



정보통신 수학 및 실습

Lab assignment



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편성 : 20조 2017년 5월 1일

Chapter 8 Lab Assignment

1. If the outlet is a pipe that discharges to atmospheric pressure p_a and provides a resistance, R , to flow that is proportional to the pressure difference across its ends, then find the outlet flow rate q_{mo} and the differential equation of $h(t)$. Hint: q_{mo} is $(1/R)^*$ (the pressure difference across its ends).

Now solve your differential equation of $h(t)$ using MATLAB and plot $h(t)$ against the time. The values of the parameters are as follows: (units are ignored)

$q_{mi} = 25$, $R = 5$, $A = 10$, $h(0) = 10$, $\rho = 2$.

$$q_{mo} = q_{mi} - \rho A \frac{dh}{dt} = \frac{1}{R} P = \frac{\rho h(t)}{R}$$

$$q_{mi} - \rho A \frac{dh(t)}{dt} = \frac{\rho h(t)}{R}$$

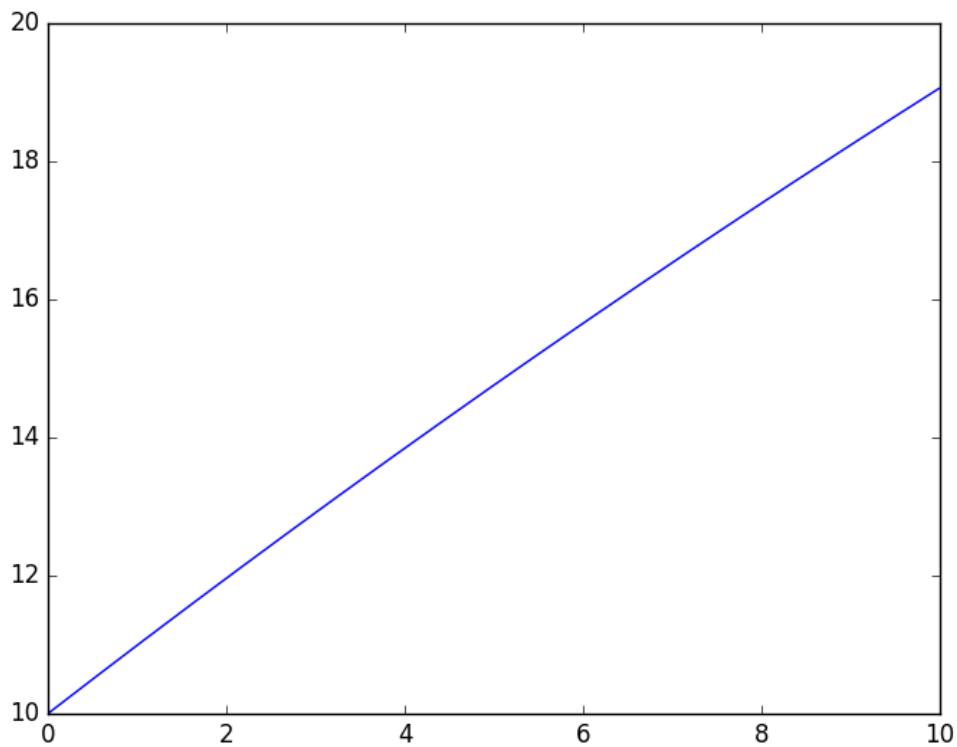
$$\frac{1}{A} \left(\frac{q_{mi}}{\rho} - \frac{h(t)}{R} \right) = \frac{dh(t)}{dt}$$

$$\frac{1}{A} \left(\frac{q_{mi}}{\rho} - \frac{h(t)}{R} \right) = \frac{h(t + \Delta t) - h(t)}{\Delta t}$$

$$h(t + \Delta t) = \frac{\Delta t}{A} \left(\frac{q_{mi}}{\rho} - \frac{h(t)}{R} \right) + h(t)$$

$$h(k + 1) = \frac{\Delta t}{A} \left(\frac{q_{mi}}{\rho} - \frac{h(k)}{R} \right) + h(k)$$

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k = 1
delta = 0.0001
h = [0: delta :0.1];
h(1) = 10
A = 10
qmi = 25
r = 2
R = 5
for t = [0: delta :0.1]
    h(k+1) = delta / A * (qmi / r - h(k) / R) + h(k)
    k = k + 1
end
plot(t, h(1, end-1))
```



2. Solve the following 2 order differential equation using MATLAB.

$$y'' + 2y' + y = 0, y(0) = 1, y'(0) = 3$$

$$y''(t) + 2y'(t) + y(t) = 0$$

$$y'(t) = z(t)$$

$$\frac{y(t + \Delta t) - y(t)}{\Delta t} = z(t)$$

$$y(k + 1) = z(k)\Delta t + y(k)$$

$$z'(t) + 2z(t) + y(t) = 0$$

$$\frac{z(t + \Delta t) - z(t)}{\Delta t} + 2z(t) + y(t) = 0$$

$$z(k + 1) = -\Delta t(2z(k) + y(k)) + z(k)$$

$$z(0) = 3$$

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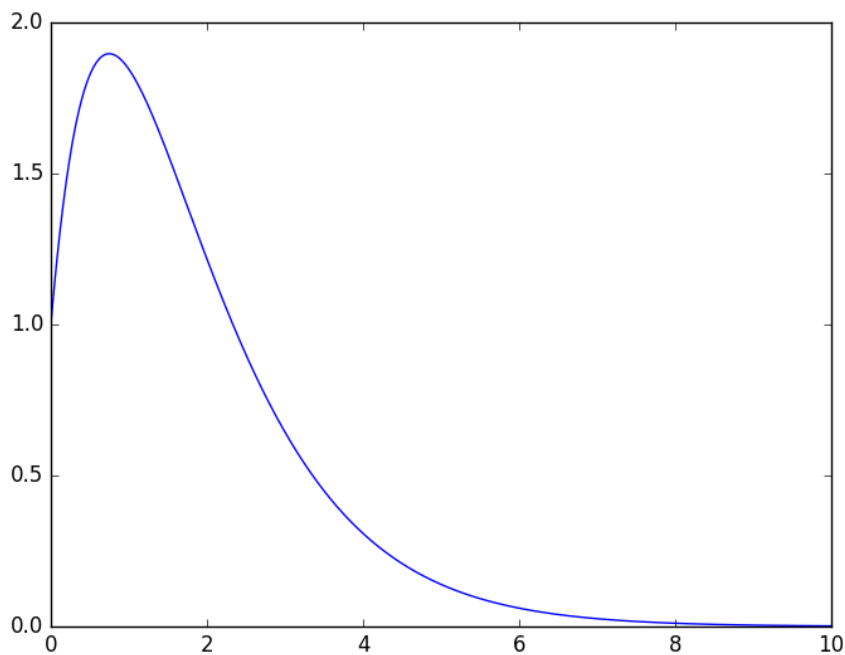
delta = 0.01
t = [0: delta :10];
z(1) = 3;
y(1) = 1;
k = 1
for x = [0: delta :10]
    y(k+1) = delta * z(k) + y(k);
    z(k+1) = -delta * (2 * z(k) + y(k)) + z(k);

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    k = k+1;
end
plot(t, y(1,end-1), 'r')

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3. For the following differential equation, solve the response $y[n]$ when $x[n]$ is the sampling values of $\sin(2 \cdot \pi \cdot t)$, $0 \leq t \leq 2 \cdot \pi$, $\Delta t = 0.01$. Plot $y[n]$ and $x[n]$ against n .
- $$y[n] = 0.7 \cdot x[n] + 0.3 \cdot x[n-1]$$

