

Homework 2

$$a) \lim_{x \rightarrow \infty} x \cdot \cos^2 \frac{x+2}{x} \Rightarrow \infty$$

$$x \cdot \cos^2 \frac{x+2}{x} = x \cdot \cos^2 \left(1 + \frac{2}{x}\right)$$

$$b) \lim_{x \rightarrow 1} \frac{x}{x^2 + 1} = \frac{1}{2}$$

$$c) \lim_{x \rightarrow \infty} \frac{x^2 + 5}{x^3} = \lim_{x \rightarrow \infty} \frac{x^2 \left(1 + \frac{5}{x^2}\right)}{x^3 \left(1 + \frac{1}{x^3}\right)} = \frac{1}{x} = 0$$

$$d) \lim_{x \rightarrow \infty} \frac{(x+2)(2x+1)}{x^2 + 3x + 5} = \lim_{x \rightarrow \infty} \frac{2x^2 + 2x + \frac{1}{2}x + 2}{x^2 + 3x + 5} = 2$$

$$e) \lim_{x \rightarrow 1} \frac{x^2 - 1}{x^3 - 1} = \frac{(x-1)(x+1)}{(x-1)(x^2 + x + 1)} = \lim_{x \rightarrow 1} \frac{x+1}{x^2 + x + 1} = \frac{2}{3}$$