

Si $E_p \{ |k(x, x)|^{1/2} \} < \infty$; entonces $\mu_p \in \mathcal{F}$.

El operador lineal $T_p f = E_p \{ f(x) \}$; $\forall f \in \mathcal{F}$, es acotado dado que:

$$|T_p f| = |E_p \{ f(x) \}| \leq E_p \{ |f(x)| \} = E_p \{ |\langle f, \varphi(x) \rangle_f| \}$$

↳ Desigualdad de Jensen

$$\Rightarrow E_p \{ |\langle f, \varphi(x) \rangle_f| \} \leq E_p \{ \|f\|_f \|\varphi(x)\|_f \}$$

$$= E_p \{ \sqrt{k(x, x)} \|f\|_f \}$$

$$|T_p f| \leq E_p \{ \sqrt{k(x, x)} \|f\|_f \}$$

Por ende existe un $\mu_p \in \mathcal{F}$ tal que $T_p f = \langle f, \mu_p \rangle_f$

$$\text{Si } f(x) = \varphi(x) = k(x, \cdot):$$

$$\mu_p(x) = \langle \mu_p, k(x, \cdot) \rangle_f = E_p \{ k(x, x') \}$$