

K. J. SOMAIYA COLLEGE OF ENGINEERING

AFFILIATED TO THE UNIVERSITY OF MUMBAI)

(1)

Module

1-3

Candidate Roll No. _____
(In figures)Time Advance:
Algorithm
Test Exam.

Name : _____

Date : _____ 20

Examination : _____ Branch/Semester _____

Subject : _____

Question No.	1	2	3	4	5	6	7	8	9	10	11	12	Total
Marks Obtained													

Junior Supervisor's full
Signature with Date* Manner Simulation using Event-Scheduling.

→ In conducting of an event-scheduling simly. a simly table is used to record the successive system snapshots as time advances.

Single channel queue

→ Reconsider the grocery store with one check-out counter that was simulated by an ad-hoc method. The system consists of those customers in waiting line plus the one (if any) checking out. A stopping time of 60 minutes is set for this example.

Model has following components

System state :- $[L_Q(t), S(t)]$, where $L_Q(t)$ is no of customers in waiting line and $S(t)$ is no being served (0 or 1) at time t.

Entities - The server and customers are not explicitly modelled, except in terms of state variables

Event -

Arrival (A);

Departure (D);

Stopping event (E), scheduled to occur at time t_c

Activities

Interarrival time, given in table.

Service time

Customer time spent in waiting line.

Delay

Interarrival Times :- 1 1 6 3 7 5 2 4 1 ...
Service Times :- 4 2 5 4 1 5 4 1 4 ...

Cumulative Statistics

Simulation Table											
clock	LQ(t)	LS(t)	Future event list		Comment		B	M			
	Waiting	Served									
0	0	1	(A, 1)	(D, 4)	(E, 6)		First: A occurs.	0	0		
							(at = 1) Schedule next: A				
							(st = 4) Schedule first: D.				
1	1	1	(A, 2)	(D, 4)	(E, 6)		Second A occurs, (A, 1)	1	1		
							(at = 1) Schedule next: A,				
							(customer delayed)				
2	2	1	(D, 4)	(A, 8)	(E, 6)		Third, A occurs (A, 2)	2	2		
							(at = 6) Schedule next: A.				
							(Two customers delayed).				
4	1	1	(D, 6)	(A, 8)	(E, 6)		First: D occurs : (D, 4)	4	2		
							(at = 2) Schedule next: D.				
							(customer delayed).				
6	0	1	(A, 8)	(D, 11)	(E, 6)		Second, D occurs ; (D, 6).	6	2		
							(at = 5) Schedule next: D.				
8	1	1	(D, 11)	(A, 11)	(E, 6)		Fourth A occurs (A, 8).	8	2		
							(at = 3) Schedule next: A)				
							(customer delayed).				

<u>11</u>	<u>1</u>	<u>1</u>	<u>(D,15)(A,18)(E,60)</u>	Fifth A occurs (A,11) ($a^* = 7$) Schedule next A. Third D occurs (D,11) ($s^* = 4$) Schedule next D. (customers delayed.)	<u>11</u>	<u>2</u>
<u>15</u>	<u>0</u>	<u>1</u>	<u>(D,16)(A,14)(E,60)</u>	Fourth D occurs (D,15). ($s^* = 1$) Schedule next D.	<u>15</u>	<u>2</u>
<u>16</u>	<u>0</u>	<u>0</u>	<u>(A,18)(E,60)</u>	Fifth D occurs (D,16)	<u>16</u>	<u>2</u>
<u>16</u>	<u>0</u>	<u>1</u>	<u>(D,23)(A,23)(E,60)</u>	Sixth A occurs. ($a^* = 5$) Schedule next A. ($s^* = 5$) Schedule next D.	<u>16</u>	<u>2</u>
<u>23</u>	<u>0</u>	<u>1</u>	<u>(A,25)(D,27)(E,60)</u>	Seventh A occurs (A,23) ($a^* = 2$) Schedule next A. arrival sixth D occurs. (D,23).	<u>21</u>	<u>2</u>

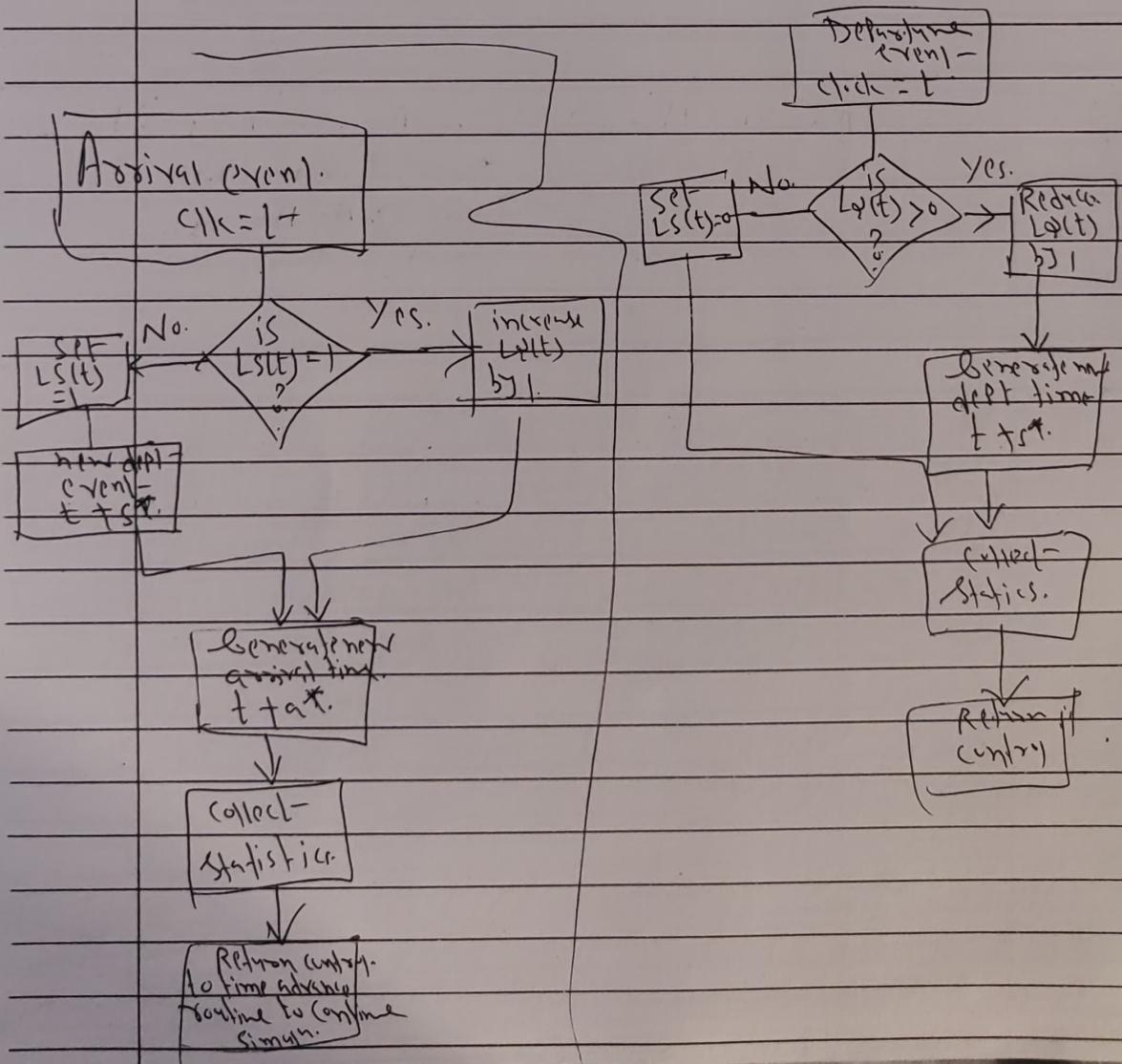
* Initial conditions are that the first customer arrives at time 0 and begin service. This is reflected in table by system snapshot at time zero ($clock = 0$), with $L_Q(0) = 0$, $L_S(0) = 1$ and both the departure event and arrival event on FEL. Also one simu is scheduled to stop at time 60. Only two statistics, server utilization and max queue length, will be collected.

Server utilization is defined by total served busy time (B) divided by total time (T_F). Total busy time B and maximum queue length, M_Q will be accumulated as simulation progresses.

As soon as system snapshot at time clock = 0 is complete, the sim begins. At time 0, one imminent event is $(A, 1)$. The clock is advanced to time 1, and $(A, 1)$ is removed from FEL.

Bcoz $LS(t) = 1$ for $0 \leq t \leq 1$ (i.e Server was busy for 1 minute) the cumulative busy time is increased from $B=0$ to $B=1$.

B_1 event, logic flow chart. Set $LS(t) = 1$ (as server becomes busy). The FEL left with three further events $(A, 2)$, $(B, 4)$ and $(E, 60)$. The sim clock is next advanced to time 2, and arrival event is executed.



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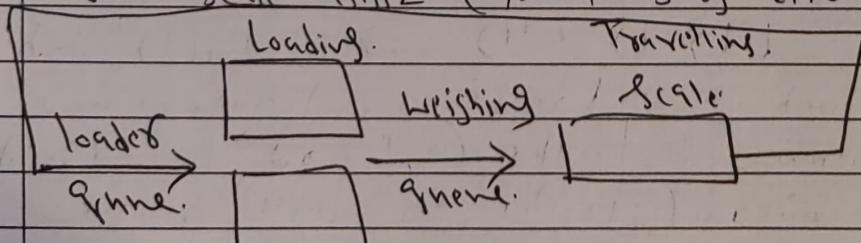
Subject: _____

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The Dump Truck Problem

→ Six dump trucks are used to haul coal from the entrance of a small mine to the railroad. Fig. Provides a schematic of dump truck opern. Each truck is loaded by one of two loaders. After a loading the truck immediately moves to the scale to be weighed as soon as possible. Both the loaders and scale have a first-come-first-served waiting line (queue) for trucks. Travel time from a loader to the scale is considered negligible. After being weighed a truck begins a travel time (during which the truck unloads) and then afterward returns to the loader queue. The distribution of loading time, weighing time and travel time are given in table, together with random digit assignment. For generating three variables by using random digits. The purpose of simm is to estimate the loader and scale utilz (% of busy time).



* Distribution of Loading time for Dump trucks

<u>Loading Time</u>	<u>Probability</u>	<u>Cumulative Probability</u>	<u>Random digit Assignment</u>
5	0.30	0.30	1 - 3
10	0.10	0.80	4 - 8
15	0.20	1.00	9 - 0

* Distribution of Weighing time for Dump trucks

<u>Weighing Time</u>	<u>Probability</u>	<u>Cumulative Probability</u>	<u>Random digit Assignment</u>
12	0.70	0.70	1 - 7
16	0.30	1.00	8 - 0

* Distribution of Travel time for Dump trucks

<u>Travel Time</u>	<u>Probability</u>	<u>Cumulative Probability</u>	<u>Random digit Assignment</u>
40	0.40	0.40	1 - 4
60	0.30	0.70	5 - 7
80	0.20	0.90	8 - 9
100	0.10	1.00	0

System State [$L_q(t)$, $L(t)$, $W_q(t)$, $W(t)$] where.

$L_q(t)$ = number of trucks in loader queue.

$L(t)$ = number of trucks (0, 1, or 2) being loaded.

$W_q(t)$ = number of trucks in weigh queue.

$W(t)$ = number of trucks (0 or 1) being weighed, all at time t .

Event notices :-

(ALQ, t, DTi) dump truck i arrives at loader queue (ALQ) at time t.

(EL, t, DTi) dump truck i ends loading (EL) at time t.

(EW, t, DTi) dump truck i ends weighing (EW) at time t.

Entities :- The six dump trucks (DT1, ---DT6).

Lists:-

Loader queue all trucks waiting to begin loading ordered on first come first served basis.

Weigh queue all trucks waiting to be weighed ordered on first come, first served basis.

Activities Loading time, Weighing time and Travel time.

Delay at loader queue and delay at scale.

* It has been assumed that five of the trucks are at the loaders and one is at the scale at time 0. The activity times are taken from the following list as needed.

Truck	DT1	DT2	DT3	DT4	DT5	DT6
Loading Time	10	5	5	10	15	10
Weighing Time	12	12	12	16	12	16
Travel time	60	100	40	40	80	

When an end loading (EL) event occurs say for truck i at time t other events might be triggered. If the scale is idle ($WLT = 0$), truck i begins weighing and an end weighing event (EW) is scheduled on the FEL.

Otherwise block 3 joins the weigh queue. If at this time there is another block waiting for a loader, it will be removed from loader queue and will begin loading by scheduling of end loading event (EL) on the FEL.

→ Both this logic for occurrence of end loading event and appropriate logic for the other two events should be incorporated into an event diagram.

→ In simulation table, whenever a new event is scheduled, its event time is written as $t + (\text{activity time})$. For e.g., at time 0 imminent event is an EL event. With event time 5. The clock is advanced to time $t = 5$ where block 3 joins the weigh queue (beacause the scale is occupied) and block 4 begins to load. Thus an EL event is scheduled for block 4 at future time 10, computed by (present time) $+ (\text{loading time}) = 5 + 5 = 10$

→ In order to estimate the loader and scale utilization, two cumulative statistics are maintained,

$BL = \text{total busy time of both loaders from time 0 to time } t$

$BS = \text{total busy time of scale from 0 to time } t$

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Question No.	1	2	3	4	5	6	7	8	9	10	11	12	Total
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→ Both loaders are busy from time 0 to 20.
 $B_{BL} = 40$ at time 20, but from time 20 to 24, only one loader is busy, then B_{BL} increases by only 4 minutes over one interval $[20, 24]$. Similarly from time 25 to 36, both loaders are idle. $L(25) = 0$, so B_{BL} does not change.

Formulae

$$\therefore \underline{\text{Avg. Loader Utiliz}} = \frac{49}{2} = \underline{0.32}$$

$$\underline{\text{Avg. Scale Utiliz}} = \frac{76}{76} = \underline{1.00}$$

Simulation Table:-

clock	System state	Lists	FFL	Cumulative Statistics
t	$L(t)$ $W(t)$ $W(t)$	Loader Work queue given.		B_L B_S

0	3	2	0	1	DT4	(EL, 5, DT3)	0	0
					DT5	(EL, 10, DT2)		
					DT6.	(EW, 12, DT1)		

5	2	2	1	1	DT5	DT3	(EL, 10, DT2)	10	5
					DT6		(EL, 5+5, DT4)		

CK

F L(1t) L(t) L(1t) W(1t). loaded wrist FEL BL RS

0 1 2 2 1 - DT₅ DT₃ (EL, 1°, DT₄) 20 10
DT₆ DT₂ (EW, 12, DT₁).
(EL, 10+1°, DT₅)

10 0 2 3 1 - DT₃ (EW, 12, DT₁) 20 10
DT₂ (EL, 2°, DT₅)
DT₄ (EL, 10+15, DT₁)

12 0 2 2 1 - DT₂ (EL, 2°, DT₅) 24 12
DT₄ (EW, 12+12, DT₃)
(EL, 25, DT₆).
(ALφ, 12+6°, DT₁)

20 0 1 3 1 - DT₂ (EW, 24, DT₃) 40 20
DT₄ (EL, 25, DT₆).
DT₅ (ALφ, 72, DT₁)

24 0 1 2 1 - DT₄ (EL, 25, DT₆) 44 24
DT₅ (EW, 24+12, DT₂)
(ALφ, 72, DT₁)
(ALφ, 24+100, DT₃)

25 0 0 3 1 - DT₄ (EW, 36, DT₂) 45 25
DT₅ (ALφ, 72, DT₁)
DT₆ (ALφ, 124, DT₃)

36 0 0 2 1 - DT₅ (EW, 36+16, DT₄) 45 36
DT₆ (ALφ, 72, DT₁)
(ALφ, 36+40, DT₂)
(ALφ, 124, DT₃)

52 0 0 1 1

-

DT6 (EL_L, 52+12, DT5) 45 52

(AL φ , 72, DT1)

(AL φ , 76, DT2)

(AL φ , 52+40, DT4).

(AL φ , 124, DT3).

64 0 0 0 1

-

- (AL φ , 72, DT1) 45 64

(AL φ , 76, DT2)

(EW, 64+16, DT6)

(AL φ , 92, DT4)

(AL φ , 124, DT3).

(AL φ , 64+80, DT5).

72 0 1 0 1

- -

(AL φ , 76, DT2) 45 72

(EW, 52, DT6)

(EL, 72+10, DT1)

(AL φ , 92, DT4)

(AL φ , 124, DT3)

(AL φ , 144, DT5).

76 0 2 0 1

- -

(EW, 80, DT6) 49 76

(EL, 82, DT1).

(EL, 76+10, DT2).

(AL φ , 92, DT4).

(AL φ , 124, DT3)

(AL φ , 144, DT5).