

Objectives: To understand how a graph can be used to solve graph algorithms.

To start the lab: Download and unzip the lab12.zip file from eLearning.

Part A: In IDLE open the `PriorityQueue` class file: `lab12/priorityQueue.py`. The changes to our familiar `BinHeap` class that we discussed in lecture are included:

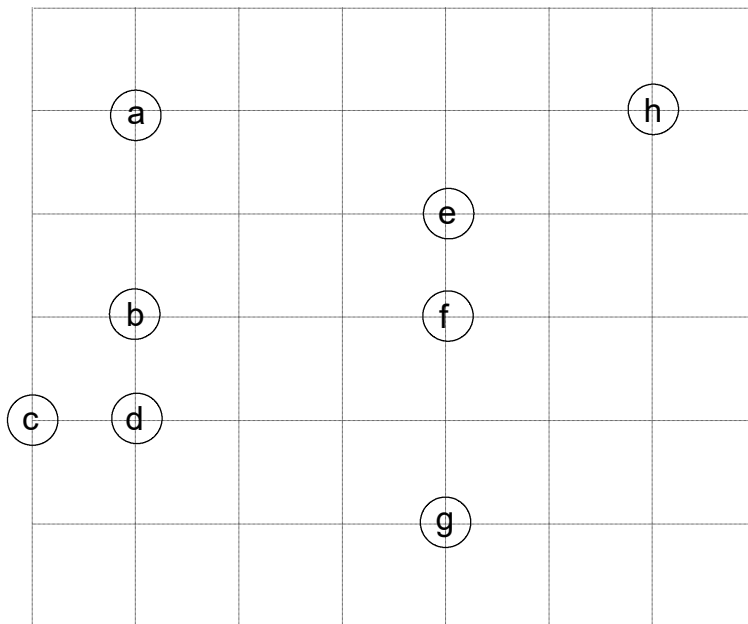
- `self.heapArray` is a list of tuples with the first tuple value (tuple index 0) being the “priority” and second tuple value (tuple index 1) being its associated “key” value.
- a `__contains__` method is added to check if a value is in the priority queue.
- a `decreaseKey` method is added to allow a priority value to be reduced (i.e., increasing its priority).

a) Why do the methods `percDown`, `minChild`, and `percUp` used the tuple index 0 when comparing tuples in the `self.heapArray`?

b) Why do the methods `decreaseKey` and `__contains__` used the tuple index 1 when comparing tuples in the `self.heapArray`?

c) Run the `lab12/make_min_spanning_tree.py` program which uses Prim’s algorithm on the graph from lecture starting at vertex “a”. Does it give the expected output?

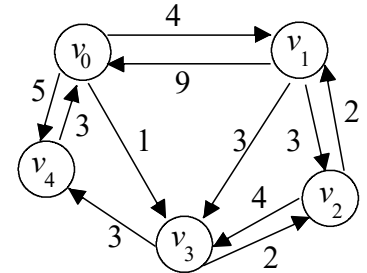
d) Predict the order of edges added by Prim’s algorithm if we start at vertex “e”:



d) Modify the `lab12/make_min_spanning_tree.py` program to verify your prediction. NOTE: This is a very easy modification. You just need to start Prim’s algorithm starting at the vertex labeled “e”.

Part B: The textbook's Dijkstra's Algorithm code (Listing 7.11 p. 341 and same on-line) is in the `lab12/graph_algorithms.py` file.

a) Run the `lab12/test_dijkstra.py` program which uses Dijkstra's algorithm on the graph from lecture. Does it give the expected output?



b) Modify the `dijkstra` function in the `lab12/graph_algorithms.py` file by comparing it to the similar `prim` function. (HINT: Vertex objects are created with a default distance attribute value of 0. Dijkstra's algorithm is missing initialization code similar to Prim's algorithm is `lab12/graph_algorithms.py` file)

After you have fixed the `dijkstra` function in `lab12/graph_algorithms.py`, test your code by running the `lab12/test_dijkstra.py` program.

Part C: In IDLE open the `PriorityQueue` class file: `lab12/Part_C/priorityQueue.py`. This version adds a data attribute `self.keyToIndexDict` dictionary where the keys are all the second tuple values in the `self.heapArray` and their values are their corresponding index locations in `self.heapArray`.

The methods `buildHeap`, `percDown`, `minChild`, and `percUp` have all been modified to correctly update the `self.keyToIndexDict` dictionary.

Your task for Part C is to complete the methods `decreaseKey` and `__contains__` so that they use the `self.keyToIndexDict` dictionary. Thus, greatly improving the efficiency of `decreaseKey` and `__contains__` methods. Test your methods by running the `lab12/Part_C/make_min_spanning_tree.py` program.

After you have answers and correct code for all parts of the lab, submit a `lab12.zip` containing your code on eLearning. If you do not get done today, then submit it by next Wednesday (11/25) at noon.

The EXTRA CREDIT Opportunities related to Part B:

Add code to the end of the `test_dijkstra.py` program to print the shortest paths from `v0` to each of the other vertices. One line of output might look something like:

“Shortest path from `v0` to `v4` is `v0 > v3 > v4` with a total distance of 4”