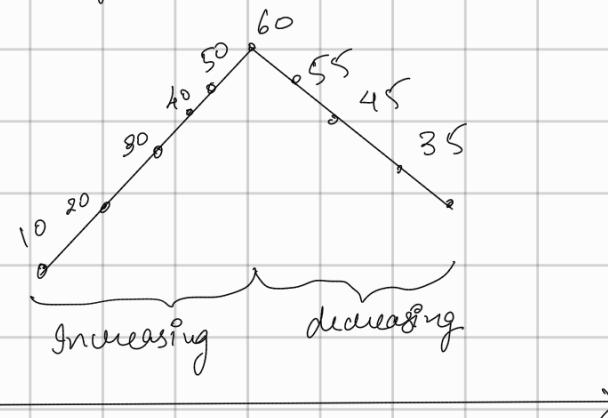


- ① Maximum element in Bitonic array
 - ② Search element in Bitonic array
 - ③ Peak element.
 - ④ Unique element - Sorted array
 - ⑤ Missing element of Arithmetic Progression
- } Bitonic array

① Bitonic array / graph

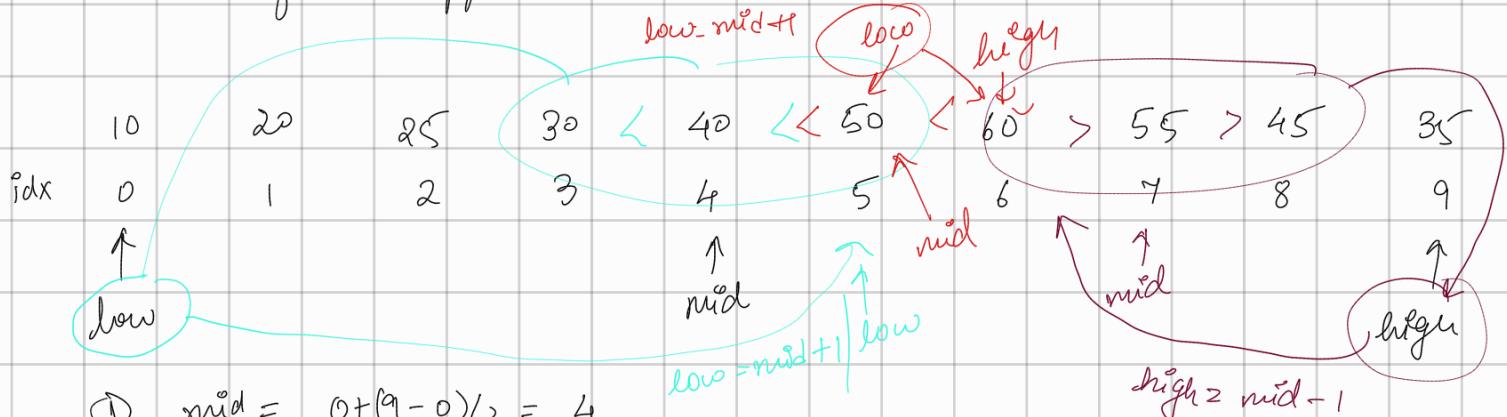
*Value increases
after Decreasing*



Bitonic array will either increase to a point then decrease

Repetition is allowed

Brute force approach $\rightarrow O(n) \rightarrow$ Linear Search



$$\textcircled{1} \quad \text{mid} = 0 + (9 - 0)/2 = 4.$$

if ($\text{mid} \geq \text{mid} - 1 \& \& \text{mid} \geq \text{mid} + 1$)

then peak found

else {

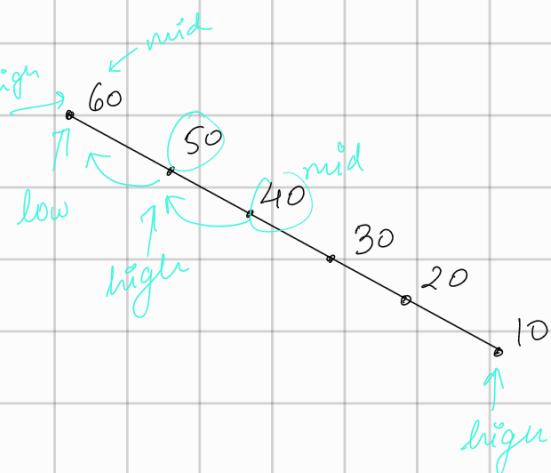
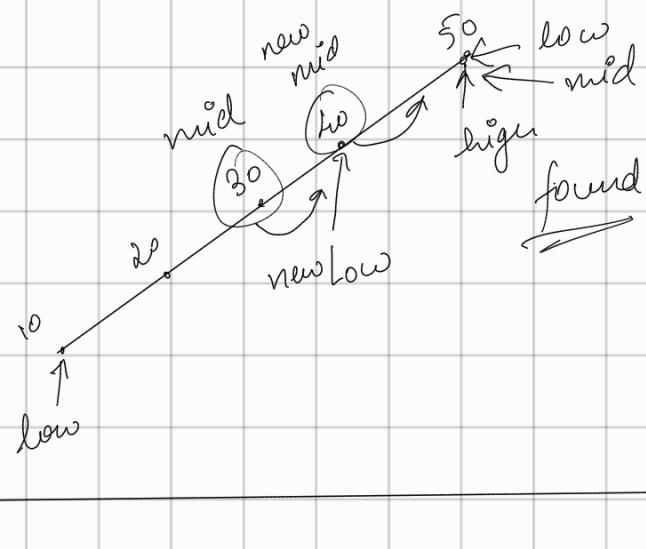
move towards higher

if ($\text{mid} + 1 > \text{mid}$) $\rightarrow \text{low} = \text{mid} + 1$

else $\rightarrow \text{high} = \text{mid} + 1$

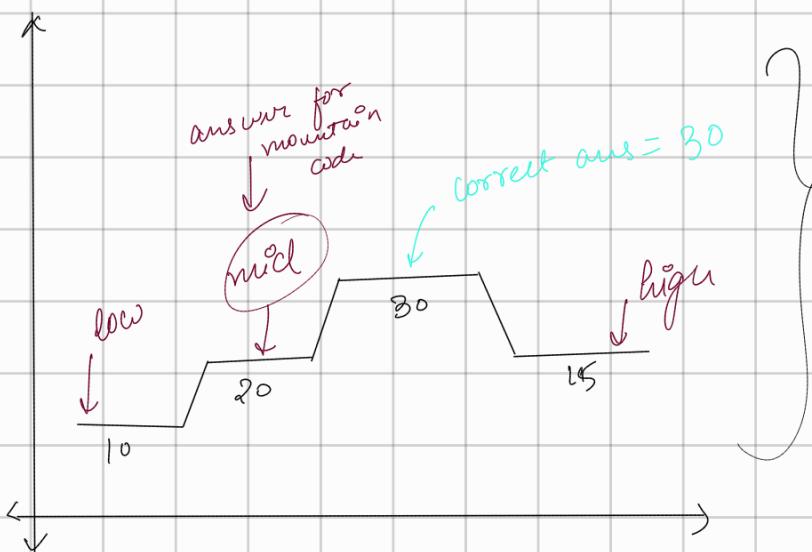
at $\text{idx} = 6$, $\text{low} = \text{high} = \text{mid}$ & it is peak element.

Corner cases: non monotonic:



Code will fail in duplicate elements.

Eg 10 10 10 20 20 20 30 30 30 15 15 15



or discard lower
one of (high, low)
linearly upto where
low == high.
at that point, low = high =
 $O(N)$

Variation needed, check for left & right of equal values. & compare using them

⇒ Approaches $O(n)$ from $O(\log_2 n)$

∴ CODE

```
int low=0, high=n-1;
```

```
while (low <= high){
```

```
    int mid= low + (high - low)/2;
```

```
    int lval=(mid>0)? arr[mid-1]: INT_MIN;
```

int eval = (mid < n - 1) ? arr[mid + 1] : INT_MIN;

if (arr[mid] > eval && arr[mid] < rEval) ↗

return mid;

else if (arr[mid] < eval)

high = mid - 1;

else

low = mid + 1;



}

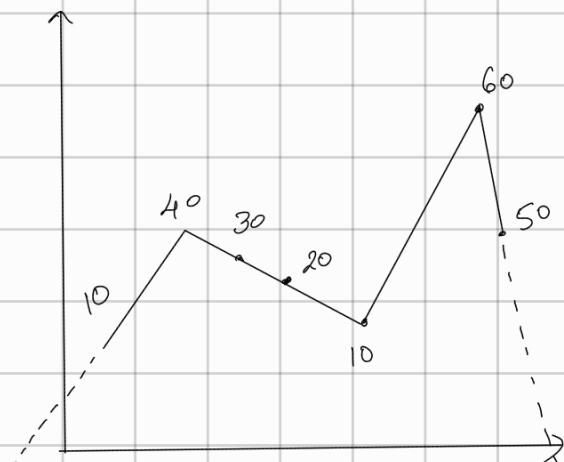
return -1;

② Peak element

* Array is not sorted *

* No two adjacent elements are equal

* $\text{nums}[-1] = \text{nums}[n] = -\infty$



0	1 ✓	2	3	4	5	6
10	40	30	20	10	60	50
↑	↑	↑	↑		↑	↑
l	mid	high	mid		h	

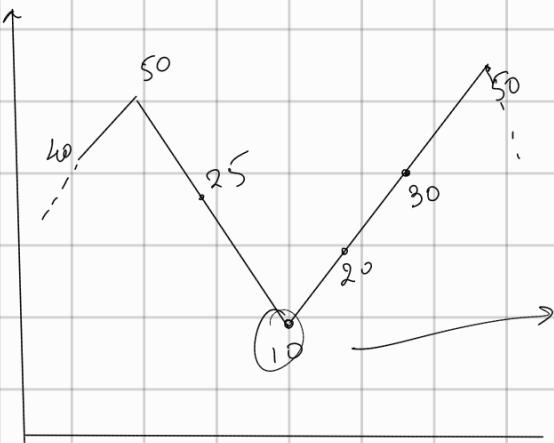
10 < 40 > 30

30 > 20 > 10

50
local
maxima
is
found.

50
search
on
left
half

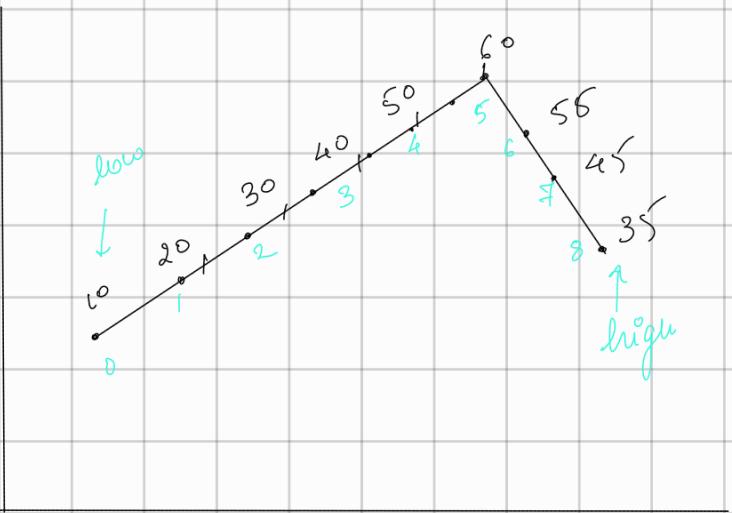
If mid element is valley



go either ways, both sides are guaranteed to have a peak.

③ Search in Bitonic array

Bitonic array: first increasing & then decreasing



Approach: find peak in $O(\log n)$

& apply 2 binary search in $O(\log n)$

$\rightarrow 3 \times \log n \Rightarrow O(\log n)$

(4) Single Elements in a Sorted Array

XOR approach \Rightarrow XOR all elements & return ans
 because $x \wedge x = 0$

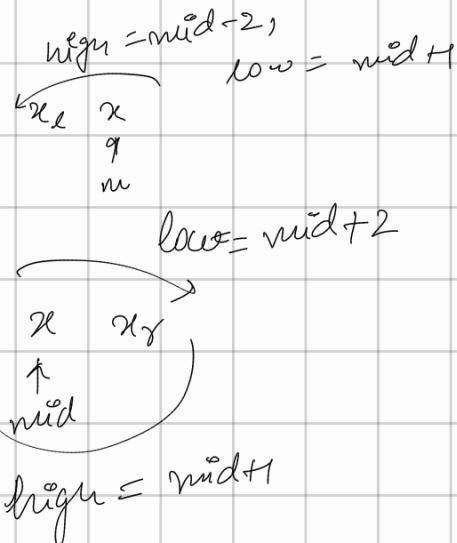
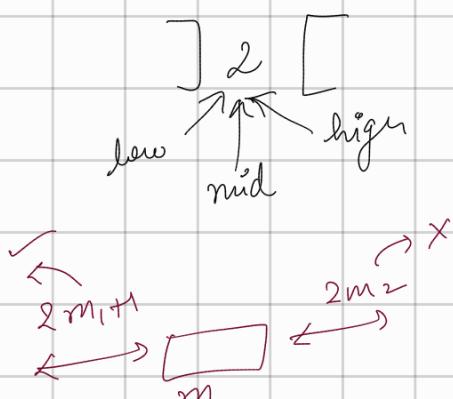
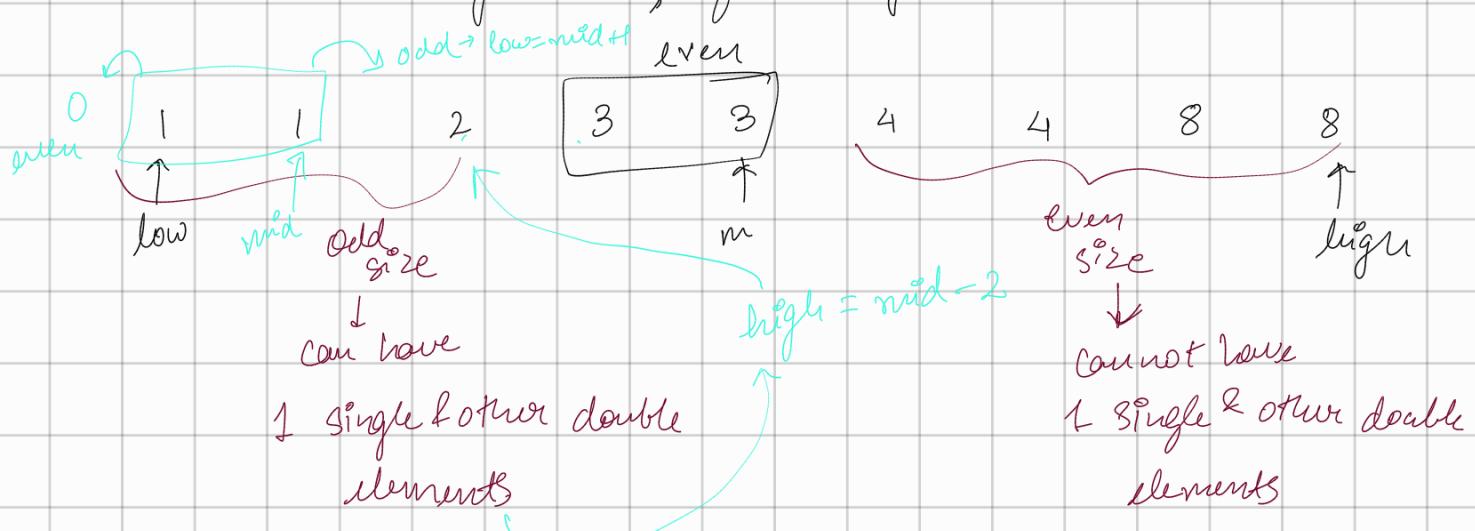
$$\{ 1, 1, 2, 3, 3, 4, 8, 8 \}$$

$$\text{XOR} \rightarrow 1, 0, 2, 1, 2, 6, 2 \rightarrow (2) \checkmark$$

But this is $O(n)$

$$\begin{array}{r} 10 \\ 10 \\ \hline 10 \\ 1000 \\ 8+2=10 \end{array}$$

So use binary search, for $O(\log n)$



x_1 x_2

m

left range = $m - l - 1$

high range = $h - m$

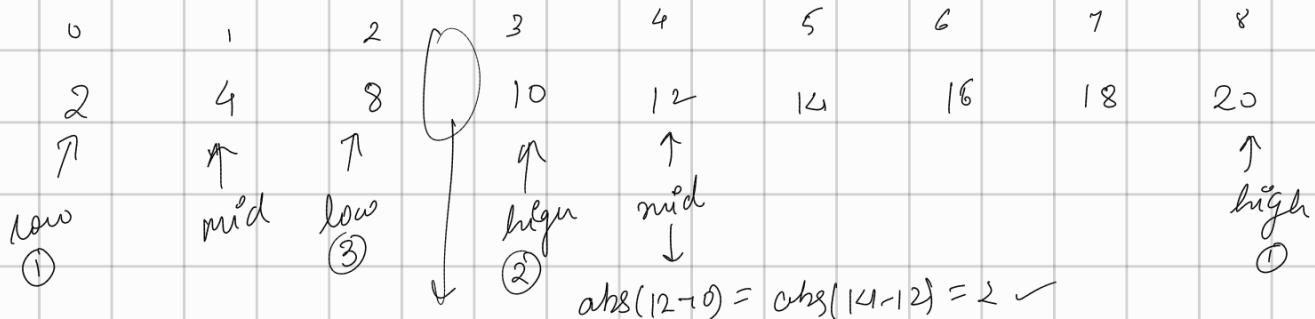
x x_2

m

left range = $m - l$

right range = $h - m - 1$

(Q) Missing element in AP



found.
return 8 + d
=