

Identificación de perfiles estudiantiles con técnicas de clustering

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```
rm(list=ls())
library(dplyr)

## 
## Adjuntando el paquete: 'dplyr'

## The following objects are masked from 'package:stats':
## 
##     filter, lag

## The following objects are masked from 'package:base':
## 
##     intersect, setdiff, setequal, union

library(fastDummies)

## Warning: package 'fastDummies' was built under R version 4.4.2

library(grid)
library(cluster)
library(factoextra)

## Cargando paquete requerido: ggplot2

## Warning: package 'ggplot2' was built under R version 4.4.3

## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa

library(caret)

## Warning: package 'caret' was built under R version 4.4.2

## Cargando paquete requerido: lattice

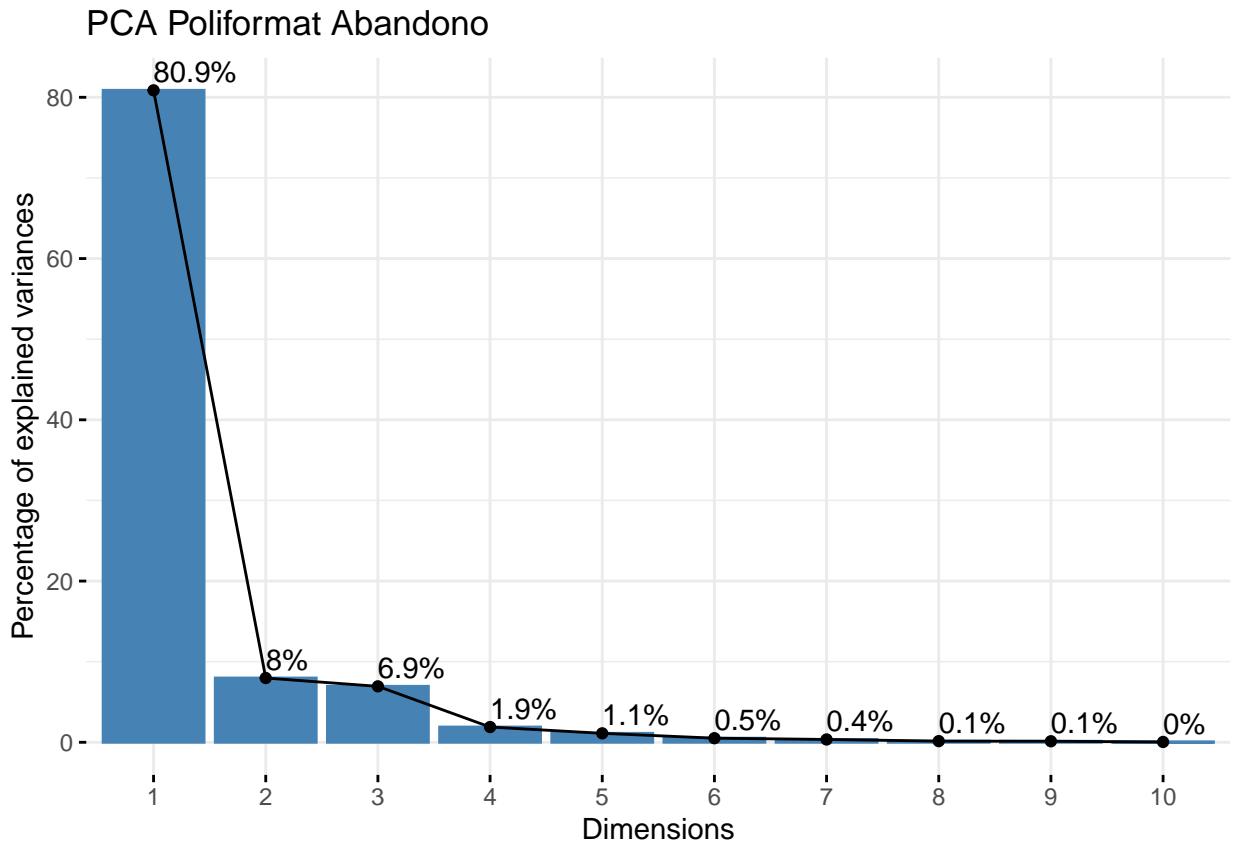
library(gridExtra)

## 
## Adjuntando el paquete: 'gridExtra'
```

```
## The following object is masked from 'package:dplyr':  
##  
##      combine  
  
load("../Datos/Capítulos/Caracterización.Rdata")
```

Preparar y concatenar

```
num_vars <- poliformat[poliformat$abandono==1, ] %>% select(where(is.numeric))  
  
## Adding missing grouping variables: 'dni_hash'  
  
num_vars= num_vars[,2:length(num_vars)]  
  
datos_pca <- num_vars  
  
preprocess <- preProcess(datos_pca, method = "medianImpute")  
datos_imputados <- predict(preprocess, newdata = datos_pca)  
  
datos_filtrados <- datos_imputados[, sapply(datos_imputados, function(col) var(col, na.rm = TRUE) != 0)]  
  
pca_poliformat <- prcomp(datos_filtrados, scale. = TRUE)  
  
fviz_eig(pca_poliformat, addlabels = TRUE, main="PCA Poliformat Abandono")
```



```
ambas=academicas[academicas$abandono==1,] %>% left_join(sociodemografia[academicas$abandono==1,], by="dn

numeric_vars <- ambas %>% select(where(is.numeric))
categorical_vars <- ambas %>% select(where(~is.factor(.)))

categorical_dummy <- fastDummies::dummy_cols(categorical_vars, remove_first_dummy = TRUE, remove_select=TRUE)

combined <- bind_cols(numeric_vars, categorical_dummy)

combined$actividades <- NULL

combined$nota14[is.na(combined$nota14)] <- median(combined$nota14, na.rm = TRUE)

combined <- combined %>%
  select(-rend_total_ultimo, -rend_total_penultimo, -rend_total_antepenultimo)
```

```

combined_scaled <- scale(combined)

pca_df=pca_poliformat$x[,1:3]

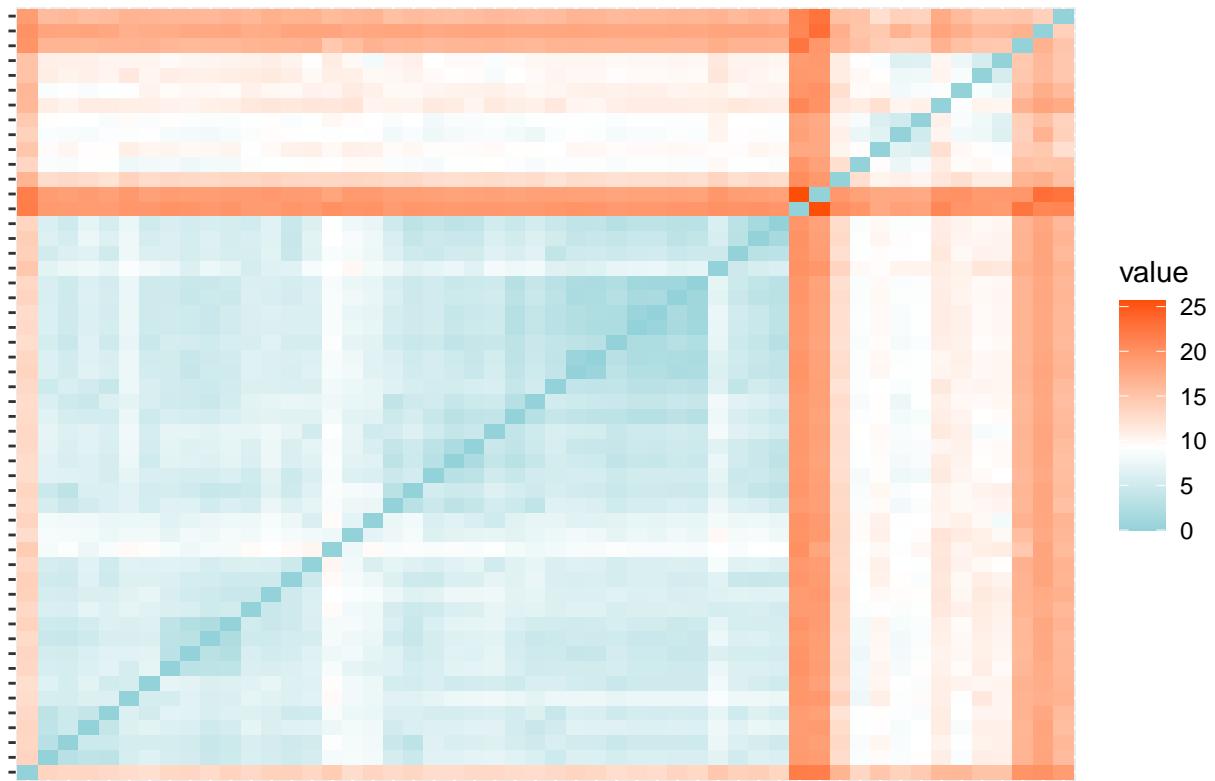
final_dataset <- as.data.frame(cbind(combined_scaled, pca_df))
final_dataset <- final_dataset[, colSums(is.na(final_dataset)) < nrow(final_dataset)]

rownames(final_dataset)=1:52

midist <- get_dist(final_dataset, stand = TRUE, method = "euclidean")
fviz_dist(midist, show_labels = TRUE, lab_size = 0.3,
          gradient = list(low = "#00AFBB", mid = "white", high = "#FC4E07"))+labs(title = "Distancia or"

```

Distancia original euclídea



```

set.seed(10)
myN = c(7,25,37) # m
myhopkins = NULL
myseed = sample(1:52, 2)
for (i in myN) {
  for (j in myseed) {
    tmp = get_clust_tendency(data = final_dataset, n = i, graph = FALSE, seed = j)
    myhopkins = c(myhopkins, tmp$hopkins_stat)
  }
}

```

```

}

summary(myhopkins)

##      Min. 1st Qu. Median    Mean 3rd Qu.    Max.
## 0.7353 0.7629 0.7902 0.7801 0.7961 0.8128

```

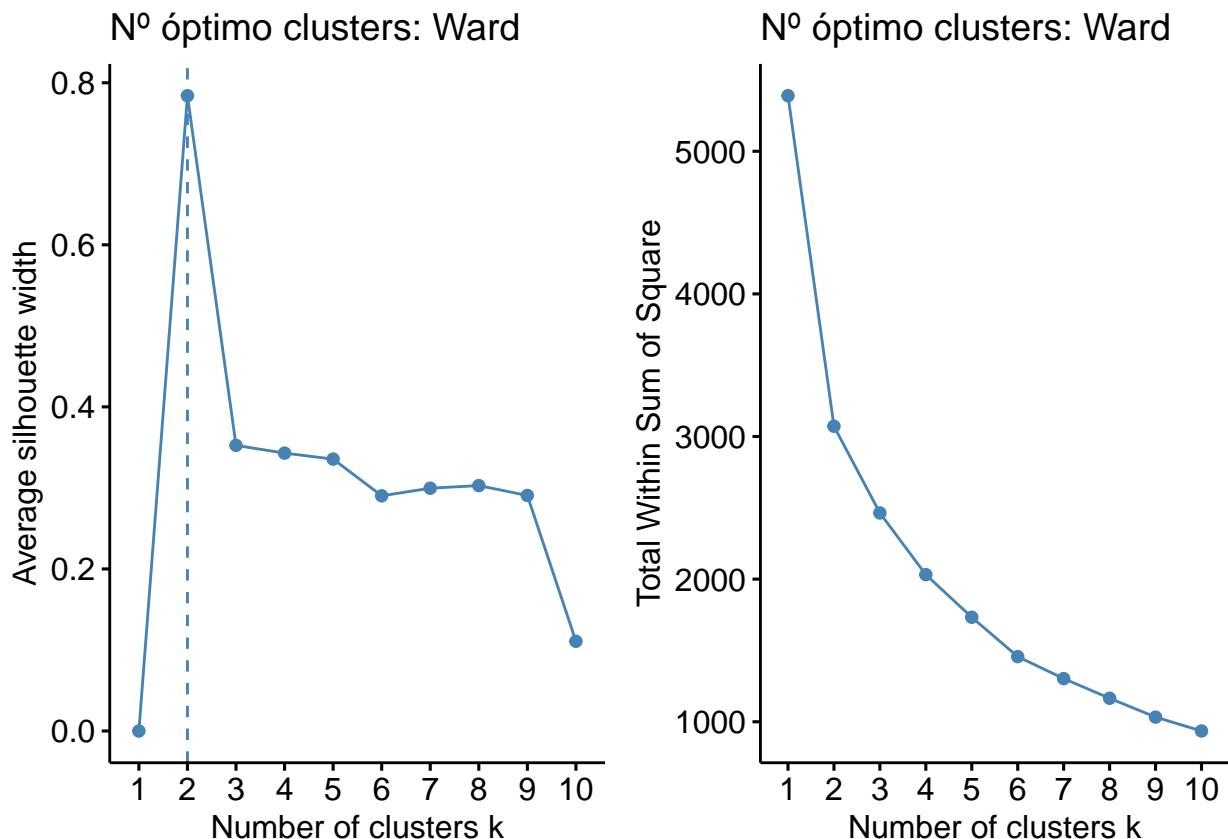
```
datos_elegidos=final_dataset
```

Método de Ward

```

p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "silhouette",
                   hc_method = "ward.D2", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Ward")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "wss",
                   hc_method = "ward.D2", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Ward")
grid.arrange(p1, p2, nrow = 1)

```



```

K=4

clust1 <- hclust(midist, method="ward.D2")
grupos1 <- cutree(clust1, k=K)

fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,

```

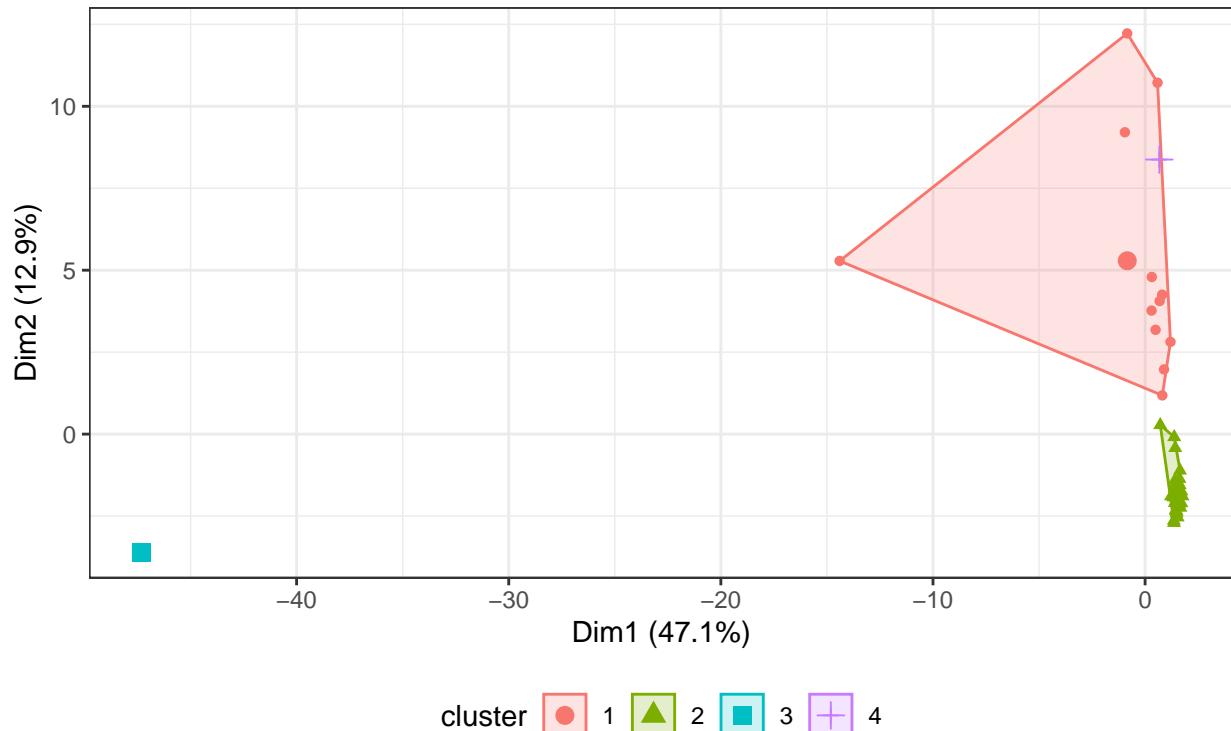
```

    ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
    labelsize = 8) +
  labs(title = "Modelo jerarquico + Proyeccion PCA",
       subtitle = "Dist euclidea, Metodo de Ward, K=2") +
  theme_bw() +
  theme(legend.position = "bottom")

```

Modelo jerarquico + Proyeccion PCA

Dist euclidea, Metodo de Ward, K=2

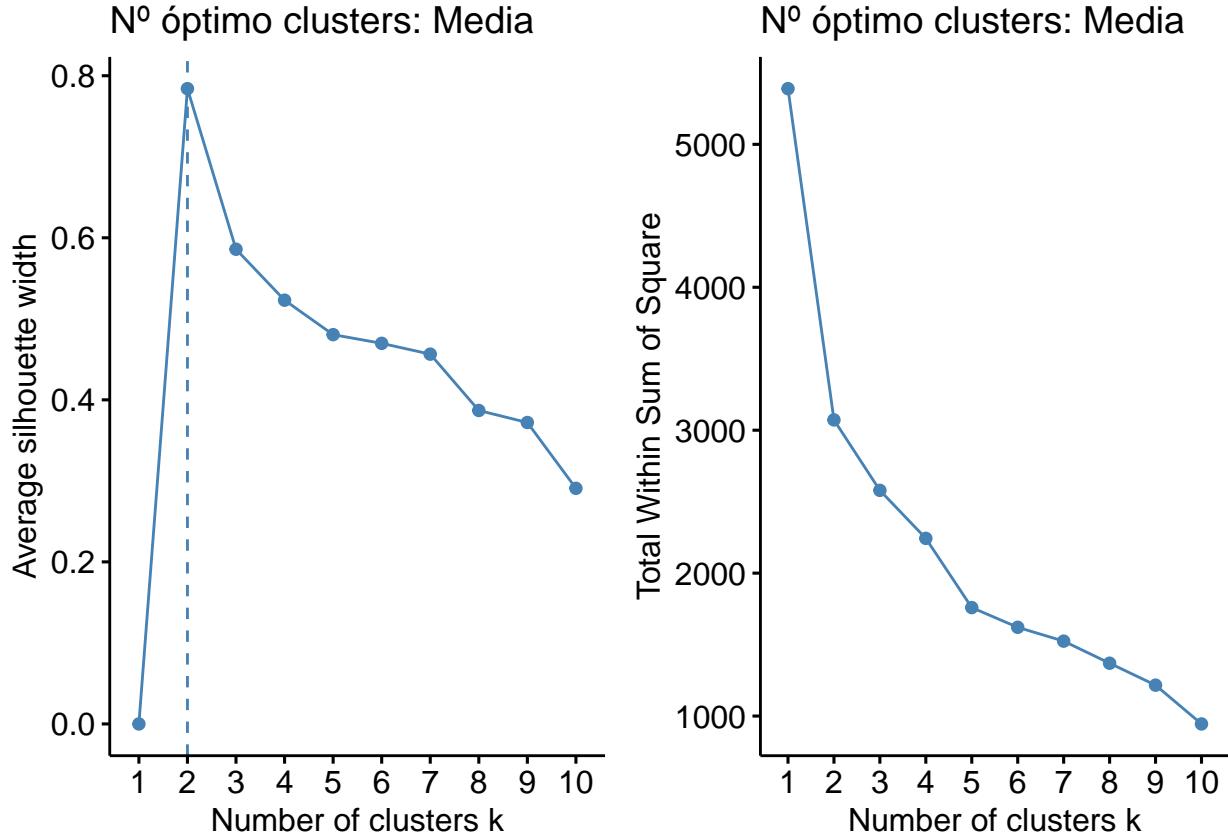


Método de la media

```

p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "silhouette",
                   hc_method = "average", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Media")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "wss",
                   hc_method = "average", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Media")
grid.arrange(p1, p2, nrow = 1)

```



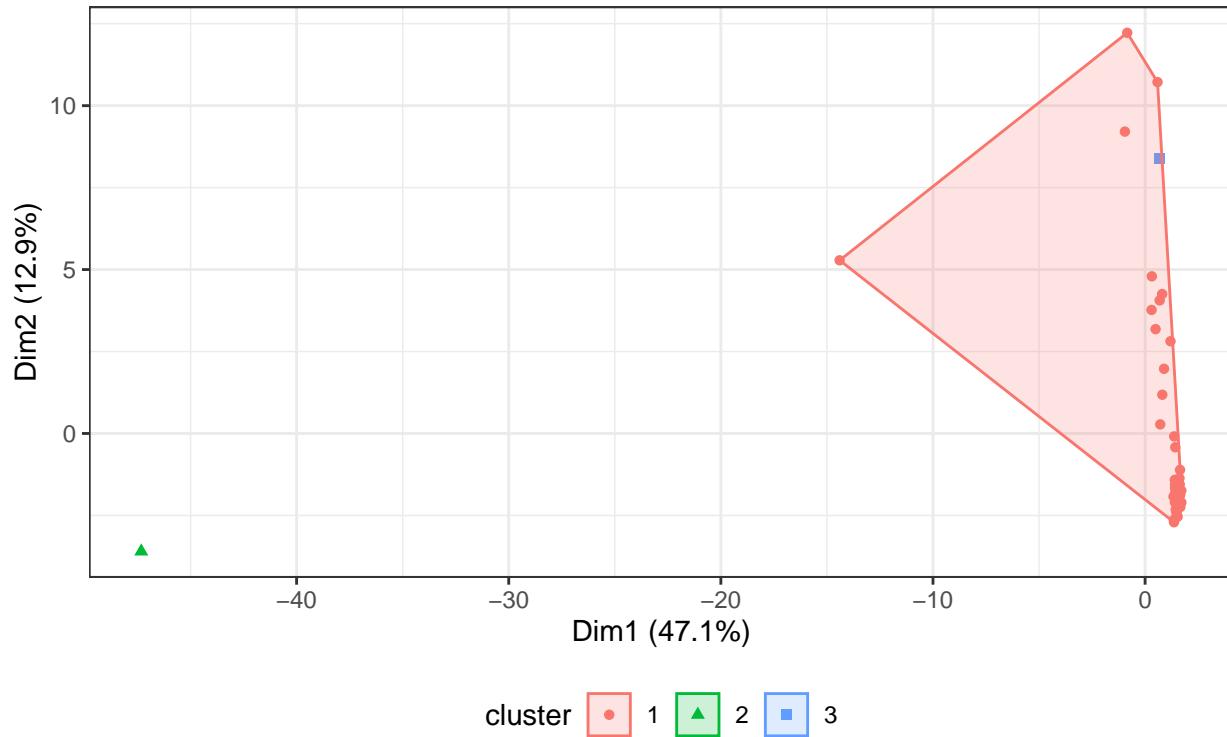
K=3

```
clust1 <- hclust(midist, method="average")
grupos1 <- cutree(clust1, k=K)

fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,
             ellipse.type = "convex", geom = "point", show.clust.cent = FALSE,
             labelsize = 8) +
  labs(title = "Modelo jerarquico + Proyeccion PCA",
       subtitle = "Dist euclidea, Metodo Media, K=3") +
  theme_bw() +
  theme(legend.position = "bottom")
```

Modelo jerarquico + Proyeccion PCA

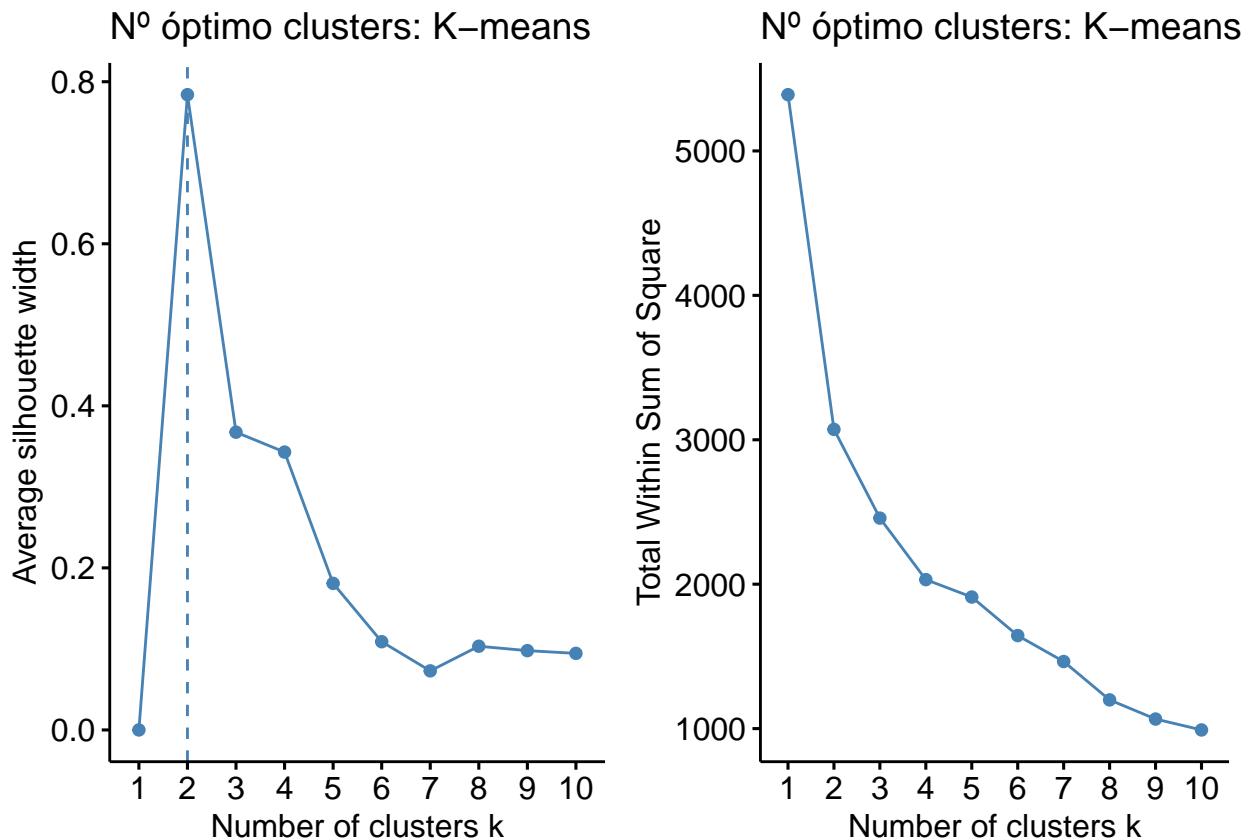
Dist euclidea, Metodo Media, K=3



Partición

k-means

```
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = kmeans, method = "silhouette",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: K-means")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = kmeans, method = "wss",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: K-means")
grid.arrange(p1, p2, nrow = 1)
```



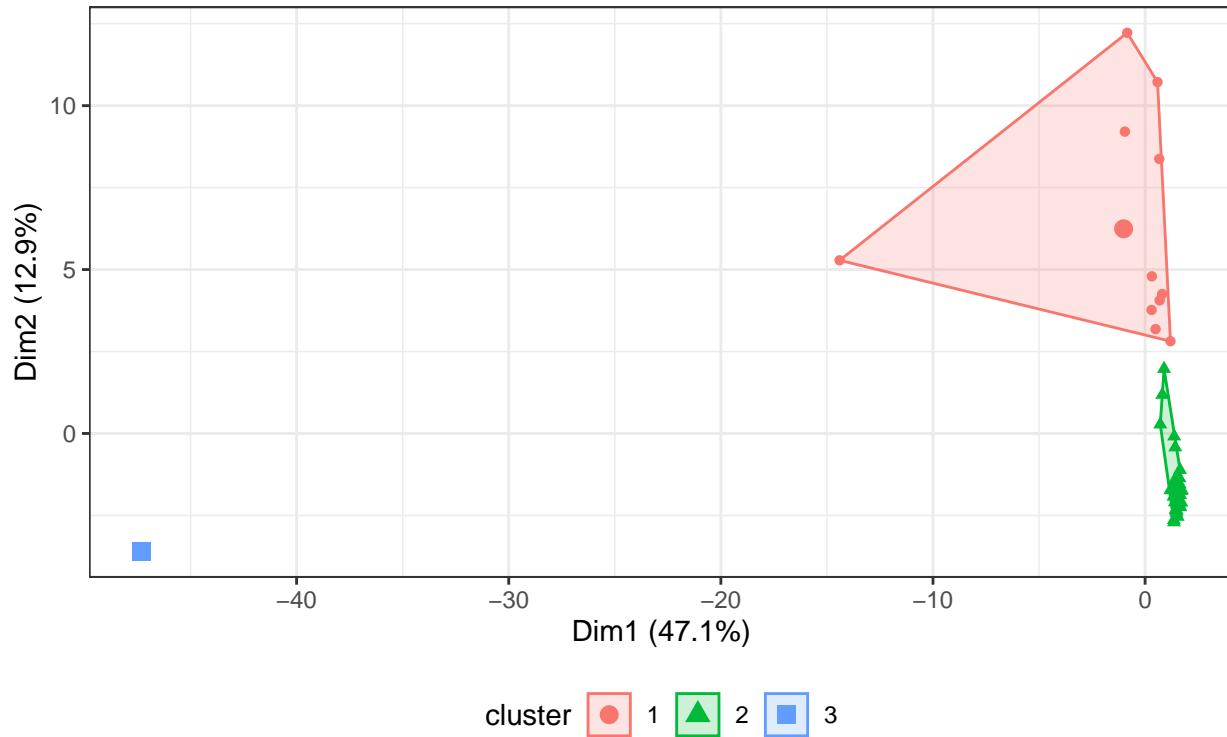
```
k=3
clust3 <- kmeans(datos_elegidos, centers = k, nstart = 20)

p1 = fviz_cluster(object = list(data=datos_elegidos, cluster=clust3$cluster), stand = FALSE,
                  ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
                  labelsize = 8) +
  labs(title = "K-MEDIAS + Proyeccion PCA",
       subtitle = "Dist euclidea, K=3") +
  theme_bw() +
  theme(legend.position = "bottom")

grid.arrange(p1,nrow = 1)
```

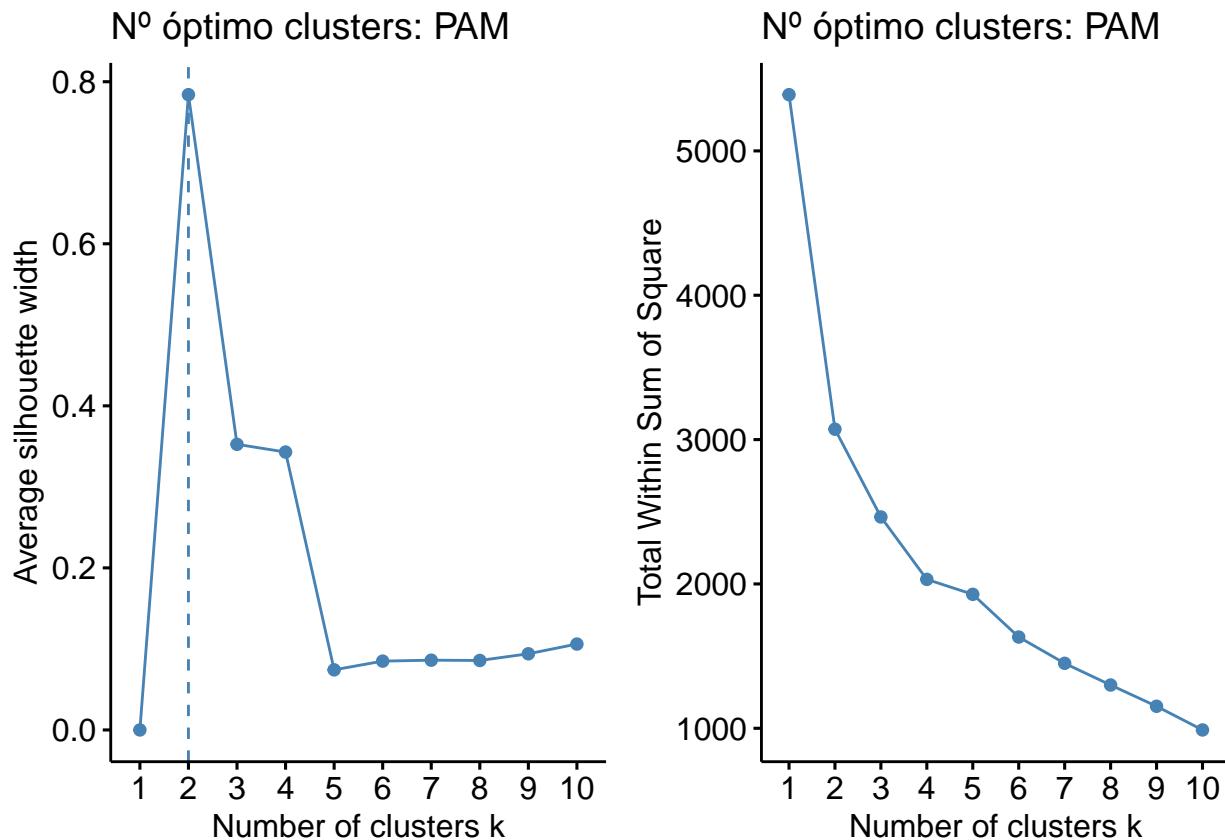
K-MEDIAS + Proyeccion PCA

Dist euclidea, K=3



pam

```
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = pam, method = "silhouette",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: PAM")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = pam, method = "wss",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: PAM")
grid.arrange(p1, p2, nrow = 1)
```



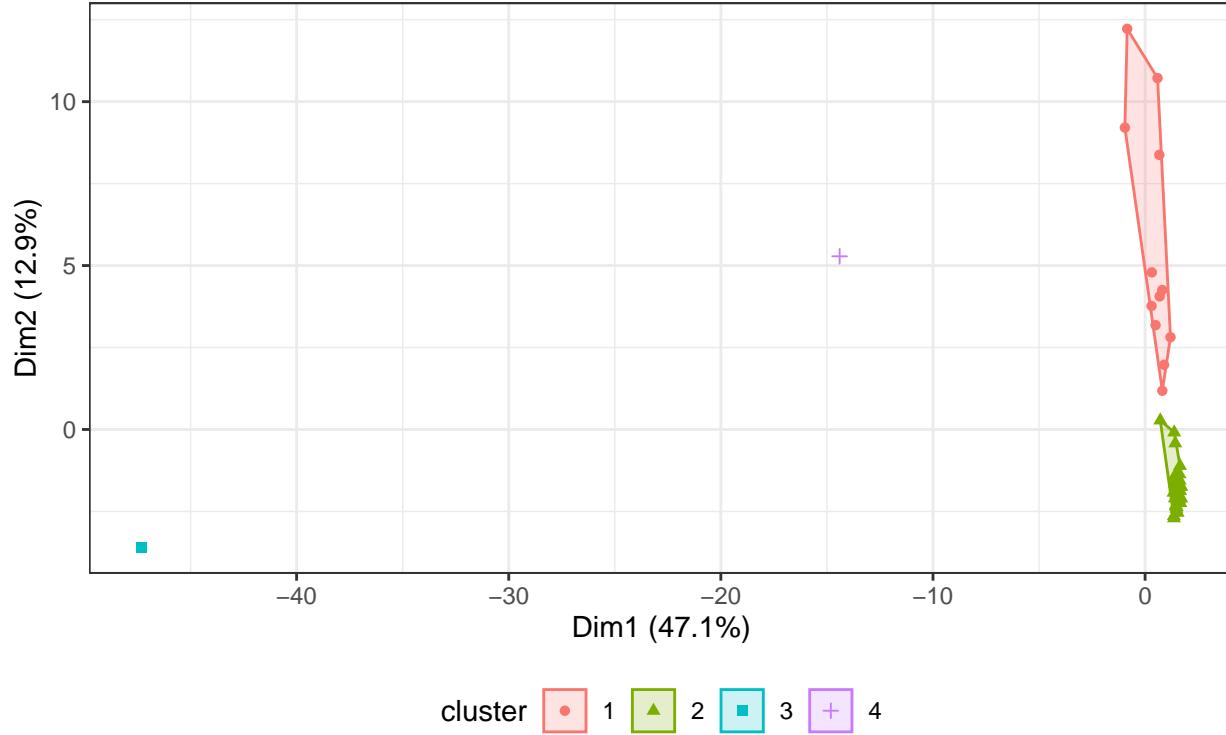
```
k=4
clust4 <- pam(datos_elegidos, k = k)
table(clust4$clustering)
```

```
##
##   1   2   3   4
## 12 38   1   1
```

```
p1 = fviz_cluster(object = list(data=datos_elegidos, cluster=clust4$clustering), stand = FALSE,
                   ellipse.type = "convex", geom = "point", show.clust.cent = FALSE,
                   labelsize = 8) +
  labs(title = "K-MEDOIDES + Proyeccion PCA",
       subtitle = "Dist euclidea, K=7") +
  theme_bw() +
  theme(legend.position = "bottom")
grid.arrange(p1,nrow = 1)
```

K-MEDOIDES + Proyección PCA

Dist euclidea, K=7



Cuáles son esos dos estudiantes porsaqueros?

```
cluster_sizes <- table(clust4$clustering)
outlier_clusters <- names(cluster_sizes[cluster_sizes == 1])

outlier_ids <- which(clust4$clustering %in% outlier_clusters)

datos_elegidos[outlier_ids, ]

##    cred_mat1  cred_mat2  cred_mat3  cred_mat4  cred_sup_espec  cred_sup
## 29 -1.785002 -0.1247317  4.772668 -0.2652387      -0.138675 -0.138675
## 32 -1.785002  1.0260189  2.044395 -0.2652387      -0.138675 -0.138675
##    cred_mat_normal  cred_ptes_acta  cred_mat_sem_a  cred_mat_sem_b  cred_mat_anu
## 29      6.3207794     6.3207794     1.9260983     3.5526505     -0.4017367
## 32     -0.2136248     -0.2136248     -0.4831793     -0.6291645     1.2052102
##    cred_mat_total anyo_inicio_estudios  cred_sup_1o  cred_sup_2o  cred_sup_3o
## 29      4.0531458          -0.5336537     1.785002     2.491429     -0.3485026
## 32      0.1177262          -1.5247250     1.785002     1.612824     1.5882141
##    cred_sup_4o  practicas  cred_sup_tit  data_nac alta_universitat anyo_ingreso
## 29     -0.2426124     -0.2450451     1.529163 -0.3810125      -0.1408913     -0.5336537
## 32     -0.2426124     -0.2450451     1.590851 -0.7058101      -0.6642017     -1.5247250
##    nota10    nota14 curso_mas_bajo_2 curso_mas_alto_2 curso_mas_alto_3
## 29     -0.7470751     -0.5044405     4.9516897      -0.138675      4.0024031
## 32     -0.8894307     -0.8119763      -0.1980676      -0.138675     -0.2450451
```

```

##      es_adaptado_1 nacionalitat_XXX     sexe_V prov_origen_ESPANYA
## 29      -0.138675          -0.138675 0.4222815          -0.4832354
## 32      -0.138675          -0.138675 0.4222815          -0.4832354
## tipo_ingreso_BMA tipo_ingreso_NAP estudios_p_3 estudios_p_4 estudios_p_5
## 29      -1.631591          1.631591 -0.5129651  -0.7514555   1.2032465
## 32      -1.631591          1.631591  1.9119609  -0.7514555  -0.8151025
## estudios_p_6 estudios_m_2 estudios_m_3 estudios_m_4 estudios_m_5
## 29      -0.138675          -0.138675 -0.357668  -0.7205767  0.9529531
## 32      -0.138675          -0.138675 -0.357668  -0.7205767  0.9529531
## dedicacion_TP desplazado_1 discapacidad_1 becado_2 preferencia_seleccion_2
## 29      -0.2450451         -0.7205767 -0.138675  7.072428    -0.3230126
## 32      -0.2450451         -0.7205767 -0.138675 -0.138675    -0.3230126
## preferencia_seleccion_3 preferencia_seleccion_Baja
## 29          -0.5424304          -0.6602253
## 32          -0.5424304          -0.6602253
## preferencia_seleccion_Desconocido mes_julio mes_septiembre mes_octubre
## 29          -0.1980676 -0.8819589  -0.7829309  -0.3230126
## 32          -0.1980676 -0.8819589  -0.7829309  -0.3230126
## mes_diciembre      PC1      PC2      PC3
## 29      -0.1980676 -44.67668 -3.951647 -2.393982
## 32      4.9516897 -14.19229 11.819561  7.025431

datos_filtrados <- final_dataset[-outlier_ids, ]

ambas=ambas[-outlier_ids, ]

```

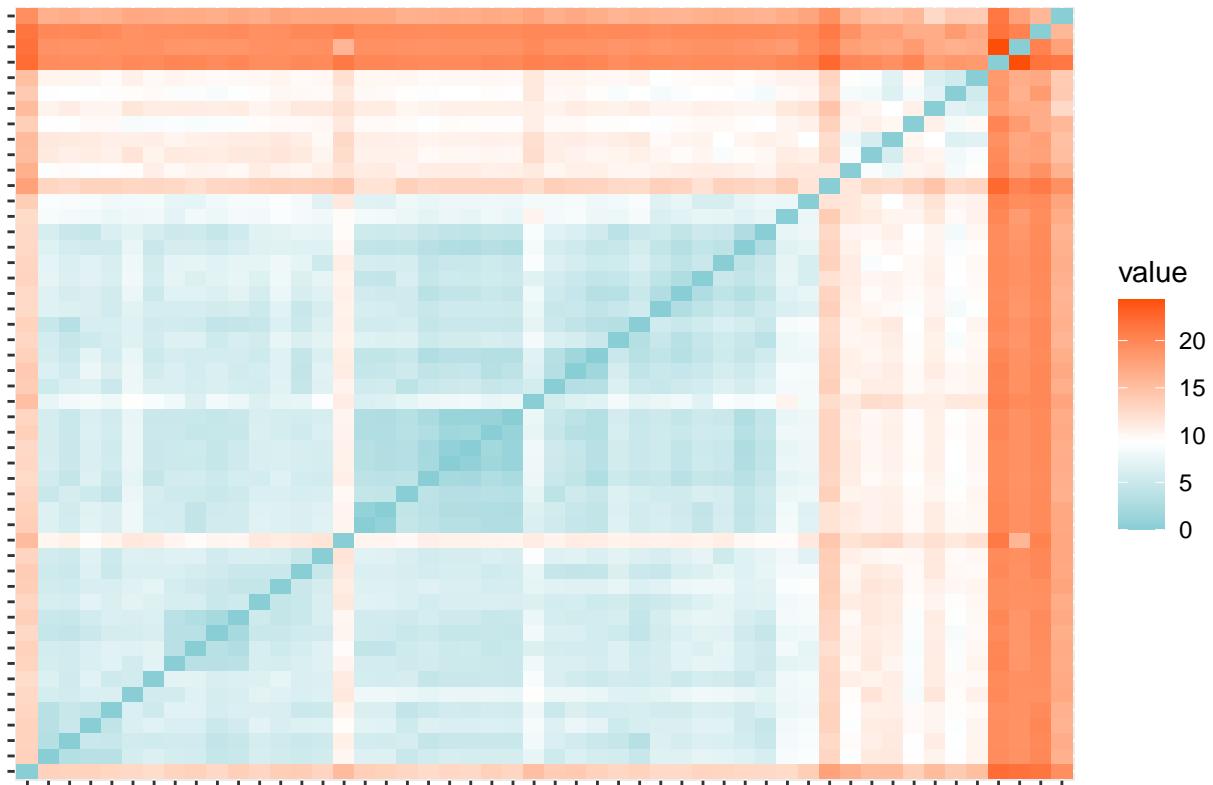
Filtrado

```

midist <- get_dist(datos_filtrados, stand = TRUE, method = "euclidean")
fviz_dist(midist, show_labels = TRUE, lab_size = 0.3,
          gradient = list(low = "#00AFBB", mid = "white", high = "#FC4E07"))+labs(title = "Distancia eu"

```

Distancia euclídea sin outliers



```
set.seed(10)
myN = c(7,25,37) # m
myhopkins = NULL
myseed = sample(1:52, 2)
for (i in myN) {
  for (j in myseed) {
    tmp = get_clust_tendency(data = datos_filtrados, n = i, graph = FALSE, seed = j)
    myhopkins = c(myhopkins, tmp$hopkins_stat)
  }
}
summary(myhopkins)
```

```
##      Min. 1st Qu. Median      Mean 3rd Qu.      Max.
## 0.7682  0.7767  0.7985  0.8042  0.8223  0.8603
```

```
datos_elegidos=datos_filtrados
```

```
K=1
```

```
clust1 <- hclust(midist, method="ward.D2")
grupos1 <- cutree(clust1, k=K)

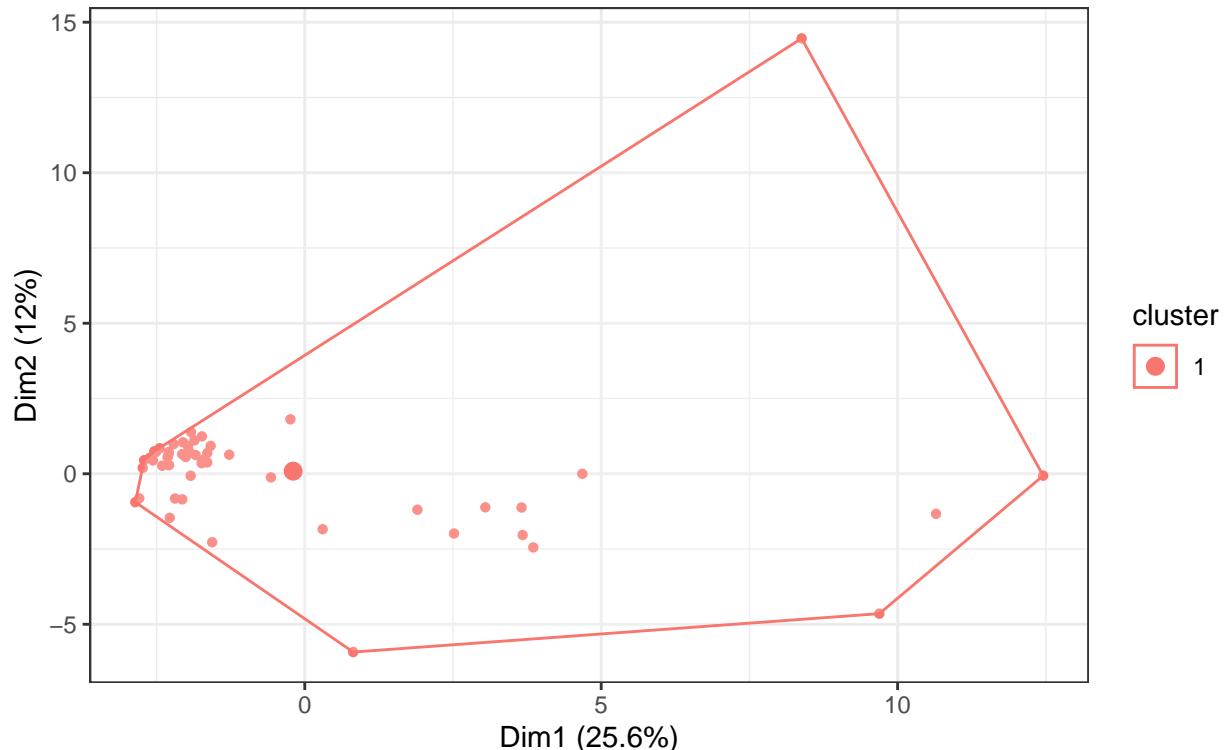
fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,
             ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
             labelsize = 8) +
```

```

  labs(title = "Proyección previa",
       subtitle = "Dist euclidea, Metodo Ward, K=1") +
  theme_bw()

```

Proyección previa
Dist euclidea, Metodo Ward, K=1



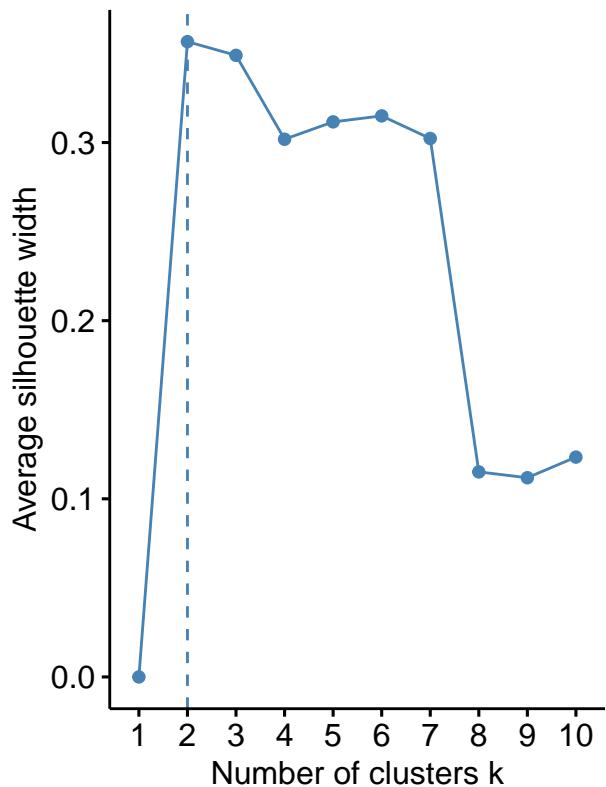
Método de Ward

```

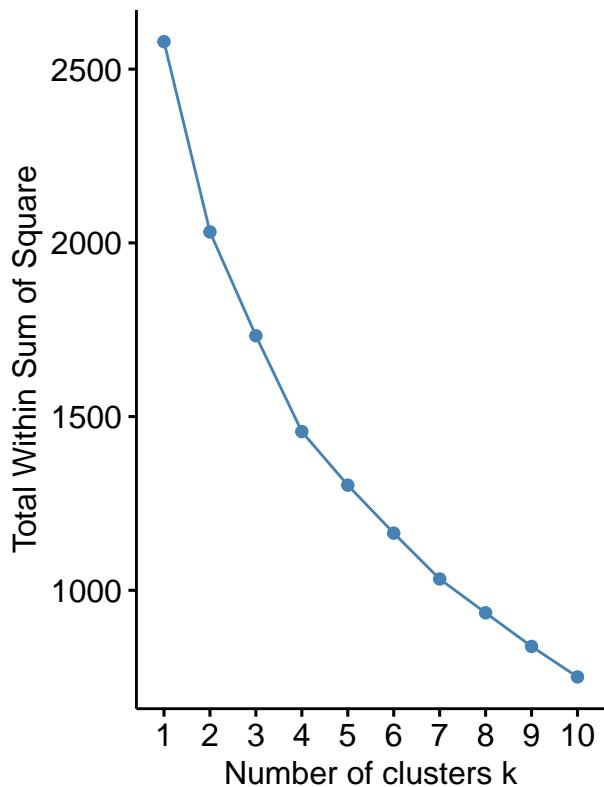
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "silhouette",
                   hc_method = "ward.D2", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Ward")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "wss",
                   hc_method = "ward.D2", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Ward")
grid.arrange(p1, p2, nrow = 1)

```

Nº óptimo clusters: Ward



Nº óptimo clusters: Ward



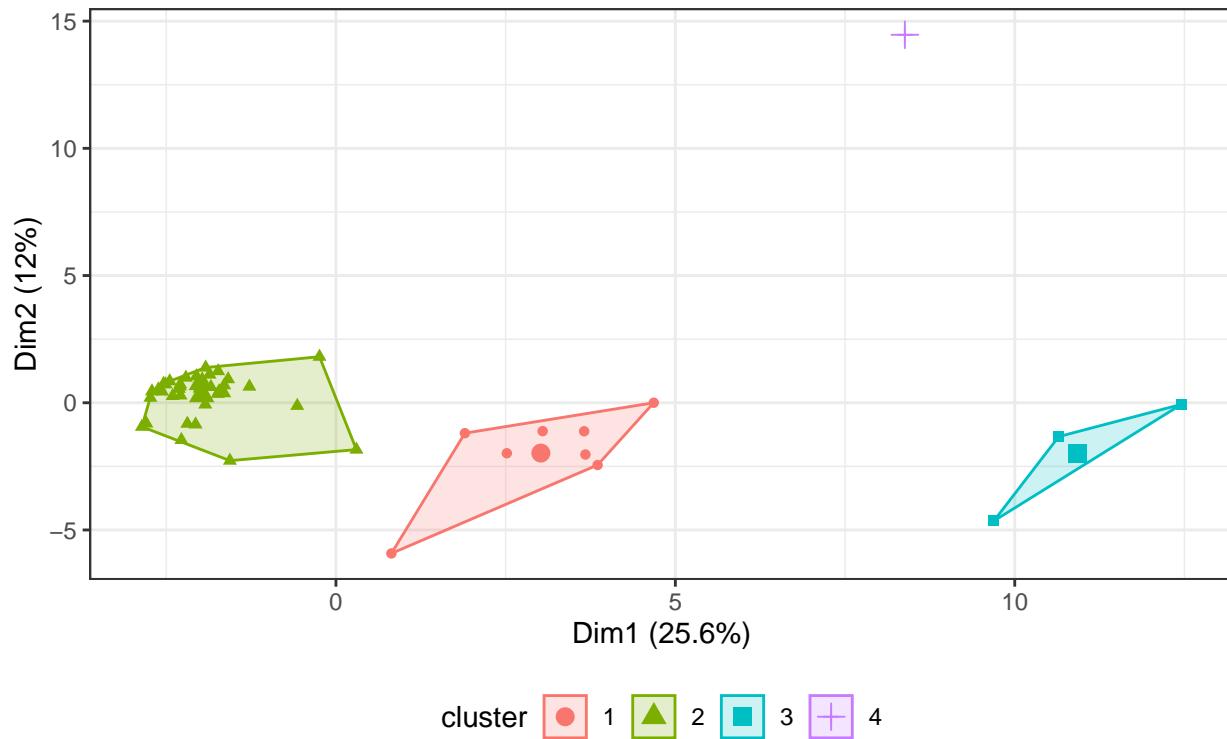
K=4

```
clust1 <- hclust(midist, method="ward.D2")
grupos1 <- cutree(clust1, k=K)

fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,
             ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
             labelsize = 8) +
  labs(title = "Modelo jerarquico + Proyeccion PCA",
       subtitle = "Dist euclidea, Metodo Ward, K=4") +
  theme_bw() +
  theme(legend.position = "bottom")
```

Modelo jerarquico + Proyeccion PCA

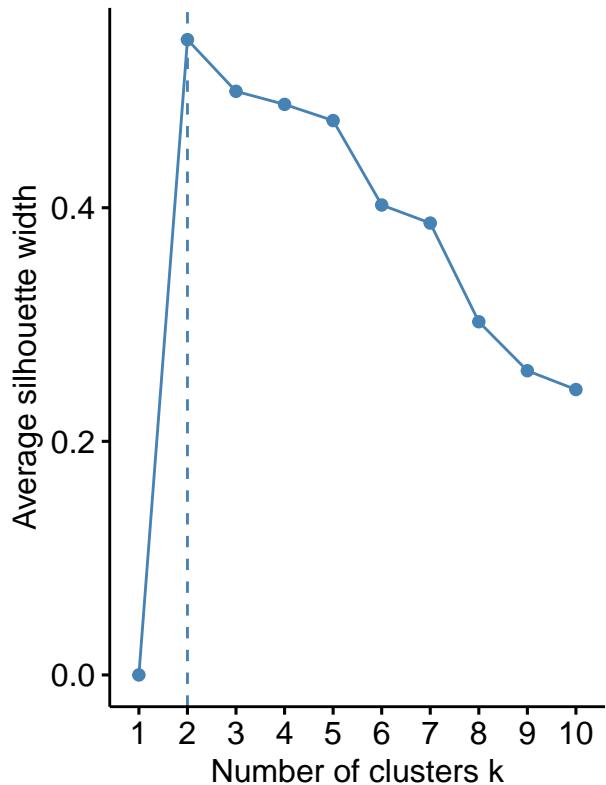
Dist euclidea, Metodo Ward, K=4



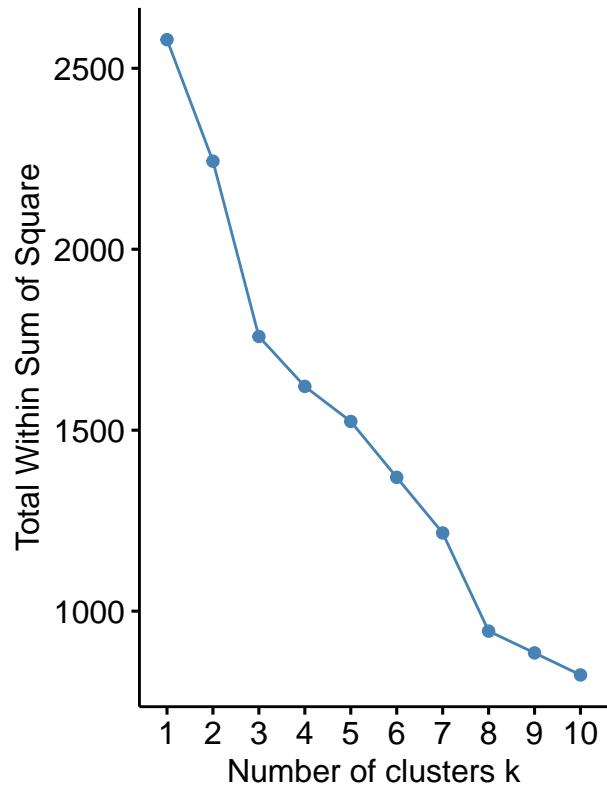
Método de la media

```
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "silhouette",
                   hc_method = "average", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Media")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = hcut, method = "wss",
                   hc_method = "average", k.max = 10, verbose = FALSE,
                   hc_metric = "euclidean") + labs(title = "Nº óptimo clusters: Media")
grid.arrange(p1, p2, nrow = 1)
```

Nº óptimo clusters: Media



Nº óptimo clusters: Media



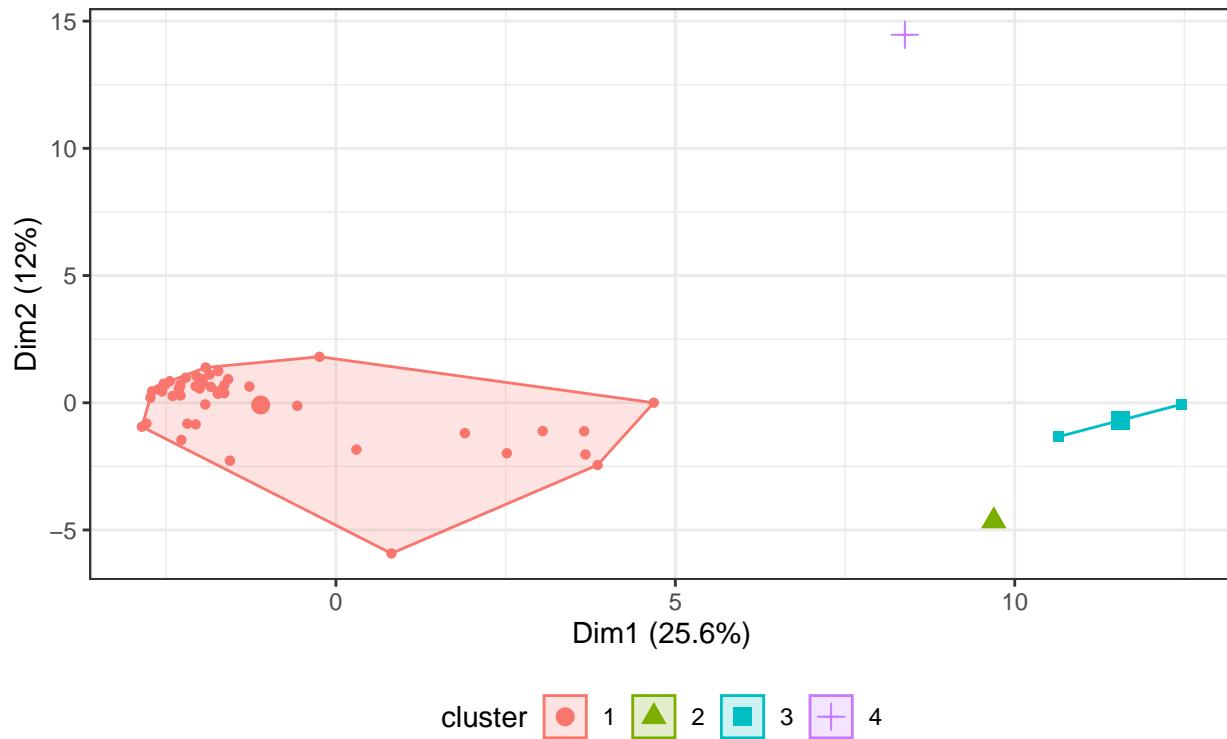
K=4

```
clust1 <- hclust(midist, method="average")
grupos1 <- cutree(clust1, k=K)

fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,
             ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
             labelsize = 8) +
  labs(title = "Modelo jerarquico + Proyeccion PCA",
       subtitle = "Dist euclidea, Metodo Media, K=4") +
  theme_bw() +
  theme(legend.position = "bottom")
```

Modelo jerarquico + Proyeccion PCA

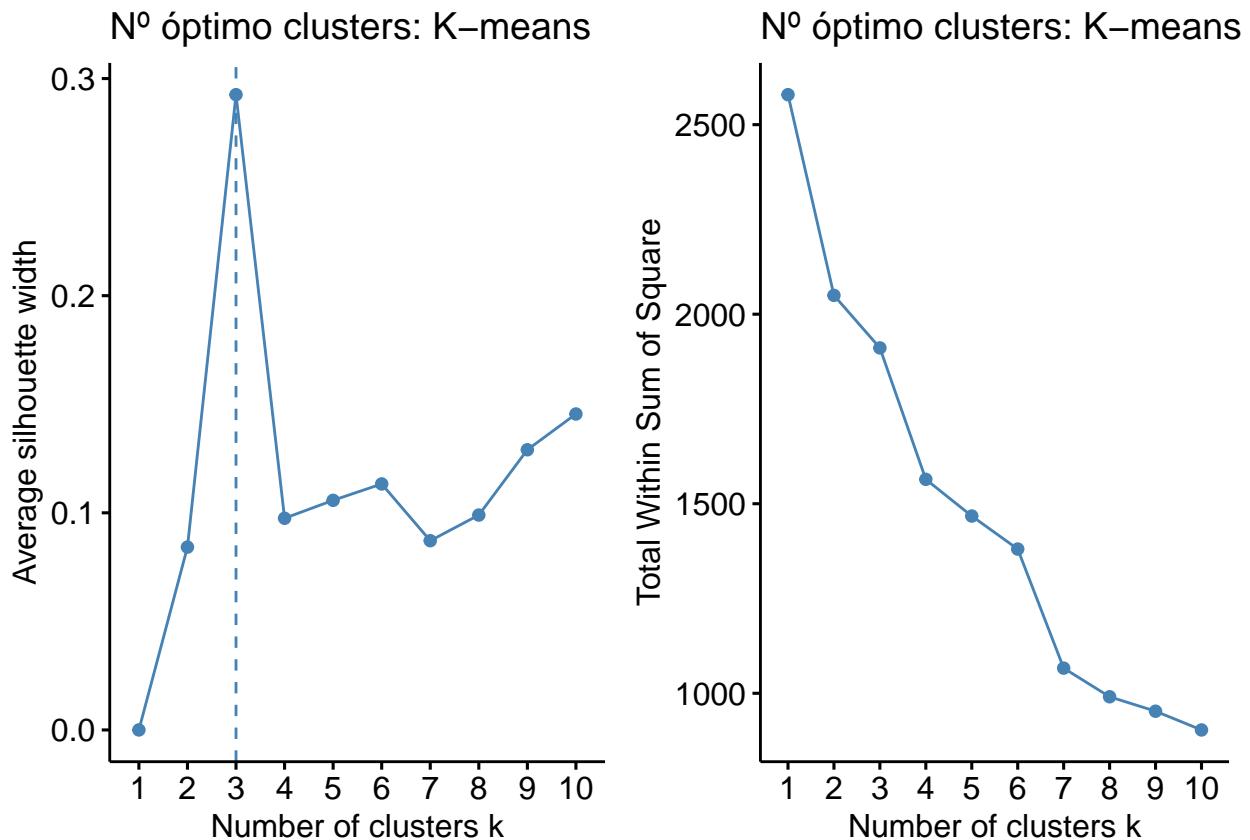
Dist euclidea, Metodo Media, K=4



Partición

k-means

```
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = kmeans, method = "silhouette",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: K-means")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = kmeans, method = "wss",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: K-means")
grid.arrange(p1, p2, nrow = 1)
```



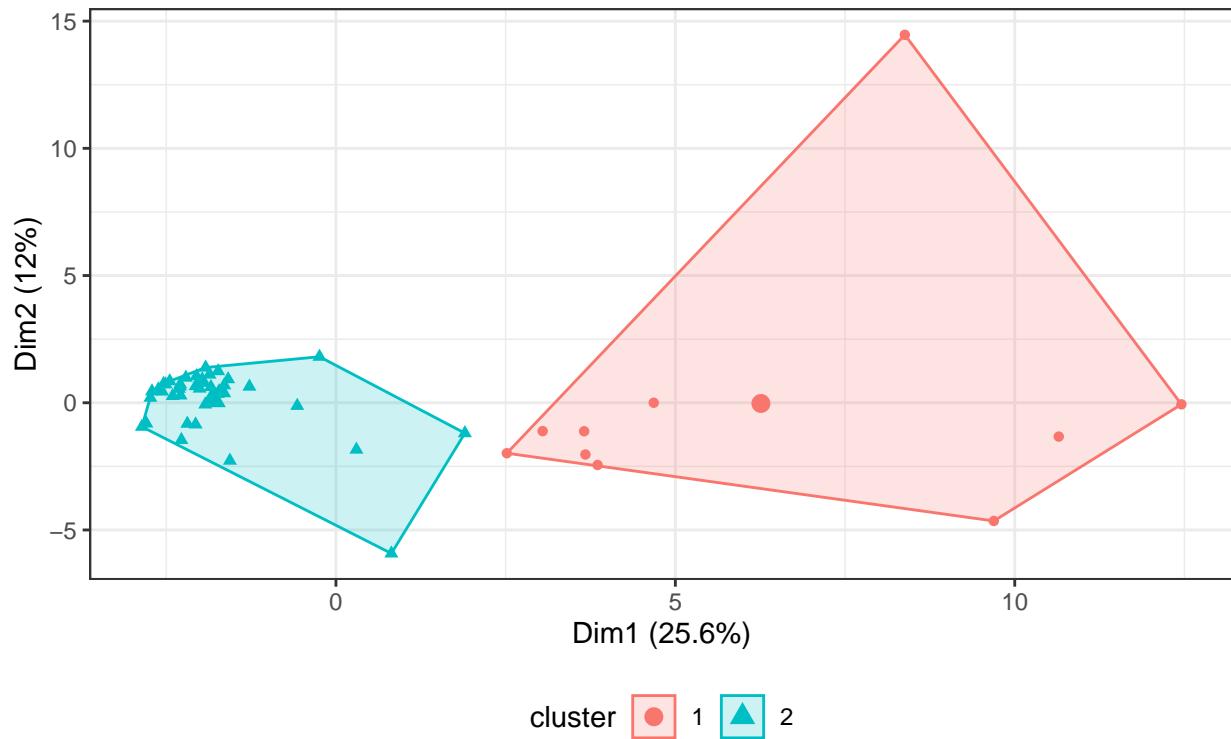
```
k=2
clust3 <- kmeans(datos_elegidos, centers = k, nstart = 20)

p1 = fviz_cluster(object = list(data=datos_elegidos, cluster=clust3$cluster), stand = FALSE,
                  ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
                  labelsize = 8) +
  labs(title = "K-MEDIAS + Proyeccion PCA",
       subtitle = "Dist euclidea, K=2") +
  theme_bw() +
  theme(legend.position = "bottom")

grid.arrange(p1,nrow = 1)
```

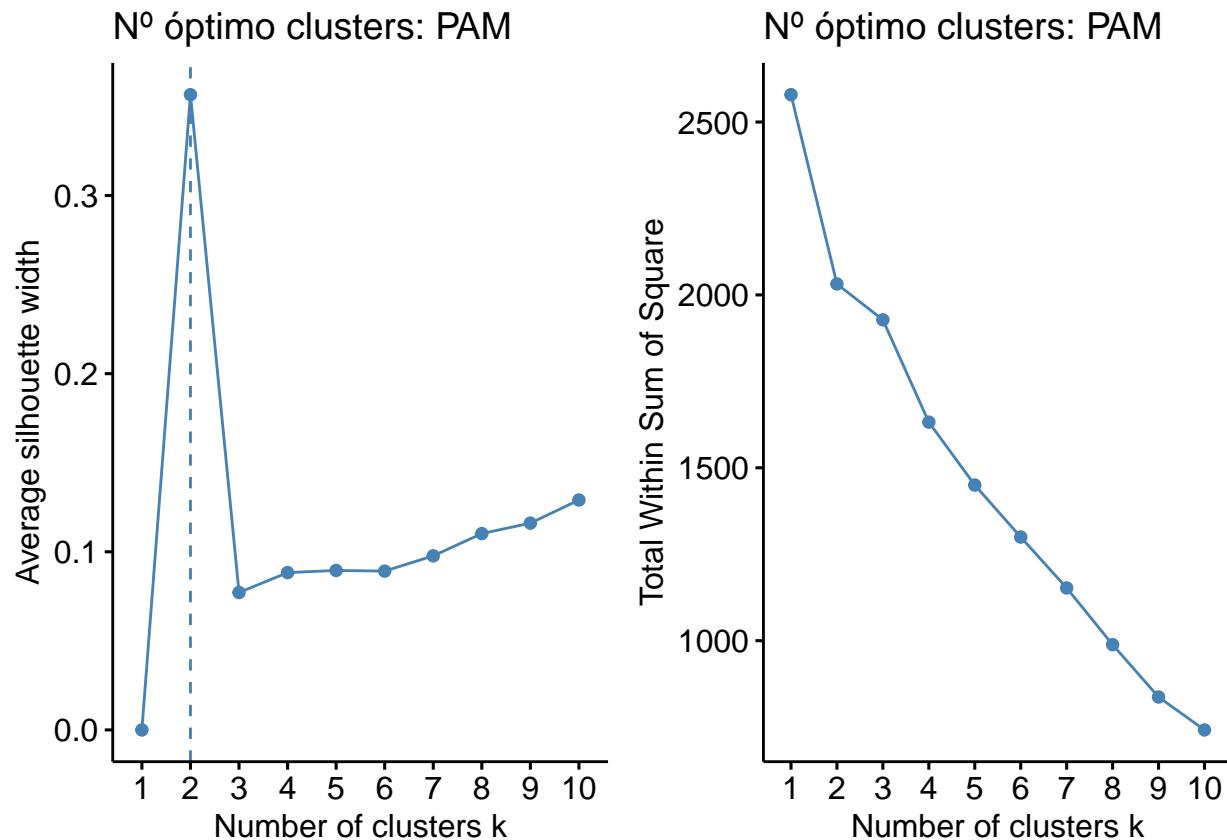
K-MEDIAS + Proyeccion PCA

Dist euclidea, K=2



pam

```
p1 = fviz_nbclust(x = datos_elegidos, FUNcluster = pam, method = "silhouette",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: PAM")
p2 = fviz_nbclust(x = datos_elegidos, FUNcluster = pam, method = "wss",
  k.max = 10, verbose = FALSE) +
  labs(title = "Nº óptimo clusters: PAM")
grid.arrange(p1, p2, nrow = 1)
```



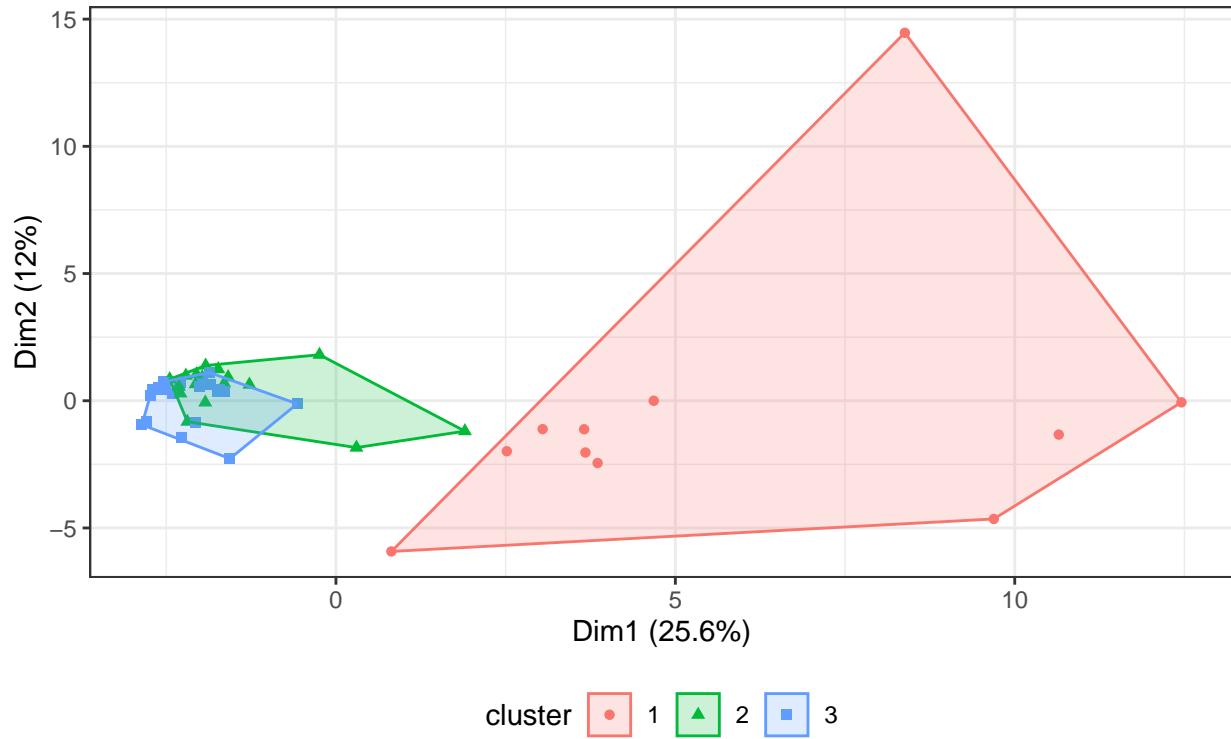
```
k=3
clust4 <- pam(datos_elegidos, k = k)
table(clust4$clustering)
```

```
##
##   1   2   3
## 11 17 22

p1 = fviz_cluster(object = list(data=datos_elegidos, cluster=clust4$clustering), stand = FALSE,
                   ellipse.type = "convex", geom = "point", show.clust.cent = FALSE,
                   labelsize = 8) +
  labs(title = "K-MEDOIDES + Proyeccion PCA",
       subtitle = "Dist euclidea, K=3") +
  theme_bw() +
  theme(legend.position = "bottom")
grid.arrange(p1,nrow = 1)
```

K-MEDOIDES + Proyeccion PCA

Dist euclidea, K=3



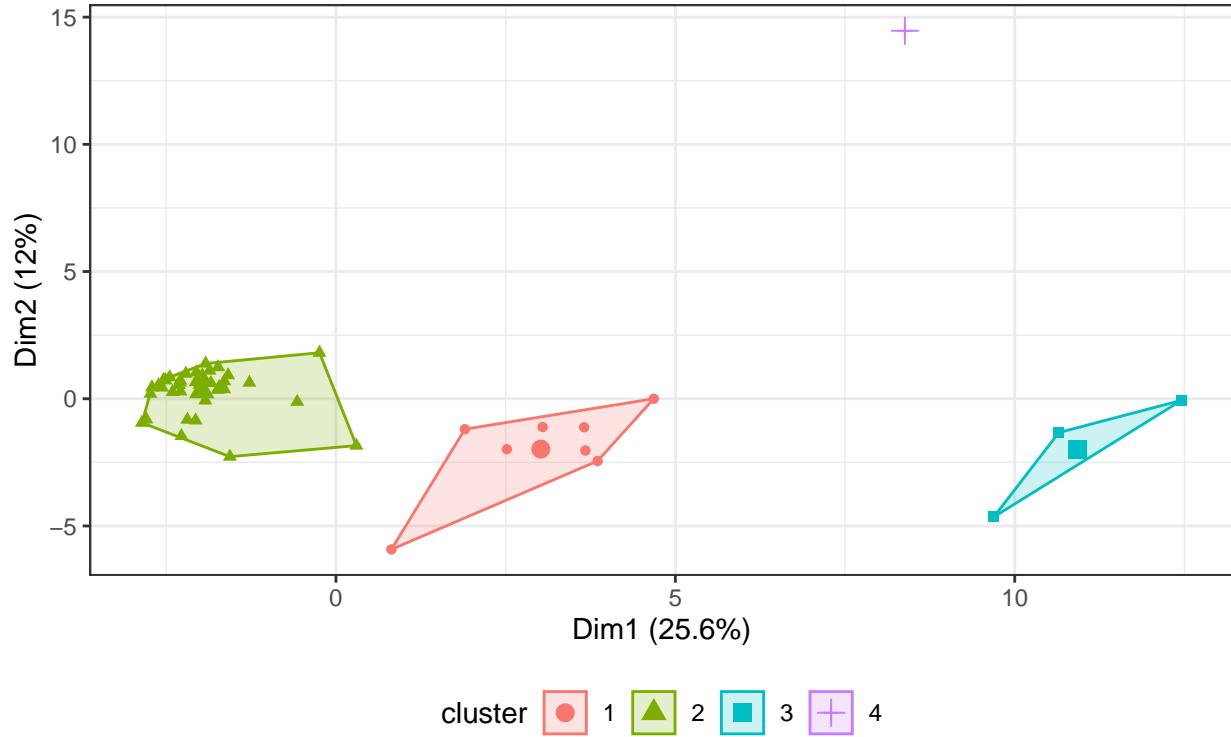
Final: Ward

```
clust1 <- hclust(midist, method="ward.D2")
grupos1 <- cutree(clust1, k=4)

fviz_cluster(object = list(data=datos_elegidos, cluster=grupos1), stand = FALSE,
             ellipse.type = "convex", geom = "point", show.clust.cent = TRUE,
             labelsize = 8) +
  labs(title = "Modelo jerarquico + Proyeccion PCA",
       subtitle = "Dist euclidea, Metodo Ward, K=3") +
  theme_bw() +
  theme(legend.position = "bottom")
```

Modelo jerarquico + Proyeccion PCA

Dist euclidea, Metodo Ward, K=3



```
datos_filtrados$cluster <- as.factor(cutree(clust1, k = 4))
resumen_centros <- aggregate(. ~ cluster, data = datos_filtrados, FUN = mean, na.rm = TRUE)
#write.csv(resumen_centros, "resumen_centros_clusters.csv", row.names = FALSE)
print(resumen_centros)
```

```
##   cluster cred_mat1 cred_mat2 cred_mat3 cred_mat4 cred_sup_espec cred_sup
## 1       1 -1.4585890  1.8498518  0.6567394 -0.1215677    -0.138675 -0.138675
## 2       2  0.5889139 -0.4385728 -0.4016423 -0.2652387    -0.138675 -0.138675
## 3       3 -1.7850025  0.1193669  0.6645792  3.9491095    -0.138675 -0.138675
## 4       4 -1.7850025  0.6075642  1.1976900 -0.2652387    7.072428  7.072428
##   cred_mat_normal cred_ptes_acta cred_mat_sem_a cred_mat_sem_b cred_mat_anu
## 1      -0.2136248     -0.2136248     -0.3971337     -1.274886   1.6069469
## 2      -0.1620374     -0.1620374     0.2051857     0.354792  -0.4017367
## 3       0.6576291     0.6576291    -1.8599094    -1.285135   0.6695612
## 4      -0.2136248     -0.2136248     -0.4831793    -2.351088  -0.4017367
##   cred_mat_total anyo_inicio_estudios cred_sup_1o cred_sup_2o cred_sup_3o
## 1      -0.07357889            -0.8433635   1.4585890  0.5844566 -0.05453666
## 2       0.11772623            0.4574175  -0.5889139 -0.4638788 -0.34850258
## 3      -1.77710541            -3.0113319   1.7850025  2.3050578  3.61715530
## 4      -2.72452123            0.4574175   1.7850025  1.9323163  1.58821406
##   cred_sup_4o practicas cred_sup_tit data_nac alta_universitat anyo_ingreso
## 1     -0.2426124 -0.2450451   0.8076310 -0.4216122    -0.3044258  -0.8433635
## 2     -0.2426124 -0.2450451   -0.5241736  0.3540556     0.3686478   0.4574175
## 3      3.9626691  4.0024031   2.8803112 -2.1132662    -1.6236041  -3.0113319
## 4     -0.2426124 -0.2450451   1.6966023 -2.6545955    -5.8973057   0.4574175
```

```

##      nota10      nota14 curso_mas_bajo_2 curso_mas_alto_2 curso_mas_alto_3
## 1  0.24066261  0.07952094      -0.1980676     -0.138675    0.2858859
## 2  0.09876763  0.08822931      -0.1980676     -0.138675   -0.2450451
## 3 -0.34140057 -0.89837171      1.5185182     2.265026    1.1707710
## 4 -3.01776326  0.02265059      -0.1980676     -0.138675   -0.2450451
## es_adaptado_1 nacionalitat_XXX      sexe_V prov_origen_ESPANYA
## 1      -0.138675      -0.138675 -0.6070297      -0.1691324
## 2      -0.138675      -0.138675  0.1333521      0.0457802
## 3      -0.138675      2.265026 -0.4926618     -0.4832354
## 4      7.072428      -0.138675  0.4222815      2.0295888
## tipo_ingreso_BMA tipo_ingreso_NAP estudios_p_3 estudios_p_4 estudios_p_5
## 1      -1.6315906     1.6315906  0.09326638   0.27685201   -0.3105152
## 2       0.5423570     -0.5423570 -0.06626822  -0.04787666   0.1409576
## 3      -1.6315906     1.6315906  0.29534355   0.61962117   -0.8151025
## 4      0.6011123     -0.6011123 -0.51296511  -0.75145546   -0.8151025
## estudios_p_6 estudios_m_2 estudios_m_3 estudios_m_4 estudios_m_5
## 1      -0.138675     -0.13867505  0.02980567   0.32025631   -0.2858859
## 2      -0.138675     0.05109081  -0.11294780  -0.06320848   0.1183668
## 3      -0.138675     -0.13867505  0.67559517   0.66720064  -1.0291894
## 4      7.072428     -0.13867505  2.74212158  -0.72057669  -1.0291894
## dedicacion_TP desplazado_1 discapacidad_1 becado_2 preferencia_seleccion_2
## 1      -0.24504509   0.06004806  -0.13867505  -0.138675      0.51682019
## 2      -0.02149518   0.04635289   0.05109081  -0.138675     -0.05780226
## 3      1.17077098  -0.72057669  -0.13867505  -0.138675     -0.32301262
## 4      -0.24504509   1.36108931  -0.13867505  -0.138675     -0.32301262
## preferencia_seleccion_3 preferencia_seleccion_Baja
## 1          -0.5424304      -0.6602253
## 2          0.1379867      0.2432409
## 3          0.2410802      -0.6602253
## 4          -0.5424304     -0.6602253
## preferencia_seleccion_Desconocido mes_julio mes_septiembre mes_octubre
## 1                  -0.1980676 -0.8819589     0.7437843  0.09690379
## 2                  -0.1980676  0.3249322     -0.1936724 -0.05780226
## 3                  1.5185182 -0.8819589     0.5741493  0.79676446
## 4                  4.9516897 -0.8819589     1.2526894 -0.32301262
## mes_diciembre PC1      PC2      PC3
## 1      0.4456521 1.1632041 -0.3823566  0.7416181
## 2      -0.1980676 1.2204499 -0.1673215 -0.2033983
## 3      -0.1980676 0.7917431  0.3838783 -0.6864949
## 4      -0.1980676 0.8110127  0.3975199 -0.7757741

dim(resumen_centros)

## [1] 4 57

```