

BCE

$$\hat{E}_{\text{mr}} = - (1-y) \log (1 - D(G(z))) - y (\log (D(x)))$$

$$\min_G \max_D \mathcal{V}(G, D) = E_{z \in p_z} (\log (1 - D(G(z)))) + \\ E_{x \in p_{\text{data}}} (\log (D(x)))$$

$$\Rightarrow p_g \approx p_{\text{data}}$$

$$KL(P \parallel Q) = \sum_x P(x) \log \left(\frac{P(x)}{Q(x)} \right) \\ = \int_{-\infty}^{\infty} p(x) \log \left(\frac{p(x)}{q(x)} \right) dx$$

$$JSD(P \parallel Q) = \frac{1}{2} (KL(P \parallel M) + KL(Q \parallel M))$$

$$\text{Jank } M = \frac{P + Q}{2}$$

$$\Rightarrow p^* = \frac{p_{\text{data}}(x)}{p_{\text{data}}(x) + p_g(x)}$$

$$\mathcal{V}(G, D) = \int_x p_{\text{data}}(x) \log (D(x)) dx + \int_z p_z(z) \log (1 - D(G(z))) dz$$

$$\begin{aligned}
 V(G, D) &= \int_{\mathcal{X}} p_{data}(x) \log(D(x)) dx + \int_{\mathcal{X}} p_g(x) \log(1 - D(x)) dx \\
 &= \int_{\mathcal{X}} (p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x))) dx
 \end{aligned}$$