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 - Generalization to Arrows
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Functions

```
1 public static int fib(int x) {  
2     if (x<=0)  
3         return 0;  
4     else if (x==1)  
5         return 1;  
6     else  
7         return fib(x-2) + fib(x-1);  
8 }
```

```
1 fib :: Int -> Int  
2 fib x  
3   | x <= 0 = 0  
4   | x == 1 = 0  
5   | otherwise =  
6     ( fib (x - 2))  
7     + (fib (x - 1))
```

- Functional programming equally powerful as imperative programming
- focused on the "what?" instead of the "how?"
⇒ more concise ⇒ easier to reason about
- based on Lambda Calculus

Monad Definition

```
1 class Monad m where
2   (>>=) :: m a -> (a -> m b) -> m b
3   return :: a -> m a
```

Similar to Java's Optional, we have Maybe a:

```
1 instance Monad Maybe where
2   (Just a) >>= f = f a
3   Nothing >>= _ = Nothing
4   return a = Just a
```

⇒ composable computation descriptions

Monad Usage

With monadic functions like

```
1 func :: Int -> Maybe Int
2 func x
3   | x < 0 = Nothing
4   | otherwise = Just (x * 2)
```

we can compose computations:

```
1 complicatedFunc :: Int -> Maybe Int
2 complicatedFunc x = (return x) >>= func >>= ...
```

Arrow Definition

Another way to compose computations are arrows:

```
1 class Arrow arr where
2   arr :: (a -> b) -> arr a b
3   (>>>) :: arr a b -> arr b c -> arr a c
4   first :: arr a b -> arr (a,c) (b,c)
```

Functions \in Arrows

Functions (\rightarrow) are arrows:

```
1 instance Arrow ( $\rightarrow$ ) where
2   arr f = f
3   f >>> g = g . f
4   first f = \ (a, c)  $\rightarrow$  (f a, c)
```

The Kleisli Type

The Kleisli type

```
1 data Kleisli m a b = Kleisli { run :: a -> m b }
```

is also an arrow:

```
1 instance Monad m => Arrow (Kleisli m) where
2   arr f = Kleisli $ return . f
3   f >>> g = Kleisli $ \a -> f a >>= g
4   first f = Kleisli $ \(a,c) -> f a >>= \b -> return (b,c)
```


Combinators & Arrow Example

Some Combinators:

```
1 second :: Arrow arr => arr a b -> arr (c, a) (c, b)
2 second f = arr swap >>> first f >>> arr swap
3   where swap (x, y) = (y, x)
```

```
1 (***) :: Arrow arr => arr a b -> arr c d -> arr (a, c) (b, d)
2 f *** g = first f >>> second g
```

```
1 (&&&) :: Arrow arr => arr a b -> arr a c -> arr a (b, c)
2 f &&& g = arr (\a -> (a, a)) >>> (f *** g)
```

Arrow usage example:

```
1 add :: Arrow arr => arr a Int -> arr a Int -> arr a Int
2 add f g = (f &&& g) >>> arr (\(u, v) -> u + v)
```

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In general, Parallelism can be looked at as:

```
1 parEvalN :: [a -> b] -> [a] -> [b]
```

Roadmap:

- Implement using existing Haskell's
 - Multicore
 - ParMonad
 - Eden
- Generalize to Arrows
- Profit

Multicore Haskell

```
1 parEvalN :: (NFData b) => [a -> b] -> [a] -> [b]
2 parEvalN fs as = zipWith ($) fs as 'using' parList rdeepseq
```

with

zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]

using :: a -> Strategy a -> a

parList :: Strategy a -> Strategy [a]

rdeepseq :: NFData a => Strategy a

ParMonad

```
1 parEvalN :: (NFData b) => [a -> b] -> [a] -> [b]
2 parEvalN fs as = runPar $
3 (sequenceA $ map (spawnP) $ zipWith ($) fs as) >>= mapM get
```

Eden

```
1 parEvalN :: (Trans a, Trans b) => [a -> b] -> [a] -> [b]
2 parEvalN fs as = spawnF fs as
```

The ArrowParallel typeclass

```
1 parEvalN :: [a -> b] -> [a] -> [b]
```

```
1 parEvalN :: (Arrow arr) => [arr a b] -> arr [a] [b]
```

```
1 class Arrow arr => ArrowParallel arr a b where  
2   parEvalN :: [arr a b] -> arr [a] [b]
```

```
1 class Arrow arr => ArrowParallel arr a b conf where  
2   parEvalN :: conf -> [arr a b] -> arr [a] [b]
```

mapArr

The `mapArr` combinator lifts any arrow `arr a b` to an arrow `arr [a] [b] [2]`,

```
1 mapArr :: ArrowChoice arr => arr a b -> arr [a] [b]
2 mapArr f =
3   arr listcase >>>
4   arr (const []) ||| (f *** mapArr f >>> arr (uncurry ()))
5   where
6     listcase [] = Left ()
7     listcase (x:xs) = Right (x,xs)
```

with

```
1 (|||) :: ArrowChoice arr a c -> arr b c -> arr (Either a b) c
```


zipWithArr & listApp

`zipWithArr` lifts any arrow `arr (a, b) c` to an arrow
`arr ([a], [b]) [c]`:

```

1 zipWithArr :: ArrowChoice arr => arr (a, b) c -> arr ([a], [b]) [c]
2 zipWithArr f = (arr $ \(as, bs) -> zipWith (,) as bs) >>>
3   mapArr f

```

`listApp` converts a list of arrows `[arr a b]` to a new arrow
`arr [a] [b]`:

```

1 listApp :: (ArrowChoice arr, ArrowApply arr) =>
2   [arr a b] -> arr [a] [b]
3 listApp fs = (arr $ \(as -> (fs, as)) >>> zipWithArr app

```

with the `ArrowApply` that defines `app :: arr (arr a b, a) c`.

Multicore

```
1 instance (NFData b, ArrowApply arr, ArrowChoice arr) =>
2   ArrowParallel arr a b conf where
3     parEvalN _ fs = listApp fs >>> arr (flip using $ parList rdeepseq)
```

ParMonad

```
1 instance (NFData b, ArrowApply arr, ArrowChoice arr) =>
2   ArrowParallel arr a b conf where
3     parEvalN _ fs =
4       (arr $ \as -> (fs, as)) >>>
5       zipWithArr (app >>> arr spawnP) >>>
6       arr sequenceA >>>
7       arr (>>= mapM get) >>>
8       arr runPar
```

Eden

```
1 instance (Trans a, Trans b) => ArrowParallel (->) a b conf where  
2   parEvalN _ fs as = spawnF fs as
```

and the Kleisli type.

```
1 instance (Monad m, Trans a, Trans b, Trans (m b)) =>  
2   ArrowParallel (Kleisli m) a b conf where  
3   parEvalN conf fs =  
4     (arr $ parEvalN conf (map (\(Kleisli f) -> f) fs)) >>>  
5     (Kleisli $ sequence)
```

```
1 class (Arrow arr) => ArrowUnwrap arr where  
2   arr a b -> (a -> b)
```

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With the `ArrowParallel` typeclass in place and implemented, we can now implement some basic parallel skeletons.

parEvalNLazy

```
1 parEvalNLazy :: ( ArrowParallel arr a b conf, ArrowChoice arr, ArrowApply a
2   conf -> ChunkSize -> [arr a b] -> (arr [a] [b])
3 parEvalNLazy conf chunkSize fs =
4   arr (chunksOf chunkSize) >>>
5   listApp fchunks >>>
6   arr concat
7 where
8   fchunks = map (parEvalN conf) $ chunksOf chunkSize fs
```

parEval2

```
1 arrMaybe :: (ArrowApply arr) => (arr a b) -> arr (Maybe a) (Maybe b)
2 arrMaybe fn = (arr $ go) >>> app
3   where
4     go Nothing = (arr $ \Nothing -> Nothing, Nothing)
5     go (Just a) = ((arr $ \(Just x) -> (fn, x)) >>> app >>> arr Just, (
```


parEval2 cnt.

```

1 parEval2 :: ( ArrowParallel arr a b conf,
2   ArrowParallel arr (Maybe a, Maybe c) (Maybe b, Maybe d) conf,
3   ArrowApply arr) =>
4   conf -> arr a b -> arr c d -> (arr (a, c) (b, d))
5 parEval2 conf f g =
6   (arr $ \(a, c) -> (f_g, [(Just a, Nothing), (Nothing, Just c)])) >>>
7   app >>>
8   (arr $ \comb -> (fromJust (fst (comb !! 0)), fromJust (snd (comb !!
9   where
10    f_g = parEvalN conf $ replicate 2 $ arrMaybe f *** arrMaybe g

```

parMap

```
1 parMap :: ( ArrowParallel arr a b conf, ArrowApply arr) =>
2   conf -> (arr a b) -> (arr [a] [b])
3 parMap conf f =
4   (arr $ \as -> (f, as)) >>>
5   ( first $ arr repeat >>>
6     arr (parEvalN conf)) >>>
7   app
```

parMapStream

```
1 parMapStream :: (ArrowParallel arr a b conf, ArrowChoice arr, ArrowApply a) =>
2   conf -> ChunkSize -> arr a b -> arr [a] [b]
3 parMapStream conf chunkSize f =
4   (arr $ \as -> (f, as)) >>>
5   ( first $ arr repeat >>>
6     arr (parEvalNLazy conf chunkSize)) >>>
7   app
```

farm

```
1 farm :: (ArrowParallel arr a b conf, ArrowParallel arr [a] [b] conf,  
2   ArrowChoice arr, ArrowApply arr) =>  
3   conf -> NumCores -> arr a b -> arr [a] [b]  
4 farm conf numCores f =  
5   (arr $ \as -> (f, as)) >>>  
6   ( first $ arr mapArr >>> arr repeat >>>  
7     arr (parEvalN conf)) >>>  
8   (second $ arr (unshuffle numCores)) >>>  
9   app >>>  
10  arr shuffle
```

The definition of `unshuffle` is

```
1 unshuffle :: Int  
2   -> [a]  
3   -> [[a]]  
4 unshuffle n xs = [takeEach n (drop i xs) | i <- [0..n-1]]
```

, while `shuffle` is defined as:

farmChunk

```
1 farmChunk :: ( ArrowParallel arr a b conf, ArrowParallel arr [a] [b] conf,
2   ArrowChoice arr, ArrowApply arr) =>
3   conf -> ChunkSize -> NumCores -> arr a b -> arr [a] [b]
4 farmChunk conf chunkSize numCores f =
5   ( arr $ \as -> (f, as)) >>>
6   ( first $ arr mapArr >>> arr repeat >>>
7     arr (parEvalNLazy conf chunkSize)) >>>
8   (second $ arr ( unshuffle numCores)) >>>
9   app >>>
10  arr shuffle
```

```

1 (|>>>|) :: (Arrow arr) => [arr a b] -> [arr b c] -> [arr a c]
2 (|>>>|) = zipWith (>>>)

```

```

1 (|***|) :: (ArrowParallel arr a b (),
2   ArrowParallel arr (Maybe a, Maybe c) (Maybe b, Maybe d) (),
3   ArrowApply arr) =>
4   arr a b -> arr c d -> arr (a, c) (b, d)
5 (|***|) = parEval2 ()

```

```

1 (|&&&|) :: (ArrowParallel arr a b (),
2   ArrowParallel arr (Maybe a, Maybe a) (Maybe b, Maybe c) (),
3   ArrowApply arr) =>
4   arr a b -> arr a c -> arr a (b, c)
5 (|&&&|) f g = (arr $ \a -> (a, a)) >>> f |***| g

```

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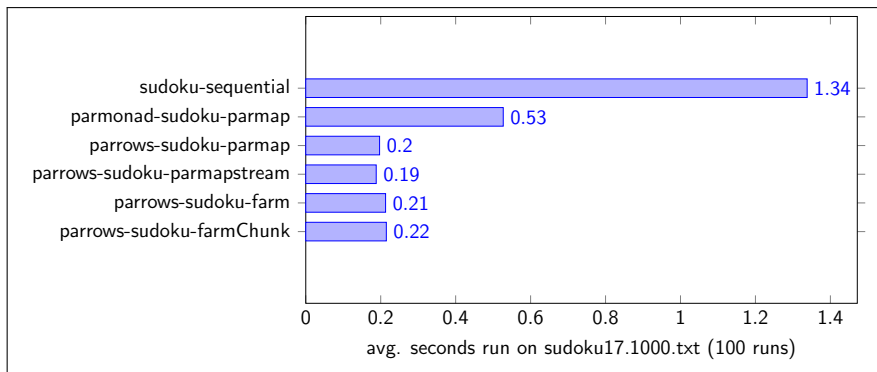
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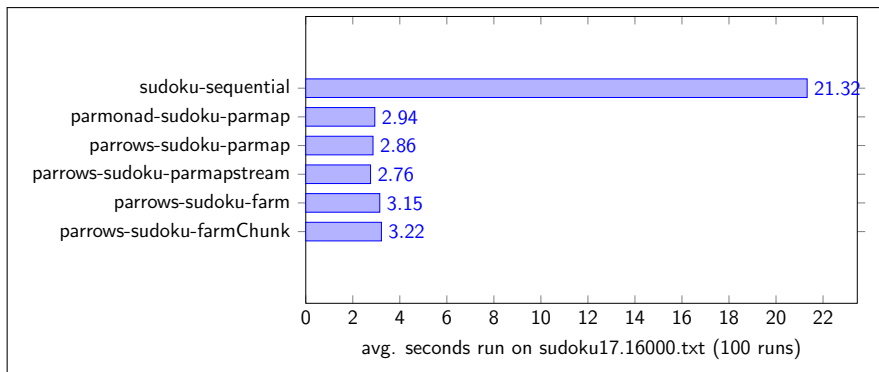
3 Usability

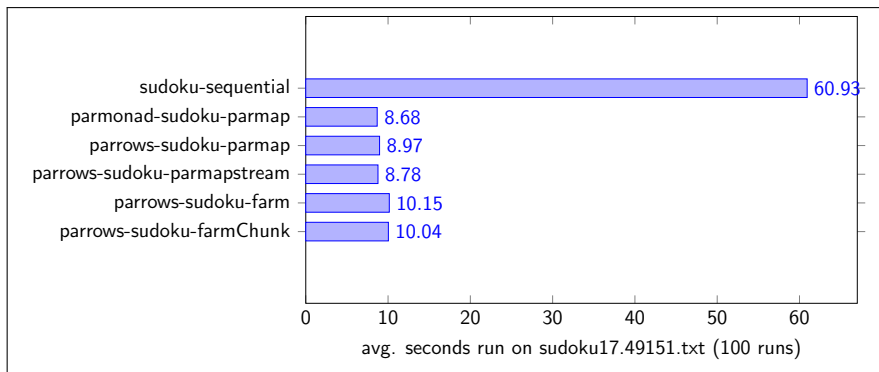
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4 Benchmarks

The Benchmarks were run on a Core i7-3970X CPU @ 3.5GHz with 6 cores and 12 threads. For sake of comparability with Simon Marlow's parallel version which uses the ParMonad, we use the ParMonad backend for the parallel arrow versions as well.







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