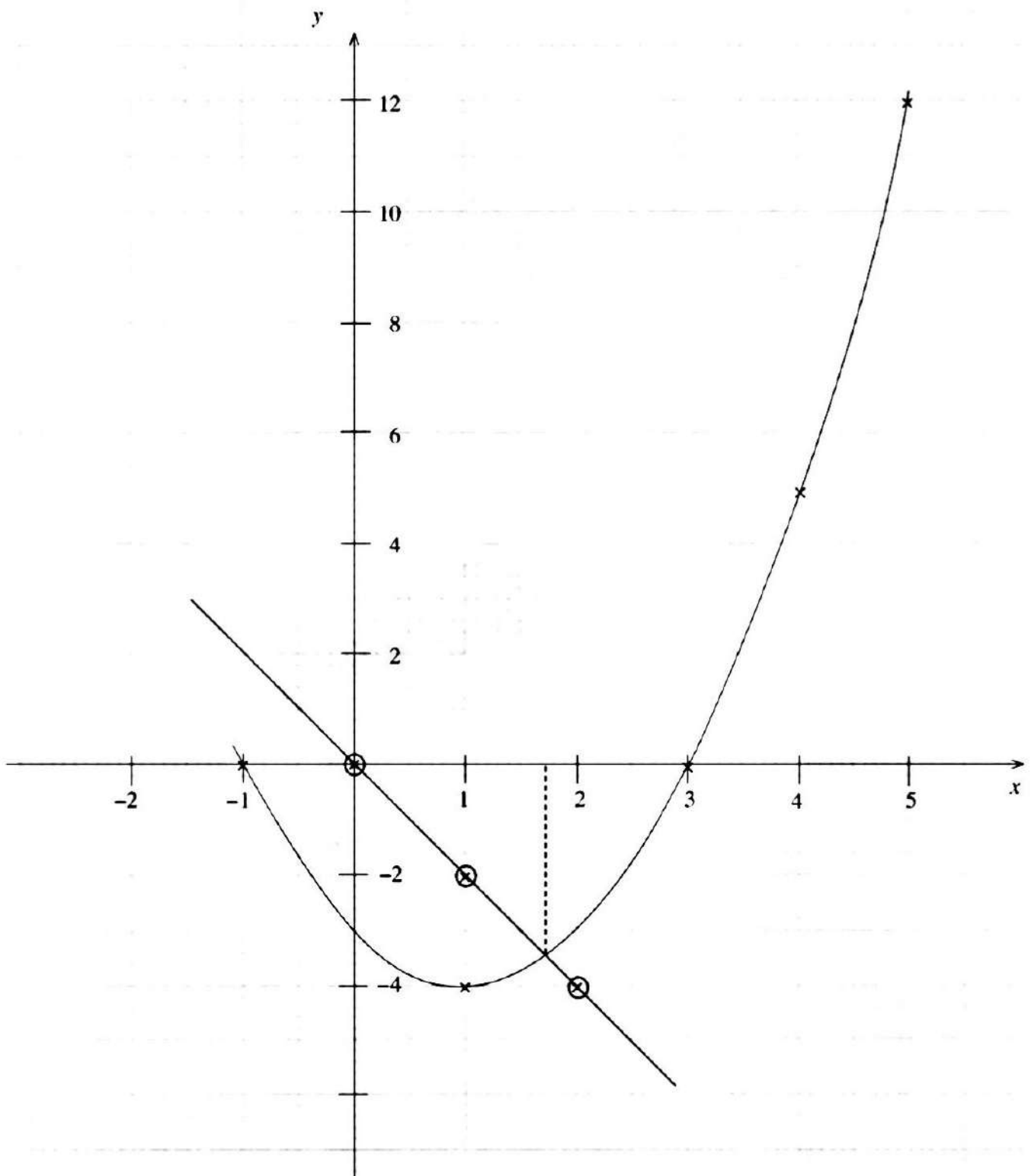
Question Number			Answer		Marks		Other facts
5.	(a)	(i)	<p>Second picking (play an instrument)</p> <p>First picking (sing)</p> 	2	(2)		For $\frac{4}{6}$ and $\frac{2}{6}$
		(ii)	<p>Extending the tree diagram</p> <p>Probability of a boy performing on one occasion and a girl performing on the other occasion. } $= \frac{4}{6} \times \frac{2}{6} + \frac{2}{6} \times \frac{4}{6}$</p> <p>$= \frac{16}{36}$</p>	1	1 + 1		
	(b)	(i)	 <p>Representing on the grid</p>	1	(4)	6	
		(ii)	<p>Marking the event on the grid</p> <p>Probability = $\frac{20}{25}$ or $\frac{4}{5}$</p>	1	(1)		
				2	(3)	4	10

Answer Guide

[illegible]

[See page 2

2. (a) (ii)



[See page 3

Question Number		Answer	Marks				Other facts																																				
3.	(i)	2	1	①																																							
	(ii)	<table><thead><tr><th>Class interval</th><th>Mid value (x)</th><th>Frequency (f)</th><th>fx</th></tr></thead><tbody><tr><td>4 – 8</td><td>6</td><td>2</td><td>12</td></tr><tr><td>9 – 13</td><td>11</td><td>3</td><td>33</td></tr><tr><td>14 – 18</td><td>16</td><td>5</td><td>80</td></tr><tr><td>19 – 23</td><td>21</td><td>8</td><td>168</td></tr><tr><td>24– 28</td><td>26</td><td>15</td><td>390</td></tr><tr><td>29 – 33</td><td>31</td><td>5</td><td>155</td></tr><tr><td>34 – 38</td><td>36</td><td>2</td><td>72</td></tr><tr><td></td><td></td><td>$\Sigma f = 40$</td><td>$\Sigma fx = 910$</td></tr></tbody></table>	Class interval	Mid value (x)	Frequency (f)	fx	4 – 8	6	2	12	9 – 13	11	3	33	14 – 18	16	5	80	19 – 23	21	8	168	24– 28	26	15	390	29 – 33	31	5	155	34 – 38	36	2	72			$\Sigma f = 40$	$\Sigma fx = 910$					
		Class interval	Mid value (x)	Frequency (f)	fx																																						
		4 – 8	6	2	12																																						
		9 – 13	11	3	33																																						
		14 – 18	16	5	80																																						
		19 – 23	21	8	168																																						
		24– 28	26	15	390																																						
		29 – 33	31	5	155																																						
		34 – 38	36	2	72																																						
				$\Sigma f = 40$	$\Sigma fx = 910$																																						
	For the mid value column	1																																									
For the fx column	1																																										
$\Sigma fx = 910$	1																																										
Mean number of trips = $\frac{910}{40}$	1																																										
$= 22.75$																																											
$= 23$ (to the nearest whole number)	1	⑤																																									
(iii)	Cost of the soil = Rs. $23 \times 4 \times 2000$																																										
	= Rs. 184 000	1	①																																								
(iv)	Expected cost for 2 days = Rs. $184\,000 \times 2 \times 40$																																										
	= Rs. 14 720 000	1																																									
	Since $14\,000\,000 < 14\,720\,000$, the engineer's statement could be true.	1	③		10																																						
4.		Number of children = x or any other unknown term																																									
		Number of adults = y or any other unknown term																																									
		$3x + 2y = 186$ _____ ①	1																																								
		$2x + y = 114$ _____ ②	1																																								
		② $\times 2$ $4x + 2y = 228$ _____ ③	1																																								
		③ - ① $x = 42$	1																																								
		By substituting $x = 42$ in ②																																									
		$2 \times 42 + y = 114$	1																																								
		$y = 114 - 84$																																									
		$y = 30$	1																																								

For the fd column - 1

Σfd - 1

$A + \frac{\Sigma fd}{40}$ - 1

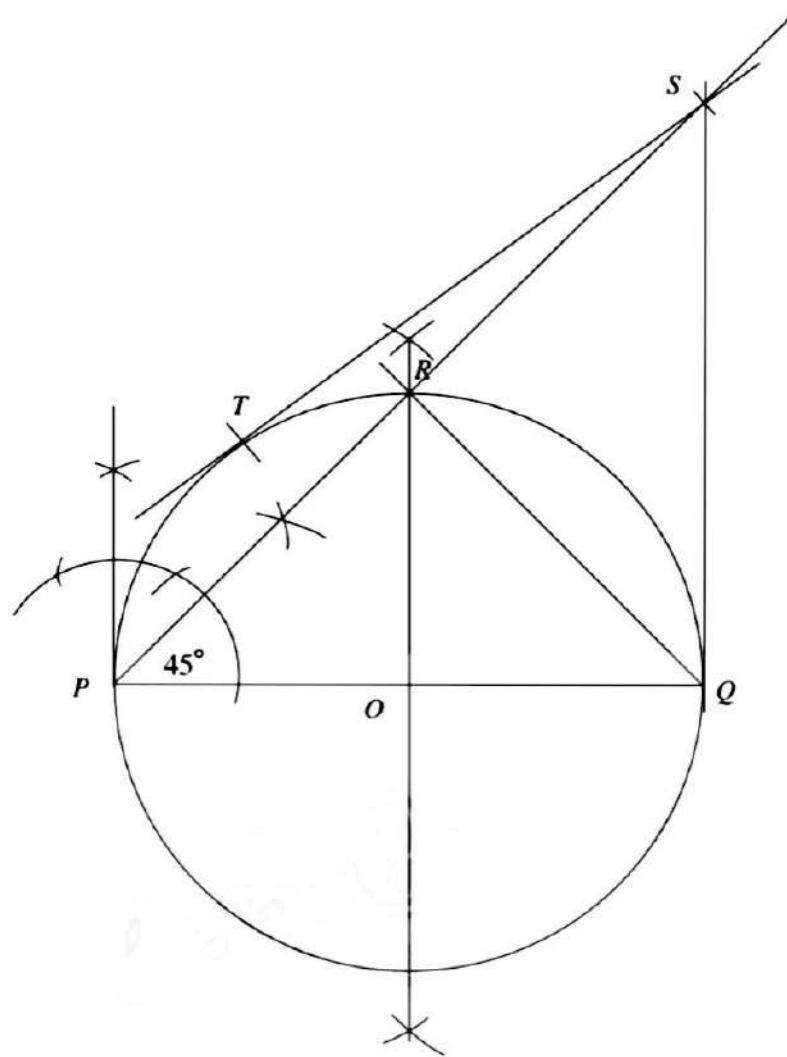
Question Number		Answer	Marks				Other facts
	(iii)	$\tan \hat{EAD} = \frac{13 + 25}{12 + 15}$					
		$= \frac{38}{27}$	1				
		$= 1.4074$	1				
		$\hat{EAD} = 54^\circ 36'$	1				
		$\sin 54^\circ 36' = \frac{38}{AD}$	1				
		$0.8151 = \frac{38}{AD}$	1				
		$AD = 46.62 \text{ m}$	1	6		10	

Part B

Question Number		Answer	Marks				Other facts
7.	(i)	$T_n = a + (n - 1) d$					
		$a = 50, d = 25, n = 12$					
		$T_{12} = 50 + (12 - 1) \times 25$	1				
		$= 50 + 275$	1	2			
		$= \text{Rs. } 325$					
	(ii)	$T_n + T_{n+1} = 425$					
		$a + (n - 1) d + a + nd = 425$	1				
		$2a + 2nd - d = 425$					
		$2 \times 50 + 2n \times 25 - 25 = 425$	1				
		$50n = 350$					
	(iii)	$n = 7$	1				
		Question numbers 7 and 8	1	4			
		$S_n = \frac{n}{2} \{2a + (n - 1) d\}$					
		$1300 \times 2 = \frac{n}{2} \{2 \times 50 + (n - 1) 25\}$	1				
		$5200 = n (75 + 25n)$					
	(iv)	$208 = n^2 + 3n$					
		$n^2 + 3n - 208 = 0$	1				
		$(n + 16)(n - 13) = 0$					
		$n = -16 / n = 13$	1				
		\therefore Number of questions $13 + 1 = 14$	1	4		10	

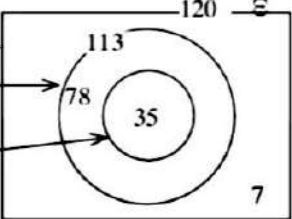
[See page 6

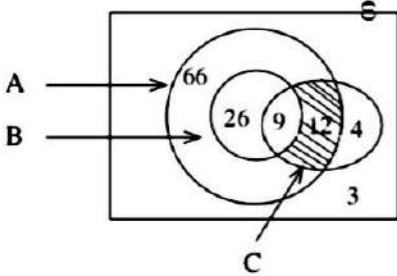
8.

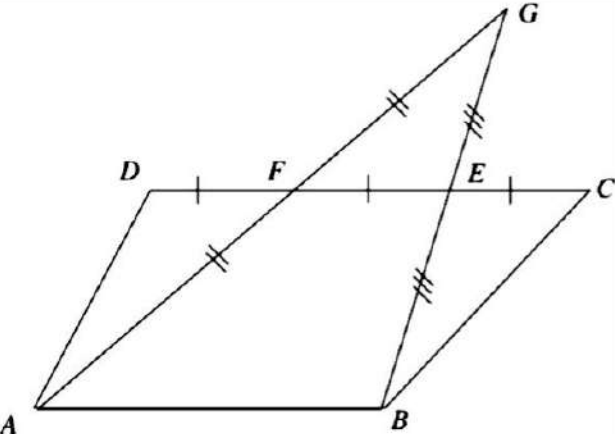


Question Number		Answer	Marks			Other facts
8.	(i)	Constructing $PQ = 8 \text{ cm}$	1	①		
	(ii)	Constructing $\angle QPR = 45^\circ$.	1			
		Constructing the perpendicular bisector of PQ .	1			
		Marking R	1	③		
	(iii)	Marking the centre	1			
		Constructing the circle	1	②		
	(iv)	Obtaining S	1	①		
	(v)	Obtaining T	1			
		Since $\angle PRQ = 90^\circ$, $\angle QRS = 90^\circ$. \therefore Since				
		$PR = RS = RQ$, $\angle PQR = \angle RQS = 45^\circ$. $\therefore \angle OQS = 90^\circ$				
		and hence QS is a tangent.	1			
		Since $QS = ST$, ST is also a tangent.	1	③		10

[See page 7

Question Number	Answer	Marks				Other facts
9.	<p>Volume of the prism = $\frac{1}{2} \times 2a \times 3a \times 8a$</p> <p>Volume of the cone = $\frac{1}{3} \times \pi(2r)^2 \times h$</p> <p>$\frac{1}{2} \times 2a \times 3a \times 8a = \frac{1}{3} \times \pi \times 4r^2 \times 15$</p> <p>$\frac{4}{3} \pi r^2 \times 15 = 24a^3$</p> <p>$20\pi r^2 = 24a^3$</p> <p>$r^2 = \frac{24a^3}{20\pi}$</p> <p>$r^2 = \frac{6a^3}{5\pi}$</p> <p>$\lg r^2 = \lg 6 + 3 \lg 4.55 - (\lg 5 + \lg 3.14)$</p> <p>$= 0.7782 + 3 \times 0.6580 - (0.6990 + 0.4969)$</p> <p>$= 0.7782 + 1.9740 - 1.1959$</p> <p>$\lg r^2 = 1.5563$</p> <p>$r^2 = \text{antilog } 1.5563$</p> <p>$r^2 = 36.0$</p> <p>$r = 6 \text{ cm}$</p> <p>Radius of the cone = 2×6</p> <p>$= 12 \text{ cm}$</p>	1	1	1	1	<p>1 mark for 2 logarithms</p> <p>10</p>
10.	<p>(i)</p> <p>Houses in the village Ranala →</p> <p>A – Houses with television sets →</p> <p>B – Houses with radios →</p>  <p>Naming A and B</p> <p>Marking 78 and 35</p> <p>(ii) 35</p> <p>(iii) $\frac{85}{120}$</p>	1	1 + 1	3	1	1

Question Number		Answer	Marks				Other facts
	(iv)	 <p>Drawing C Obtaining 9, 12, 4, 66, 26 and 3 (1 mark for each pair of correct values)</p>	1 3	(4)			
	(v)	Shading	1	(1)		10	
11.	(i)	$\hat{PQX} = 20^\circ$ The angle subtended by an arc at the centre of a circle is twice the angle subtended on the circumference.	1 1	(2)			
	(ii)	$RT = TQ$ Since the straight line joining the centre of a circle to the midpoint of a chord is perpendicular to the chord, $\hat{OTQ} = 90^\circ$ Since a tangent is perpendicular to the radius at the point of contact, $\hat{OXY} = 90^\circ$ $\hat{OTQ} + \hat{OXY} = 180^\circ$ $OTYX$ is a cyclic quadrilateral since a pair of opposite angles is supplementary.	1 1 1	(4)			
	(iii)	$\hat{XOT} = 140^\circ$ (the angles on a straight line are supplementary) $\hat{XYZ} = 140^\circ$ (the exterior angle of a cyclic quadrilateral is equal to the interior opposite angle)	1 1	(2)			
	(iv)	Diameter is OY . $\therefore \hat{OTY} = 90^\circ$ (the angle in a semicircle is 90°)	1 1	(2)		10	

Question Number		Answer	Marks	Other facts
12.	(i)	 <p>For drawing the figure</p>	<div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div>	
	(ii)	<p>$CE = EF$ (data)</p> <p>$BE = EG$ (data)</p> <p>\therefore Quadrilateral $BCGF$ is a parallelogram since its diagonals bisect each other.</p> <p>$AF = FG$ (data)</p> <p>$BE = EG$ (data)</p> <p>According to the midpoint theorem,</p> <p>$FE \parallel AB$</p> <p>$\therefore AB \parallel FC$</p> <p>$BC \parallel FG$ (opposite sides of a parallelogram)</p> <p>$\therefore BC \parallel AF$</p> <p>$\therefore$ Quadrilateral $ABCF$ is a parallelogram since pairs of opposite sides are parallel.</p> <p>$BC \parallel AG$</p> <p>Since parallelograms on the same base (base BC) and between the same pair of parallel lines ($BC \parallel AG$) are equal in area, $BCGF$ and $ABCF$ are of equal area.</p>	<div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div> <div>1</div>	<div>10</div>