

Q1to Q15

1. What is central limit theorem and why is it important?

Central limit theorem statement

The central limit theorem (CLT) says that as sample sizes grow higher, the distribution of sample means approaches a normal distribution, independent of the population's distribution. For the CLT to hold, sample sizes of 30 or more are frequently regarded as sufficient.

The central limit theorem statement looks technical, but it can be comprehended if we think about it step by step. First, we can take a random sample where the number of individuals is n . Then it is easy to make a sample mean that will correspond to the mean of the measurement we want to make in our population.

Central Limit Theorem's importance

The central limit theorem is important in statistics for two reasons:

The normality assumption

The information that the sample distributions could approximate a normal distribution has some important applications. The normality assumption is essential for the parametric hypothesis test of the mean. However, it may look like these tests are invalid because the data is not distributed normally. If the sample size is large enough, then the central limit theorem will help make the sampling distributions that will approximate a normal distribution.

Precision of estimates

When we prepare graphs, we notice that when the sample size increases, the sampling distributions of the mean are grouped more strongly around the population mean. When we use a sample to estimate the mean of the whole population, this property becomes applicable. When we have a large sample size, then it is possible that the mean would be close to the real population, or we can say that we have a more precise estimate.

On the other hand, the sample distributions of the mean are wider for small samples. In the case of smaller sample sizes, it is normal for them to be away from the actual mean of the population, or it can be said that the obtained estimate would be less precise.

2. What is sampling? How many sampling methods do you know?

The sampling method or sampling technique is the process of studying the population by gathering information and analysing that data. It is the basis of the data where the sample space is enormous.

There are several different sampling techniques available, and they can be subdivided into two groups. All these methods of sampling may involve specifically targeting hard or approach to reach groups.

Types of Sampling Method:

There are different sampling techniques available to get relevant results from the population. The two different types of sampling methods are:

- Probability Sampling: It involves random selection, allowing us to make strong statistical inferences about the whole group.
- Non-probability Sampling: It involves non-random selection based on convenience or other criteria, allowing us to easily collect data.

3. What is the difference between type1 and type2 error?

BASIS FOR COMPARISON	TYPE I ERROR	TYPE II ERROR
Meaning	Type I error refers to non-acceptance of hypothesis which ought to be accepted.	Type II error is the acceptance of hypothesis which ought to be rejected.
Equivalent to	False positive	False negative
What is it?	It is incorrect rejection of true null hypothesis.	It is incorrect acceptance of false null hypothesis.
Represents	A false hit	A miss
Probability of committing error	Equals the level of significance.	Equals the power of test.
Indicated by	Greek letter ' α '	Greek letter ' β '

4. What do you understand by the term Normal distribution?

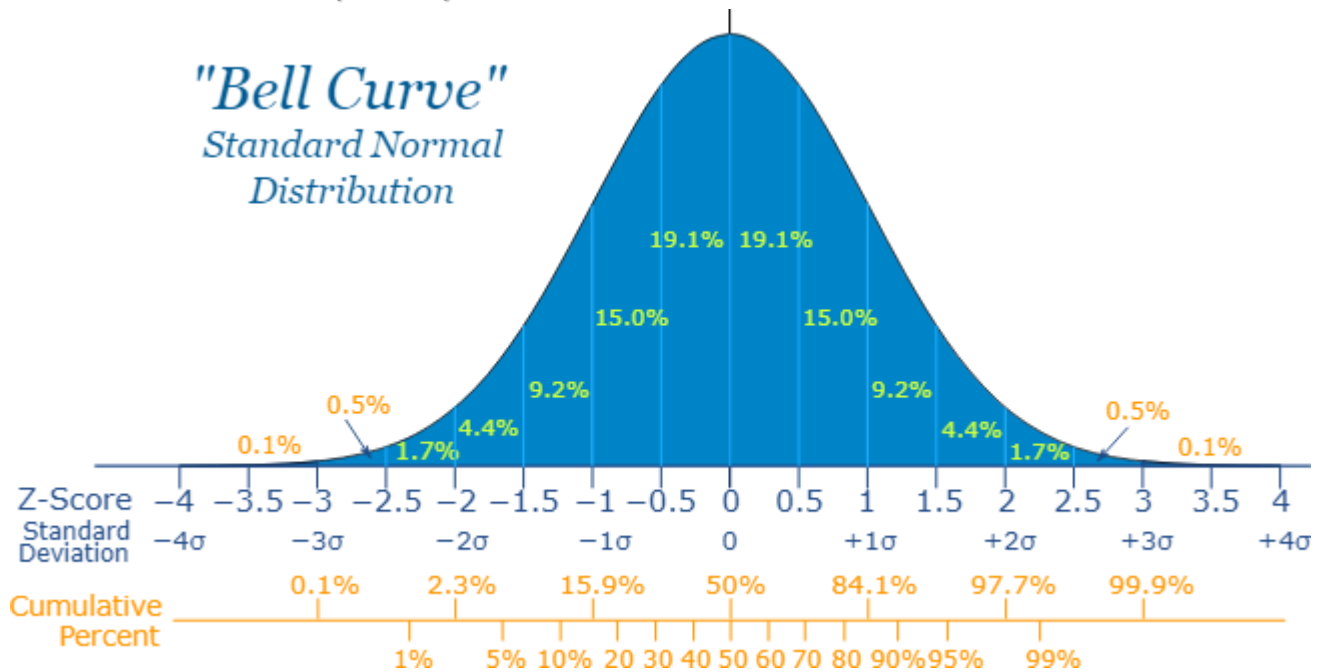
The Normal Distribution, also called the Gaussian Distribution, is the most significant continuous probability distribution for independent, randomly generated variables. Sometimes it is also called a bell curve. A large number of random variables are either nearly or exactly represented by the normal distribution, in every physical science and economics. Furthermore, it can be used to approximate other probability distributions, therefore supporting the usage of the word 'normal' as in about the one, mostly used. Normal Distribution Formula:

$$f(x, \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} e^{\frac{-(x-\mu)^2}{2\sigma^2}}$$

Where,

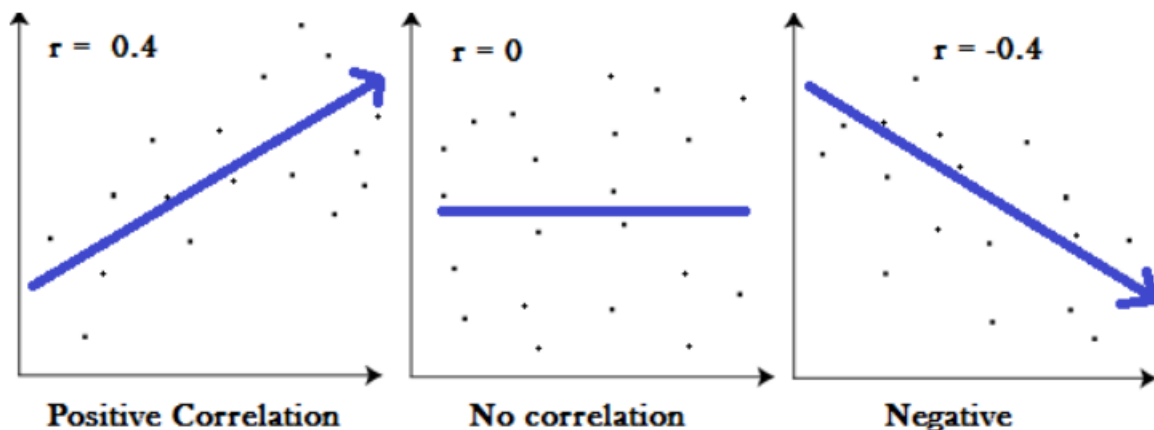
- x is the variable
- μ is the mean
- σ is the standard deviation

The graph of the normal distribution is characterized by two parameters: the mean, or average, which is the maximum of the graph and about which the graph is always symmetric; and the standard deviation, which determines the amount of dispersion away from the mean.



5. What is correlation and covariance in statistics?

Correlation: Correlation is a statistical measure that expresses the extent to which two variables are linearly related. It's a common tool for describing simple relationships without making a statement about cause and effect. It is used to test relationships between quantitative variables or categorical variables. In other words, it's a measure of how things are related. The study of how variables are correlated is called correlation analysis. A correlation coefficient is a way to put a value to the relationship. Correlation coefficients have a value of between -1 and 1. A "0" means there is no relationship between the variables at all, while -1 or 1 means that there is a perfect negative or positive correlation. The graph of Correlation is:



Correlation is of three types:

- **Simple Correlation:** In simple correlation, a single number expresses the degree to which two variables are related.
- **Partial Correlation:** When one variable's effects are removed, the correlation between two variables is revealed in partial correlation.
- **Multiple correlation:** A statistical technique that uses two or more variables to predict the value of one variable.

Correlation coefficient Formula:

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

Parth Makwana (0722)

Where,

n: Quantity of Information

Σx : Total of the First Variable Value

Σy : Total of the Second Variable Value

Σxy : Sum of the Product of & Second Value

Σx^2 : Sum of the Squares of the First Value

Σy^2 : Sum of the Squares of the Second Value

Covariance:

Covariance is a statistical tool that is used to determine the relationship between the movements of two random variables. When two stocks tend to move together, they are seen as having a positive covariance; when they move inversely, the covariance is negative. Covariance is different from the correlation coefficient, a measure of the strength of a correlative relationship. It is a significant tool in modern portfolio theory used to ascertain what securities to put in a portfolio. Risk and volatility can be reduced in a portfolio by pairing assets that have a negative covariance.

Types of Covariance:

- **Positive Covariance:** If the covariance for any two variables is positive, that means, both the variables move in the same direction.
- **Negative Covariance:** If the covariance for any two variables is negative, that means, both the variables move in the opposite direction.

6. Differentiate between univariate ,Biavariate,and multivariate analysis.

- **Univariate:** It summarize only one variable at a time. The analysis of univariate data is thus the simplest form of analysis since the information deals with only one quantity that changes. It does not deal with causes or relationships and the main purpose of the analysis is to describe the data and find patterns that exist within it. The example of a univariate data can be height.
- **Bivariate:** It compare two variables. The analysis of this type of data deals with causes and relationships and the analysis is done to find out the relationship among the two variables. Example of bivariate data can be temperature and ice cream sales in summer season.
- **Multivariate:** It compare more than two variables. It is similar to bivariate but contains more than one dependent variable. The ways to perform analysis on this data depends on the goals to be achieved. Some of the techniques are regression analysis, path analysis, factor analysis and multivariate analysis of variance (MANOVA). Example of this type of data is suppose an advertiser wants to compare the popularity of four advertisements on a website, then their click rates could be measured for both men and women and relationships between variables can then be examined.

7. What do you understand by sensitivity and how would you calculate it?

Sensitivity analysis determines how different values of an independent variable affect a particular dependent variable under a given set of assumptions. This model is also referred to as a what-if or simulation analysis. It can be used to help make predictions in the share prices of publicly traded companies or how interest rates affect bond prices. It allows for forecasting using historical, true data. While sensitivity analysis determines how variables impact a single event, scenario analysis is more useful to determine many different outcomes for more broad situations.

Calculate Sensitivity Analysis:

Sensitivity analysis is often performed in analysis software, and Excel has built in functions to help perform the analysis. In general, sensitivity analysis is calculated by leveraging formulas that reference different input cells. For example, a company may perform NPV analysis using a discount rate of 6%. Sensitivity analysis can be performed by analyzing scenarios of 5%, 8%, and 10% discount rates as well by simply maintaining the formula but referencing the different variable values.

Parth Makwana (0722)

8. What is hypothesis testing? What is H0 and H1? What is H0 and H1 for two-tail test?

Hypothesis Testing:

Hypothesis Testing is a type of statistical analysis in which we put our assumptions about a population parameter to the test. It is used to estimate the relationship between 2 statistical variables. Example of statistical hypothesis is:

A doctor believes that 3D (Diet, Dose, and Discipline) is 90% effective for diabetic patients.

Types of Hypothesis Testing: Two types of hypothesis testing are:

Null Hypothesis: It is denoted by symbol H_0 . The Null Hypothesis is the assumption that the event will not occur. A null hypothesis has no bearing on the study's outcome unless it is rejected.

Alternate Hypothesis: It is denoted by symbol H_1 . The Alternate Hypothesis is the logical opposite of the null hypothesis. The acceptance of the alternative hypothesis follows the rejection of the null hypothesis.

Two-Tailed Hypothesis Testing: In two tails, the test sample is checked to be greater or less than a range of values in a Two-Tailed test, implying that the critical distribution area is two-sided.

Example 1:

Suppose,

H_0 : mean = 50 and H_1 : mean \neq 50 (the mean can be greater than or less than 50 but not equal to)

Example 2:

The average height of students in a batch is 100 cm and the standard deviation is 15. However, one teacher believes that this has changed, so he/she decides to test the height of 75 random students in the batch. The average height of the sample comes out to be 105. The steps for performing hypothesis testing are:

- Specify the Null(H_0) and Alternate(H_1) hypothesis
- Choose the level of Significance(α)
- Find Critical Values
- Find the test statistic
- Draw conclusion

Specify the Null(H_0) and Alternate(H_1) hypothesis for Two-Tailed Hypothesis Testing:

• Null hypothesis (H_0): The null hypothesis here is what currently stated to be true about the population. In this example, it will be the average height of students in the batch is

$$100 \quad H_0: \mu = 100$$

• Alternate hypothesis (H_1): The alternate hypothesis is always what is being claimed. In this example, teacher believes (Claims) that the actual value has changed. He/she doesn't know whether the average has gone up or down, but he/she believes that it has changed and is not 100 anymore.

$$H_1: \mu \neq 100$$

If the alternate hypothesis is written with a \neq sign that means that we are going to perform a two-tailed test because chances, are it could be more than 100 or less than 100 which makes it two-tailed as an alternate hypothesis is always written with a \neq or $<$ or $>$ sign.

9. What is quantitative data and qualitative data?

Quantitative data is anything that can be counted or measured; it refers to numerical data. Qualitative data is descriptive, referring to things that can be observed but not measured—such as colours or emotions.

Quantitative data: It refers to any information that can be quantified. If it can be counted or measured, and given a numerical value, it's quantitative data. Quantitative data can tell us "How many," "how much," or "how often"—for example, how many people attended last week's webinar? How much revenue did the company make in 2019? How often does a certain customer group use online banking?

Parth Makwana (0722)

Qualitative data: It cannot be measured or counted. It's descriptive, expressed in terms of language rather than numerical values. Researchers will often turn to qualitative data to answer "Why?" or "How?" questions. For example, if our quantitative data tells us that a certain website visitor abandoned their shopping cart three times in one week, we'd probably want to investigate why—and this might involve collecting some form of qualitative data from the user. Perhaps we want to know how a user feels about a particular product; again, qualitative data can provide such insights. In this case, we're not just looking at numbers; we're asking the user to tell us, using language, why they did something or how they feel. Qualitative data also refers to the words or labels used to describe certain characteristics or traits—for example, describing the sky as blue or labelling a particular ice cream flavour as vanilla.

10. How to calculate range and interquartile range?

To calculate the range, we need to find the maximum value of a variable and subtract the minimum value. The range only takes into account these two values and ignore the data points between the two extremities of the distribution. It's used as a supplement to other measures, but it is rarely used as the sole measure of dispersion because it's sensitive to extreme values

To calculate the range, we need to find the maximum value of a variable and subtract the minimum value. The range only takes into account these two values and ignore the data points between the two extremities of the distribution. It's used as a supplement to other measures, but it is rarely used as the sole measure of dispersion because it's sensitive to extreme values

Formula: $IQR = Q3 - Q1$

11. What do you understand by bell curve distribution ?

A bell curve is a type of graph that is used to visualize the distribution of a set of chosen values across a specified group that tend to have a central, normal values, as peak with low and high extremes tapering off relatively symmetrically on either side. Bell curves are visual representations of normal distribution, also called Gaussian distribution. A normal distribution curve, when graphed out, typically follows a bell-shaped curve, hence the name. While the precise shape can vary according to the distribution of the population, the peak is always in the middle and the curve is always symmetrical. Bell curves are useful for quickly visualizing a data set's mean, mode and median because when the distribution is normal, the mean, median and mode are all the same. The long tail refers to the part of the bell curve that stretches out in either direction. If the diagram above represents a population under study, the fat area under the bell curve is where most of the population falls.

12. Mention one method to find outliers.

Outliers are data points that are far from other data points. In other words, they're unusual values in a dataset. Outliers are problematic for many statistical analyses because they can cause tests to either miss significant findings or distort real results.

There are four ways to identify/detect outliers:

- Sorting method.
- Data visualization method.
- Statistical tests (z scores)
- Interquartile range method.

Z-scores:

Z-scores can quantify the unusualness of an observation when our data follow the normal distribution. Z-scores are the number of standard deviations above and below the mean that each value falls.

For example, a Z-score of 2 indicates that an observation is two standard deviations above the average while a Z-score of -2 signifies it is two standard deviations below the mean. A Z-score of zero represents a value that equals the mean.

Parth Makwana (0722)

To calculate the Z-score for an observation, take the raw measurement, subtract the mean, and divide by the standard deviation.

Formula of Z-score:

$$z = \frac{x - \mu}{\sigma}$$

μ = Mean

σ = Standard Deviation

13. What is p-value in hypothesis testing?

A p value is used in hypothesis testing to help you support or reject the null hypothesis. The p value is the evidence against a null hypothesis. The smaller the p-value, the stronger the evidence that you should reject the null hypothesis. P values are expressed as decimals although it may be easier to understand what they are if you convert them to a percentage. For example, a p value of 0.0254 is 2.54%. This means there is a 2.54% chance your results could be random. That's pretty tiny. On the other hand, a large p-value of .9(90%) means your results have a 90% probability of being completely random and not due to anything in your experiment. Therefore, the smaller the p-value, the more important our results

14. What is the Binomial Probability Formula?

The binomial distribution forms the base for the famous binomial test of statistical importance. A test that has a single outcome such as success/failure is also called a Bernoulli trial or Bernoulli experiment, and a series of outcomes is called a Bernoulli process. Consider an experiment where each time a question is asked for a yes/no with a series of n experiments. Then in the binomial probability distribution, the Boolean-valued outcome the success/yes/true/one is represented with probability p and the failure/no/false/zero with probability q (q = 1 - p). In a single experiment when n = 1, the binomial distribution is called a Bernoulli distribution.

Formula for binomial distribution:

$$P(X) = {}_n C_x p^x (1 - p)^{n-x}$$

Where,

- n = the number of experiments
- x = 0, 1, 2, 3, 4, ...
- p = Probability of success in a single experiment
- q = Probability of failure in a single experiment (= 1 - p)

15. Explain ANOVA and it's applications.

- Analysis of variance (ANOVA) is an analysis tool used in statistics that splits an observed aggregate variability found inside a data set into two parts: systematic factors and random factors. The systematic factors have a statistical influence on the given data set, while the random factors do not. Analysts use the ANOVA test to determine the influence that independent variables have on the dependent variable in a regression study. Analysis of variance, or ANOVA, is a statistical method that separates observed variance data into different components to use for additional tests.

Types of ANOVA:

- **One Way ANOVA**– It is also known as one factor ANOVA. Here, we are using one criterion variable (or called as a factor) and analyze the difference between more than two sample groups. Suppose in glass industry, we want to compare the variation of three batches (glass) for their average weight (factor)

Parth Makwana (0722)

- **Two Way ANOVA**– Here, we are using two independent variables (factors) and analyze the difference between more than two sample groups. Similarly, we want to compare the variation of three batches of glass w.r.t weight and hardness (two factors)

The Formula for ANOVA is:

$$F = \text{MST} / \text{MSE}$$

where:

F=ANOVA coefficient

MST=Mean sum of squares due to treatment

MSE=Mean sum of squares due to error