# Module 2.3: Perceptron



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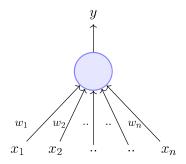
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## The story ahead ...

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- Do we always need to hand code the threshold ?
- Are all inputs equal? What if we want to assign more weight (importance) to some inputs?
- What about functions which are not linearly separable?

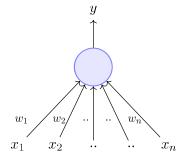


• Frank Rosenblatt, an American psychologist, proposed the classical perceptron model (1958)

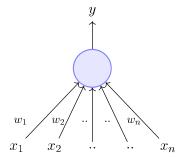


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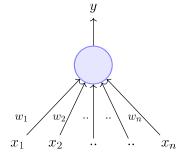


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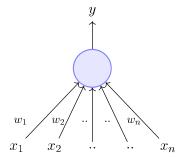


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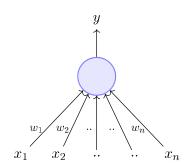


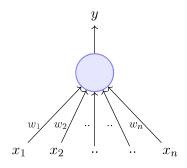
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- Main differences: Introduction of numerical weights for inputs and a mechanism for learning these weights
- Inputs are no longer limited to boolean values
- Refined and carefully analyzed by Minsky and Papert (1969) - their model is referred to as the **perceptron** model here





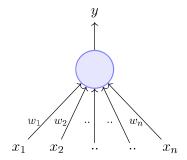


$$y = 1 \quad if \sum_{i=1}^{n} w_i * x_i \ge \theta$$

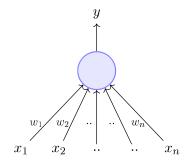


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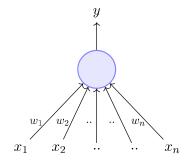
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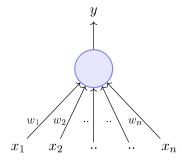
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Rewriting the above,

$$y = 1 \quad if \sum_{i=1}^{n} w_i * x_i - \theta \ge 0$$



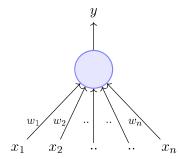
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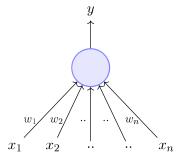


A more accepted convention,

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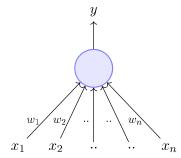
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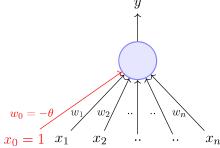
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where,  $x_0 = 1$  and  $w_0 = -\theta$ 



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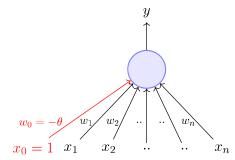
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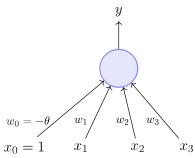
We will now try to answer the following questions:

- Why are we trying to implement boolean functions?
- Why do we need weights?
- Why is  $w_0 = -\theta$  called the bias?

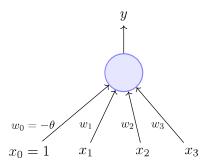


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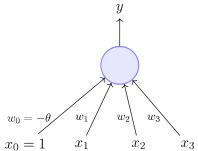


• Consider the task of predicting whether we would like a movie or not

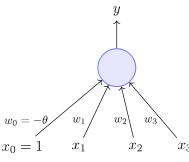


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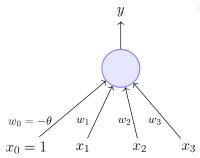


- Consider the task of predicting whether we would like a movie or not
- Suppose, we base our decision on 3 inputs (binary, for simplicity)
- Based on our past viewing experience (**data**), we may give a high weight to *isDirectorNolan* as compared to the other inputs
- $x_3$  Specifically, even if the actor is not *Matt Damon* and the genre is not *thriller* we would still want to cross the threshold  $\theta$  by assigning a high weight to *isDirect-orNolan*



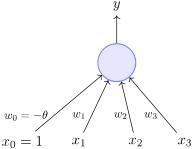
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•  $w_0$  is called the bias as it represents the prior (prejudice)

 $x_1 = isActorDamon$   $x_2 = isGenreThriller$  $x_3 = isDirectorNolan$ 

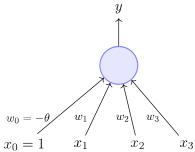


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- A movie buff may have a very low threshold and may watch any movie irrespective of the genre, actor, director  $[\theta=0]$



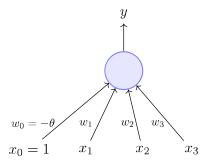
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- The weights  $(w_1, w_2, ..., w_n)$  and the bias  $(w_0)$  will depend on the data (viewer history in this case)



What kind of functions can be implemented using the perceptron? Any difference from McCulloch Pitts neurons?

(assuming no inhibitory inputs)

$$y = 1 \quad if \sum_{i=0}^{n} x_i \ge 0$$
$$= 0 \quad if \sum_{i=0}^{n} x_i < 0$$

#### Perceptron

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# McCulloch Pitts Neuron

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- Then what is the difference? The weights (including threshold) can be learned and the inputs can be real valued
- We will first revisit some boolean functions and then see the perceptron learning algorithm (for learning weights)



$$\begin{array}{c|cc} x_1 & x_2 & \text{OR} \\ \hline 0 & 0 & \end{array}$$

$x_1$	$x_2$	OR	
0	0	0	



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$\overline{x_1}$	$x_2$	OR	
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$

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$\overline{x_1}$	$x_2$	OR	
0	0	0	
1	0	1	$w_0 + \sum_{i=1}^2 w_i x_i \ge 0$

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$\overline{x_1}$	$x_2$	OR	
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^2 w_i x_i < 0$ $w_0 + \sum_{i=1}^2 w_i x_i \ge 0$
0	1	1	

$x_1$	$x_2$		
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
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1	1	1	$w_0 + \sum_{i=1}^{2^{n-1}} w_i x_i \ge 0$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0$$



$x_1$	$x_2$	OR	
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$$\begin{aligned} w_0 + w_1 \cdot 0 + w_2 \cdot 0 &< 0 \implies w_0 < 0 \\ w_0 + w_1 \cdot 0 + w_2 \cdot 1 &\ge 0 \implies w_2 &\ge -w_0 \end{aligned}$$

$\overline{x_1}$	$x_2$	OR	
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
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$$\begin{split} & w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0 \\ & w_0 + w_1 \cdot 0 + w_2 \cdot 1 \ge 0 \implies w_2 \ge -w_0 \\ & w_0 + w_1 \cdot 1 + w_2 \cdot 0 \ge 0 \implies w_1 \ge -w_0 \\ & w_0 + w_1 \cdot 1 + w_2 \cdot 1 \ge 0 \implies w_1 + w_2 \ge -w_0 \end{split}$$

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$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0$$

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$$w_0 + w_1 \cdot 1 + w_2 \cdot 1 \ge 0 \implies w_1 + w_2 \ge -w_0$$

• One possible solution to this set of inequalities is  $w_0 = -1, w_1 = 1.1, w_2 = 1.1$  (and various other solutions are possible)



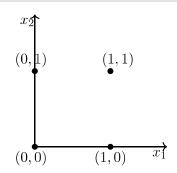
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$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0$$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 1 \ge 0 \implies w_2 \ge -w_0$$

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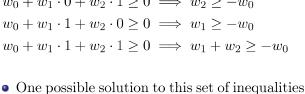
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0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
0	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
1	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$

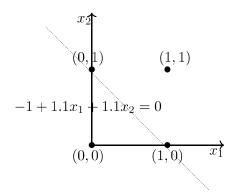
$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0$$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 1 \ge 0 \implies w_2 \ge -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 0 \ge 0 \implies w_1 \ge -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 1 \ge 0 \implies w_1 + w_2 \ge -w_0$$





is  $w_0 = -1, w_1 = 1.1, w_2 = 1.1$  (and various other solutions are possible)

$x_1$	$x_2$	OR	
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
0	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
1	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$

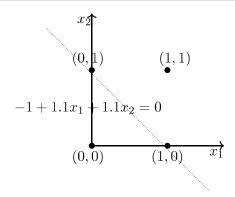
$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \implies w_0 < 0$$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 1 \ge 0 \implies w_2 \ge -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 0 \ge 0 \implies w_1 \ge -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 1 \ge 0 \implies w_1 + w_2 \ge -w_0$$

• One possible solution to this set of inequalities is  $w_0 = -1, w_1 = 1.1, w_2 = 1.1$  (and various other solutions are possible)

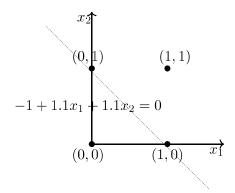


• Note that we can come up with a similar set of inequalities and find the value of  $\theta$ for a McCulloch Pitts neuron also

$\overline{x_1}$	$x_2$	OR	
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
1	0	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
0	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$
1	1	1	$w_0 + \sum_{i=1}^{2} w_i x_i \ge 0$

$$\begin{aligned} & w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 & \Longrightarrow w_0 < 0 \\ & w_0 + w_1 \cdot 0 + w_2 \cdot 1 \ge 0 & \Longrightarrow w_2 \ge -w_0 \\ & w_0 + w_1 \cdot 1 + w_2 \cdot 0 \ge 0 & \Longrightarrow w_1 \ge -w_0 \\ & w_0 + w_1 \cdot 1 + w_2 \cdot 1 \ge 0 & \Longrightarrow w_1 + w_2 \ge -w_0 \end{aligned}$$

• One possible solution to this set of inequalities is  $w_0 = -1, w_1 = 1.1, w_2 = 1.1$  (and various other solutions are possible)



• Note that we can come up with a similar set of inequalities and find the value of  $\theta$  for a McCulloch Pitts neuron also (Try it!)

