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```
function latticeout
```

Optima

This script outputs a fairly large lattice plot comparing V_cruise, Range and L/D max. The output axis for the lattice plot will be Wing loading, WS and power req, P

```
% Alex M Granata  
% 03 OCT 2015
```

```
close all; clear; clc
```

Initial Assumptions and Requirments of flight

```
% Payload  
% 19 Passengers w/ Cargo @ 225 lbs each, plus crew and attendant  
Wfix=(19+2+1)*225; % lbm  
% Initial Performance Constants  
sfc=0.55; % specific fuel consumption, lb_fuel per hour / lb_thrust  
E=0; % i.e. 25 min loiter time  
AR=10; % Aspect Ratio  
Cd0=0.022; %  
e=0.8; % Oswald Efficiency  
% Cruise Enviromental Conditions  
p_c=1.267e-3; % slugs per ft^3  
% Takeoff Distance  
s_T=3000; % ft  
% WS Restraint Constants  
Cl_max=1.7; % Max C_L for takeoff  
V_stall=75*1.688; % Stall speed in ft/s, Sea Level, max 75 knots  
% Convience Conditions  
K=1/(e*pi*AR);  
V_md=@(ws,p) sqrt(2*ws/(p*sqrt(Cd0/K)));  
V_mp=@(ws,p) sqrt(2*ws/p)*(K/3*Cd0)^(1/4);  
p_sl=2.3769e-3; %slugs/ft^3, sea level density  
% Service Ceiling  
p_sc=.958e-3; % slugs per ft^3
```

Domains of independent variables

```
Rl=5; Rd=linspace(800,1200,Rl)*1.151; %miles
Vl=6; Vd=linspace(250,300,Vl)*1.466667; %ft/sec
LDl=2; LDd=linspace(18,22,LDl); % Keep resolution of LD <5
WTOl=4; % Number of isolines for the WTO contours
```

Numerical Calculations

For loops to calculate WS, TW and P for independent Variables

```
tic
optimzd=zeros(Rl,Vl,LDl,3);
poolobj = gcp('nocreate'); % If no pool, do not create new one.
if isempty(poolobj)
    parpool('local')
end

for it_LD=1:LDl
    LD=LDd(it_LD);
    for it_R=1:Rl
        R=Rd(it_R);
        for it_V=1:Vl
            V_c=Vd(it_V);

            % Fuel Weight Fraction
            % Fuel ratios
            Wr=exp(-R*sfc/(V_c/1.46666667*(0.943*LD)));
            We=exp(-E*sfc/(LD));
            % Full ratio
            Wl_6=0.97*0.985*Wr*1*We*0.985;
            Wf_Wto=1.06*(1-Wl_6);
            % Empty Weight
            % From Trend line data, We=XX Wto ^ YY, XX=0.911, YY=0.947
            Wept=@(Wt) 0.911*Wt^0.947;
            % Takeoff Weight Estimation
            % Compare We_est to Wto_est - Wfix - Wfuel
            Wto=fsolve(@(wt) wt*(1-Wf_Wto)-Wfix-
Wept(wt),30e3,optimoptions('fsolve','Display','off')); % Estimate
W_TO

            % Wing-loading min to meet C_L_max and V_stall assumptions
            WS_s=0.5*p_c*V_stall^2*C_L_max;
            % Min loading for to meet Range requirement
            WS_r=fsolve(@(x) Wf_Wto*Wto*1.07/
sfc*(x/(p_c))^0.5*(AR*e)^(1/4)/Cd0^(3/4)*(1/Wto)-
R,10,optimoptions('fsolve','Display','off'));
            % Limit on W/S for Landing Distance within required
            distance, 3 degree
            % angle of approach
            WS_l=fsolve(@(ws) s_T-(79.4*ws/(1*C_L_max)+50/tand(3)),...
50,optimoptions('fsolve','display','off'));
```

```

        % Drag for Power
        D=@(ws,V,p,dhdt,n) (Wto*dhdt)/V + (Cd0*V^2*Wto*p)/(2*ws) +
        (2*K*Wto*n^2*ws)/(V^2*p);

        % Calculations for Power
        % Straight, Level Flight
        Preq_cruise=@(ws) D(ws,V_c,p_c,0,1)*V_c/(p_c/p_sl);
        % Service Ceiling
        Preq_serv=@(ws)
        (D(ws,V_mp(ws,p_sc),p_sc,100/60,1).*V_mp(ws,p_sc)/(p_sc/p_sl));
        % Cruise Ceiling
        Preq_cc=@(ws)
        D(ws,V_mp(ws,p_c),p_c,300/60,1).*V_mp(ws,p_c)/(p_c/p_sl);
        % 2.5g Maneuver at Sea Level
        Preq_man=@(ws) D(ws,V_c,p_sl,0,2.5)*V_c/(p_sl/p_sl);

        % Takeoff Power, from Takeoff T/W
        VTO=V_stall*1.2;
        n=6; d=5;
        T0=@(p) 0.25*(p./n.*d).^(2/3);
        T0t=@(p) T0(p).*n;
        a=@(p) ((p/VTO)-T0t(p))/(VTO)^2;
        A=@(p) 32.2*(T0t(p)/15000-0.04);
        mu=0.04; % Firm Turf
        Cd_g=0.0527; %Ground roll drag
        CL_g=1.7; % max ground lift
        B=@(p,ws) 32.2/Wto*(0.5*p_sl*(Wto/ws)*(Cd_g-mu*CL_g)+a(p));
        s=@(p,ws) 1./(2*B(p,ws)).*log(A(p)./(A(p)-
        B(p,ws)*(VTO)^2));
        Preq_TOop=@(ws) fsolve(@(p)
        s(p,ws)-2000,600*550,optimoptions('fsolve','Display','off'));

        mat=[{Preq_cruise};{Preq_cc};{Preq_man};{Preq_serv};
        {Preq_TOop}];
        [wsx,py]=fminbnd(@(ws) ...
        max([mat{1}(ws),mat{2}(ws),mat{3}(ws),mat{4}
        (ws),mat{5}(ws)]),...
        max(WS_r,WS_s),WS_l);
        if numel(wsx>1)
            wsx=wsx(1);
        end
        optm=[wsx,py/550]; % in lbs/ft^2 and hp

        optimzd(it_R,it_V,it_LD,:)=[optm,Wto]; % Save Optimized
Data
    end
end
end
toc

```

Figure Setup

Base figure will be used to output the optimized Ws/Power, and control the other two design space and optimizer plots

```
r=groot;
if size(r.MonitorPositions,1)>1
    bspos=r.MonitorPositions(1,:);
    f_detpos=r.MonitorPositions(2,:);
else
    bspos=r.MonitorPositions(1,:).*[1 1 1 0.5];

    f_detpos=[r.MonitorPositions(1,1),r.MonitorPositions(1,4)/2,r.MonitorPositions(1,
    0.5)];
end

bs=figure('Name','Optimized Power and Wing Loading',...
    'NumberTitle','off',...
    'DockControls','off',...
    'MenuBar','none',...
    'Units','pixels',... 'Resize','off',...
    'Position',bspos,...
    'deletefcn','close all; clear; clc;');

% Setup the axes for
abse=axes('Parent',bs);
abse.XLimMode='manual';
abse.Title.String='Power Requirments and Wing Loading';
abse.XLabel.String='Wing Loading W/S, lbs/ft^2 by LD_{max}';
abse.YLabel.String='Power_{Required}, hp';
abse.Color='none';
hold(abse,'on')

% Details figure will be a split plot graphic the details of the
% selected
% point int he bas figure
f_det=figure('Name','Point Specifc Details',...
    'NumberTitle','off',...
    'DockControls','off',...
    'MenuBar','none',...
    'Units','pixels',... 'Resize','off',...
    'Position',f_detpos,...
    'deletefcn','close all; clear; clc;');
aTW=axes('Parent',f_det);
aTW.XLimMode='manual';
subplot(1,2,1,aTW);
aTW.Title.String='Constraints on Wing Loading and Specifc Thrust';
aTW.XLabel.String='Wing Loading W/S';
aTW.YLabel.String='Specifc Thrust: T/W';
hold(aTW,'on')
aPW=subplot(1,2,2);
aPW.Title.String='Operational Power Curves';
aPW.XLabel.String='Wing Loading W/S';
```

```
aPW.YLabel.String='Power_{Required}, hp';
hold(aPW,'on')
```

```
clear r bspos f_detpos
```

Setup Xaxis for Lattice Plot

```
abse.Units='pixels';
szax=abse.Position;
abse.Units='normalized';
catlim=round(szax(3)/LD1/50-2,0);
rng=[min(min(min(optimzd(:, :, :, 1)))) , max(max(max(optimzd(:, :, :, 1))))];
magni=round(log10(diff(rng)))-1;
% Determined magnitude of steps
optmsmag=[1,2,5];
rangeoptions=optmsmag*10^magni*catlim;
[~,ir]=min(abs(rangeoptions-diff(rng)));
stepsz=optmsmag(ir)*10^(magni); %determine size of nominal steps
lbs=floor(rng(1)/stepsz)*stepsz:stepsz:ceil(rng(2)/
stepsz)*stepsz; %Actual steps
x_ticklabel={' ',lbs};
x_tickvalue=1:((length(lbs)+1)*LD1);
abse.XTickLabel=x_ticklabel;
abse.XTick=x_tickvalue;
abse.XLim=[1 ((length(lbs)+1)*LD1)];
```

```
clear szax catlim rng magni optmsmag rangeoptions ir stepsz
```

Plot the V/R Optimized Data

Split Lattice plot in order to display data

```
figure(bs);
axes(abse);
xint=zeros(R1,V1,LD1);
yint=zeros(R1,V1,LD1);
% Plot Each Carpet by successive LD settings
for a=1:LD1
    % Velocity Dependant
    for b=1:V1

xint(:,b,a)=(a-1)*((length(lbs)+1)+1+interp1(lbs,1:length(lbs),optimzd(:,b,a,1),'p
plot(abse,xint(:,b,a), optimzd(:,b,a,2),'Color',0.8*[1 1 1])
if V1*LD1>20
    if b==1 || b==V1 || b==round(V1/2)
        text(xint(1,b,a),...
            optimzd(1,b,a,2),...
            sprintf('%.4g mph',Vd(b)/1.46666667),...

'Verticalalignment','top','horizontalAlignment','left')
    else
        continue
    end
```

```

        else
            text(xint(1,b,a),...
                optimzd(1,b,a,2),...
                sprintf('%.4g mph',Vd(b)/1.46666667),...

            'Verticalalignment','top','horizontalAlignment','left')
        end
    end

    % Range Dependant
    for c=1:Rl

yint(c,:,a)=(a-1)*(length(lbs)+1)+1+interp1(lbs,1:length(lbs),optimzd(c,:,a,1),'p
    plot(abse,yint(c,:,a),optimzd(c,:,a,2),'Color',0.8*[1 1 1])
    if Rl>5
        if c==1 || c==Rl || c==round(Rl/2)
            text(yint(c,1,a),...
                optimzd(c,1,a,2),...
                sprintf('%.4g nm',Rd(c)/1.151),...

            'Verticalalignment','middle','horizontalAlignment','right')
        else
            continue
        end
    else
        text(yint(c,1,a),...
            optimzd(c,1,a,2),...
            sprintf('%.4g nm',Rd(c)/1.151),...

        'Verticalalignment','middle','horizontalAlignment','right')
    end
end
end

clear yint

```

LD Max Indicators

Connection Lines for LD_max boxes

```

ldconres=25;
for b=[1 V1]
    for c=[1 R1]
        tstr0(1:LD1)=optimzd(c,b,:,1); outr0(1:LD1)=optimzd(c,b,:,2);
        tstr1=((1:LD1)-1)*(length(lbs)+1)+1+...
            interp1(lbs,1:length(lbs),tstr0,'pchip');

        outr1=interp1(tstr1,outr0,linspace(tstr1(1),tstr1(end),ldconres),'pchip');

        plot(abse,linspace(tstr1(1),tstr1(end),ldconres),outr1,'Color',0.8*[1
            1 1]);
    end
end

```

```

% Text Label for LD_Max
for a=1:LD1
    text((a-1)*(length(lbs)+1)+round(length(lbs)/2+1),...
        abse.YLim(1)+0.93*diff(abse.YLim),...
        sprintf('LD_{max}: %.3g',LDd(a)),...
        'HorizontalAlignment','center','Color','r')
end

clear tstr0 tstr1 outr0 outr1

```

Gross Takeoff Weight Isolines

Draw isolines on each independante carpet plot of the W_TO for the V/R pairing. This plot is unique such that it all has to be done at once, so that a colorbar may be added to the side of the plot for indications

```

% First, define an axis that matches directly on top of abse
abs2=axes('Parent',bs);
abs2.Units='pixels';
abs2.XLimMode='manual';
abs2.Title.String='';
abs2.XLabel.String='';
abs2.YLabel.String='';
hold(abs2,'on')
abs2.XTickLabel='';
abs2.XTick=x_tickvalue;
abs2.XColor='none'; abs2.YColor='none';
abs2.XLimMode='manual'; abs2.XLim=abse.XLim;
abs2.YLimMode='manual'; abs2.YLim=abse.YLim;
abs2.ZLimMode='manual';
bs.Children=[bs.Children(2);bs.Children(1)];

% Grab C data from each WTO/LD system,
for a=1:LD1
    xint0=xint(:, :, a);
    optimzd0=optimzd(:, :, a, 2);
    optimzd1=optimzd(:, :, a, 3)/1000;
    contour(abs2,xint0,optimzd0,optimzd1,WTO1,'LineWidth',1.3);
end
clb=colorbar;
clb.Label.String='W_{gross takeoff}, 1,000 lbs';
abse.Units='pixels';
abse.Position=abs2.Position;
abse.Units='normalized'; abs2.Units='normalized';

clear xint optimzd0 optimzd1

```

Data Tip Details and Updater

Turn on Data Cursor mode for base figure, and assign the appropriate callback function to graph the details

```

bs.CurrentAxes=abse;
bsdc=datacursormode(bs);

```

```

bsdc.UpdateFcn=@drawdetails;
bsdc.Enable='on';

function output_txt = drawdetails(~,evntobj)
    % Used to output custom datatip information, as well as update
the detail
    % graphs that show specic information about the selected data.
    pos = get(evntobj,'Position');
    ldind=floor(pos(1)/(length(lbs)+1))+1;
    ldout=LDd(ldind);
    [ri,ci]=find(optimzd(:, :, ldind, 2)==pos(2));
    WSout=optimzd(ri,ci,ldind,1);
    Wto_out=optimzd(ri,ci,ldind,3);
    posout=[interp1(1:length(lbs),lbs,pos(1)-floor(pos(1)/
(length(lbs)+1))*(length(lbs)+1)-1),...
    pos(2)];
    output_txt = {[ 'LDmax: ',num2str(ldout,3)],...
    [ 'WS: ',num2str(WSout,4)],...
    [ 'P: ',num2str(pos(2),4)],...
    [ 'W_{takeoff}: ',num2str(Wto_out)]}];

    % Begin graphics
    [Rin,V_cin]=find(optimzd(:, :, floor(pos(1)/
(length(lbs)+1))+1, 2)==pos(2));
    R=Rd(Rin);
    V_c=Vd(V_cin)/1.46666;
    LD=LDd(floor(pos(1)/(length(lbs)+1))+1);
    WS_r=[]; WS_s=[]; WS_l=[]; TW_c=[]; TW_cruise=[]; TW_serv=[];
    TW_cc=[];
    TW_man=[]; ym=[]; xm=[]; WSD=[]; s_tm=[];
    Preq_TO=[]; Pr=[];

    ymabs=abse.YLim;
    keyboard
    cnstr_n
    power_cnstr_n
end

end

```

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