

# PyPinT

Towards a framework for rapid prototyping of iterative parallel-in-time algorithms

May 28, 2014 | Dieter Moser, Torbjörn Klatt, Dr. Robert Speck <[{d.moser,t.klatt,r.speck}@fz-juelich.de](mailto:{d.moser,t.klatt,r.speck}@fz-juelich.de)> | 3rd Workshop on Parallel-in-Time Integration Methods

# Overview

- 1 Recap of existing Parallel-in-Time Algorithms
- 2 The *PyPinT* Framework Explained
- 3 Goals
- 4 Proof of Concept — Examples Analyzed



# PyPinT

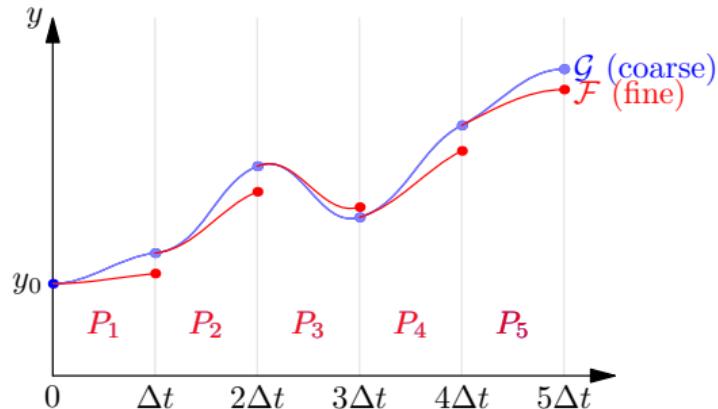
## Part I: Existing Parallel-in-Time Approaches

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# Parareal

## Reference

- coarse  $\mathcal{G}$  and fine  $\mathcal{F}$  propagators make parareal flexible and modular
- an initial value is improved iteratively
- order is controllable through the fine propagator  $\mathcal{F}$



[Courtesy of M. Emmett, LBNL]

$$y_{m+1}^{k+1} = \mathcal{F}(y_m^k) + \mathcal{G}(y_m^{k+1}) - \mathcal{G}(y_m^k)$$

## IDC and DC

$$y'(t) = f(y(t), t), \quad y(0) = y_0$$

Using the residual

$$r(t) = f(t, \tilde{y}(t)) - \tilde{y}(t)$$

to compute the error

$$\begin{aligned} e'(t) &= f(t, \tilde{u} + e) - f(t, \tilde{y}) + r'(t) \\ e(0) &= 0 \end{aligned}$$

for the next update

$$\tilde{y}_{j+1} = \tilde{y}_j + e_j$$

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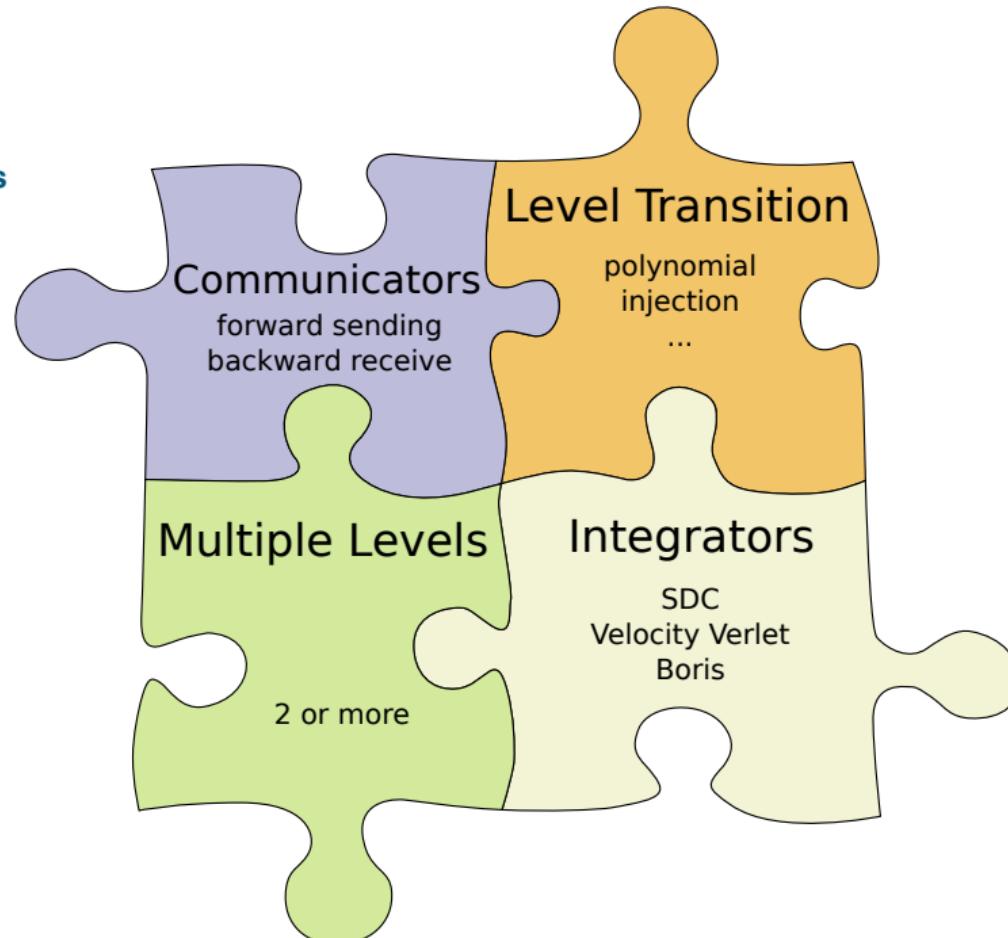
$$\tilde{y}_{j+1} = \tilde{y}_j + e_j$$

# RIDC

# RIDC

# PFASST

## Building Blocks





# PyPinT

## Part II: The PyPinT Framework Explained

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## Basic Concept

- *Python ≥3.2* as language of choice
  - for ease of use and extensibility (cf. *NumPy*, *SciPy*)
- well-conceived and intuitive abstract interfaces
  - for reusable code ensuring DRY principle
- modular building blocks
  - for fast exchange of algorithms' building blocks
- integrated analyzation tools
  - for introspection and plotting (cf. *matplotlib*)
- usage of a sophisticated testing framework
  - nobody writes bug-free code



# Modules

## Abstract Modelling of PinT Algorithms

pypint

- ~.problems
- ~.solvers
- ~.integrators
- ~.communicators
- ~.multi\_level\_providers
- ~.solutions
- ~.plugins

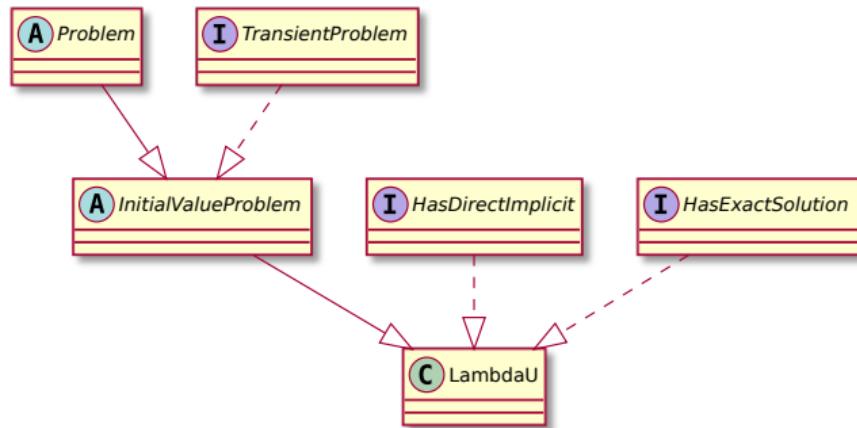


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```

- interfaces for problem setups
- generic problem with specializations via mixins



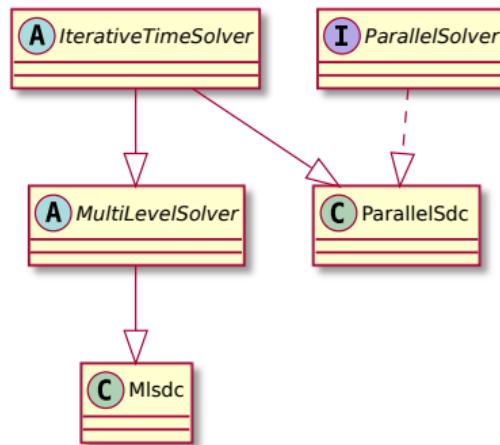
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- interfaces for iterative time solvers
- providing generic building blocks of solvers



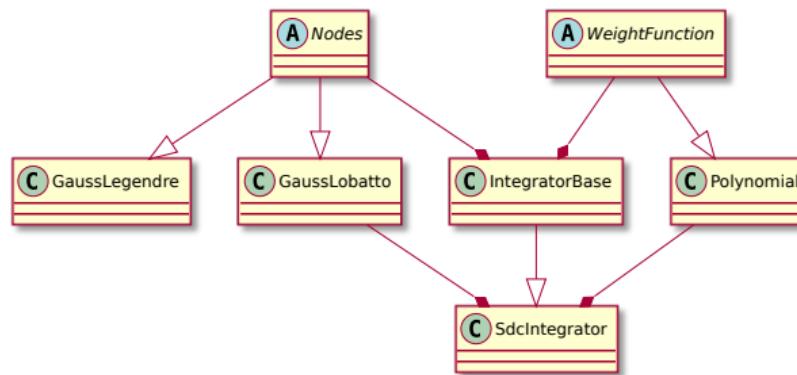
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- providers of various quadrature nodes and weight functions  
e.g. Gauss-Lobatto, Gauss-Legendre, polynomial, etc.
- providers aggregated in integrators  
for intuitive `.integrate(data, from_node=0, to_node='last')` method



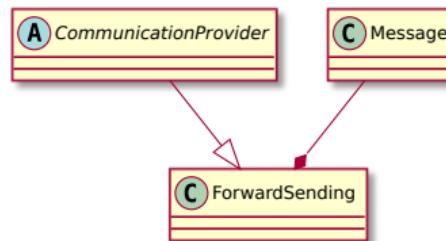
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- generic abstract interfaces for communication patterns e.g. implemented as *forward sending*, etc.
- extendable basic message buffer holding data, solver flags and other meta information



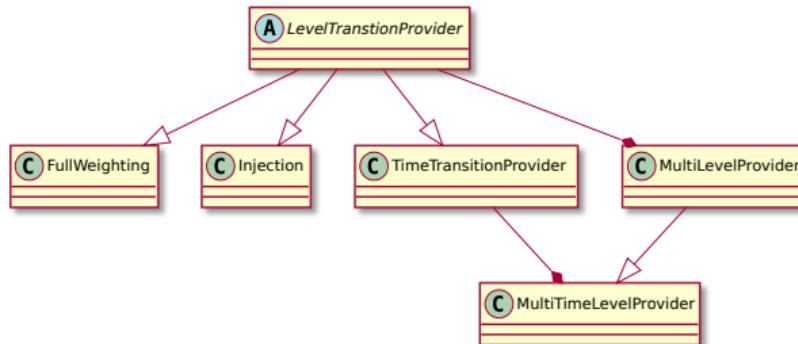
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- abstract interface for generic level transitions  
e.g. *full weighting, injection, Legendre-polynomial integration* etc.
- containers for multiple levels  
providing access to integrators of each level
- unified generic interface for transitions between levels  
via methods `.restringate(data, fine_id, coarse_id)` and  
`.prolongate(data, coarse_id, fine_id)`



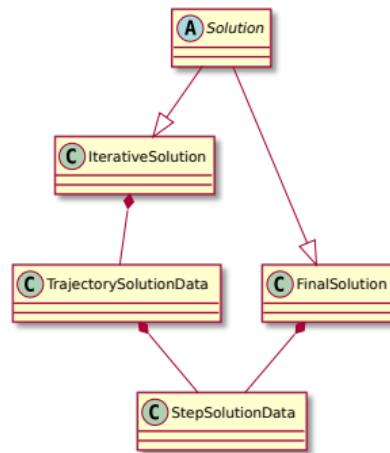
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- containers for solution data + meta information
  - e.g. time-node/step-wise, trajectory (consecutive time nodes)
- container interface for complete solutions
  - e.g. only last time node of last iteration or all nodes of all iterations



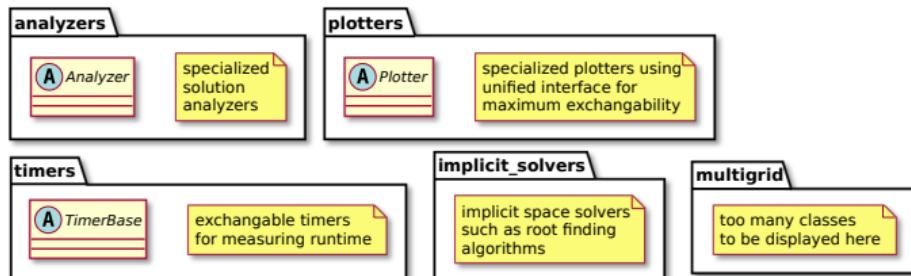
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# PyPinT

## Part III: Goals for PyPinT

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- well-tested and well-documented implementations of PINT algorithms

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⇒ suited for educational use
- open-source hosted on  GitHub  
⇒ reaching young & rising developers and scientists promoting PINT algorithms



# PyPinT

## Part IV: Proof of Concept

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# Implementation of SDC and MLSDC

Stability Regions of  $u'(x, t) = \lambda u(x, t)$ ,  $t \in [0, 1]$

SDC

MLSDC

3 Gauss-Lobatto nodes

3 Gauss-Lobatto nodes

5 Gauss-Lobatto nodes

5 Gauss-Lobatto nodes

# Thank you for your attention!

## Questions?

(now or later)

*PyPinT* is on  GitHub: <https://github.com/Parallel-in-Time/PyPinT>

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