## CLASS 11 CHAPTER-11 LINES

## Excercise 10.2

Q18.P(a,b) is the mid-point of the line segment between axes. Show that the equation of the line is  $\frac{x}{a} + \frac{y}{b} = 2$  Solution: Let

$$\mathbf{A} = \begin{pmatrix} x \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ y \end{pmatrix} \text{ and } \mathbf{P} = \begin{pmatrix} a \\ b \end{pmatrix}$$
 (1)

as shown in Figure 1

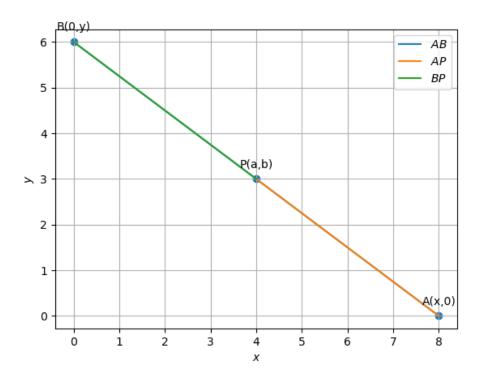


Figure 1:

Now we know

$$\mathbf{P} = \frac{\mathbf{A} + \mathbf{B}}{2} \tag{2}$$

So, from here we can say that

$$x = 2a \tag{4}$$

$$y = 2b \tag{5}$$

$$\mathbf{A} = \begin{pmatrix} 2a \\ 0 \end{pmatrix} \tag{6}$$

$$\mathbf{B} = \begin{pmatrix} 0\\2b \end{pmatrix} \tag{7}$$

(8)

Now direction vector is

$$\mathbf{m} = \mathbf{A} - \mathbf{B} \tag{9}$$

$$= \begin{pmatrix} 2a \\ -2b \end{pmatrix} = \begin{pmatrix} 1 \\ \frac{-b}{a} \end{pmatrix} \tag{10}$$

so normal vector is

$$\mathbf{n} = \begin{pmatrix} 1 \\ \frac{a}{b} \end{pmatrix} \tag{11}$$

So, the equation of line passing through P

$$\mathbf{n}^{\top} \left( \mathbf{x} - \mathbf{P} \right) = 0 \tag{12}$$

$$\begin{pmatrix} 1 & \frac{a}{b} \end{pmatrix} \left( \mathbf{x} - \begin{pmatrix} a \\ b \end{pmatrix} \right) = 0 
\tag{13}$$

$$\left(1 \quad \frac{a}{b}\right)\mathbf{x} = 2a \tag{14}$$

$$\begin{pmatrix} 1 & \frac{a}{b} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = 2a \tag{15}$$

$$x + \frac{ay}{b} = 2a \tag{16}$$

$$bx + ay = 2ab (17)$$

$$\frac{x}{a} + \frac{y}{b} = 2\tag{18}$$

Hence proved.