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1st SEMESTER

MID SEMESTER EXAMINATION

MA - 101 Mathematics- I

Time : 90 mins

Roll No. 1123

B.Tech ( All groups)

SEP 2015

Max. Marks: 25

Note: Attempt All questions. All are of equal marks. Assume missing data if any.

- 1 Discuss the convergence of the following infinite series

$$\sum \frac{n^2-1}{n^2+1} x^n.$$

- 2 Expand the function  $f(x) = e^{\tan^{-1}x}$  in infinite series using Maclaurin's theorem up to 4<sup>th</sup> term.

- 3 Show that for rectangular hyperbola  $r^2 \cos 2\theta = a^2$ . The radius of curvature at any point is given as  $\rho = \frac{r^3}{a^2}$ .

- 4 Sketch the curve and find the length of the loop of the curve  $3ay^2 = x(x-a)^2$ .

- 5 The part of parabola  $y^2 = 4ax$  cut off by latus rectum revolves around the tangent at vertex. Find the volume of the reel thus generated.