3. An electric car that runs on batteries must be periodically recharged for a certain number of hours. The battery technology in the car requires that the charge time not be interrupted.

The cost for charging is based on the hour(s) during which the charging occurs. A rate table lists the 24 one-hour periods, numbered from 0 to 23, and the corresponding hourly cost for each period. The same rate table is used for each day. Each hourly cost is a positive integer. A sample rate table is given below.

Hour	Cost
0	50
1	60
2	160
3	60
4	80
5	100
6	100
7	120

Hour	Cost
8	150
9	150
10	150
11	200
12	40
13	240
14	220
15	220

Hour	Cost
16	200
17	200
18	180
19	180
20	140
21	100
22	80
23	60

The class BatteryCharger below uses a rate table to determine the most economic time to charge the battery. You will write two of the methods for the BatteryCharger class.

```
public class BatteryCharger
  /** rateTable has 24 entries representing the charging costs for hours 0 through 23. */
  private int[] rateTable;
  /** Determines the total cost to charge the battery starting at the beginning of startHour.
        @param startHour the hour at which the charge period begins
                 Precondition: 0 \le \text{startHour} \le 23
        @param chargeTime the number of hours the battery needs to be charged
                 Precondition: chargeTime > 0
        @return the total cost to charge the battery
    * /
  private int getChargingCost(int startHour, int chargeTime)
   \{ /* \text{ to be implemented in part (a) } */ \}
   /** Determines start time to charge the battery at the lowest cost for the given charge time.
        @param chargeTime the number of hours the battery needs to be charged
                 Precondition: chargeTime > 0
        @return an optimal start time, with 0 \le \text{returned value} \le 23
  public int getChargeStartTime(int chargeTime)
  { /* to be implemented in part (b) */
  // There may be instance variables, constructors, and methods that are not shown.
```

(a) Write the BatteryCharger method getChargingCost that returns the total cost to charge a battery given the hour at which the charging process will start and the number of hours the battery needs to be charged.

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of	Hours of Charge	Last Hour of	Total Cost
Charge	Time	Charge	
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

- /** Determines the total cost to charge the battery starting at the beginning of startHour.
- * Oparam startHour the hour at which the charge period begins
- * **Precondition**: $0 \le \text{startHour} \le 23$
- * @param chargeTime the number of hours the battery needs to be charged
- * **Precondition**: chargeTime > 0
- * @return the total cost to charge the battery

*/
private int getChargingCost(int startHour, int chargeTime)

(b) Write the BatteryCharger method getChargeStartTime that returns the start time that will allow the battery to be charged at minimal cost. If there is more than one possible start time that produces the minimal cost, any of those start times can be returned.

For example, using the rate table given at the beginning of the question, the following table shows the resulting minimal costs and optimal starting hour of several possible charges.

Hours of Charge Time	Minimum Cost	Start Hour of Charge	Last Hour of Charge
1	40	12	12
		0	1
2	110	or	
		23	0 (the next day)
7	550	22	4 (the next day)
30	3,710	22	3 (two days later)

- /** Determines start time to charge the battery at the lowest cost for the given charge time.
- * @param chargeTime the number of hours the battery needs to be charged
- * **Precondition**: chargeTime > 0
- * Greturn an optimal start time, with $0 \le \text{returned value} \le 23$
- public int getChargeStartTime(int chargeTime)

2009 A Question 3: Battery Charger — Assessment Rubric

Part A: getChargingCost 5 pts

- +1½ access array elements
 - +½ accesses any element of rateTable
 - +1/2 accesses an element of rateTable using an index derived from startHour
 - +1/2 accesses multiple elements of rateTable with no out of bounds access potential
- +2½ accumulate values
 - +½ declares and initializes an accumulator
 - +½ accumulates values from elements of rateTable
 - +1/2 selects values from rateTable using an index derived from startHour and chargeTime
 - +1 determines correct sum of values from rateTable based on startHour and chargeTime
 - +1 value returned
 - +½ returns any non-constant (derived) value
 - +½ returns accumulated value

Part B: getChargeStartTime 4 pts

- +1/2 invokes getChargingCost or replicates functionality with no errors
- +1 determine charging cost
 - +½ considers all potential start times; must include at least 0 ... 23
 - +½ determines charging cost for potential start times

Note: No penalty here for parameter passed to getChargingCost that violates its preconditions (e.g., 24)

- +1 compares charging costs for two different start times
- +1 determines minimum charging cost based on potential start times

Note: Penalty here for using result of call to getChargingCost that violates its preconditions (e.g., 24)

+½ returns start time for minimum charging cost

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2009 A Question 3: Battery Charger — Canonical Solution

PART A:

PART B:

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# AP® SUMMER INSTITUTE SCORING NOTES 2009 AP COMPUTER SCIENCE A

#### Question 3

Sample Identifier: A3 A

Score: 9

part a: correctpart b: correct

Sample Identifier: A3 B

Score: 9

part a: correctpart b: correct

Sample Identifier: A3 C

Score: 8

- part a: loses 1/2 (dec/init). The accumulator is not initialized.
- part b: loses 1/2 (return start). The local variable optimalStart is not initialized and is not guaranteed to have a value when the return is executed.

Sample Identifier: A3 D

Score: 6

- part a: loses 1/2 (oob/multi). There is no attempt to wrap around when the loop control variable exceeds 23. This results in an out of bounds error.
- part a: loses 1 point (det sum). The correct sum will not be determined in the case where a wrap around is necessary and there is no attempt to wrap around.
- part b: loses 1/2 point (cons all). Only elements 0..22 are considered.
- part b: loses 1 point (deter min cost). The local variable lowPrice is initialized to a constant. There is no guarantee that all charging costs will be lower than this constant.

# AP® SUMMER INSTITUTE SCORING NOTES 2009 AP COMPUTER SCIENCE A

Sample Identifier: A3 E

Score: 5

- part a: loses 1/2 point (oob/multi). There is no attempt to wrap around when the loop control variable exceeds 23. This results in an out of bounds error.
- part a: loses 1/2 point (dec/init). The accumulator is not initialized.
- part a: loses 1 point (deter sum). In the loop, the <= should be a < and there is no attempt to wrap around.</li>
- part b: loses 1/2 point (cons all). Only elements 0..22 are considered.
- part b: loses 1 point (deter min cost). The local variable lowest is set to a constant. There is no guarantee that all charging costs will be lower than this constant. In fact, in this case, no charging cost will be less than lowest.
- part b: loses 1/2 point (ret start). No value is returned.

### Sample Identifier: A3F

#### Score: 4

- part a: loses 1 point (deter sum). In the loop, the <= should be a < . (There is no deduction for confusing the mathematical \le with <=.)
- part b: loses 1/2 point (getCharg). Does not invoke getChargingCost.
- part b: loses 1/2 point (cons all). Does not consider any start times.
- part b: loses 1/2 point (det). Does not determine any charging cost.
- part b: loses 1 point (compare costs). Never compares charging costs.
- part b: loses 1 point (deter min cost). No attempt to determine the minimum cost.
- part b: loses 1/2 point (ret start). Does not return a start time.

#### Question 2

#### Sample Identifier: A3 G

Score: 3

- part a: loses 1/2 point (oob/multi). cTime may be greater than 23 which would result in an out of bounds error
- part a: loses all *accumulates values* points because there is no accumulator.
- part a: loses value ret points because no value is returned.
- part b: loses 1/2 point (cons all). Only elements 0..22 are considered.
- part b: loses 1 point (deter min cost). The local variable big is not initialized.
- part b: loses 1/2 point (ret start). The start time is not returned.

## Sample Identifier: A3 H

Score: 2

- part a: loses 1/2 point (oob/multi). The upper bound of the loop is a value in rateTable and will cause an out of bounds error.
- part a: loses all accumulates values points because there is no accumulator.
- part a: loses the last 1/2 point (accum val). The value returned is not an accumulated value.
- part b: loses 1/2 point (getCharg). Does not invoke getChargingCost.

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# AP® SUMMER INSTITUTE SCORING NOTES 2009 AP COMPUTER SCIENCE A

- part b: loses 1/2 point (det). Does not determine any charging cost.
- part b: loses 1 point (compare costs). Never compares charging costs.
- part b: loses 1 point (deter min cost). No attempt to determine the minimum cost.
- part b: loses 1/2 point (ret start). Does not return a start time.

### Sample Identifier: A3 I

Score: 2

- part a: loses 1/2 (oob/multi). There is no attempt to wrap around when startHour exceeds 23. This results in an out of bounds error.
- part a: loses all accumulates values points because there is no accumulator.
- part a: loses 1/2 (accum val). The value returned is not an accumulated value.
- part b: loses 1/2 point (getCharg). Does not invoke getChargingCost correctly (time does not have a value).
- part b: loses 1/2 point (cons all). Does not consider any start times.
- part b: loses 1/2 point (det). Does not determine any charging cost.
- part b: loses 1 point (compare costs). Never compares costs.
- part b: loses 1 point (deter min cost). No attempt to determine the minimum cost.
- part b: loses 1/2 point (ret start). Does not return a start time.

This problem scores a 1 1/2 which is rounded up to a 2.

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

	Start Hour of	Hours of Charge Time	Last Hour of	Total Cost
ļ.	Charge	111116	Charge	<u> </u>
L	. 12	1	12	40
L	0	2	1	110
	22	7	4 (the next day)	550
	22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost	
12	1	12	40	
0	2	1	110	
22	7	4 (the next day)	550	
22	30	3 (two days later)	3,710	

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

```
/** Determines the total cost to charge the battery starting at the beginning of startHour.

* @param startHour the hour at which the charge period begins

* Precondition: 0 \le startHour \le 23

* @param chargeTime the number of hours the battery needs to be charged

* Precondition: chargeTime > 0

* @return the total cost to charge the battery

private int getChargingCost(int startHour, int chargeTime)

* Int Noun = 0;

int Noun = 3tan+Hour;

Por(int x = 0; x \( \) unargeTime: x++)

* If Indur == 24;

Sum += rateTable[nour];

Nour + +;

* Nour Sum;

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Out of the period begins

* Precondition: 0 \le startHour \le 23

* Out of the period begins

* Out of the period begi
```

A3B

A3C

(a) Write the BatteryCharger method getChargingCost that returns the total cost to charge a battery given the hour at which the charging process will start and the number of hours the battery needs to be charged.

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	. 1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

```
Determines start time to charge the battery at the lowest cost for the given charge time.
    eparam chargeTime the number of hours the battery needs to be charged
            Precondition: chargeTime > 0
    @return an optimal start time, with 0 \le \text{returned value} \le 23
public int getChargeStartTime(int chargeTime)
      int optimalstart;
int low Cost = get Charging Cost (O, charge Time);
      Ro (inti=0, i <= 23; i+t)
              if (low Cost > get Charging Cost (i, chargetime)
                     optimal Start = 1;
                     low Cost = get charging tost (i , charge Time);
               7
      return optimal Start
```

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7.	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

```
/** Determines the total cost to charge the battery starting at the beginning of startHour.

* @param startHour the hour at which the charge period begins

* Precondition: 0 \leq startHour \leq 23

* @param chargeTime the number of hours the battery needs to be charged

* Precondition: chargeTime > 0

* @return the total cost to charge the battery

*/

private int getChargingCost(int startHour, int chargeTime)

{

int price = 0;

for (int := 0; i < chargeTime; i ++)

coice += rateTable [ startHour + i];

}

return price;
```

```
/** Determines start time to charge the battery at the lowest cost for the given charge time.
    @param chargeTime the number of hours the battery needs to be charged
            Precondition: chargeTime > 0
    Greturn an optimal start time, with 0 \le \text{returned value} \le 23
public int getChargeStartTime(int chargeTime)
    int Start How = 0;
   int low Price = 500000;
   for(intx=0; x < 23 / x ++)
      if (bwfice > getChargingCost(x, charge Time);

{

lowfrice = getChargingCost(x, charge Time);
        5+art Hour = x/
   return start Harr,
```

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

- /** Determines the total cost to charge the battery starting at the beginning of startHour.
- @param startHour the hour at which the charge period begins
- **Precondition**:  $0 \le \text{startHour} \le 23$
- @param chargeTime the number of hours the battery needs to be charged
- **Precondition**: chargeTime > 0
- @return the total cost to charge the battery

private int getChargingCost(int startHour, int chargeTime)

Fiso; ischargetime; i++)
to cote Toble Isto #Hour + J;

A3E

Assume that getChargingCost works as specified, regardless of what you wrote in part (a). Complete method getChargeStartTime below.

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

- /** Determines the total cost to charge the battery starting at the beginning of startHour.
- * Gparam startHour the hour at which the charge period begins
- * **Precondition**:  $0 \le \text{startHour} \le 23$
- * @param chargeTime the number of hours the battery needs to be charged
- * **Precondition**: chargeTime > 0
- * @return the total cost to charge the battery

private int getChargingCost(int startHour, int chargeTime)

For 
$$(in+k=0)$$
;  $k \le Charge Time; k++) \le total = total + rate Table (start + How + k) % 24];$ 

Tetura total;

- /** Determines start time to charge the battery at the lowest cost for the given charge time.
- * @param chargeTime the number of hours the battery needs to be charged
- * **Precondition**: chargeTime > 0
- * Greturn an optimal start time, with  $0 \le \text{returned value} \le 23$
- public int getChargeStartTime(int chargeTime)

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

- /** Determines the total cost to charge the battery starting at the beginning of startHour.
- * Oparam startHour the hour at which the charge period begins
- * **Precondition**: 0 ≤ startHour ≤ 23
- * Gparam chargeTime the number of hours the battery needs to be charged
- * **Precondition**: chargeTime > 0

* Greturn the total cost to charge the battery

*/

private int getChargingCost (int startHour, int chargeTime)

ifth int start = Start how;

5 tast = sateTable[5+art];

int cTime = chargeTime;

cTime = start - 2 4;

case = 5 tast - 2 4;

case = 5 tast - 2 4;

from cTime to charge, sum of all

Values is charging cost.

/** Determines start time to charge the battery at the lowest cost for the given charge time.

- @param chargeTime the number of hours the battery needs to be charged
  - Precondition: chargeTime > 0
- Greturn an optimal start time, with  $0 \le \text{returned value} \le 23$

public int getChargeStartTime(int chargeTime) \( \frac{2}{3} \) The CTIME = Charge TIME,

int bisi int tem P=0;

for (in+K=0; NZ 23, K+) } temp= get Charging Cost (N, CTIME)

if CHEMP < big) = +em/-b/9;

return tenti

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

/** Determines the total cost to charge the battery starting at the beginning of startHour.

* @param startHour the hour at which the charge period begins

**Precondition**:  $0 \le \text{startHour} \le 23$ 

* @param chargeTime the number of hours the battery needs to be charged

Precondition: chargeTime > 0

* @return the total cost to charge the battery

private int getChargingCost(int startHour, int chargeTime)

If (Start Hour <= a) & & starthour >= 0) & & chargeTime > 0) & & chargeTime > 0)

Stort Cost = rateTable[startHour]'

For Cint i = 0; i < rateTable[startHour]'

Ethor Start Cost * rateTable[startHour + 1]; i+t)

Return Start Cost * rateTable[startHour];

E

For example, using the rate table given at the beginning of the question, the following table shows the resulting costs of several possible charges.

Start Hour of Charge	Hours of Charge Time	Last Hour of Charge	Total Cost
12	1	12	40
0	2	1	110
22	7	4 (the next day)	550
22	30	3 (two days later)	3,710

Note that a charge period consists of consecutive hours that may extend over more than one day. Complete method getChargingCost below.

```
/** Determines the total cost to charge the battery starting at the beginning of startHour.

* @param startHour the hour at which the charge period begins

* Precondition: 0 \le startHour \le 23

* @param chargeTime the number of hours the battery needs to be charged

* Precondition: chargeTime > 0

* @return the total cost to charge the battery

*/

private int getChargingCost(int startHour, int chargeTime)

{

int total = 0;

while (startHour <= chargeTime)

* total = rateTable[startHour] + rateTable[trutHour+1];

* TartHour++;

* return total;

}
```

```
/** Determines start time to charge the battery at the lowest cost for the given charge time.

* @param chargeTime the number of hours the battery needs to be charged

* Precondition: chargeTime > 0

* @return an optimal start time, with 0 \le returned value \le 23

*/

public int getChargeStartTime(int chargeTime)

{

int to tal = get Charging Cost(time, chargeTime);

int time = 0;

While (total > 0)

{

total = total = rateTable [time];

return time;

}

return time;
```