

# Digital Image Processing HW1

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### 1 Question 5

The following are the three figures for the nearest neighbour interpolation:



(a) Image 1



(b) Image 2



(c) Image 3

Figure 1: Nearest Neighbour Interpolation

The following is the same for bilinear interpolation:



(a) Image 1



(b) Image 2



(c) Image 3

Figure 2: Bilinear Interpolation

Assume the  $n$  points used as references for physically corresponding points were colinear. Referring to our affine transformation calculations we would get the following: Let the affine transformation be  $A$ . Let  $P_1$  be

the matrix  $\begin{bmatrix} x_1^1 & x_2^1 & \dots & \dots & x_{12}^1 \\ y_1^1 & y_2^1 & \dots & \dots & y_{12}^1 \\ 1 & 1 & \dots & \dots & 1 \end{bmatrix}$  and  $P_2 \begin{bmatrix} x_1^2 & x_2^2 & \dots & \dots & x_{12}^2 \\ y_1^2 & y_2^2 & \dots & \dots & y_{12}^2 \\ 1 & 1 & \dots & \dots & 1 \end{bmatrix}$

Then we have

$$A \cdot P_1 = P_2 \quad (1)$$

$$A = (P_2 \cdot P_1^T) \cdot (P_1 \cdot P_1^T)^{-1} \quad (2)$$

$$A = P_2 \cdot P_1^{-1} \quad (3)$$

If  $P_1^{-1}$  exists.

Since  $P_1^T$  has non 0 nullity,  $(P_1 \cdot P_1^T)^{-1}$  does not exist. If we use a pseudo inverse we get a matrix  $P^{-1}$  (and hence  $A$ ) that maps points to arbitrarily large values that could be out of range. For example for a singular matrix  $B$ , if  $Bv = 0$  and a small perturbation gives  $B'v = \epsilon$  where  $\epsilon$  is a vector slightly perturbed from 0, then  $B'^{-1}\epsilon = v$  which means large enough vectors proportional to  $\epsilon$  in the image coordinate ranges are mapped to arbitrarily large values. This lack of accurate transformation power is evident from the fact that there simply isn't enough information in  $P_1$  to calculate  $A$ . Affine transformations encompass scalings, rotations and shearings, all of which cannot be captured in collinear points. Further, we use reverse transform  $A^{-1}$  which may or may not exist for  $A$ .