



$$\begin{aligned}
 \text{green} &= \{ (x', x_n) \text{ s.d. } |x' - q'| > R+1 \} \\
 \text{red} &= \{ (x', x_n) \text{ s.d. } |x'| < R, |x_n - q_n| > 2\mu \} \leftarrow \text{leave this for negative term} \\
 \text{orange} &= \{ (x', x_n) \text{ s.d. } |x'| \geq R, |x' - q'| \leq R+1, |x_n - q_n| > \Delta\mu \} \leftarrow \text{instead of } 2\mu \\
 \text{blue} &\subseteq S := \{ (x', x_n) \text{ s.d. } |x' - q'| \leq R+1, |x_n - q_n| \leq \Delta\mu \} \quad \Delta \geq 4 \\
 &\quad \uparrow \text{ enough since pos estimate from above}
 \end{aligned}$$

These changes give us: 3  $\int_{\text{orange}} \frac{\chi_{E^c} - \chi_E}{|y - q|^{n+s}} \leq c(n, s) (R-1 + \Delta\mu)^{-s} \leq c(n, s) (\Delta\mu)^{-s}$  instead of  $(R-1 + \mu)^{-s}$

$$\begin{aligned}
 S &\subset B_{R+2} \text{ for } R \geq 1 \text{ since} \\
 ((\Delta\mu)^2 + (R+1)^2)^{1/2} &\leq (R^2 + 2R + 2)^{1/2} \leq (R^2 + 4R + 4)^{1/2} \\
 \uparrow \Delta\mu \leq 1 &= R+2
 \end{aligned}$$

4 iv)

$$\int_{S \setminus B_{\Delta\mu}} \frac{\chi_{E^c} - \chi_E}{|y - q|^{n+s}} \leq \int_{B_{R+2} \setminus B_{\Delta\mu}} \frac{1}{|y|^{n+s}} = c(n, s) ((\Delta\mu)^{-s} - (R+2)^{-s})$$

Thus in total:

$$\begin{aligned}
 \int_{\mathbb{R}^n} \frac{\chi_{E^c} - \chi_E}{|y - q|^{n+s}} &\leq \overset{2.}{-c_1 \mu^{-s}} + \overset{1.}{c_0 (R^{-(1+s)})} + \overset{3.}{(\Delta\mu)^{-s}} + \overset{4 \text{ iv)}}{(\Delta\mu)^{-s} - (R+2)^{-s}} + \overset{4 \text{ iii)}}{\Delta^{1-s} \mu^{1-s}} \\
 &\leq -c_1 \mu^{-s} \left( 1 - \frac{c_0}{c_1} (R^{-(1+s)}) \mu^s + 2\Delta^{-s} - (R+2)^{-s} \mu^s + \Delta^{1-s} \mu \right) \\
 &\leq -c_2 \mu^{-s}
 \end{aligned}$$

Now choose  $\Delta$  large  
and  $\mu$  small enough