
Algorithm 1 Q- λ learning

```
1: function QLAMBDALEARNING( $\alpha, \gamma, \lambda$ )
2:   Initialize  $\theta$ , hidden state  $x_0$  and belief state  $b_0$ 
3:    $t \leftarrow 0$ 
4:    $a_0, a_0^* \leftarrow \text{CHOOSEACTION}(\theta, b_0)$ 
5:    $\xi_0 \leftarrow \text{GRIDWEIGHTS}(b_0, a_0^*)$ 
6:    $e \leftarrow \mathbf{0}$ 
7:   loop
8:     Observe reward  $r_t$  and observation  $y_{t+1}$ 
9:      $b_{t+1} \leftarrow \text{UPDATEBELIEFSTATE}(b_t, a_t, y_{t+1})$ 
10:     $a_t, a_t^* \leftarrow \text{CHOOSEACTION}(\theta, b_t)$ 
11:    if  $a_t \neq a_t^*$  then
12:       $e \leftarrow \mathbf{0} + \xi_t$ 
13:    else
14:       $e \leftarrow e + \xi_t$ 
15:       $\xi_{t+1} \leftarrow \text{GRIDWEIGHTS}(b_t, a_t)$ 
16:       $\xi_{t+1}^* \leftarrow \text{GRIDWEIGHTS}(b_t, a_t^*)$ 
17:       $\delta \leftarrow r_t + \gamma \cdot \theta^T \xi_{t+1}^* - \theta^T \xi_t$ 
18:       $\theta \leftarrow \theta + \alpha \cdot \delta \cdot e$ 
19:       $e \leftarrow \gamma \cdot \lambda \cdot e$ 
20:       $t \leftarrow t + 1$ 

21: function CHOOSEACTION( $\theta, b$ )  $\triangleright \epsilon$ -greedy
22:    $a^* \leftarrow \arg \max_a \theta^T [\text{GRIDWEIGHTS}(b, a)]$ 
23:   if Uniform(0,1)  $\leq \epsilon$  then
24:      $a \leftarrow$  random action
25:   else
26:      $a \leftarrow a^*$ 
27:   return  $a, a^*$ 

28: function GRIDWEIGHTS( $b, a$ )
29:    $\xi \leftarrow \mathbf{0}$ 
30:   for each particle  $p \in b$  do
31:      $\xi_a \leftarrow \xi_a + \text{INTERPOLANTS}(p)$ 
32:    $\xi \leftarrow \frac{\xi}{\sum_{a,i} (\xi_{ai})}$ 
33:    $\xi_{a \ i+1} \leftarrow \text{var}(\xi)$ 
34:   return  $\xi$ 
```

Algorithm 2 Modified Upper Confidence Bound for Trees

```
1: function SELECTACTION( $b, d$ )
2:   Initialize  $Q$  and  $N$ 
3:    $s \leftarrow$  random state from belief state  $b$ 
4:   loop
5:     SIMULATE( $s, d$ )
6:   return  $\arg \max_a Q(a)$ 
```

```
7: function SIMULATE( $s, d$ )
8:   if  $d = 0$  then
9:     return 0
10:  if  $S \notin T$  then
11:    for  $a \in A(s)$  do
12:       $(N(a), Q(a)) \leftarrow (N_0(a), Q_0(a))$ 
13:     $T = T \cup \{s\}$ 
14:    return ROLLOUT( $s, d$ )
15:   $a \leftarrow$  CHOOSEACTION( $s$ )
16:   $(s', r) \sim G(s, a)$ 
17:   $q \leftarrow r + \gamma \text{SIMULATE}(s', d - 1)$ 
18:   $N(a) \leftarrow N(a) + 1$ 
19:   $Q(a) \leftarrow Q(a) + \frac{q - Q(a)}{N(a)}$ 
```

```
20: function ROLLOUT( $s, d$ )
21:  if  $d = 0$  then
22:    return 0
23:   $a \leftarrow$  random action  $a \in A$ 
24:   $(s', r) \sim G(s, a)$ 
25:  return  $r + \gamma \text{ROLLOUT}(s', d - 1)$ 
```

```
26: function CHOOSEACTION( $s$ )
27:  for  $a \in A$  do
28:    if  $N(s, a) = 0$  then return  $a$ 
29:  return  $\arg \max_a Q(a) + c \sqrt{\frac{\log(\sum_a N(a))}{N(a)}}$ 
```
