

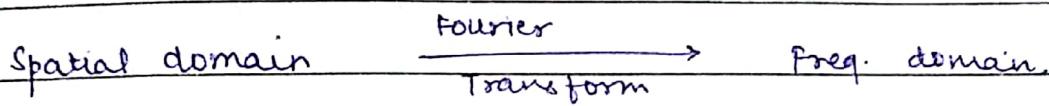
Contd. --

Frequency Domain : Fourier Transform

→ Earlier, we talked about ~~image~~ ~~the~~ image restoration in spatial domain. Now, we will talk about freq. domain.

low frequency : not much change in intensity, smoothening

high " : sudden change " " edge.

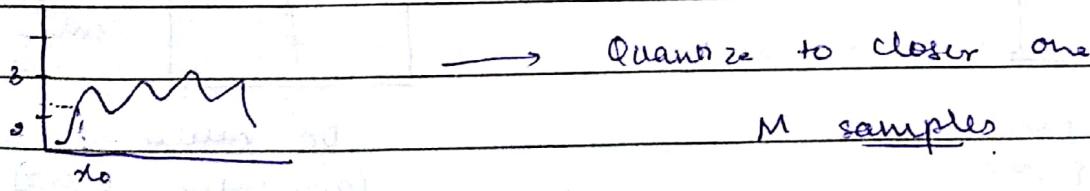


Fourier Series : for periodic signal

" Transform : " aperiodic "

Any transform : signal can be represented by sum of sine & cos

Continuous \rightarrow Discrete [sampling + Quantization]



1-D

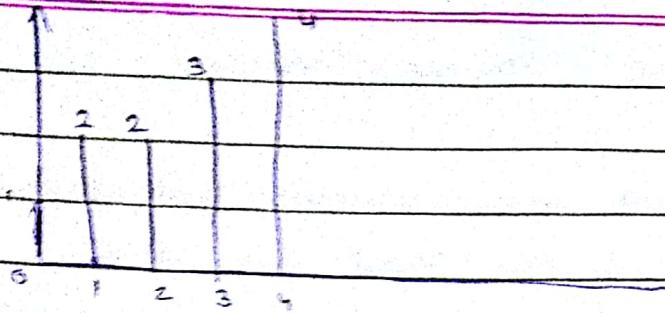
$$F(u) = \frac{1}{M} \sum_{n=0}^{M-1} f(n) e^{-j 2\pi u n / M}$$

u → freq.
n → coordinate
in spatial domain

$$f(n) = \sum_{u=0}^{M-1} F(u) e^{j 2\pi u n / M}$$

(go back to spatial
→ Inverse Fourier)

Find Fourier



$|F(0)| \rightarrow$ gives avg. value of the signal

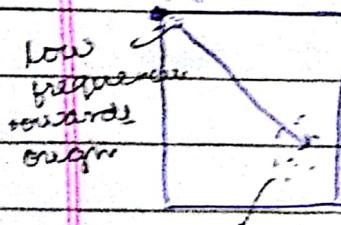
$|F(u)|^2 \rightarrow$ Power spectrum of signal ($f(x)$)

2-D :

$$F(u,v) = \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) e^{-j2\pi \left(\frac{ux}{M} + \frac{vy}{N}\right)}$$

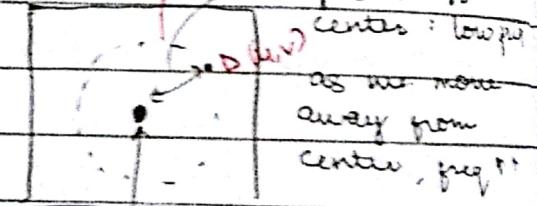
$F(0,0) \rightarrow$ gives avg. intensity.

$F(0,0)$



high frequency away from origin

for better visualization



DC value
(avg value: $F(0,0)$)

Basic filtering :

1. Multiplying i/p image by $(-1)^{ux}$: move DC-value to center

suppose img is corrupted by high freq. noise.

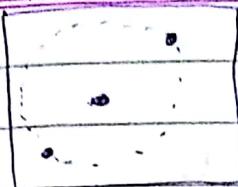
apply formula : add some filter so all high freq. are removed & inverse

e.g. → Botori corrupted by sine wave
(glare)

H/W : Convert into Fourier transform
shift image towards center. Check high freq components & remove them. Do Inverse Fourier transform

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Why only getting 1 point in freq. domain?

If it has 1 sine wave : it'll have 1 freq.
so, just have a point.

In Fourier Transform : each freq. has ^{component} conjugate pair also. (complex)

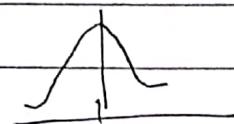
can have filter in circle form. st all points on the circumference = 0. (by masking) [Rest values are 1]

Place Mask & multiply. Then, freq. at circumference of circle will be 0 \Rightarrow removed them.

Then, we can do inverse Fourier to get original image

\rightarrow Salt & Pepper Noise : impulse noise

\rightarrow low pass : all ~~freq.~~ high freq. \rightarrow rejected
 \Downarrow
only smooth areas are observed.
no edges \Rightarrow ..



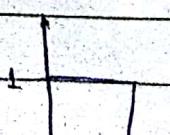
\rightarrow high pass : all edges are clearly defined.



\Rightarrow Spatial domain?

low pass : Avg. filter high pass : laplacian

Ideal low pass filter



D_c \rightarrow cut off freq.

Gaussian & Butterworth is almost same

slightly
narrow

⁴ slightly broader

distance from center

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$$H(u,v) = \begin{cases} 1 & D(u,v) \leq D_0 \\ 0 & D(u,v) > D_0 \end{cases}$$

→ Butterwooth :

Graph : $n=4$: steep cut-off \rightarrow tells about
 $n=1$: smooth \rightarrow smoothening of w_{eff}
 $n \rightarrow$ Order of filter \rightarrow gradual cut-off

\rightarrow Ideal High Pass:

$$H(u,v) = \begin{cases} 0 & D(u,v) \leq D_0 \\ 1 & D(u,v) > D_0 \end{cases}$$

$\text{Do } z \in S \rightarrow \text{ everything outside } S \text{ is allowed}$

$D_0 = 30 \rightarrow$ only one wave. * very high freq. are allowed.

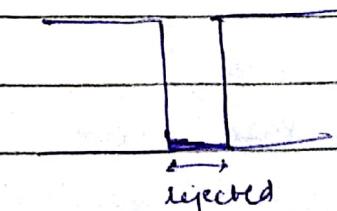
Reject filter = 1 - Pass filter

Selective filter \rightarrow

Periodic Noise Red? → have to see, isolate point

have burst kind of freq.

→ Band Reject filter :

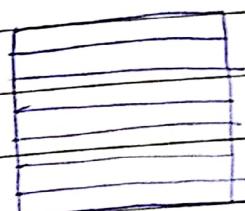


Notch filter - very similar to bandreject (remove freq within specific band).

→ better to have its conjugate reflection also. (to restore conjugate filter pair also).

89 noise :

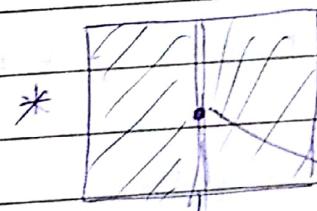
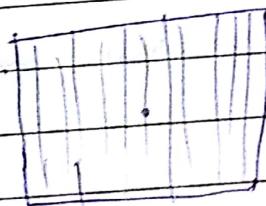
freq. : change of Intensity



in horizontal dir : No Δ freq.
in vertical = : If Δ freq.

in vertical - : f Δ freq.

Fourier transform



• got
→ ~~fixed~~ (get only vertical bed
image
only the noise
in, they have removed,
because, don't want to change
low freq.

1 - this noise = good image

or → apply Band reject image.

Mers : (b) \rightarrow Not very sharp freq. comp. \Rightarrow diff. to decide what to remove & what not to

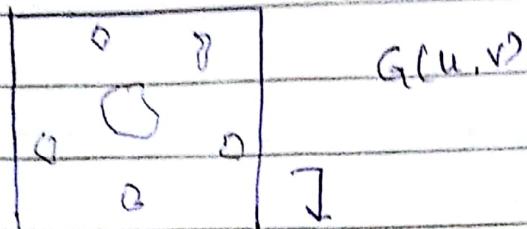
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Optimum Notch
filter

Optimum Notch Filtering

$\hat{f}(x,y)$: estimate of original image $f(x,y)$



$$\text{don't know } g(x,y) - \eta(x,y) = \hat{f}(x,y)$$

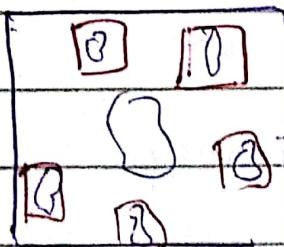
how much is (degraded noise)
image & how
much is original
image

$$g(x,y) = f(x,y) * H(x,y) + \eta(x,y)$$

Task \rightarrow minimize diff. b/w $f(x,y)$ & $\hat{f}(x,y)$

Here, we do unweighted filtering & try to min. weight

H_{NP} : Notch Pass filter



allowing
these freq. (high freq)
in notch pass
filter (noise
in freq domain)

Frequency
Transform of
Noise $N(u,v) = H_{NP}(u,v) G(u,v)$

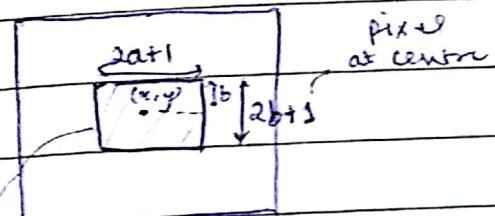
Take inverse to get noise.

→ says, do a weighted noise subtraction, don't remove noise directly as it may contain original image.

$$\hat{f}(x,y) = g(x,y) - w(x,y) \eta(x,y)$$

select $w(x,y)$ st variance of $\hat{f}(x,y)$ is minimized

↓
image is app. is the same.



$$s = a \quad t = b$$

local variance

$$\sigma^2(x,y) = \frac{1}{(2a+1)(2b+1)} \sum_{s=0}^{2a+1} \sum_{t=0}^{2b+1} [\hat{f}(x+s, y+t) - \hat{f}(x,y)]^2$$

Suppose, in a noise nbd weight is almost const.

$$\Rightarrow w(x,y) = w(x,y) = w(x+s, y+t)$$

Since for w,

→ Now, we can obtain $\hat{f}(x,y)$

" Till now, we didn't consider Degradation funcn."

Estimating the Degradation Function

① Mathematical modeling

Use mathematical func's to get degradation func'.

If $k \downarrow t \Rightarrow$ turbulence is ↑

Inverse filtering

$$\hat{f}(u,v) = \frac{G(u,v)}{H(u,v)}$$

$$= \frac{F(u,v) H(u,v) + N(u,v)}{H(u,v)} = \frac{F(u,v)}{H(u,v)} + \frac{N(u,v)}{H(u,v)}$$

If $H(u,v)$ is high & small noise is added to $f(u,v)$

Won't able to get original image

Now → estimate will be wrong

Ex. → Guessing cut-off frequency seeing responses

Min. Mean square Error Filtering \Rightarrow Wiener

$$\min. E^2 = E \left\{ (f - \hat{f})^2 \right\}$$

S_n : Power spectrum of noise

S_f : Power spectrum of estimated undegraded image

→ SNR Ratio should be ↑

- ① math. modelling of optimum NP & weiner filters
- ② Try to remove img.

Image Compression

Reason to Compress:

- 1) Transmission
- 2) Storage

→ Video : $720 \times 480 \rightarrow$ have 30 frames per sec.
2 hr movie

No. of bits in each pixel : 24 (RGB)

Size for 2 hr movie = $30 \times 2 \times 60 \times 60 \times 720 \times 480 \times 24$

$\approx 200 \text{ GB}$ (DVD Capacity : max 8.5GB)

diff. to transmit data

→ irrelevant / repeated

→ Will compress it (remove the redundant data)

→ Will use some coding technique

Relative Data Redundancy

Compression Ratio

$C = \frac{b}{b'} \rightarrow$ Original ~~message~~ Representation
 $b' \rightarrow$ New Representation

$R = 1 - \frac{1}{C} \rightarrow$ relative data redundancy

Teacher's Signature.....

$$\text{if } b = 8 \quad \& \quad b' = 2 \quad \Rightarrow \quad C = 4$$

$R = 0.75 \rightarrow 75\% \text{ of data is redundant}$
(in original image)

→ Implement Compression :

(1) coding redundancy

e.g. gray image just using 3 or 4 gray levels.

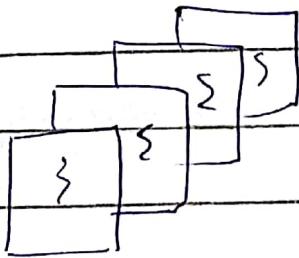
now, we don't need 8 bits but we're representing it in 8 bits

(2) Spatial & temporal redundancy :

spatial (nbd) e.g. large areas of gray / some color [current pixel is same
can I represent it in other way next ---]

Temporal = In videos

(time) represented by : $f(x, y, t)$



All images are almost same
Can I represent it in some other
way ?

(3) Irrelevant information :

Take broader view of image (removing detailed part)
Can I remove this info. to compress image ?

Fig 2.1 (a) Only 4 or 8 gray levels have but we're using 8 bits \rightarrow Coding redundancy

(b) Many areas of same color \rightarrow Spurious

10 for every gray color, not interested in details.

Coding Redundancy

\rightarrow intensity with highest prob, give it smallest code. others, give some length
code 2, $c_2 = 2$ in each, or do as above

$r_{21} = 39$	(0.25)	01	2
$r_{100} = 128$	(0.47)	1	1
$r_{136} = 196$	(0.25)	000	3
$r_{135} = 205$	(0.03)	001	3

}

Code is assigned in such a way that when you get a seq of codes, there's no discrepancy in decoding (only 1 possible way of decoding)

No. of bits used

$$\text{Avg. } = (0.25)(2) + (0.47)(1) + (0.25)(3) + (0.03)(3)$$

$$= 1.81 \text{ bits}$$

$$C = \frac{b}{b'} = \frac{8}{1.81} \approx 4.42$$

$$R = 1 - \frac{1}{C} = 0.774$$

If I assign 2 bits to each, then

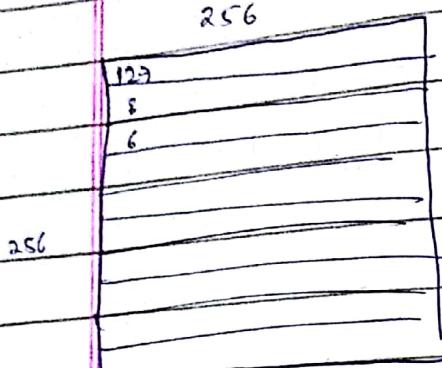
$$C = \frac{b}{b'} = \frac{8}{2} = 4$$

Spatial & Temporal Redundancy

spatial :- In histogram : all intensities are equally probable

→ Eliminate by using a seq. of run-length pairs

256



↑ specifies start of new

intensity & no. of consecutive pixels that have that intensity

Right Now : Using $256 \times 256 \times 8$ bits

Now, we can represent as :

(127, 256), (8, 256), (2, 256)

↑ ↑

Intensity frequency
of 127
(run length)

Now : Using $256 \times 8 \times 2$ bits

$$C = \frac{256 \times 256 \times 8}{256 \times 8 \times 2} = \underline{\underline{128}}$$

* If 100 intensity comes 2 times, we can add them together.

Relevant Information

slide

→ did some histogram equalisation

→ If you need that info., code it. (Otherwise, not)

$$C = \frac{256 \times 256 \times 8}{8}$$

8 → whole img is 1 color \Rightarrow Just need 8 bits

$$I(E) = \log_m \frac{1}{P(E)} = -\log_m P(E)$$

$m = 2 \Rightarrow$ info. is bit

$P(E) = 1/2 \Rightarrow 2$ options (Y/N) \Rightarrow need 1 bit

$P(E) = 1 \Rightarrow$ it will definitely occur \Rightarrow no info.

\rightarrow Entropy tells how many pixels should be atleast there so that property of image is not lost.

\rightarrow If $I_{rms} = 0 \Rightarrow$ lossless compression

$I_{rms} \neq 0 \Rightarrow$ lossy "

Original image : $f(x, y)$

compressed & transmitted : decoded at destⁿ : $\hat{f}(x, y)$
 ↑
 signal

Some basic Compression Models

① Huffman Coding

symbol \rightarrow may be intensity values

- \rightarrow combine lowest prob.
 - \rightarrow put in descending order.
 - \rightarrow ultimately, I just've 2 prob.
- $\left. \begin{matrix} \\ \\ \end{matrix} \right\}$ Src
Redⁿ

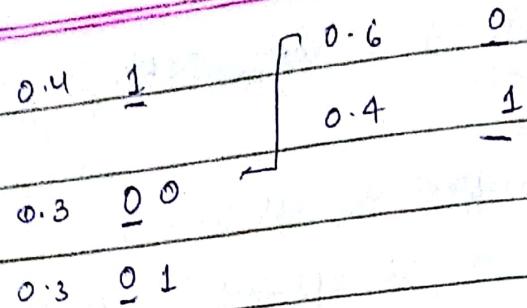
\hookrightarrow Most frequently occurring gray value has shortest code.

Higher prob. \rightarrow Assign 0

Lower prob. \rightarrow " 1

\rightarrow Trace back route

Teacher's Signature.....



* whenever I write a sequence, I will always ~~find~~ same unique way

$a_2 \ a_6 \ a_1$, * code by which you encoded should be available at decoding side also
1 0 0 0 1 1

decoding end: $a_2 \ a_6 \ a_1$

eg. $\begin{array}{ccccccccc} & & & & & & & 3 & 1 \end{array}$
 $\begin{array}{ccccccccc} 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 1 \\ \underbrace{\quad\quad\quad}_{a_3} \quad \underbrace{\quad\quad}_{a_1} \quad \underbrace{\quad\quad}_{a_2} \quad \underbrace{\quad\quad}_{a_6} & & & & & & & 2 & 2 \end{array}$
 $\begin{array}{ccccccccc} & & & & & & & 6 & 6 \end{array}$

② LZW (Dictionary Coding)

(We're providing code for patterns)

→ don't require prob.

eg.	3 9	3 9	126	126	3
(an enc over length)	3 9	3 9	126	126	3
	3 9	3 9	126	126	1
	3 9	3 9	126	126	1

$$(39, 2) \times (126, 4) / (126, 2), \dots$$

Dictionary is not needed here at decoding side as it'll be automatically created.

We know 256 gray levels are there

0 to 255 → give entries 0 - 255.

256 to 511 → empty right now.

) 9-bits
for dictionary

→ Algo will try to find next intensity (to check spatial constraint)

39 → next pixel value : also 39

stored pattern 39-39 & gave value 256

[There is no entry for 39-39 earlier, only for 39]
↓
39

Once it has recognized a sequence 39-39, it is checking for next pixel also.

Currently Recognized Sequence	Pixel being recognized	Encoded Opp	Dictionary Location	Dictionary Entry
	39			
39	39	39	256	39-39
39-	126	39	257	39-126
126	126	126	258	126-126
126	39	126	259	126-39
39	39			whole pattern is replaced by 39-39-126 (earlier 16 bits)
39-39	126	256	260	39-39-126
126	126			
126-126	39	258	261	126-126-39
39	39			
39-39	-126			
39-39-126	126	260	262	39-39-126-126
126	39			

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- Don't need to send dictionary at destⁿ side
- Don't need probability knowledge

(3). Run Length Coding

Ex : from slide (Ws & Bs)

Run length coding : 12W 1B 12W 3B 24W 1B 14W

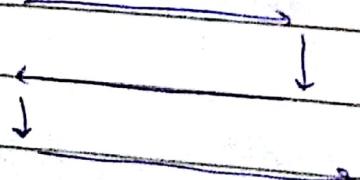
can write also as : (count , symbol)

→ Can keep any code for symbols which should be uniquely decodable on other side

↳ More use when few brightness values : (^{less no. of} intensity levels)

Reason If you've just 2 intensity level = run length will ↑↑ & so, you can compress more.

For run length , we usually go this way



why like this ?

every high prob. that nos would have same values.
so, more like this.

(4) symbol based Coding

Assign code for each symbol

wave triplet (x, y, t)
 starting point of symbol

(<u>0</u>)	b
(<u>1</u>)	a
(<u>2</u>)	n
(<u>3</u>)	A
(<u>4</u>)	N
(<u>5</u>)	a

(5) Bit plane Coding

Code the bit planes separately using RLE

39 39 126 126

00100111 00100111 01111110 01111110

RLE

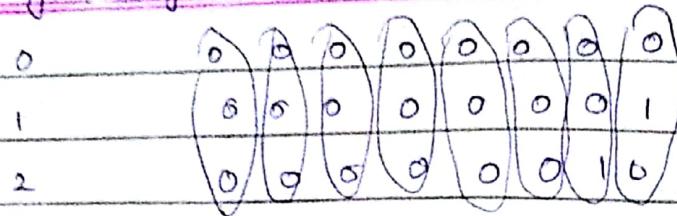
Bit Plane 0 \rightarrow 1100 (bit 0 of each pixel) $\rightarrow (2,1)(2,0)$

Bit 1 \rightarrow 111...

8 \rightarrow .

After separating bit plan, do RLE for each bit plane

very using this?

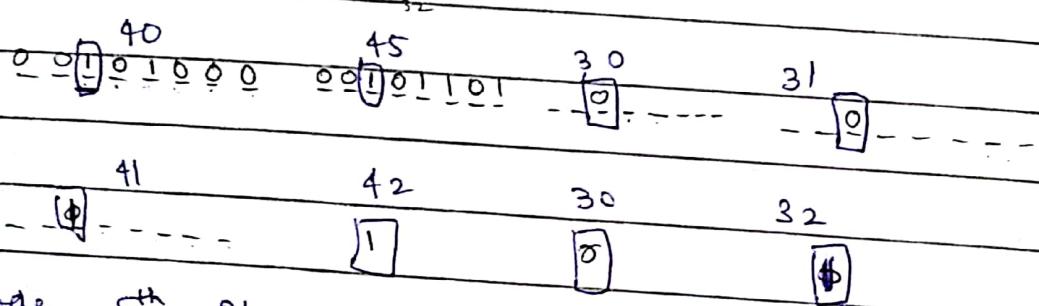


→ many bit planes will have
(long) cont. run lengths (of 0 & 1).
which'll make it easier to comp.

→ Downfall:

neighboring intensity but there's change in bit (last bit)

Ex.



Code 5th Plane using RLE

+ 1 0 0 1 1 0 # → we go like ↗ ↙
~~(2,1) (2,0) (2,1) (1,0) (1,1)~~ in RLE
 ↓ ↓

Count symbol

so, code will be:

(2,1) (2,0) (1,1) (1,0) (2,1)

Ex.

slide :

5 6
7 3

Corresponding 3 bit planes

1	1	0	1	1	1	0
---	---	---	---	---	---	---

5, 6, 7 → m^{ing} intensity

2nd bit plane bits are same
1st & 0th → ~ " diff.) what we like? All should be same.

→ A small ~~diff~~ change in intensities of m^{ing} pixels disrupt in our length.

Ex. 127 & 128 → Bits are totally changed although we have small Δ in intensity

↙ so! (Instead of binary code, use gray code)

GRAY CODE

$$5 = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 101$$

In gray code : MSB remains as it is

Other bits : XOR b/w that bit & just prev. bit.

$$5 = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 101$$

$$\text{Gray code} = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 111$$

$$6 = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 110$$

$$\text{Gray code} = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 101$$

$$7 = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 111$$

$$G_7 = \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} \underline{\quad} 100$$

→ Adv. : If there are adj. gray levels, change would only be in 1 bit

Eg.

$$\begin{array}{r} 7 \ 4 \ 8 \\ + \quad + \\ 0 \ 1 \ 1 \ 1 \quad 1 \ 0 \ 0 0 \end{array} \rightarrow \text{all bits changed}$$

Teacher's Signature

I₂₇ : 0 0 1 1 1 1 1

G₇ : 0 0 1 0 0 0 0 0

I₂₈ : 1 0 0 0 0 0 0 0

G₈ : 1 0 0 0 0 0 0 0

→ More or less, i^{th} bit plane code will be smooth
(same everywhere)

Slide : Binary \rightarrow Intensity level changing very freq.
Gray \rightarrow " " almost const.

MSB \rightarrow get general view) \rightarrow Bit Plane
LSB \rightarrow ~ detailed ~

Decoding Gray code

XDR with ~~⊕~~ prev. we got in decoding part (below line)

got \rightarrow 0 0 0 0 0 1 0 0 (G₇)

decode : (a) \rightarrow 0 0 0 0 1 1 1 \rightarrow 7
①

Block Transform Coding

- Now, we take blocks of image
- Take square blocks (if not possible \rightarrow do padding)

Quantizer = ceil / floor / ...

→ Decompressed will not be same as Input Image

Reason : Quantization (Quantized 5-2 to 5, ~~got~~ lost some extra info.) \rightarrow losing some part of image here

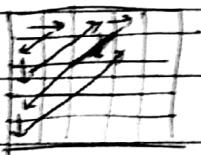
If I want, I can convert it into some color space also & then convert block $\xrightarrow{!}$ transform

maybe using Fourier transform

Entropy code: code after calculating entropy

DCT: discrete cosine transform

Zig-zag technique: Convert 2-D array \rightarrow 1-D



size ex. \rightarrow Quantizing using Normalization Matrix.

(dividing by values in that Matrix)

After quantise \Rightarrow $\begin{bmatrix} 39 & 0 \\ 0 & \dots \end{bmatrix} \rightarrow$ freq components
now (DC value - 79)

\hookrightarrow Most 've become 0.

can be neglected or
run length of 0

Since $\alpha(u/v)$, either u or v.

SubImage Size Selection

With size of 8, error is min. usually for all cases.

So, 8×8 is used usually.

JPEG Compression

3 coding system
→ lossy baseline : used mostly.

→ level shift :

$\exists \pm 256$ intensity levels : from each pixel, subtract 128
 (2^k) (2^{k-1})

→ DCT is being used in JPEG

→ Quantize using std. Normalizⁿ matrix

shape : after DCT : high freq. have smaller values (bottom right)
low — large values (In top left)

8x8	8x8	1

→ computed for each block (top-left block) ↪ DC value

from each DC value, subtract ~~DC~~ the DC value in ~~just~~ left block just left to it. Then, convert to binary & do Huffman coding.

JPEG 2000 → lossless

Project → Mosaicing Assignment (20%)

Documentation → Literature review ↗

Coding

Bottom Have to do :

- ① Report
- ② Code
- ③ Presentation / Viva

Good Programming Practices

- ① Comments
- ② Indentation
- ③ Modularity
- ④ Structured
- ⑤ significant variable name
- ⑥ Exception Handling

project → 10% Coding

→ 10% Documentation /
Presentation / Viva

Documentation : → Have heading called Design decision & write
at least 3 para on your thoughts

+ May use other algo (other than what we will do in class today)

↳ Explain algo + Design decisions

(where you applied Reverse / forward Mapping)

↳ Paste Result after each & every step.

↪ Inbuilt func can only be used for mathematical op's (eg. → Inverse)

Projective

- ① Need to choose 4 pts (corresponding)
Have to choose pt on blackboard only, because only
it is planar.

i) load images 0.jpg & 1.jpg

```
FILE *srcfile;
    argv[3], "r"
if (srcfile fopen( ) == NULL) {
    cout << "error";
    exit 0;
}
```

read src file to get all coordinates

```
for (i=0; i<8; i++)
```

,

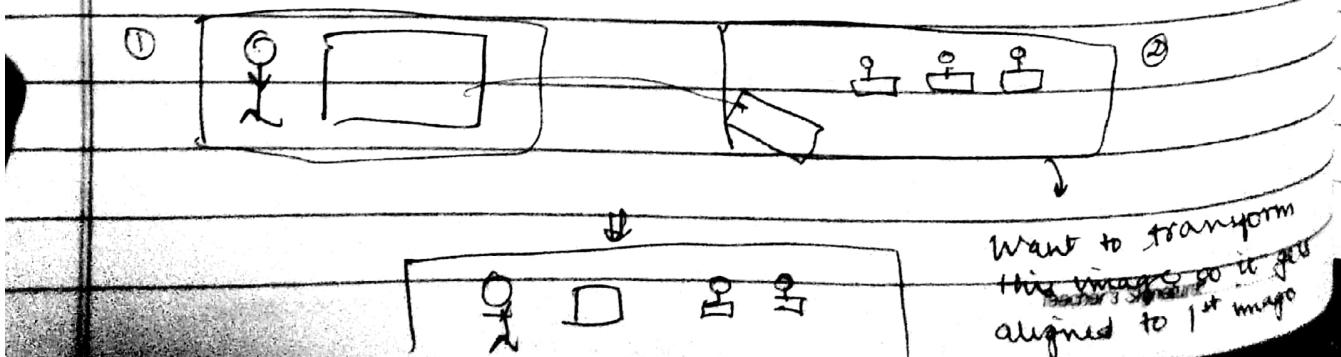
2) Find homography matrix

do using SVD

Write now: find homography,

C++: Mat H12 = findHomography (SrcCoord, DistCoord);

can check if $H12 \text{ at } <\text{float}>(2,2)$



then ② is transformed to get aligned

We want to get ② aligned with ①

Take inverse of homography matrix you got

$$H_{21} = H_{12} \text{ inv}()$$

Have to apply this matrix on corner points of 2nd image & store these points in a vector (C++) or a list (python) (Keep corner points of 1st image also in a vector)

$$\begin{pmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{pmatrix} \cdot H \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$px = \frac{ax \cdot h_1 + y \cdot h_2 + h_3}{x \cdot h_2 + y \cdot h_8 + h_9} \quad (1, 4) \quad (0, 1664)$$

$$py = \frac{ax \cdot h_4 + y \cdot h_5 + h_6}{x \cdot h_2 + y \cdot h_8 + h_9} \quad (1, 2496) \quad (9)$$

$$(1, 1) \quad (1664, 1) \quad (1, 2496) \quad (166)$$

→ Why doing it?

To find range (min & max) of 2nd image so we can get iterate whole image Then, find

max X

min X

Out of

→ won't get

max Y

min Y

corner points

→ value in negative

Most of cases, dimension are ↑. So, not necessary to store corner points

We get:

2496 x 1664

width height

0.007 -0.0010
0.0035 0.0023

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this much

→ has overlapped
with original
image

266 C

maxWidth

2197

height
minWidth

0

minHeight

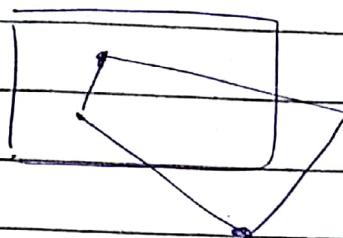
0

height
minWidth

2496

2496

4992



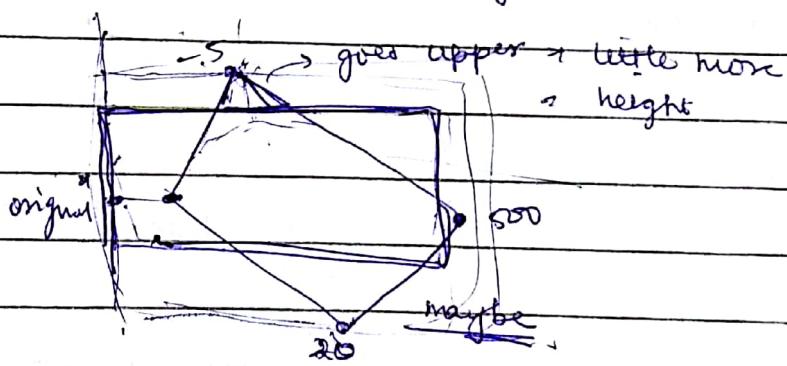
$$y \quad \min X = 0$$

$$\min Y = -130$$



jyaada left nhi
jaa rahi h

upper jaarahi h
image



$$\text{height New} = \text{max Height} + \text{abs}(\text{Y offset})$$

$$y \quad (y < 0)$$

$$y\text{offset} = \text{abs}(\min Y) \quad \begin{cases} \text{adding upper} \\ \text{max part} \end{cases}$$

$$\text{width New} = \text{max Width} + \text{abs}(\text{X offset})$$

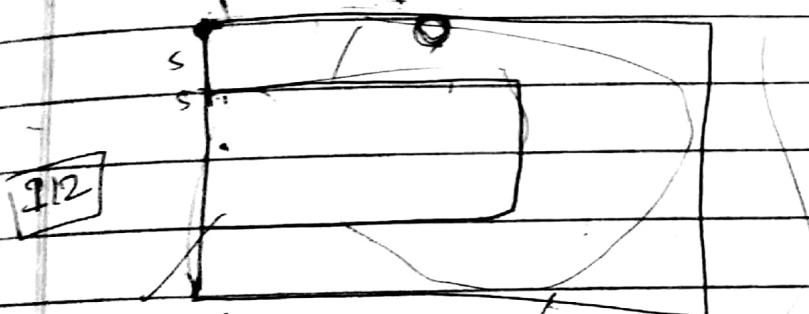
↓
which we
calculated
above

Eg $\min_x = 0 \quad \min_y = -130$

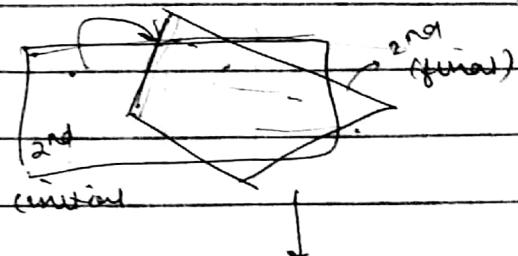
$\rightarrow \text{Offset}_x = 0 \quad \text{Offset}_y = 130$

\rightarrow Want to paste 2nd image as it is on 1st image

starting
Iterate from $y + y_{\text{offset}}$



Paste 2nd image
on empty canvas



For pasting 2nd image,
can check where no color is
assigned on canvas & assign
color to it. If

Create canvas
acc to final
image coordinate
you got earlier

Apply :

$H12 \times \text{Pasting Coord}$

→ Iterate it. If you
get corresponding point
in 2nd image (final). If
it exists, → assign on canvas
otherwise (if get out of bound)

discard it

25/10/18

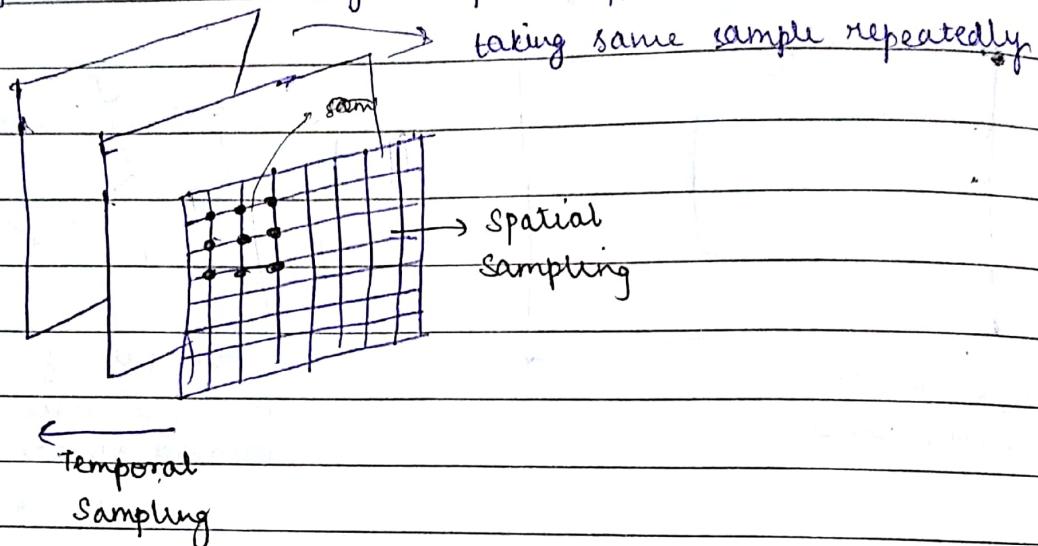
PAGE NO.:
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Digital Video Processing

Represent " of visual scene at a particular time : Digital Image instance of Sampling

Sampling gives → frame / image.

Digital Video : Taking sample repeatedly at diff. instances.



Adv. of digital videos : (vs Analog Video)

→ compatibility
→ compression & trans.

- ↳ Converts to digital (In analog, need a h/w to support video digital conversion easily)
- ↳ Noise can affect Analog video

Digital : less noise sensitive, noise

Other adv. : Same as digital images (storage, etc.)

Spatial

Why to do Sampling ?

- ↳ Just to avoid need of storage.
(Don't want that much of detail in some cases)
- ↳ More detailed : High sampling

Temporal sampling : After what dur. of time I'm generating a frame.

Generally : $\frac{1}{30}$ or $\frac{1}{24}$ sec.

But we can have $\frac{1}{10^{th}}$ sec: not smooth but our work will be done

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2 things:

→ ① Bandwidth " kitni badi image pass karte h"

→ ② Data rate " kitne frames pass karte h at a point of time
↓
with more costlier"

① & ② \Rightarrow expensive

2 ways to do Temporal Sampling:

1) Progressive Sampling (P)



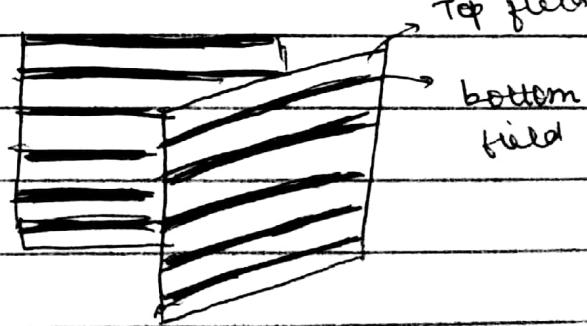
complete frames are sampled

e.g. 480p, 720p, 1080p (movies)

2.) Interlaced sampling (I)

Ex: 480i, 720i, 1080i
At a time, I either sample
even lines or odd lines

1st sample even, then
odd (or vice-versa)



→ If I sample very fast, they appear very smooth.

bandwidth

↑ ↑

* When bandwidth is small, I can't transport whole image
(don't have enough bandwidth) That case, I can ↑ ~~data~~
data rate.

- Progressive : talk about frames
- Interlaced : " " field

Color Spaces for Digital Videos

Color Space : \rightarrow unique universally std. color model (like RGB)
 in which colors in diff. proportion make a unique color

intensity (value) Luminance / \downarrow ^{luma} of src

") Brightness : what we perceive (subjective) } can't be measured
 chroma / color : to specify color

\hookrightarrow RGB : In RGB, each R, G, B have equal proportion
 (8 bits each) ("Resol" is same for all)

In videos, we've color model :

$\frac{Y}{\text{luminance}} \frac{Cr}{\text{color}} \frac{Cb}{\text{color}}$ → because: Human Visual System has more sensitivity to luminance than color (Intensity values), so, we use this color space in which luminance is given more resol" than color.

no. of pixels
 (can see more clearly)
 (more details clearly)

→ For display : use RGB

" transmission " \rightarrow YCrCb \rightarrow because it component to resolution kam kar dia h.

YCrCb

$$Y = k_r R + k_g G + k_b B$$

Luminance \rightarrow weighted average of R, G, B

$k \rightarrow$ weights

colour difference $C_r = Y - R$

$$C_g = Y - G \quad \Rightarrow \begin{matrix} \text{storing} \\ \text{using} \end{matrix} 4 \text{ things}$$

$$C_b = Y - B \quad (Y, C_r, C_b, C_g)$$

In RGB :

(R, G, B)

\rightarrow so, YCrCb is bad than RGB

because size Θ is \uparrow than in RGB.

\rightarrow But, it's good, because

$$C_r + C_g + C_b = \text{const.} \quad , \quad \text{so even if I know 2 values we can get 3rd value.}$$

generally, we store 3 value only: Y, Cr, Cb

Conversion formula :

$$Y = 0.299 R + 0.587 G + 0.144 B$$

$$C_b = 0.564 (B - Y)$$

$$C_r = 0.713 (R - Y)$$

$$R = Y + 1.402 C_r$$

$$G = Y - 0.344 C_b - 0.714 C_r$$

$$B = Y + 1.772 C_b$$

Diff. sampling std. :

1) 4 : 4 : 4 Sampling :

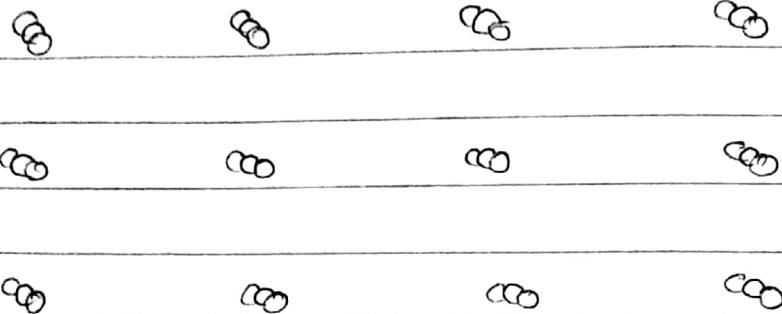
each pixel has equal proportion of all three components

(Y, Cr, Cb)

○ — Y

○ — Cr

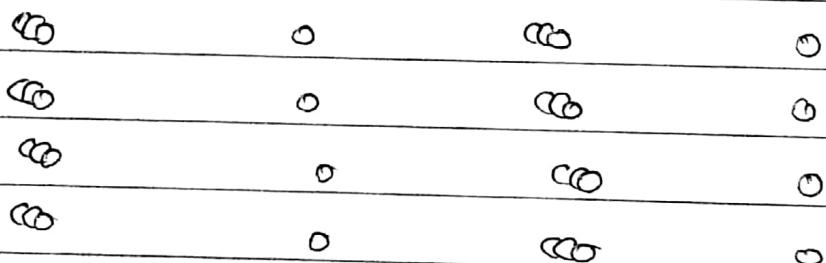
○ — Cb



→ In each row,
propor" of each
component is 1/4.

2) 4 : 2 : 2 Sampling : (YUV2)

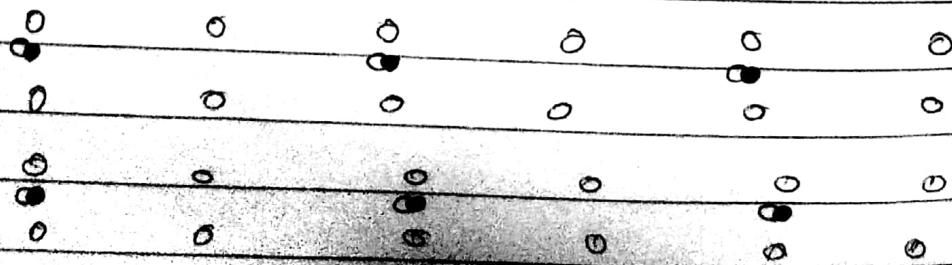
In vertical dir", chroma has equal proportion as luma,
in horizontal direction, it is half



→ Used in case of DVDs & std. Definition TV displays

3) 4 : 2 : 0 sampling ('YV12') :

Cr and Cb have ^{half} the resolution of Y in both horizontal & vertical dir".



Used in Video Conferencing, video compression of Multimedia

Teacher's Signature

Page

width

height

Ex: Image Resolution : 720×576 pixels

Y (luminance) resolution 720×576 samples each with 8 bits

4:4:4 $720 \times 576 \times 3 \times 8$ (each has same resolution)

$$\left\{ \begin{array}{l} (720 \times 576 \times 8) \times 3 \\ \downarrow \text{luminance} \end{array} \right. \quad \left. \begin{array}{l} \text{all have same resolution} \\ (360 \times 288) \end{array} \right.$$

$$4:2:0 \quad 720 \times 576 \times 8 + \frac{720 \times 576 \times 8 \times \frac{2}{8} \times 2}{4}$$

$$= 720 \times 576 (8 + 4)$$

$$= 720 \times 576 \times 12$$

(360×288)

$$4:2:2 \quad 720 \times 576 \times 8 + \frac{720 \times 576 \times 8 \times 2}{2}$$

$$= 720 \times 576 \times 16$$

used in HDs

→ 4:4:4

↓ primitive 4:2:2

4:2:0

→ chroma sub-sampling methods

→ taking least amount of bandwidth

Best method = depends on our appln.
(out of 3)

Video Formats

- 1) Intermediate
- 2) Standard Definition
- 3) High Definition

① → convert 1 format to another

Basic one : + Common Intermediate Format (CIF)

~~16 bits per frame~~ ~~352 x 288~~

Luminance Resⁿ : Bits per frame

352 x 288

(4:2:0 ; 8 bits per pixel)

Bits in each frame = $352 \times 288 \times 12$ ~~bits~~

$$\approx 1216512 \text{ bits}$$

$$\approx 152064 \text{ B}$$

$$\approx 148.5 \text{ MB}$$

Other

QCIF (Quarter CIF : half resⁿ in both → & ↓ data) $\left[\frac{352}{2} \times \frac{288}{2}\right]$

4CIF (: twice " " " " ") $\left[2 \times 352 \times 288\right]$

② standard Definition

720 x 576

③ High Definition

720p Resⁿ : 1280×720 25 frames per second

1080i

1920 x 80

1080p

→ 25 frames per sec

50 fields per sec

Resⁿ
Total no. of bits will
be same in both i.e.

bits → talk about
even-odd frame pairs

Video Compression

- In compression : Try to remove redundancy without affecting quality
 - Quality : $\frac{Fidelity}{Objective\ criteria}$
 - measure on basis of parameters, ex:
 - Signal to Noise Ratio
 - Peak mean square error.
- Subjective Criteria
Depends on your perspective,
whether you like it or not.
Can't measure

- Q. Why to have subjective & when we already have Objective ?
- MSE : match pixel by pixel Even if small error : square error \uparrow
- If I shift my image : MSE \uparrow (Intensity value changed completely)
subjective : won't make any diff.

- ⇒ Depends on appⁿ (compression)
- For storage : Higher \sim
- Redundancy is removed

Image Compression : Transform Coding \rightarrow JPEG

KLT, FFT

- Q1 How you choose Transfⁿ funcⁿ ? (why DCT, not others?)
- Q2 Why divide into $n \times n$ sub-image ? How to decide value of n ?

can restore complete image
Quantizer \rightarrow causes lossy in compression

MJPEG

To compress video:

We can compress each frame of video. \rightarrow Motion JPEG
(using JPEG)

\rightarrow We're only talking about spatial redundancy here (like images)
 \downarrow
intra-frame

Temporal Redundancy:

\rightarrow In video: successive frames are also similar.

Intuitive Methods:

- Sub-sampling \rightarrow drop frames which are similar
 \downarrow
lossy.

Fluid motion won't come, it'll become jerky. Won't look good as a video

For visual: \downarrow so we'll add same frames

- " transmission/ storage \rightarrow drop similar frames

\hookrightarrow can store 1 frame & write its freq. (3, 4, ...) \rightarrow will take less storage

- Differencing \rightarrow (To find changes in 1 frame)

Lossless \rightarrow white area: diff. was more (more motion)
(ex. in slide)

- Block Diff.

- Motion Compensation: most widely used.

Block Diff.: same ex: Background me no change
Foreground me only small A
&
have to encode \downarrow blocks.
(pixels will be same)

\hookrightarrow good for gradual motion
(not abrupt)

Teacher's Signature

* Ques. why motion compensatⁿ & estimⁿ is better for video compression

than differencing?

Ans. when I take diff. b/w frames - I may get white regions (large difference in intensities) while in error frame: Nearly 0 (most of frames). And we use motion vector for a block \rightarrow giving more compression.

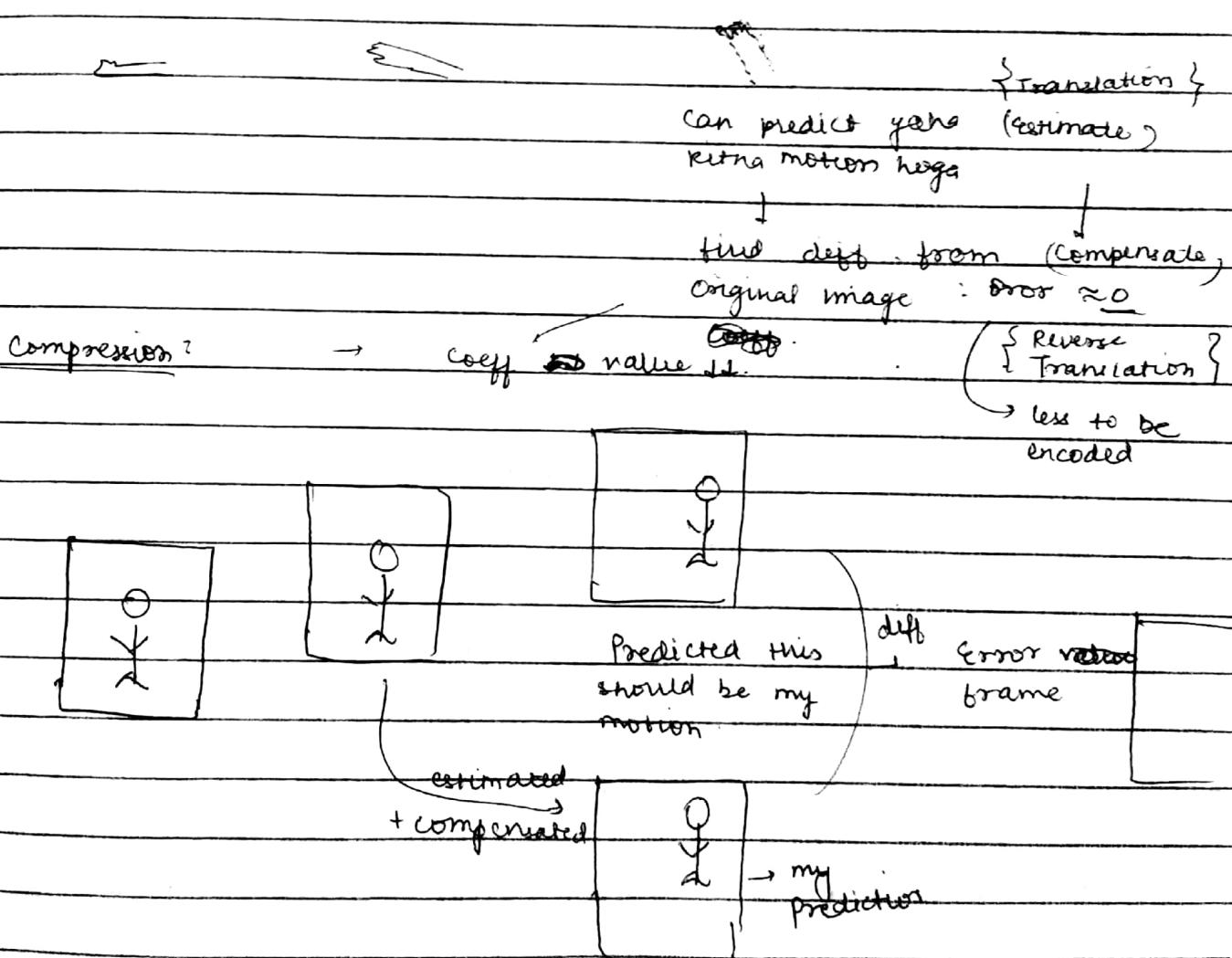
Top 3 \rightarrow good for gradual motion

Motion Compensation

\rightarrow Estimate where motion is occurring. (+5, +15)

\rightarrow Compensate this by subtracting motion from original image

(Error) : $(x - 5, y - 15)$: small diff. will come (almost 0)



In case of video: for 1st frame: we don't consider

Temporal Redundancy, only takes care of spatial

2nd frame onwards: both spatial & temporal

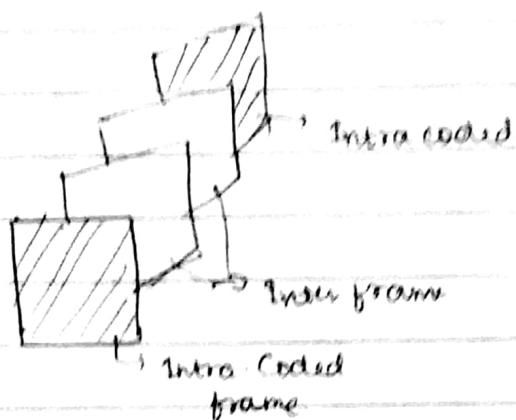
Periodically introduce to prevent accumulation of error over frame.

If true acceleration - we are ~~estimating~~ moving linearly.

so, total error will get ~~a tiny~~ ^{linear} accumulation.

What we do? After some frames, we again encode next frame as IFO (don't consider temporal, just spatial).

↓
2-frame - now prob.,
using original frame



Motion Estimation

How to estimate motion?

1) segment video into moving objects

describes (model) object motion → Difficult

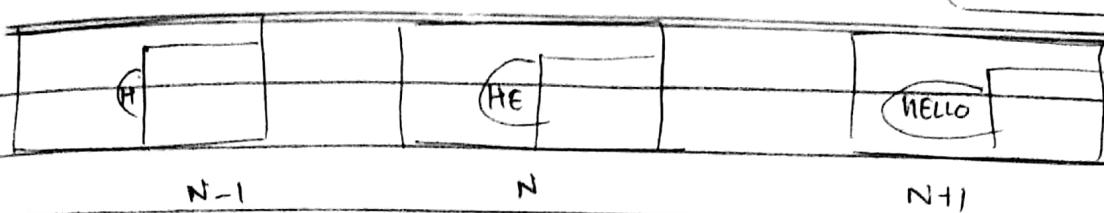
2) Segmentation "free"

3) compare displacement b/w current frame & stored (reference) frame

↓
Motion vector (x as well as y)

→ Previous backward, Current ← forward Future
frame Estimation frame Estimation frame

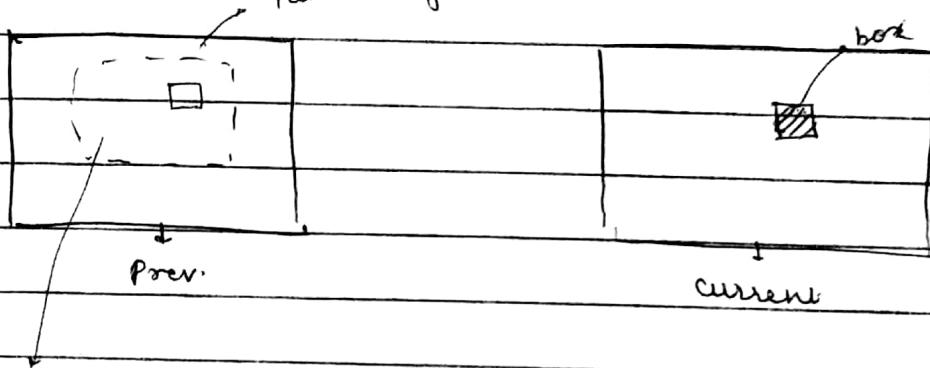
If use both: will have twice no. of motion vectors
bidirectional → take avg. of both



Bidirectional gives better result in most cases

Basic approaches for Motion Estimation

i) Pixel-based. take larger ~~box~~ than box (Reference window)



check each pixel & if they match ✓

- If have shadow in 1 case & not in other: though Object is moving, it won't have motion
- Though ~~image~~ obj is not moving, it appears moving due to Δ in brightness: Optical flow

↳ computationally not efficient.

* In MOT

→ we're sending Motion vector + Error frame also along current frame with compression. Isn't this much to send? why is a better compression method

Matching criteria for Block-Based Motion Estimation

- 1) Mean square error (each pixel in block) → computational cost ↑
- 2) " of abs diff
- 3) Matching Pixel count → In every dir, find matching pixel : whenever max → take that vector.

- Block size : 16×16
- Search Range = Acc. to size of block.
(Reference window) ⇒ If $P \uparrow$: Window size should be ↑
accuracy ↑
- mostly, we have linear motion (translation)
- complex : include Projective, Affine motion

Motion Estimation

- Uniform motion inside each block.
 - Only consider 'Y' component (luminance)
 - for each block : motion vector
-
- Inverse Quantize / DCT : for our feedback (correct or not)
 - Generally : 4:2:0 subsampling

18

video compression : used in WhatsApp, Video Calls.

Video Coding stds

- Error in temporal predictor is encoded by transform domain techniques (eg. DCT)

Book → Ch - 11

Since we exploit both spatial & temporal : called hybrid

→ Video compression system consists of :

- An encoder

- Compressed bit stream

- A decoder

) → don't describe how encoding / decoding is done

↓
provides great flexibility

(we can design our own algo.)

Major Video Coding Standards

1) VCEG : limited bandwidth

2) MPEG : store videos in devices

MPEG-1 Std. → low bit rate data
(video conferencing)

→ supports only non-interlaced video

→ 4:2:0 chroma - subsampling

Motion Compensation in MPEG-1

P-frame : Predicted frame (Using forward / backward prediction)
↓
MPEG uses this in general

→ Bidirectional : better → 2 motion vectors (1 for fwd, 1 for bwd)

In general case : we take avg. of

If we don't get proper match in fwd : we will only consider 1 motion vector of bwd

① I-frame : spatial → least compression in 1 frame.

② P-frame : Temporal (Bwd)

③ B-frame : Temporal → Maxⁿ Compression
(even fwd & bwd)

Considering compression in just 1 frame [not video compression]

Error frame : less info. than video frame.

need 2 frames (near to 0) color info, channel info.
at least ↓ less bits needed.

Inter-frame has more compression than Intra-frame

↳ If 2 frames aren't almost same. (error frame not near to 0)
Ex. : T.V. pe ekdam se commercial aa gaya) → can't remove temporal redundancy there (Inter frame). Have to consider spatial (Intra frames).

P-frame : Just taking 1 frame & finding error frame

B : ~ 2 ~ —

gives Prediction will be better.

max^m compression → error b/w " & original will be LL

* DCT ~~ko~~ motion vector nhi dete, error frame dekh
given at time of entropy.

have P-frame : if only B-frame → quality may be ↓
so, have P-frame in b/w.

B \rightarrow P-frame : can be predicted only using I or P frame (Prev.)

B-frame : " I or P frame

{ (Prev./Next)}

Hierarchical structure for MPEG-1 Bitstream

→ GOP : collection of pictures → I/B/P.

Interval b/w 2 I-frames : create 1 GOP.

- In starting of every GOP, + an I-frame.

→ Group of GOPs : sequence.

MPEG-2 std. → high bit rate data (HD systems)

- supports interlaced videos.

| adv. | disadv. |

(supports progressive also)

More the no. of frames,
better is the quality of video

→ Scalable bit stream : scalable for diff. video quality

Q. Why interlaced?

How it helps in HD videos → that MPEG supports interlaced?

Ans. Frame pictures are good → slower frame field
→ faster (rate is double)

→ Frames & fields : supports both.

→ Seq. can contain comb" of frames & fields.

| for prediction

We need to know whether

it's coming from frame & field.

→ Field = separated into 2 pictures.

→ Frame prediction : same as in MPEG-1

Teacher's Signature.....

Field predⁿ:

Top \Rightarrow field :

prev. top field of 1/P

bottom " "

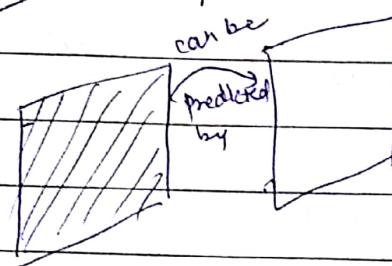
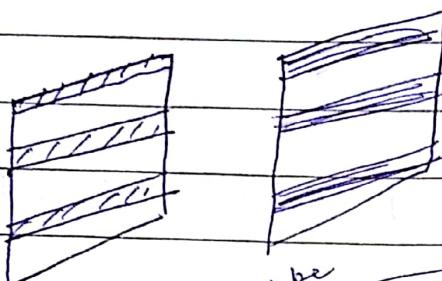
Bottom - - - : - - -

top - - -

" bottom - - -

field

Bottom field can be predicted from top ~~frame~~ of same frame. (frame predⁿ \rightarrow can't do this)



Frame & Field:

\rightarrow ~~Diff.~~ of size

\Rightarrow frame

$$\text{size (field)} = \frac{\text{size (frame)}}{2}$$

\rightarrow Frame \Rightarrow can't predict predⁿ using diff

prev. field \Rightarrow

can't use top field

of same frame to predict bottom field.

\rightarrow Scalability:

Bit stream organized into layers.

- Base layer: mandatory (carry min. req. info)
- Enhancement layer (can be > 1)

To \uparrow quality, Enhancement layers \uparrow

) Enhancement (To \uparrow quality)

Base

decoder
can just
use base
layer

o If my appⁿ need don't need high quality:

\rightarrow Sending 1 bit stream, decoder can use that many layers, that it needs \rightarrow Robustness \uparrow . (on basis of appⁿ)

→ SNR scalability :

For base layer : take very

enhanc ... : take inverse of DCT coeff & use very fine DCT

→ spatial :

Base : More subsampling

→ Temporal : drop frames

Base : reduce to 1/2.

* → Data Partitioning : not exactly scaling

MPEG 4

MPEG 1 & 2 : doing frame wise coding.

→ Here, it is content based video coding.

will separate objects in video & apply coding on separate
objects → Video object

Snapshot : 1 frame me 1 " → video object in plane

Ex. News me ~~anyone~~ video chat thi h aur kisi ko encircle
kr rakhna h.

- combine synthetic & natural scene & objects.

Ex. Animations, Cheetah ji ke same aarti ki thali phoom thi h

- 1 video object can be in multiple frames

→ can change locations of video object
or exchange

→ Each VO has texture, shape.

Have to encode : " " & motion

→ VOL : pos" details should also be sent.

↓ 3 components

- shape

- motion

- Texture
features

combine into
bit stream me
jagya

Each VO is sent separately by VOL.

For e

- doing this frame by frame : Motion Coding

shape Coding

- need to compress shape while transmitting.

side : first : identifying object (like blob)



① → Identify boundary

② → Divide into 16×16 macroblocks

(can be space in sides of boundary
(Bounding box of object) is not divisible by 16)

Binary & plane

→ certain blocks : all black

: all white

Do Binary & Plane

: comb" of black & white → Binary & Block

These are needed to
be encoded to
transmit.

Teacher's Signature

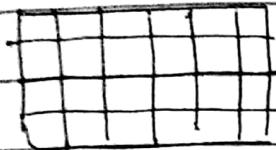
Scanned by CamScanner

→ the context based Arithmetic coding. (CAE)

↓
take nbd instead of
just 1 pixel

→ Name : I - VOP, P - VOP, B - VOP

→ Intra - CAE : limited to that frame only



→ Take 10 nbd pixels.

$2^{10} \rightarrow 1024$ (Considering Binary & Plane)

Prev. states ke basis pe me form a table of prob. using context info. (The pixels w ke baad 1 B ke aane ki prob. kya h). I have seq. of prob. → can apply Arithmetic encoding then.

→ Uses motion estimation & compensation (VOPs, not VOPS)

→ Inter - CAE : have Reference & Target frame in just 1 frame

- Find best matching macroblock.

Qⁿ : Can't use B-frame for Pred. Why?

Qⁿ : Have just I & B. Have to use B. How to maintain quality (if p is - nt) ↓
(don't have much I-frames)

4 pixels : Target frame $\rightarrow 2^9 : 512$
5 -- : Reference "

again, apply above method & apply CAE.

Texture Coding

Bounding box are used.

we're just doing for object. Background is almost static.

so error frame will be 0 for large area.

Error will be ↓ as compared to frame based coding in Object based coding.

↳ can add artificial thing

↳ can change content in bit stream

Sprite Coding

Sprite : Large part of image almost static

Panorama : stitch multiple images.

↳ sprite panorama

→ Here, stitch multiple scenes which are almost static.

Can't apply mosaicing wala algo (not planar here)
(if distance ↑ → can be treated as "u")

naya object we got
due to rot" of camera

Send panorama only once, send object & camera param
obj change huge, bhej diff. So, not sending whole image
everyone.

↳ Used in Animations : sprite coding

Masking + Texture info : sent as sprite

MPEG-7

→ advanced version of MPEG-4

Used : ↳ Searching & Retrieval from video

↳ not