# QBS177\_FINAL PROJECT

Data Exploration and Visualization-Parinitha Kompala, PCA-Xing Cheng, Kmenas- Avani Kuthe, Heirac

### 2/25/2022

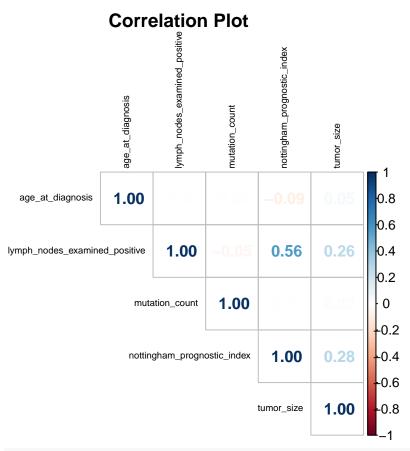
This data set contains 31 clinical attributes, m-RNA levels z-score for 331 genes, and mutation in 175 genes for 1904 breast cancer patients. Here, we just used the clinical variables of the data set. Clinical attributes in the dataset have 31 variables.

```
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5
                     v purrr
                               0.3.4
## v tibble 3.1.6
                     v dplyr
                               1.0.7
## v tidyr
            1.1.4
                     v stringr 1.4.0
## v readr
           2.1.1
                     v forcats 0.5.1
## -- Conflicts ----- tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
RNA_Mutation<-read.csv("/Users/parinithakompala/Desktop/QBS177/METABRIC_RNA_Mutation.csv") #reading the
RNA_Mutation_updated <- RNA_Mutation[ -c(0,521:693) ] #removing all the mutation columns for better anal
#(is.na(RNA_Mutation_updated))#checking for NA
str(RNA_Mutation_updated)
                  1904 obs. of 520 variables:
## 'data.frame':
## $ patient_id
                                 : int 0 2 5 6 8 10 14 22 28 35 ...
## $ age_at_diagnosis
                                  : num 75.7 43.2 48.9 47.7 77 ...
                                 : chr
                                        "MASTECTOMY" "BREAST CONSERVING" "MASTECTOMY" "MASTECTOMY" .
## $ type_of_breast_surgery
## $ cancer_type
                                        "Breast Cancer" "Breast Cancer" "Breast Cancer" "Breast Canc
                                 : chr
## $ cancer_type_detailed
                                        "Breast Invasive Ductal Carcinoma" "Breast Invasive Ductal C
                                        "" "High" "High" "Moderate" ...
## $ cellularity
                                  : chr
   $ chemotherapy
                                 : int
                                        0 0 1 1 1 0 1 0 0 0 ...
## $ pam50_._claudin.low_subtype
                                 : chr
                                        "claudin-low" "LumA" "LumB" "LumB" ...
                                        1 1 1 1 1 1 1 1 1 1 ...
                                  : num
                                        "Positve" "Positve" "Positve" ...
## $ er_status_measured_by_ihc
                                  : chr
   $ er_status
                                        "Positive" "Positive" "Positive" ...
                                  : chr
## $ neoplasm_histologic_grade
                                  : num
                                        3 3 2 2 3 3 2 2 3 2 ...
  $ her2_status_measured_by_snp6 : chr
                                        "NEUTRAL" "NEUTRAL" "NEUTRAL" ...
                                        "Negative" "Negative" "Negative" "Negative" ...
   $ her2_status
                                  : chr
   $ tumor_other_histologic_subtype: chr
                                        "Ductal/NST" "Ductal/NST" "Mixed" ...
##
## $ hormone_therapy
                                        1 1 1 1 1 1 1 1 0 ...
                                 : int
                                        "Post" "Pre" "Pre" "Pre" ...
## $ inferred_menopausal_state
                                  : chr
## $ integrative_cluster
                                  : chr
                                        "4ER+" "4ER+" "3" "9" ...
## $ primary_tumor_laterality
                                 : chr "Right" "Right" "Right" "Right" ...
## $ lymph_nodes_examined_positive : num 10 0 1 3 8 0 1 1 1 0 ...
```

```
## $ mutation count
                                   : num NA 2 2 1 2 4 4 1 4 5 ...
## $ nottingham_prognostic_index : num
                                          6.04 4.02 4.03 4.05 6.08 ...
                                          "IDC" "IDC" "IDC" "MDLC" ...
## $ oncotree code
                                 : chr
                                         140.5 84.6 163.7 164.9 41.4 ...
## $ overall_survival_months
                                   : num
## $ overall survival
                                   : int
                                          1 1 0 1 0 0 1 0 0 0 ...
## $ pr status
                                          "Negative" "Positive" "Positive" "Positive" ...
                                  : chr
## $ radio therapy
                                  : int
                                          1 1 0 1 1 1 1 1 1 0 ...
                                 : chr
## $ X3.gene_classifier_subtype
                                          "ER-/HER2-" "ER+/HER2- High Prolif" "" "" ...
##
   $ tumor size
                                   : num
                                          22 10 15 25 40 31 10 29 16 28 ...
## $ tumor_stage
                                  : num
                                          2 1 2 2 2 4 2 2 2 2 ...
## $ death_from_cancer
                                   : chr
                                          "Living" "Living" "Died of Disease" "Living" ...
## $ brca1
                                          -1.399 -1.38 0.067 0.674 1.293 ...
                                   : num
## $ brca2
                                          -0.574 0.278 -0.843 -0.543 -0.904 ...
                                   : num
## $ palb2
                                   : num
                                          -1.622 -1.215 0.211 -1.659 -0.722 ...
## $ pten
                                          1.452 0.53 -0.333 0.637 0.217 ...
                                   : num
## $ tp53
                                          0.3504 -0.0136 0.5141 1.6708 0.3484 ...
                                   : num
## $ atm
                                         1.1517 -0.2659 -0.0803 -0.888 0.3897 ...
                                   : num
## $ cdh1
                                          0.0348 1.3594 1.1398 1.2491 0.9131 ...
                                   : num
## $ chek2
                                   : num 0.127 0.796 0.419 -1.189 0.936 ...
## $ nbn
                                   : num
                                          -0.836 0.542 -0.403 -0.417 0.767 ...
## $ nf1
                                   : num
                                         -0.858 -2.606 -1.131 -0.617 -0.294 ...
## $ stk11
                                         -0.429 0.512 0.236 1.008 -0.296 ...
                                   : num
## $ bard1
                                   : num -1.12 0.439 -0.172 -0.401 0.632 ...
## $ mlh1
                                   : num -0.484 1.227 -1.791 -1.391 -0.358 ...
## $ msh2
                                   : num -0.748 0.761 3.095 4.88 0.303 ...
## $ msh6
                                   : num
                                         -1.666 0.1821 0.6608 0.0615 0.8747 ...
## $ pms2
                                          -0.125 1.01 2.613 2.941 0.632 ...
                                   : num
## $ epcam
                                         -0.372 0.56 2.555 4.116 0.335 ...
                                   : num
## $ rad51c
                                         -0.6508 -0.4018 -0.0391 -0.3098 -0.2652 ...
## $ rad51d
                                         -0.128 -0.291 -0.442 -1.347 -0.154 ...
                                   : num
## $ rad50
                                          1.733 0.744 1.453 1.21 -0.763 ...
## $ rb1
                                   : num
                                         -0.277 -1.749 1.414 1.534 1.016 ...
## $ rbl1
                                         -1.067 0.46 0.314 -0.635 1.9 ...
## $ rbl2
                                   : num 0.0615 0.7835 -0.0662 0.7279 0.6618 ...
## $ ccna1
                                         0.1034 -0.269 -0.5558 0.0219 -0.7454 ...
                                   : num
## $ ccnb1
                                         -1.663 -0.272 0.697 1.88 0.286 ...
                                   : num
## $ cdk1
                                         -2.0649 0.3895 1.2949 0.0476 1.1035 ...
## $ ccne1
                                   : num -1.339 -0.627 -0.124 -0.665 -1.051 ...
## $ cdk2
                                          -0.621 0.181 -0.111 -1.446 1.542 ...
                                   : num
## $ cdc25a
                                   : num -1.731 -1.264 -0.392 -0.383 1.217 ...
## $ ccnd1
                                         -0.806 1.106 -1.275 -0.454 0.117 ...
                                   : num
## $ cdk4
                                   : num -1.104 0.411 -0.531 -1.525 1.765 ...
## $ cdk6
                                   : num 0.0744 -0.604 0.2585 0.3689 0.8892 ...
## $ ccnd2
                                         1.4313 0.0546 0.8958 1.1455 -1.0195 ...
                                   : num
## $ cdkn2a
                                         -0.5785 0.2754 -0.227 0.0432 0.3664 ...
                                   : num
## $ cdkn2b
                                          1.218 -0.0952 1.1899 1.0868 0.7145 ...
                                   : num
## $ myc
                                   : num
                                         2.56 0.725 -0.721 -0.524 0.522 ...
## $ cdkn1a
                                         2.315 0.439 1.483 0.212 1.564 ...
## $ cdkn1b
                                         -0.249 1.876 3.07 3.462 0.156 ...
                                   : num
## $ e2f1
                                          0.16 -1.898 2.225 0.461 -0.267 ...
                                   : num
## $ e2f2
                                          -1.88 -0.333 -1.486 -1.54 0.451 ...
                                   : num
## $ e2f3
                                         -1.363 -1.456 -0.413 -0.212 -0.445 ...
## $ e2f4
                                   : num 0.199 1.001 -0.833 -0.833 -0.318 ...
## $ e2f5
                                   : num -0.0907 0.0519 0.2885 1.8323 2.2129 ...
```

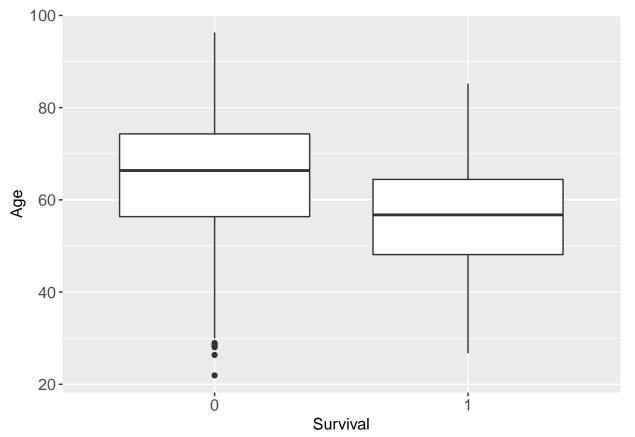
```
##
      $ e2f6
                                                                       -0.117 -0.379 -0.35 0.387 1.106 ...
## $ e2f7
                                                             : num -1.392 -0.491 -0.355 1.343 -0.065 ...
## $ e2f8
                                                                       -0.8178 -1.3693 0.0908 0.0409 1.4216 ...
## $ src
                                                             : num -1.074 -0.33 -0.718 -0.38 0.972 ...
## $ jak1
                                                             : num
                                                                      1.1097 0.9804 1.5835 0.6194 0.0461 ...
                                                                      1.6186 -0.0104 0.7379 0.8552 0.1645 ...
## $ jak2
                                                             : num
                                                                       0.0413 -1.194 -0.8346 0.3317 0.2677 ...
## $ stat1
                                                             : num
                                                                        -0.756 -0.799 -1.349 -0.551 0.331 ...
## $ stat2
## $ stat3
                                                             : num 0.977 -0.843 -0.224 -1.24 -0.505 ...
## $ stat5a
                                                                       3.9189 -0.4983 0.0434 -0.8535 -0.3295 ...
                                                                      2.5773 -1.3251 -1.0832 -0.0195 -0.4278 ...
## $ stat5b
                                                             : num
## $ mdm2
                                                                        0.3126 0.8803 -0.8822 0.2551 -0.0063 ...
## $ tp53bp1
                                                                       -0.627 -1.592 0.759 -1.006 0.106 ...
                                                             : num
## $ adam10
                                                                       -0.532 -1.267 2.036 1.466 0.938 ...
## $ adam17
                                                                        0.872 -0.201 -1.123 -1.049 -0.238 ...
                                                             : num
## $ aph1a
                                                             : num
                                                                        0.002 1.313 3.133 2.365 0.123 ...
## $ aph1b
                                                                       -0.0098 0.688 -0.4959 -1.2458 0.369 ...
                                                             : num
## $ arrdc1
                                                                       -1.465 1.337 -1.06 1.492 0.922 ...
                                                             : num
                                                             : num -0.275 1.591 1.674 2.644 0.202 ...
## $ cir1
## $ ctbp1
                                                             : num
                                                                        -1.102 1.193 -2.269 -0.727 -0.877 ...
## $ ctbp2
                                                             : num 0.841 0.301 0.24 -0.462 1.85 ...
## $ cul1
                                                                      0.447 -0.411 0.162 0.193 -0.684 ...
                                                             : num
## $ dll1
                                                                        0.631 -1.548 -1.044 0.448 -1.216 ...
                                                             : num
## $ dll3
                                                             : num -0.507 -0.158 0.949 1.611 -0.821 ...
## $ dll4
                                                             : num 1.693 -0.101 -1.746 -0.592 0.276 ...
      [list output truncated]
#To replace " " with NA
RNA_Mutation_updated[RNA_Mutation_updated == ""] <- NA
# To change character variables to factor
RNA_Mutation_updated$type_of_breast_surgery <- as.factor(RNA_Mutation_updated$type_of_breast_surgery)
RNA_Mutation_updated$cellularity <- as.factor(RNA_Mutation_updated$cellularity);</pre>
RNA_Mutation_updated$chemotherapy <- as.factor(RNA_Mutation_updated$chemotherapy)
RNA_Mutation_updated$pam50_._claudin.low_subtype <- as.factor(RNA_Mutation_updated$pam50_._claudin.low_
RNA_Mutation_updated$er_status <- as.factor(RNA_Mutation_updated$er_status);</pre>
RNA_Mutation_updated$neoplasm_histologic_grade <- as.factor(RNA_Mutation_updated$neoplasm_histologic_gr
RNA_Mutation_updated$her2_status <- as.factor(RNA_Mutation_updated$her2_status);</pre>
RNA_Mutation_updated$tumor_other_histologic_subtype <- as.factor(RNA_Mutation_updated$tumor_other_histo
RNA_Mutation_updated$hormone_therapy <- as.factor(RNA_Mutation_updated$hormone_therapy);</pre>
RNA\_Mutation\_updated\\sinferred\_menopausal\_state\\<-\ as.factor\\(RNA\_Mutation\_updated\\sinferred\_menopausal\_state\\<-\ as.factor\\(RNA\_Mutation\_updated\\sinferr
RNA_Mutation_updated$integrative_cluster <- as.factor(RNA_Mutation_updated$integrative_cluster );
RNA_Mutation_updated$primary_tumor_laterality<- as.factor(RNA_Mutation_updated$primary_tumor_laterality
RNA_Mutation_updated$pr_status<- as.factor(RNA_Mutation_updated$pr_status);
RNA_Mutation_updated$radio_therapy <- as.factor(RNA_Mutation_updated$radio_therapy)
RNA_Mutation_updated$overall_survival<- as.factor(RNA_Mutation_updated$overall_survival);
# exploring numeric data
# To remove Redundant column
RNA_Mutation_updated$patient_id <- NULL
RNA_Mutation_updated$cancer_type <- NULL
RNA_Mutation_updated$death_from_cancer <- NULL
RNA_Mutation_updated$cancer_type_detailed <- NULL
RNA_Mutation_updated$oncotree_code <- NULL
RNA_Mutation_updated$cohort <- NULL</pre>
```

```
RNA_Mutation_updated$tumor_stage <- NULL</pre>
RNA_Mutation_updated$overall_survival_months <- NULL
RNA_Mutation_updated$X3.gene_classifier_subtype <- NULL</pre>
RNA_Mutation_updated$er_status_measured_by_ihc <- NULL
RNA_Mutation_updated$her2_status_measured_by_snp6 <- NULL
clinical<-RNA Mutation updated[, c(1:20)]</pre>
                                                                                                                                                       # To make clinical data set
library(visdat)
clinical %>%
       visdat::vis_miss()
                                                                                                                                     Statute Utol Histologic subtype (0.79%)
                                                                                                                                                                                                      Multiply Todas axaning of orest of the Moles of the Moles
                                                                                                          Jalus Uriol histologic grade [3, 180]
                                                                                Danto Livering Supple (00)
                                                                                                                                                                                                                                 dun zunn Arognostic inder (Oolo)
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                                                                                                                                                               Lune iterated the notalisal state (00)
                                        at Joseph Jase of Meder In chart 1, 1600)
                           age at diagrasis look
                                                                   trandharady (0%)
                  0
            500
Observations
          1000
         1500
                                                                                                                                          Missing
                                                                                                                                                                                 Present
                                                                                                                                         (0.9\%)
                                                                                                                                                                                 (99.1\%)
clinical_n <- select_if(clinical, is.numeric)</pre>
corrmatrix <- cor(clinical_n)</pre>
clinical_n<-clinical_n[complete.cases(clinical_n),]</pre>
corrmatrix <- cor(clinical_n)</pre>
corrplot::corrplot(corrmatrix, method="number", type = "upper",tl.cex=.6
, tl.col="black", title="Correlation Plot",number.font = 2, mar=c(0,0,1,0), )
```

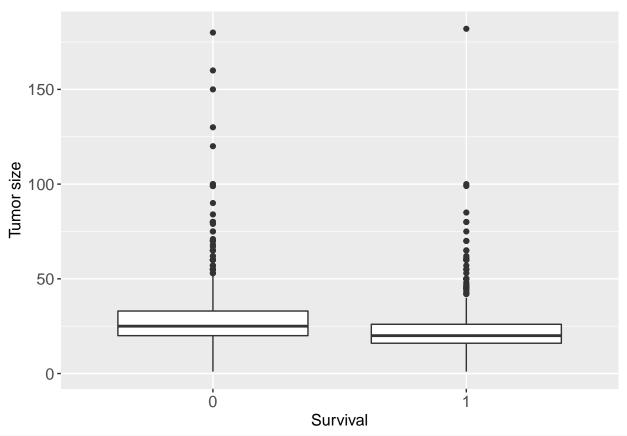


#### library(ggformula)

```
## Loading required package: ggstance
##
## Attaching package: 'ggstance'
## The following objects are masked from 'package:ggplot2':
##
##
       geom_errorbarh, GeomErrorbarh
## Loading required package: scales
##
## Attaching package: 'scales'
## The following object is masked from 'package:purrr':
##
##
       discard
## The following object is masked from 'package:readr':
##
##
       col_factor
## Loading required package: ggridges
## New to ggformula? Try the tutorials:
  learnr::run_tutorial("introduction", package = "ggformula")
## learnr::run_tutorial("refining", package = "ggformula")
```

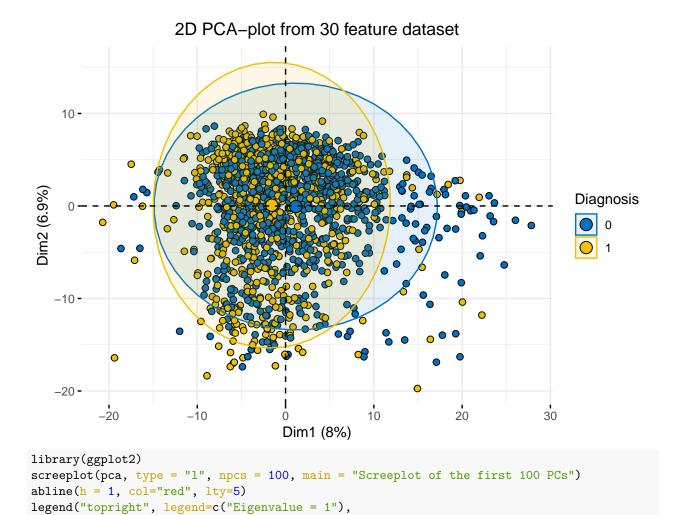


## Warning: Removed 20 rows containing non-finite values (stat\_boxplot).



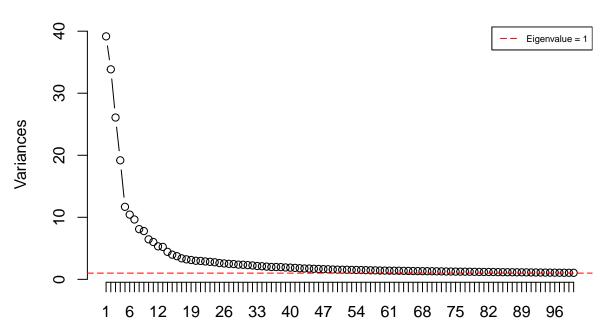
data.nona=RNA\_Mutation\_updated[complete.cases(RNA\_Mutation\_updated),] #delete all rows with any NA genes=data.nona[,21:509] #subset gene columns

```
#PCA analysis
pca=prcomp(genes,scale=TRUE)
#summary(pca)
#install.packages("factoextra")
library(factoextra)
```

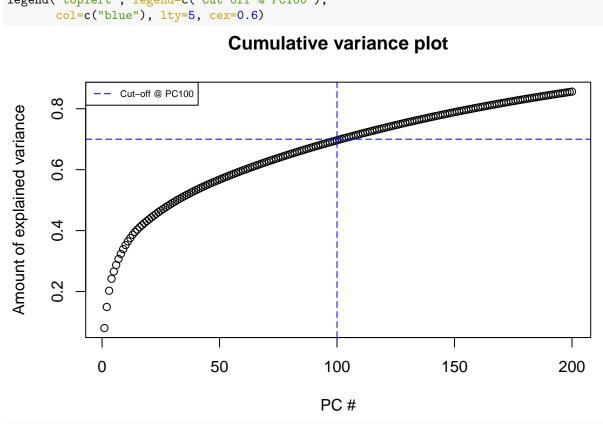


# Screeplot of the first 100 PCs

col=c("red"), lty=5, cex=0.6)



```
cumpro <- cumsum(pca$sdev^2/sum(pca$sdev^2))</pre>
plot(cumpro[0:200], xlab = "PC #", ylab = "Amount of explained variance", main = "Cumulative variance p
abline(v = 100, col="blue", lty=5)
abline(h = 0.7, col="blue", lty=5)
legend("topleft", legend=c("Cut-off @ PC100"),
       col=c("blue"), lty=5, cex=0.6)
```



```
comp=data.frame(pca$x[,1:100]) #retain the first 100 principal components
cluster.data=cbind(data.nona[,1:20],comp) #dataset for cluster analysis
```

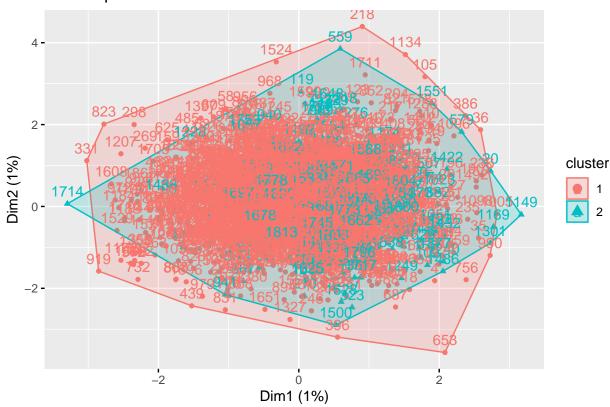
K-Means Cluster Analysis

```
#looking purely at gene expression subset of the data - numeric values for kmeans clustering
kvars <- paste("PC", 1:100, sep = "")</pre>
k.df <- cluster.data[kvars]</pre>
\#head(k.df)
#scale the data - no dependency to arbitrary variable unit
k.df <- scale(k.df)</pre>
\#head(k.df)
#euclidean distance
k.dist <- get_dist(k.df)</pre>
k.check <- kmeans(k.df, centers = 2, nstart = 25)
#k.check
```

Two clusters gives clusters with sizes 205 and 1403

```
fviz_cluster(k.check, data = k.df)
```

## Cluster plot



Starting with two clusters, we can see there is serious overlap in clusters. There is no clear division. We can find optimal cluster number with log-elbow method

```
#compute total within cluster sum of squares
set.seed(429)
wss <- function(k) {
    kmeans(k.df, k, nstart = 10 )$tot.withinss
}

#consider 1 to 100 clusters
kc.vals <- 1:100

#extract within cluster sum of squares for all number of clusters
wss.vals <- map_dbl(kc.vals, wss)

## Warning: did not converge in 10 iterations

## Warning: did not converge in 10 iterations</pre>
```

```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
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```
## Warning: did not converge in 10 iterations
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## Warning: did not converge in 10 iterations
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## Warning: did not converge in 10 iterations
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```
## Warning: did not converge in 10 iterations
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## Warning: did not converge in 10 iterations
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```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
```

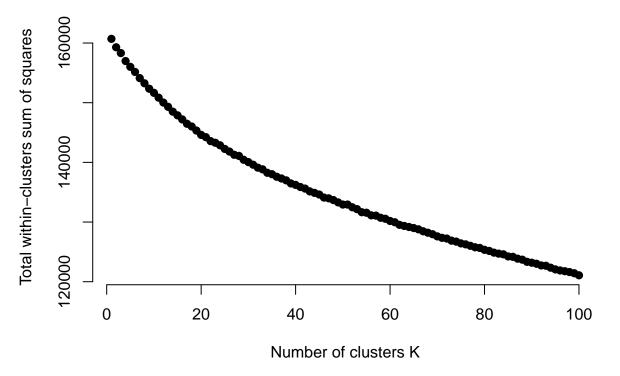
```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
```

```
## Warning: did not converge in 10 iterations
#plot log-elbow method
plot(kc.vals, wss.vals,
      type="b", pch = 19, frame = FALSE,
      xlab="Number of clusters K",
      ylab="Total within-clusters sum of squares")
```



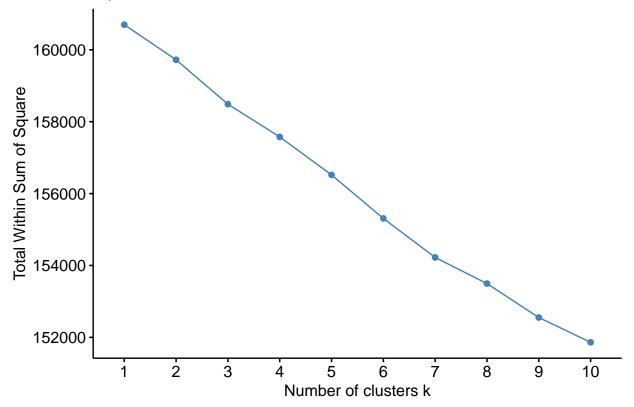
We can say about 20 clusters looking at this. We can double check as well. From here we can move onto the optimal model

```
set.seed(429)
fviz_nbclust(k.df, kmeans, method = "wss")
```

## Warning: did not converge in 10 iterations

## Warning: did not converge in 10 iterations

# Optimal number of clusters



# set.seed(429) k.fin <- kmeans(k.df, 20, nstart = 25)</pre>

## Warning: did not converge in 10 iterations

```
## Warning: did not converge in 10 iterations
## K-means clustering with 20 clusters of sizes 113, 168, 125, 17, 51, 105, 131, 100, 33, 45, 67, 15, 2
##
## Cluster means:
##
             PC1
                        PC2
                                   PC3
                                               PC4
                                                           PC5
                                                                      PC6
     -0.159401375 -0.72905351 -0.253570661
                                       0.146945197
                                                   0.947674847 -0.14752010
      0.354612381 \quad 0.48801472 \quad 0.022993690 \quad -0.016902101
                                                   0.134391082 -0.45336079
## 2
## 3
      0.191558559  0.20376114  1.238933064  0.380364971
                                                   0.123937075
                                                               0.29040407
      ## 4
                                                   0.477225609
                                                               0.38035709
      2.896263114 -0.69961899 -0.605362405 -1.637788696
                                                   0.396646018
                                                               1.32339356
## 6
    -0.352133739  0.81691058  -0.691615860  0.027552778  -0.498156454
                                                               0.61289062
## 7
      0.230950217 \quad 0.85100763 \quad 0.301324573 \quad 0.228028729 \quad -0.129233754
                                                               0.02985072
     -0.218291964 -0.46480429 -0.715422030
                                       0.185807742 -0.714860062
                                                               0.93352915
    -0.493612950 -2.01773658 -0.004662949
                                        0.467100944 -1.128835021 -0.23486334
## 10 0.284511533 0.75561382 0.761936986
                                       0.078108297 -0.772627022
                                                               0.75375178
## 11 -0.595918862 -0.05201161 -0.144294640 -1.516215288 0.346093694
                                                               0.01279563
## 12 -2.581412763 -0.30332740 1.700174762 -4.403566400 -0.771131132
## 13 -0.501686566 -1.92703817 0.032809649 0.178781255 -1.448368657 -0.68389461
## 15  0.008019155  -0.11754706  0.340285069  -0.009063371  0.824302419  -0.48657113
## 16 -0.275213074 -2.05875070 -0.119534070 0.605585887 -0.805972970 -0.46770617
## 17 -0.415634210 0.44632193 -0.321654245 0.158492129 0.554894507 -0.36854485
      0.301561871 0.64932976 0.239725265
                                       0.176375484 -0.221269464 -0.46212133
## 20 -0.349407823 -0.57045675 -0.562719124
                                        0.241366236 1.246163286 0.54927079
            PC7
##
                       PC8
                                   PC9
                                             PC10
                                                       PC11
                                                                  PC12
## 1
      0.07881138  0.90901349  0.7228768176  0.44317898
                                                   0.4467268
                                                             0.57229703
     -0.49583375
                0.46857468
                           0.1412710397 -0.20804430
                                                   0.0291441
## 3
      0.34543227 -0.63815262
                           0.3051796150 -0.10294468 -0.2994196 -0.06655065
## 4
      0.86217023 -0.02510473
                           0.5944332951
                                       0.45847934
                                                   0.4973931 -0.50718078
      ## 5
## 6
      0.04216167 \ -0.25765144 \ -0.0973682249 \ \ 0.38462485 \ -0.3730947 \ \ 0.15246398
    ## 7
      0.54544260 0.06850670 1.3938593637 -0.86658580 0.2748795 -0.20516491
## 8
```

```
## 9 -0.62897852 -0.13518380 -1.1517392915 -0.53853442 -0.1292969 -0.48739608
## 10 -0.42488566 -0.51288247 -1.0333333665 -0.24312531 1.6970553 0.41034193
## 11 0.22358310 -0.59735454 -0.7869754247 -0.18719917 0.3813121
## 12 0.47777297 -0.23323910 0.3172465517 -0.31821585 -0.2333481
                                                             0.42532896
## 13 -0.67950865 -0.11432644 -0.9204601307 0.63854330 -0.4819928 -0.14516959
## 14 -0.07041441 0.13435228 0.0979367594 1.19672096 -0.3719588 0.01804877
     0.44534076 -0.41003334 0.3051763986 -0.08623085 -0.1714673 -0.05840051
## 16 -0.33055401 0.14350998 -0.7650548402 0.09558910 -0.1334638 -0.16012341
## 17 -0.12627334 -0.22847666 0.0001128549 -0.11343117 -0.5894351 -0.52534710
0.06743697
      0.14845293 -1.58209246 0.5843444989 0.76168194 0.2503491
                                                             0.36788879
      0.35740272 1.57520231
##
  20
                           0.0617544758 1.12568406 0.7739261
                                                             1.84423195
##
           PC13
                      PC14
                                 PC15
                                            PC16
                                                       PC17
                                                                   PC18
## 1
     -0.20076937
                0.03760660 -0.35346553 0.05228020 0.091389824
                                                             0.005344044
                           0.28412557 -0.30511946 -0.305259168 -0.287734868
## 2
     0.17668264 0.30514698
## 3
     -0.10459960 0.12245287
                           ## 4
     0.024532303
                                                0.151060580
    -0.18623529 -0.40305702 -0.12888594 -0.33569531
                                                             0.209888239
     0.26138576  0.30258124  0.66957993  -0.10556795  0.013477025
## 6
                                                             0.012784369
     -0.10967534 -0.39026040 0.22564169 -0.25921872 0.107448675
                                                             0.522721758
## 8
      0.34958326 -0.42713152 -0.26757784 0.08866775 -0.161252326 -0.043215770
      0.14906241 \quad 0.10475440 \quad -0.21661232 \quad -0.41843170 \quad -0.162547415 \quad -0.448826412
## 10 -1.53514783 -0.16701581 -1.24579419 0.05153295 -1.019045065 -0.400751880
     1.15020992 -0.09615291 -0.05056124 0.42754455 -0.732597426
                                                             0.299832547
## 12 -1.97377138 -0.43312747 1.51326044 -1.53987055 1.247569720 -0.487668722
## 13 -0.30722402 0.04948656 -0.21426336 -0.51554324 0.454210076
                                                            0.398248897
0.432921107
## 15 -0.12274446 0.14834194 0.19238921 -0.24902164 0.199773543
                                                             0.256587534
     0.11143775 0.07602646 0.29884766 0.01252252 -0.084694296 -0.124327372
      0.17896222 -0.28334330 -0.15670772 0.23883581 -0.133757361
                                                             0.029845076
      0.23159233 0.10999041 -0.58931062 0.70099386 0.317715315 -0.691710268
## 19 -0.19201529 -0.20067698 -1.37496211 0.13436429 0.294917412 -0.302768354
## 20 -1.01746228  0.91129953  0.32027504  0.79319555 -0.006955924
                                                             0.095165957
##
          PC19
                      PC20
                                  PC21
                                             PC22
                                                       PC23
                                                                  PC24
      0.3502125 -0.350005451
                           0.000346309 -0.01738007 -0.12070171
  1
                                                             0.55449482
    -0.3889281 0.086788046 0.108803997 -0.34652025 -0.07683111
                                                             0.06289767
## 2
    -0.2333183 0.235676520 0.255242514 -0.25668068 0.07776220
    -0.0920786 -0.687756657 -0.014123771 0.04944049 -0.53003844 -0.18011655
      0.2423945 - 0.153246761 \quad 0.135772116 - 0.38888986 - 0.06886257 - 0.21639889
      ## 6
      0.3828259 0.004642981 0.131961664 0.39514070
                                                 0.07001439 -0.03599291
     -0.1354404   0.248820435   0.061938895   -0.11717396
                                                 0.28909647 0.04579135
## 8
## 9
     -0.3015770 0.363614143 0.610010112 0.38278694
                                                 0.57223054 -1.04225242
## 10 0.7444000 -0.191070798 -0.246406649 -0.20930276
                                                 0.06165109 0.66613005
## 11 -0.5317299 -0.932944077 -0.683381360 -0.03279526 0.41309002 -0.16160892
## 12 -0.2904499 -0.424155149 0.308106030 -0.13283180 -2.02273646 -0.51015260
## 13 -0.1595156 -0.201163743 0.372421179 0.93845225 0.96800466 0.87007003
## 14 -0.3062581 -0.451007769 -0.004571833 -0.08749829 0.16646386 -0.28744512
## 15 0.1224769 -0.212370217 -0.440282194 0.21607333 0.37421799 0.20376402
## 16 -0.1055137 0.270177877 -0.500950210 -0.31832279 -0.65158661
                                                            0.27938244
## 17 -0.1617563 0.090166296 0.043367220 0.08223813 -0.31306273 -0.18389137
## 19 -0.4178647 0.181499539 -0.156078656 0.33353914 0.01452609 -0.54297758
## 20 1.0404585 1.418919752 0.880364021 0.23503567 -0.05601606 -1.82638633
```

```
##
                            PC25
                                                       PC26
                                                                                    PC27
                                                                                                              PC28
                                                                                                                                         PC29
                                                                                                                                                                   PC30
               0.06233861 - 0.20177277 \quad 0.005494171 \quad 0.45547268 \quad 0.10314016 - 0.19540730
## 1
               0.02979452 0.16670702 0.179505248 -0.06757032 0.01224886 -0.31568723
            0.20378650
                                                                                                                                                   0.04465585
            -0.25719899 0.25985784 -0.371897268 0.65366278 0.74644652
                                                                                                                                                     0.45105976
            -0.32682721 -0.31929748 -0.163211265 0.20693966 -0.19569921
                                                                                                                                                    0.06614594
## 5
              0.12655607 -0.10461236 0.621060631 0.48382208 -0.24888299 -0.02862691
            -0.04819016 -0.23341117 -0.352880311 -0.16275235 -0.36657823 0.35861017
## 7
               -0.51722780 -0.04115477 -0.594055427 0.04976032 -0.66857266 -0.70276932
## 10 -0.47451643 0.19617828 0.710837287 -0.70811530 0.41955566 -0.28122876
             1.05566525 -0.03965200 0.188459465 -0.16761773 0.11475690 0.44021508
## 12 -0.64974184 -0.58064414 -1.309413765 0.84025478 -0.00861170 -1.25829967
             1.22008248 1.01610588 -1.279819799 -0.14814541 0.25910416 1.69711407
## 14 -0.66212477 -0.25034449 -0.249037083 -0.29915633 0.95859929 0.11538854
               0.00362014 \quad 0.24031898 \quad -0.176424917 \quad -0.18393526 \quad -0.10672241 \quad -0.040280911 \quad -0.0402809
## 16 -0.16229441 -0.16018121 0.642134809 -0.18552660 -0.31552850 0.01544319
## 17 -0.16214460 0.12236603 0.015337967 -0.02532875 -0.01045095 -0.10963329
## 19 -0.15176570 -0.23629843 0.300463346 0.08786877 -0.57952267 -0.27537479
##
      20 -0.16648650 0.25554759 -0.277565228 -0.57751407 -0.18140424
                                                                                                                                                      1.03321745
                                                           PC32
                                                                                      PC33
                                                                                                                PC34
                                                                                                                                           PC35
                               PC31
            ## 1
                                                                                                                                                      0.049070338
            -0.040583781 -0.009123084 0.08296171 0.16953235 0.47309462
## 2
                                                                                                                                                      0.145598756
## 3
              0.399419823  0.360683748  0.16997084  0.20851075  -0.08750926  0.003773005
               0.073598510 -1.157435377 0.54216520
                                                                                                 0.98671411 0.42258258 -0.027017430
               0.228411086 \ -0.052421439 \ -0.01994763 \quad 0.33353605 \ -0.67143707 \quad 0.112373733
## 5
## 6
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                                                                                                                                                      0.184105057
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## 7
## 8
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## 9
             -0.572820510 1.816163272 -0.27360754 0.13311068 0.73377692 -0.655920494
## 10 -1.087235843 -0.343957897 -0.21394438 -0.17902074 0.14610377 -0.253696369
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               0.198839942 \quad 0.530431068 \quad -0.30024389 \quad 0.52719602 \quad 0.73995644 \quad 1.099924073
## 12
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               0.225390949 \ -0.174767128 \ \ 0.21239828 \ \ 0.21701936 \ -0.20967177 \ -0.481307299
## 15 -0.492138405 -0.072103001 -0.02617451 -0.09850989 0.06180526 -0.324173367
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               0.131459543 \ -0.061731727 \ -0.21868780 \ \ 0.03205905 \ -0.14242196 \ \ 0.074977937
      18 -0.007329232 -0.446388499 -0.11632133 -0.08043030 -0.19543649 -0.231286830
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              0.029570039 1.007712409 0.63665681 -0.61003453 -0.65735317 0.416726083
##
      20
                            PC37
                                                         PC38
                                                                                      PC39
                                                                                                                PC40
                                                                                                                                           PC41
                                                                                                                                                                     PC42
##
            -0.24247360 0.035002170 0.380241940 0.09871508 0.22130910 -0.16938626
      1
               0.31531700 0.035241799 -0.153793050 -0.11037325 -0.21500081 0.01994678
            -0.43981200 \ -0.315993243 \ \ 0.515098448 \ -0.09403113 \ -0.07767025 \ -0.11603224
## 3
## 4
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               0.03340093 \quad 0.598156977 \quad 0.121482830 \quad -0.36389339 \quad -0.24798193 \quad -0.11110087
## 5
## 6
            ## 7
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## 8
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## 11 -0.20014801 -0.166798207 -0.164119443 0.10350535 0.26624800 0.29601482
```

```
## 12 0.81790386 0.474518034 -0.036783075 0.55879417 0.17805920 -0.80283802
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     17 -0.20584996 0.044577363 -0.059676474 0.59564744 -0.36362359 -0.00256442
            0.51096475 -0.215714590 0.063520746 -0.63802375 0.21338852 -0.42103948
            0.36991151 0.342221229 -0.395531521 -0.46393149 0.35420542 0.20880016
## 19
            0.45595978 0.511935219 -0.175188491 -0.17263835 -0.85158435 0.54697366
     20
##
                         PC43
                                               PC44
                                                                       PC45
                                                                                               PC46
                                                                                                                       PC47
                                                                                                                                             PC48
          -0.247734518
                                  0.29260136  0.107728043  -0.027983995
                                                                                                         0.132973265 0.17141923
    1
            0.094779459 -0.05682700 -0.001800546 -0.292341141
##
     2
                                                                                                         0.001750859 -0.12077866
     3
          0.011803245 -0.06499841
            0.169537895 -0.68149124 -0.752117237 -0.838273131 0.705594242 0.51154322
          -0.039953901 \ -0.30463232 \ \ 0.206449039 \ \ \ 0.096282104 \ -0.235948575 \ -0.1422208482104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.235948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.142220848104 \ -0.255948575 \ -0.255948575 \ -0.255948575 \ -0.255948575 \ -0.255948575 \ -0.255948575 \ -0.255948
## 5
## 6
            0.246473934
                                    0.03136304 0.030242660
                                                                                 0.301006609
## 7
                                   0.38822045 -0.167634488
                                                                                 0.005862347 -0.026060072 0.11884088
            0.121765949
                                   0.10184179 0.328499682 0.074703593 -0.123666606 -0.04961027
## 9
          -0.169602022 0.17387258 1.073392843
                                                                                0.230783669 0.210137981 -0.18871751
## 10 -0.533105756 -0.39667673 -0.052497073 -0.248760917 0.307695655 -0.22616022
            0.191610055
                                  0.20509058 0.016321408 -0.367028212 0.147436839 0.19759552
## 12 -0.614853745 -0.60677701 -0.717494217 -0.071896297 -0.646762481 0.90530759
                                  0.02054519 -0.084200616 -0.643691895 0.005720572 -0.09626481
            0.446334239
## 14 -0.143589484 0.04114168 -0.298041734 -0.022884605 -0.061691547 0.04969395
            0.163351156 - 0.20269723 - 0.413183004 0.072637785 0.002073078 - 0.13953800
## 16 -0.053805530 0.16204642 -0.149909551 0.277945083 -0.087080841 -0.16593338
    17 -0.269634692 -0.32011307 0.176382038
                                                                                 0.072703900 0.003632899 0.18095827
            0.002151941 -0.04670276 -0.176877128
                                                                                0.555941000 -0.289354657 -0.10160526
            ## 20 -0.143762783 -0.79119716
                                                          0.02123048
##
                       PC49
                                                PC50
                                                                         PC51
                                                                                                 PC52
                                                                                                                         PC53
## 1
            0.05722440 - 0.086416091 0.3511298804 - 0.022319126 - 0.013601105
                                                                                                                                  0.20651466
          -0.04028942 -0.046033022 -0.0176961847 -0.128090068 0.135981516
                                                                                                                                   0.08063513
          .3
           -0.81360537 0.988582659 -1.4021773789 0.235866627 -1.407180049 -1.06763105
            0.34990076 \quad 0.028183385 \quad -0.0015759500 \quad 0.194721119 \quad 0.038078128 \quad -0.04907482
## 5
          0.364632199 0.037155067 0.10913782
## 7
            0.005911615
                                                          0.0007872413 -0.308328903 0.093038981 -0.01820721
           -0.07270022
            0.67034434 - 0.486572912 - 0.7633814854 \quad 0.218133885 - 0.080931865 - 0.83947797 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.080931865 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.08093186 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0.080986 - 0
## 9
## 10 -0.21997096 -0.145142066
                                                         0.0031441992 0.135621683 0.105758668 -0.05863838
           0.08531866 0.315486738
                                                        0.0597100748 -0.324356425 -0.045556900 -0.10922780
## 12 -0.78387942 0.271054645
                                                         0.4370210714 -0.222305890 0.564166632 0.03838014
## 13 -0.02609487 0.745764966
                                                         0.8221383786 -0.599414757 0.320587723 -0.28865553
            0.28578708 -0.395263527
                                                         16 -0.28527673 -0.234969869 -0.2923875677 0.347939669 -0.079977274 0.64774565
## 17 -0.21133941 -0.032225448 -0.1220434909 -0.206392492 0.007617446 -0.23219937
           0.04873288 -0.137355303 0.4057766415 -0.015213962 -0.094704531 -0.28764575
    19 -0.11988951 0.057160511
                                                          0.3823348780 -0.012629141 -0.194043048 0.40897352
                                                         0.3086494536 -0.225725802 0.085223223 -0.86089086
##
            0.39745466 -0.141665551
                         PC55
                                               PC56
                                                                     PC57
                                                                                               PC58
                                                                                                                   PC59
## 1 -0.005920011 -0.21406599 -0.22718084 -0.3572740418 -0.1649682 -0.15847168
         -0.194942005 \ -0.09773960 \ -0.21617669 \ -0.1364930207 \ \ 0.1078194 \ -0.20980029
```

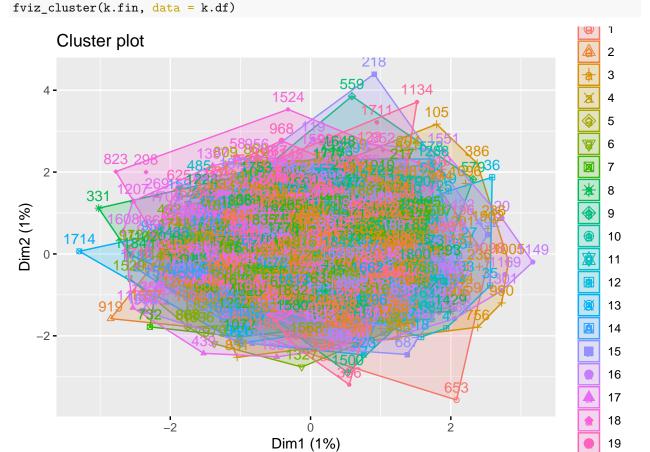
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      1.136023894 -1.46452269 -1.35729023 -0.6348191488 0.4298157 0.09362802
    -0.281089225 0.12812854 0.06988066 0.0523797740 0.1021370 -0.08888706
     0.043270543 -0.11098689 -0.35027766
                                     0.0009583132  0.2662183  0.07609362
## 6
      0.312928866 -0.12715691 0.08820419
                                     0.0836724320 -0.2140266 -0.04524788
    -0.204655181 \ -0.04831680 \ \ 0.09916894 \ \ 0.2006651198 \ \ 0.2424532 \ \ 0.11953979
## 8
    -0.163348597 -0.40326105 -0.18065946
                                     0.0044835465 -0.4015098
## 11 -0.009726881 -0.26840339 -0.06591404 0.0612804193 -0.2940315 -0.11606063
      0.737587590 \ -0.03548595 \ \ 0.12885481 \ \ 0.3660945645 \ -0.4222118 \ \ 0.30251056
      0.189030191 \quad 0.76611268 \quad 0.17639524 \quad 0.1072326183 \quad -0.1956913 \quad -0.12342774
                0.16927167 -0.06221278 -0.1751704573 -0.3680249 -0.07358071
## 14 -0.126256846
      0.008396370 0.14371715 0.16340344 0.0449692291 0.2167154 0.25327021
      0.166880974 0.01743415 0.11018011 0.2654778947 -0.0900634 -0.27541657
## 17 -0.091264380 0.14025822 0.31126653 0.2594453369 -0.1091478 0.09215514
      0.099284375
                ##
      0.092359613
                0.33318281 -0.20390077 -0.3460232030 -0.3717305 -0.12033196
  19
##
      0.034262101
                0.65637977 0.38992562 0.2995729438
                                                  0.4452204 0.22894140
##
                       PC62
                                   PC63
                                             PC64
            PC61
                                                         PC65
                                                                    PC66
## 1
      0.270192437 -0.109451769 -0.096191498 -0.19912310
                                                  0.156296091 -0.151349537
##
  2
      0.016210022 -0.132119403 0.072126075 -0.04036042 0.226980060 0.048840336
     -0.002486045 0.312071708 0.064870497 0.29071437 0.006550897 0.345444292
     -0.886426259 \ -0.496706773 \ \ 0.078169643 \ \ 0.88413021 \ -0.092971912 \ -0.643755323
     -0.227527159 -0.193227975 0.096025781 -0.18453291 0.070144479 -0.113920314
## 6
    -0.178729559 -0.178747397 -0.060065202 0.13291740 0.002321961 -0.200369048
      0.105896881 \ -0.036074935 \ \ 0.015117596 \ -0.02311756 \ -0.045442946 \ \ \ 0.150450579
## 8
## 9
      ## 10 -0.023440603 -0.232565585 -0.043790446 -0.12708127 -0.093120777 -0.009757199
## 11 -0.095273305 0.265209518 0.205795750 0.18598381 0.150194398 -0.022965514
      0.213682169 \quad 0.253643950 \quad -0.746435660 \quad -0.18184599 \quad -0.053151041 \quad -0.465134566
## 13 -0.066495445 -0.056043839 -0.354588099 0.24352769 0.270589755 -0.072144296
0.077520422 \; -0.170862209 \; -0.041799768 \; -0.25748801 \; -0.189848206 \quad 0.171220613
      0.166087409 0.274274108 0.094181800 0.05154063 -0.046637009 0.376517908
## 17 -0.042031194 -0.092845763 -0.016663498 -0.10334688 0.021830785 -0.258403298
## 19 -0.008286518 -0.054213263 -0.063645821 0.09396875 0.063888233 -0.028720067
## 20 -0.487732535 -0.317893258 0.038240346 0.37634438 0.504054257 0.174830586
                                            PC70
##
            PC67
                                 PC69
                      PC68
                                                      PC71
                                                                  PC72
    -0.082618470 -0.03825689 -0.10950024 -0.09941520 -0.20404180 -0.071739068
## 1
     -0.049206429 -0.15605813 -0.13417871 0.17098152 -0.04041255 -0.204347148
    -1.431186173 -0.41141914 -0.67039436 -1.33182904 -0.05258386 -0.036259799
## 5
      0.205715908 0.09966576 0.00448427 0.08529577 -0.12439676 0.188910781
      0.005134019 \ -0.18056179 \ 0.05269502 \ 0.26600571 \ -0.01857745 \ 0.224939419
## 6
     -0.034595064 0.05729019 -0.03728532 0.05196501 0.13190475 -0.036902110
      0.082487553 -0.07305080 0.20949259 -0.18633474 0.15625627 -0.230466449
## 9
      0.341693631 - 0.64513637 - 0.11319872 0.29259475 0.10106536 - 0.471375831
## 10 -0.019590119 -0.29452811 -0.39874686 -0.25027057 -0.38240603
                                                           0.219800343
     0.184619584 -0.25474104 -0.18837246 0.13404281 -0.06536437
                                                           0.009445049
      0.043196223 - 0.57842427 - 0.08800106 0.20997466 - 0.47958141 0.447229799
      0.483885666 \quad 0.80248934 \quad 0.26674252 \quad 0.13933153 \quad -0.15285096 \quad -0.306562284
```

```
## 15 -0.100924156  0.06085871  0.62905753 -0.18150782  0.08457021
                                                            0.211888910
## 16 -0.225832163 -0.05407595 0.06287011 0.02542395
                                                             0.314634706
                                                 0.03566844
      0.307538533 -0.07945281 -0.09678909 -0.19039455
                                                  0.07530983
  18 -0.213134532 -0.07654916 -0.23926754 -0.07693673
                                                  0.25671789
                                                             0.219513037
  0.21355745 -0.237047287
##
      0.182488932 - 0.01098533 \ 0.17427580 \ 0.32519031 - 0.32446396
                                                             0.122092840
##
            PC73
                       PC74
                                  PC75
                                            PC76
                                                        PC77
                                                                   PC78
## 1
      0.038620110
                 0.29274526
                           0.02003190 -0.15113494 -0.040412833
                                                             0.03836551
     -0.184827297
                 0.01130965 -0.01594649 -0.13652263
                                                  0.084465726 -0.19346027
  2
      0.082084038 \quad 0.12471358 \quad 0.27068855 \quad 0.05393216
                                                  0.006491563 0.07918455
## 4
      0.608603855 -0.69503888 -0.26197225 -0.25325279
                                                  0.106599701 -0.28177692
     -0.073771174 \quad 0.08585380 \quad 0.23973034 \quad -0.09720508 \quad -0.126020519 \quad -0.08828502
## 5
##
      0.231476055 -0.01092920 0.20044881 0.12395499
                                                 0.108126121
                                                             0.06946130
  6
                                                             0.02933898
     -0.268338760 -0.03805971 -0.05239980 -0.09424299
                                                 0.009253262
     -0.109117259 -0.08093855 -0.09494659 0.18034438 0.067124338
## 8
                                                             0.05766615
## 9
      0.151620788 - 0.03559521 - 0.09313591 - 0.08617705 - 0.287412430
                                                             0.31445083
0.35532051
     0.077291646
                0.04433344 0.11103021 0.06427415 -0.094414428 -0.20814552
## 12 -0.905350468 -0.19554872 -0.06347173 0.20814232 0.528217617 -0.25477966
      0.408415081 0.60193217 0.21517249 -0.11621345 -0.361856208 -0.37942369
  14
      0.367971399 -0.07840729 -0.07941739 0.26870369 0.250147720 0.04057611
## 16 -0.108906834 -0.13450782 -0.10114578 0.07674907 0.337019497 -0.14523595
## 17 -0.005350701 -0.02486047 -0.26176437 -0.13167427 -0.188565658 0.13382081
## 18 -0.002050934 -0.20733301 0.25133393 -0.14242698 -0.110723905 -0.03043135
  19 -0.385967086 -0.44287684 0.01332453 0.30138468 -0.220628052 -0.10987222
      0.097376106 0.19532833 -0.09479697 -0.13741296 -0.010439298
##
                                                             0.08716412
##
           PC79
                      PC80
                                  PC81
                                            PC82
                                                        PC83
                                                                    PC84
     -0.22685772
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## 1
                                                             0.096364900
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## 2
## 3
      0.19735394
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## 4
      0.75427939 \quad 0.86515700 \quad 1.393193764 \quad -0.24362760 \quad -1.504728070 \quad 1.003110242
     -0.17640935 -0.04751415 -0.007171128 0.02571296 0.028944756 -0.107408855
      0.19185330 \quad 0.09178366 \quad 0.282915297 \quad -0.17075178 \quad -0.007753887 \quad -0.156951636
## 6
     -0.19841940 -0.11106682 0.143035477 -0.14362552
                                                 0.069373273
                                                             0.025836553
     -0.02968421 0.08089294 -0.043696116 0.25301802 0.112677265 0.145303279
## 8
      ## 12 -0.63740230 -0.38377167 -0.002179590 0.29477644 -0.107231258 -0.145335714
      0.18760392 \quad 0.41053161 \quad 0.051056162 \quad 0.03166888 \quad -0.261981566
                                                             0.056333550
## 14 -0.16063811 -0.31863128 -0.289319934 -0.13579695 0.146748758 0.005865523
      0.08491317 -0.06514681 -0.203170341 -0.05038623 0.267421218 -0.133919963
  16 -0.06897697 -0.20671913 -0.048785787 -0.08383049 0.005270597
                                                             0.098261763
## 17 -0.05524793 -0.07355341 -0.014115031 0.18157271 -0.170166598 0.070247482
## 18 -0.06868973 -0.22208700 0.166225414 -0.16175315 0.067541136 0.215478429
  19 -0.13544641 0.05342126 0.241451952 -0.12209427 -0.159470609 -0.140100907
     0.05325715 -0.35384061 -0.029128356 0.19581369 -0.415892488 -0.172858924
##
           PC85
                       PC86
                                  PC87
                                             PC88
                                                         PC89
                                                                      PC90
##
     -0.15957981 0.102167745 -0.46141990
                                       -0.04485744 \ -0.027548842 \ -0.15589653 \ \ 0.146229196 \ -0.006189139 \ -0.1358098438
    0.22201490 0.420051161 0.46195802 -0.274882727 -0.384418223 0.1925665816
    -0.26749506 \; -0.148334641 \; -0.46121676 \quad 0.106866205 \quad 0.242088643 \quad 0.0827239191
```

```
0.25098265  0.167659020 -0.05432925 -0.227533143  0.114046871 -0.1492637419
## 7
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      0.06275217 \ -0.003078407 \ \ 0.13244994 \ \ 0.024285792 \ \ 0.035891948 \ \ 0.0028709572
     0.615317398 -0.203667266 -0.1014403353
## 9
## 10
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                            0.17854346
                                       0.166996131 -0.017285028 -0.1369813020
## 11 -0.10814157 -0.085187444
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      ## 14 -0.18912190 0.194755716 0.17826757
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                                                               0.0002129585
## 15 -0.02086360 -0.037707371 0.29617492 -0.265485975 -0.186886436
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      0.24517589 0.062196838 0.11063966 -0.246578351 0.128742221
                                                               0.1186052605
  17 -0.01839237 -0.144492246 -0.09122441 0.053637917 -0.111915695
                                                               0.2300907337
      0.05400981 0.089096921 0.41845835 0.021928865 -0.192582607
                                                               0.5273787871
  18
##
      0.13532079 -0.308088975
                            0.02896185 -0.103629718 0.342441558 -0.2620882554
## 20
      0.22014265 0.112688080
                             0.48912216 -0.521644664 -0.044263138 -0.1584809374
##
            PC91
                        PC92
                                    PC93
                                                PC94
                                                            PC95
## 1
      0.098629279
                 0.054584225
                            0.198186949 -0.062944487
                                                    0.026213697
     -0.031932085
                 0.060919102 -0.120494201 0.149225009 -0.135163532
     ##
                                         0.057679590 0.097832061
  .3
## 4
     -0.061165558 -0.454211382 0.366424120
                                         1.595409319 -0.568295637
## 5
      0.169232002  0.164920377
      0.002773903 - 0.043538975 0.007674264 - 0.080101578
## 6
                                                     0.031990680
## 7
      0.339269870 - 0.055597593 - 0.250008384 - 0.172583975
                                                     0.083638301
      0.003606051 -0.047792055 0.064233976 0.046196136
                                                     0.101639494
## 9
    -0.491774760 -0.108950218 -0.253446254 0.014678224 -0.397009665
## 10 -0.343150808 0.033754392 -0.074590211 0.081415453
                                                     0.291800670
## 11 -0.283789556 -0.053827720 0.320575991 0.127171360
                                                     0.042502743
## 12 -0.525956630 0.175656873 0.049799744 -0.349056199 -0.023381560
      0.110582966 0.129107923 -0.123735065 0.110852502 -0.140645661
      0.041407286 0.233432304 -0.103274407 -0.007110747 -0.059689190
## 15 -0.163716526 0.245955346 0.129123663 -0.445700511 -0.009678699
      0.066303650 -0.006965843 -0.033870243 -0.121431485 0.003146941
      0.048135180 -0.183335538 0.037821062 0.060399426 -0.098576222
  18 -0.060904888 -0.089695858 0.192025775 -0.013801168 0.164404649
      0.081413042 -0.097803005 -0.055357185 0.125031743 0.094684418
  20 -0.305613190 0.033605699 -0.082330609 0.092016821 -0.373364427
##
##
            PC96
                       PC97
                                  PC98
                                              PC99
                                                        PC100
## 1
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                 0.09067162 -0.08900970 -0.095497035 0.14787360
                 0.02591845 -0.16537038 0.194838784 -0.12472838
     -0.133547403
                 0.03009275 -0.04940875 -0.211287783 -0.12921985
     -0.159558978
## 3
      0.169927735 -0.78613832 0.44016858 1.325451193
                                                   0.53817387
                 0.33471957 -0.20392814 -0.103255433 0.01793765
## 5
      0.050885319
## 6
      0.132002247
                 0.04953905 0.03765414 -0.261206250
                                                   0.10318471
      0.026693351 - 0.03186351 \ 0.01047551 - 0.049098398
## 7
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      ## 9
## 10 -0.044652657 -0.08808456 -0.19806257 0.072136041 -0.15350382
     0.137697689 -0.03343006 0.15192486 -0.023919986 0.07398684
## 12 -0.196718248 0.26918442 -0.17697124 -0.163036549 -0.39309252
## 13 -0.068796081 -0.09161582 -0.06055979 -0.203894916 -0.24802354
     0.016570116 -0.15022172 0.14118690 0.171077238 0.18082197
## 15 -0.164837646 -0.10983250 0.03056265 0.099310977 -0.09530717
## 16 -0.042015672 -0.08642359 -0.27632757 0.097048088 -0.36968658
## 17 0.037314702 -0.08697977 0.15297262 -0.034200326 0.30250995
```

```
7 16
                         6
                            1
                                   3 14 16
                                                7
                                                    7 8 16
## 1452 1453 1454 1455 1456 1457 1458 1459 1460 1461 1462 1463 1464 1465 1466 1467
                    7
                         2
                              2
                                   2
                                       8
                                             2
                                                 2
                                                      2
                                                          18
                                                                1
                                                                     7
## 1468 1469 1470 1471 1472 1473 1474 1475 1476 1477 1478 1479 1480 1481 1483 1484
          1
               2
                    3
                         7
                              2
                                   2
                                     13
                                           10
                                                 7
                                                      2
                                                           2
                                                               13
                                                                     2
## 1485 1486 1487 1489 1490 1491 1492 1493 1494 1495 1496 1497 1498 1499 1500 1501
         16
              19
                    7
                        10
                              3
                                   2
                                        3
                                             2
                                                 19
                                                      2
                                                          20
                                                                2
## 1502 1503 1504 1505 1506 1508 1509 1510 1511 1512 1513 1515 1516 1517 1518 1519
     6
          2
             15
                    3
                         8
                              5
                                14
                                      10
                                            7
                                                 2
                                                      5
                                                           3
                                                              15
                                                                     2
                                                                          2
                                                                              17
## 1520 1521 1522 1523 1524 1525 1526 1527 1528 1529 1530 1531 1532 1533 1534 1535
        17
              15
                    8
                       18
                             17
                                   8
                                      15
                                            7
                                                 6
                                                     14
                                                          15
                                                                8
                                                                    16
                                                                         17
## 1536 1537 1538 1540 1541 1542 1543 1545 1546 1547 1548 1549 1550 1551 1552 1553
     9
        20
               7
                   17
                       15
                             19
                                   5
                                       8
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                                                     20
                                                           6
                                                                5
                                                                    16
                                            6
                                                                          1
## 1555 1557 1558 1559 1560 1561 1562 1563 1564 1565 1566 1567 1568 1570 1571 1572
     7
                             17
                                   4
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          2
               1
                    1
                         1
                                        6
                                           17
                                                 1
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                                                                2
                                                                    14
## 1573 1574 1575 1576 1577 1578 1579 1580 1582 1583 1584 1585 1586 1587 1588 1589
    17
         14
              5
                             17
                                   1
                                       8
                                             4
                                                17
                                                      6
                                                         17
                                                                1
                                                                     2
                                                                         16
                                                                               7
                    1
                        1
## 1590 1591 1592 1593 1594 1595 1596 1597 1598 1599 1600 1601 1602 1603 1604 1605
                                                              17
          1
               7
                    3
                       14
                             14
                                 16
                                      7
                                          19
                                                17
                                                     17
                                                           6
                                                                    17
## 1606 1607 1608 1609 1611 1612 1613 1614 1615 1616 1617 1618 1619 1620 1622 1623
     8
          2
              17
                    2
                         8
                              4
                                   1
                                       17
                                             3
                                                 8
                                                     17
                                                           2
                                                                7
                                                                     7
## 1624 1625 1626 1627 1628 1629 1630 1631 1632 1633 1634 1635 1637 1638 1639 1640
                        16
                                           10
              16
                              9
                                   7
                                       10
                                                 17
                                                      6
                                                           7
                                                              17
    18
        16
                    1
                                                                    16
                                                                         19
## 1641 1642 1643 1644 1645 1646 1647 1648 1649 1650 1651 1652 1653 1654 1655 1656
    17
          7
              17
                   19
                        18
                             10
                                   3
                                        8
                                             3
                                                 2
                                                      17
                                                          15
                                                                .3
                                                                     1
## 1657 1658 1659 1660 1661 1662 1663 1664 1665 1666 1668 1669 1670 1671 1672 1673
          3
               3
                    8
                        15
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                                   1
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                                                          19
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                                                                     6
                                                                         18
## 1674 1675 1676 1677 1678 1679 1680 1681 1682 1683 1684 1685 1686 1687 1688 1689
        18
              16
                   20
                        13
                              7
                                 15
                                       16
                                            7
                                                 15
                                                    15
                                                           9
                                                                6
                                                                    15
## 1690 1691 1693 1694 1695 1696 1697 1698 1700 1701 1703 1704 1705 1706 1708 1709
          3
               7
                   1
                        15
                              6
                                13
                                        9
                                           10
                                                  1
                                                      7
                                                         14
                                                              17
                                                                     6
                                                                         15
## 1710 1711 1713 1714 1715 1716 1717 1721 1722 1725 1729 1730 1731 1732 1733 1734
                  13
                        1
                             19
                                 16
                                       2
                                           14
                                                 6
                                                      3
                                                          20
                                                                1
## 1735 1736 1738 1739 1741 1743 1744 1745 1746 1749 1753 1754 1757 1759 1762 1763
                    3 17
                              6
                                18
                                               14
                                                      8
                                                           2
                                                              7
              6
                                      8
                                           1
                                                                     2
## 1764 1765 1766 1767 1768 1769 1771 1772 1773 1776 1777 1778 1784 1785 1786 1787
              19
                    6
                         3
                              6
                                   3
                                      17
                                            16
                                                 2
                                                      8
                                                           8
                                                                3
                                                                     7
## 1790 1791 1793 1794 1795 1796 1797 1799 1800 1802 1803 1804 1805 1808 1809 1810
               7
                         2
                            13
                                19
                                        2
                                            9
                                                 18
                                                      16
                                                           9
                                                              18
        10
                   20
                                                                    15
                                                                         19
## 1813 1814 1815 1816 1817 1818 1819 1820 1821 1822 1824 1826 1827 1831 1832 1835
         18
               6
                    6
                        15
                              6
                                   6
                                        8
                                           17
                                                 19
                                                      3
                                                          18
                                                               15
                                                                    19
                                                                          7
## 1836 1842 1845 1846 1850 1851 1852 1854 1855 1856 1863 1872 1873 1874 1877 1880
     8
         10
               2
                   17
                         6
                              7
                                   2
                                      7
                                             3
                                                 19
                                                     18
                                                          15
                                                               15
                                                                     3
                                                                         16
## 1881 1882 1885 1887 1890 1892 1900 1902
        15
               2
                    6
                         3
                             15
                                  17
##
## Within cluster sum of squares by cluster:
   [1] 10476.893 12984.858 12231.229 1854.231 6737.223 7534.825 10218.593
   [8] 7739.826 4903.815 4274.809 5091.740 1673.295 3656.989 5024.042
## [15] 11975.080 10699.877 12462.896 5463.272 6994.567 2667.258
##
   (between_SS / total_SS = 10.0 %)
## Available components:
##
```

```
## [1] "cluster" "centers" "totss" "withinss" "tot.withinss"
## [6] "betweenss" "size" "iter" "ifault"
## Warning: did *not* converge in specified number of iterations
```



We can see that K-Means clustering did yield clusters of genes that have similar properties and while the plots do look chaotic, we can attribute this to the number of dimensions associated with the data. From the PCA, we yielded about 100 genes to consider, and we use them all in our clustering analysis.

#### #HCLUSTERING

```
any(is.na(comp))
```

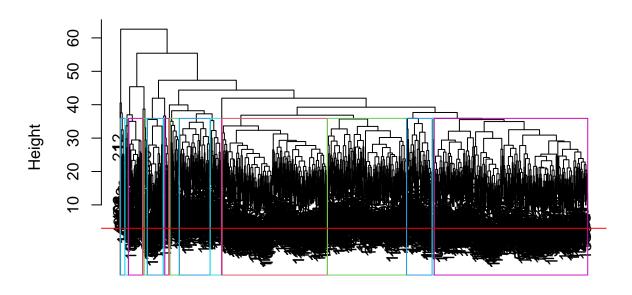
#### ## [1] FALSE

```
dist_mat <- dist(comp, method = 'euclidean')
#clust.euclid.average<- hclust(dist(comp), method="complete")
#plot(clust.euclid.average)
hclust_avg <- hclust(dist_mat, method = 'complete')
plot(hclust_avg)

cut_avg <- cutree(hclust_avg, k = 20)

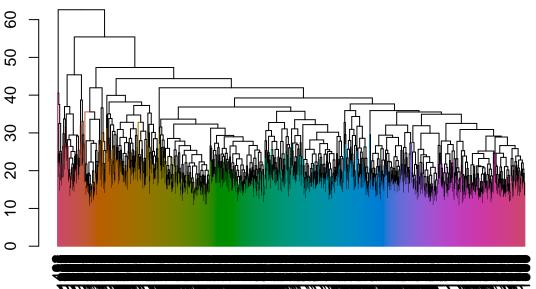
plot(hclust_avg)
rect.hclust(hclust_avg , k = 20, border = 2:6)
abline(h = 3, col = 'red')</pre>
```

# **Cluster Dendrogram**



dist\_mat
hclust (\*, "complete")

```
suppressPackageStartupMessages(library(dendextend))
avg_dend_obj <- as.dendrogram(hclust_avg)
avg_col_dend <- color_branches(avg_dend_obj, h = 3)
plot(avg_col_dend)</pre>
```



```
suppressPackageStartupMessages(library(dplyr))
seeds_df_cl <- mutate(cluster.data, cluster = cut_avg)
count(seeds_df_cl,cluster)</pre>
```

## cluster n

```
## 1
             1 272
## 2
                15
## 3
             3
                39
## 4
             4 362
## 5
## 6
             6
                32
## 7
             7
                  1
## 8
             8 106
## 9
             9 528
## 10
            10
                55
## 11
            11
                49
                88
## 12
            12
## 13
            13
                  4
                  2
## 14
            14
## 15
            15
                  5
## 16
                 5
            16
## 17
            17
                11
## 18
            18
                14
## 19
            19
                12
## 20
                 7
            20
```

suppressPackageStartupMessages(library(ggplot2))
ggplot(seeds\_df\_cl, aes(x=cluster.data\$mutation\_count, y = cluster.data\$tumor\_size, color = factor(seed

