PH 354: hw 2, problem 1

Alankar Dutta

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Python 3 has integers of arbitrary length. So calculating 200! is done without any problem in Python 3.

However changing to floating point raises an Overflow Exception. This is because 200! is a floating point number greater than what Python 3 can normally handle. On issuing the following command,

import sys sys.float_info

gives the following output:

 $\begin{array}{l} {\rm sys.\,flo\,at_info\,(max=1.7976931348623157\,e+308,\,\,max_exp=1024,\,\,max_10_exp=308,\,\,min=2.2250738585072014\,e-308,\,\,min_exp=-1021,\,\,min_10_exp=-307,\,\,dig=15,\,\,mant_dig=53,\,\,epsilon=2.220446049250313\,e-16,\,\,radix=2,\,\,rounds=1)} \end{array}$

Clearly 200! is beyond this limit which can be verified from the Stirling approximation

$$200! \approx 10^{\frac{200 \ln(200) - 200}{\ln(10)}} \approx 10^{373}$$

As a floating point, Python 3 can go up to 170!