



정보통신 수학 및 실습 Homework



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Chapter 7 Homework

1. Let $\mathbf{v} = (a, b, c)$ and $\mathbf{w} = (3a, 3b, 3c)$ be vectors. Show that $\|\mathbf{w}\| = 3\|\mathbf{v}\|$

$$3\sqrt{a^2 + b^2 + c^2} = \sqrt{9a^2 + 9b^2 + 9c^2}$$

2. Let $\mathbf{v} = (1, 5, 2)$ and $\mathbf{w} = (3, 1, 1)$.

a) Find $\mathbf{v} - \mathbf{w}$

$$(-1-3, 5-1, -2-1) = (-4, 4, -3)$$

b) Find $\mathbf{v} + \mathbf{w}$.

$$(2, 6, -1)$$

c) Find $\mathbf{v} / \|\mathbf{w}\|$

$$\|\mathbf{w}\| = \sqrt{9 + 1 + 1} = \sqrt{11}$$

$$(1/\sqrt{11}, 5/\sqrt{11}, 2/\sqrt{11})$$

d) Find $\frac{1}{2} \|\mathbf{v} - \mathbf{w}\|$

$$\frac{1}{2}\sqrt{16 + 16 + 9} = \frac{1}{2}\sqrt{41}$$

e) Find $\frac{1}{2} \|\mathbf{v} + \mathbf{w}\|$

$$\frac{1}{2}\sqrt{4 + 36 + 1} = \frac{1}{2}\sqrt{41}$$

f) Find the vector \mathbf{u} such that $\mathbf{u} + \mathbf{v} + \mathbf{w} = 2\mathbf{j} + \mathbf{k}$.

$$\mathbf{u} + \mathbf{v} + \mathbf{w} = (0, 2, 1)$$

$$\mathbf{u} = (0, 2, 1) - (2, 6, -1)$$

$$\mathbf{u} = (-2, -4, 2)$$

3. Let $\mathbf{v} = -3\mathbf{i} - 2\mathbf{j} - \mathbf{k}$ and $\mathbf{w} = 6\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}$. Calculate $\mathbf{v} - \mathbf{w}$.

$$(-3, -2, -1) - (6, 4, 2) = (-9, -6, -3)$$

4. Let $\mathbf{v} = (8, 4, 3)$ and $\mathbf{w} = (-2, 1, 4)$. Is $\mathbf{v} \perp \mathbf{w}$? Justify your answer.

$$\mathbf{v} \cdot \mathbf{w} = -16 + 4 + 12 = 0 = \|\mathbf{v}\| \|\mathbf{w}\| \cos\theta$$

$$\therefore \cos\theta = 0$$

$$\therefore \theta = \frac{\pi}{2}$$