

Limbaje Formale și Compilatoare (LFC) - Curs -

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Astăzi



- Analiza sintactică
 - Automate push-down
 - Parsere LL
 - Analiza sintactică LR

Tipuri de analiză sintactică

- Descendentă (top-down, de sus în jos)
 - Înlocuiește câte un neterminal cu partea dreaptă a unei producții, până rămâne doar cu terminali
- Ascendentă (bottom-up, de jos în sus)
 - Porneste de la sirul de atomi lexicali, abstractizează din sir simbolul de start prin reduceri succesive
- Analiza descendentă – derivare stângă
 - Tot timpul înlocuim cel mai din stâng neterminal
 - LL (Left to right, Leftmost derivation)
- Analiza ascendentă - derivarea dreaptă
 - primul neterminal înlocuit este cel mai din dreapta din forma propozițională curentă
 - LR (Left to right, Rightmost derivation)

Automatizarea parsării LL

- Echivalenta cu un automat push-down
- Parsarea se poate face cu un automat si o tabela.

Generarea vs. recunoașterea unui limbaj

- Limbaje regulate:
 - Expresiile regulate **generează** toate cuvintele unui limbaj
 - Automatele finite **recunosc (acceptă)** doar cuvinte ale unui anumit limbaj
- Limbaje independente de context:
 - **Generate** de gramatici independente de context
 - Există vreun tip de automat care să recunoască (accepte) cuvintele unui limbaj independent de context?

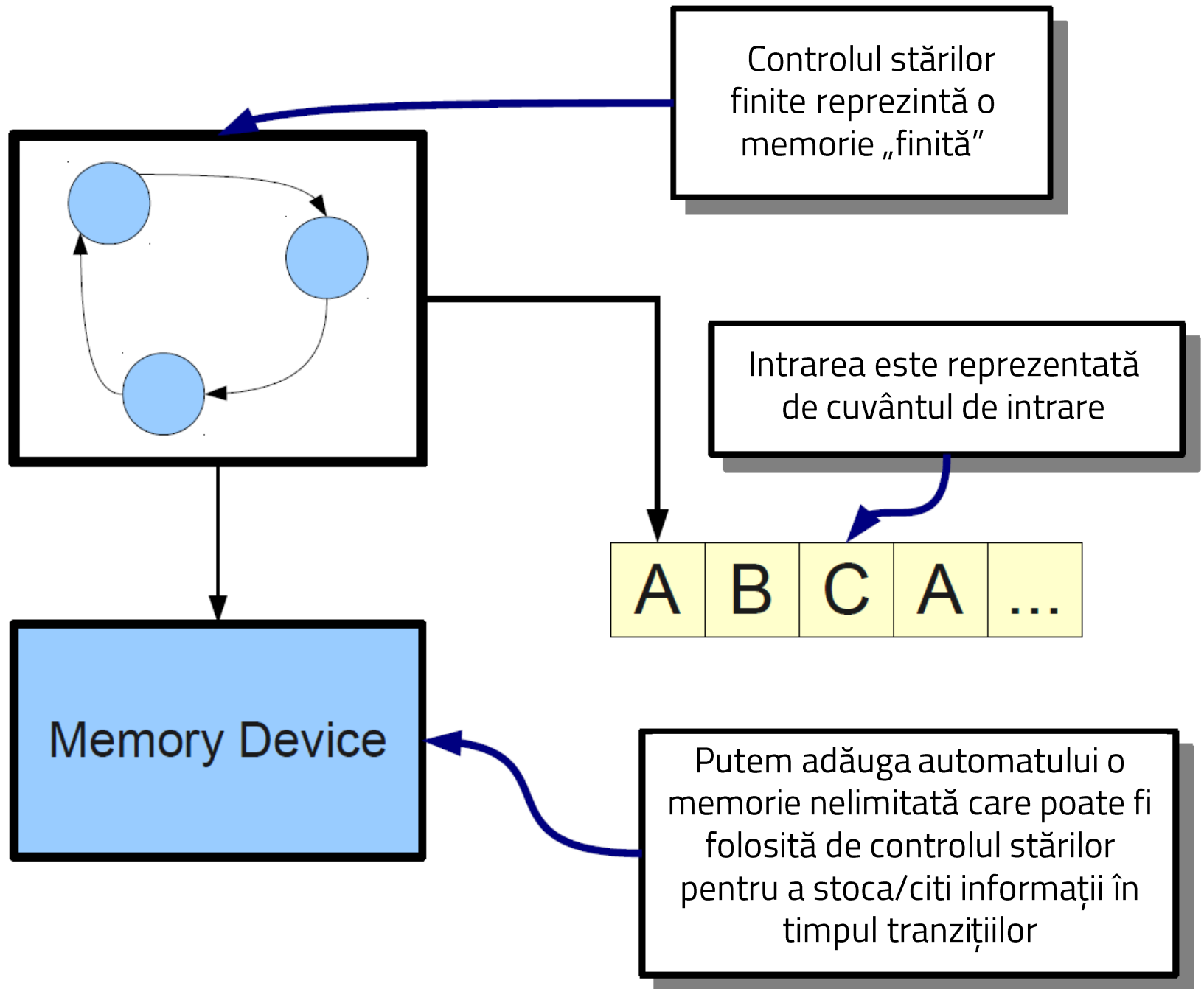


Generarea vs. recunoașterea unui limbaj

- Diferența între gramatici/limbaje regulate vs. independente de context (Chomsky):
 - Gramatici de tip 2 (independente de context)
 - reguli de forma $A \rightarrow \gamma$ unde $A \in N$ și $\gamma \in (N \cup T)^*$
 - Gramatici de tip 3 (regulate)
 - reguli $A \rightarrow a$ sau $A \rightarrow aB$ unde $A, B \in N$ și $a \in T$.
- Datorită regulilor gramaticii (și deci formei cuvintelor limbajului)

$$\text{e.g. } \{ 0^n 1^n \mid n \in \mathbb{N} \}$$

pentru a recunoaște limbaje *independente de context*, un automat finit are nevoie de o *memorie asociată „nelimitată”* (unbounded memory)



Adăugarea unei memorii automatului

- Tranzițiile automatului vor fi determinate atât de starea curentă și de simbolul de intrare, cât și de informațiile stocate în memorie
- La fiecare tranziție automatul poate efectua operații asupra memoriei: adăugare de informații noi, ștergere, modificare, etc.
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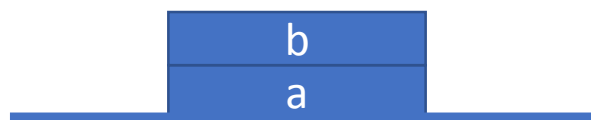
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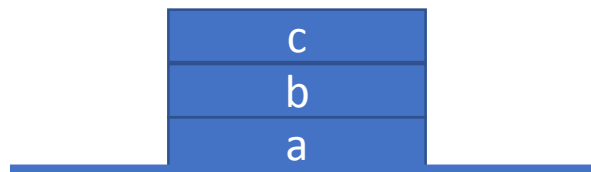
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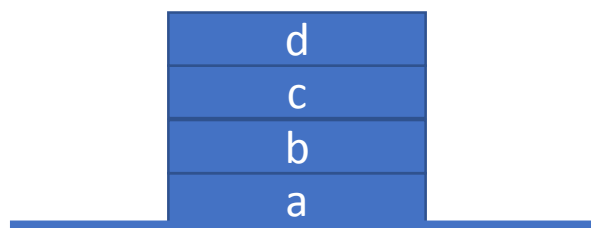
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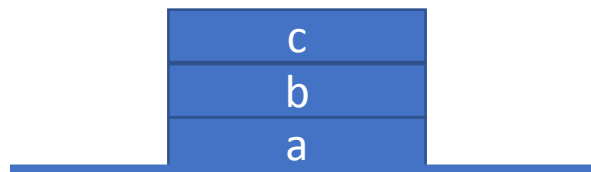
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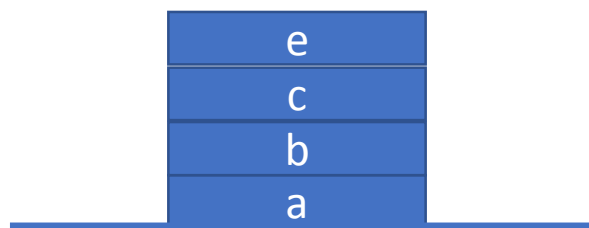
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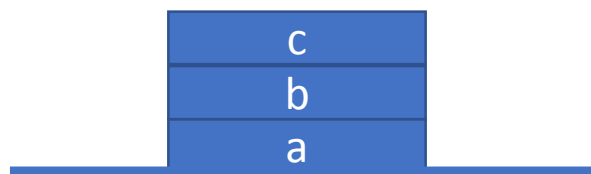
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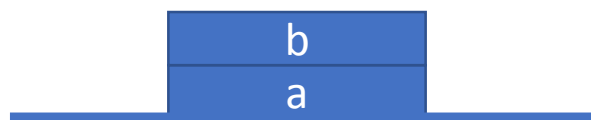
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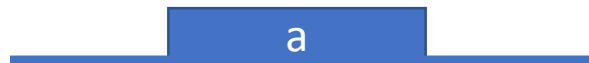
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Memoria de tip stivă

- Doar vârful stivei este vizibil la orice moment
- Noi simboluri pot fi adăugate la vârful, printr-o operațiune de *push*
- Vârful stivei poate fi eliminat printr-o operațiune de *pop*, urmând ca elementul „de sub” el să devină noul vârf

Automatul de tip push-down

- Automatul de tip push-down (PDA – Push-down automata) este un automat finit de stări echipat cu o memorie de tip stivă
- Fiecare tranziție:
 - Este determinată de simbolul de intrare curent, de starea curentă și de simbolul de la vârful stivei
 - Poate, opțional, să realizeze operațiunea de *pop* pe elementul din vârful stivei
 - Poate, opțional, să realizeze operațiunea de *push* a unui nou simbol în vârful stivei
- Inițial, stiva conține un simbol special \mathbf{z}_0 care indică faptul că stiva este goală

Un exemplu de PDA

- Considerăm limbajul $L = \{w \in \Sigma^* \mid w \text{ reprezintă un șir de caractere cu număr egal de simboluri } 0 \text{ și } 1\}$ peste alfabetul $\Sigma = \{0, 1\}$
- În acest caz, funcționarea stivei automatului ar fi următoarea:
 - La întâlnirea unui simbol 0, acesta este introdus prin push în stivă
 - La întâlnirea unui simbol 1, se realizează pop pentru simbolul 0 aflat în vârful stivei (sau eroare dacă stiva este goală)
 - Când au fost parcurse toate simbolurile din cuvântul de intrare, dacă stiva este goală atunci cuvântul este acceptat

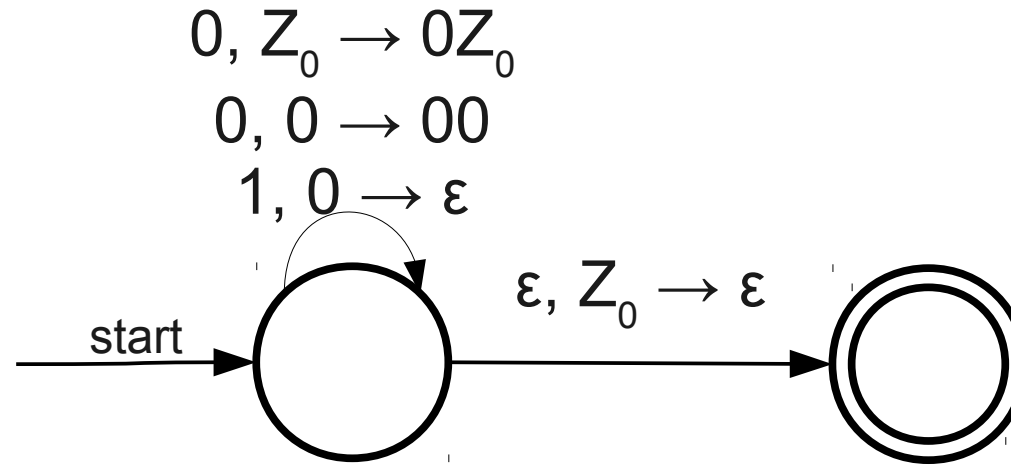
Automatele push-down

- Formal, un automat push-down este definit ca un ansamblu de 7 elemente $(Q, \Sigma, \Gamma, \delta, q_0, Z_0, F)$ unde:
 - Q este o mulțime finită de stări
 - Σ este un alfabet
 - Γ este alfabetul de simboluri al stivei
 - $\delta: Q \times \Sigma_{\varepsilon} \times \Gamma_{\varepsilon} \rightarrow \mathcal{P}(Q \times \Gamma^*)$ este funcția de tranziție
 - q_0 este starea inițială
 - $Z_0 \in \Gamma$ este simbolul inițial al stivei
 - $F \subseteq Q$ este mulțimea stărilor acceptoare
- Automatul acceptă un cuvânt dacă la parcurgerea acestuia se va regăsi într-o stare acceptoare

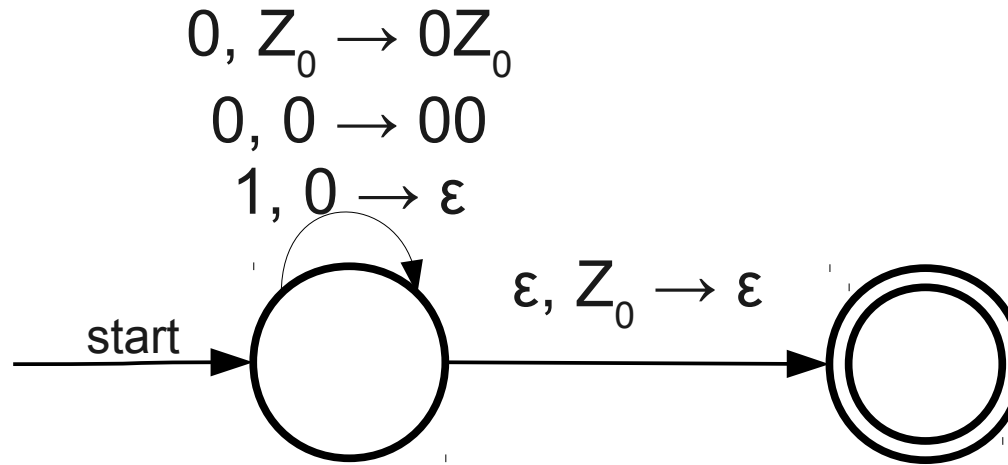
Limbajul unui automat push-down

- Limbajul unui automat push-down este mulțimea cuvintelor acceptate de acel automat:
 - $\mathcal{L}(P) = \{ w \in \Sigma^* \mid P \text{ acceptă } w \}$
- Dacă P este un automat push-down și $\mathcal{L}(P)=L$, atunci se afirmă faptul că P recunoaște L

A Simple Pushdown Automaton

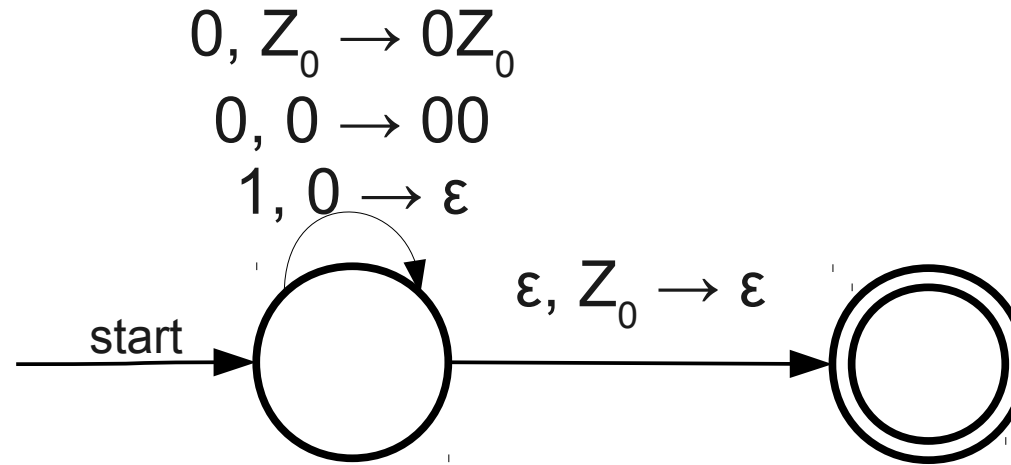


A Simple Pushdown Automaton



0 0 0 1 1 1

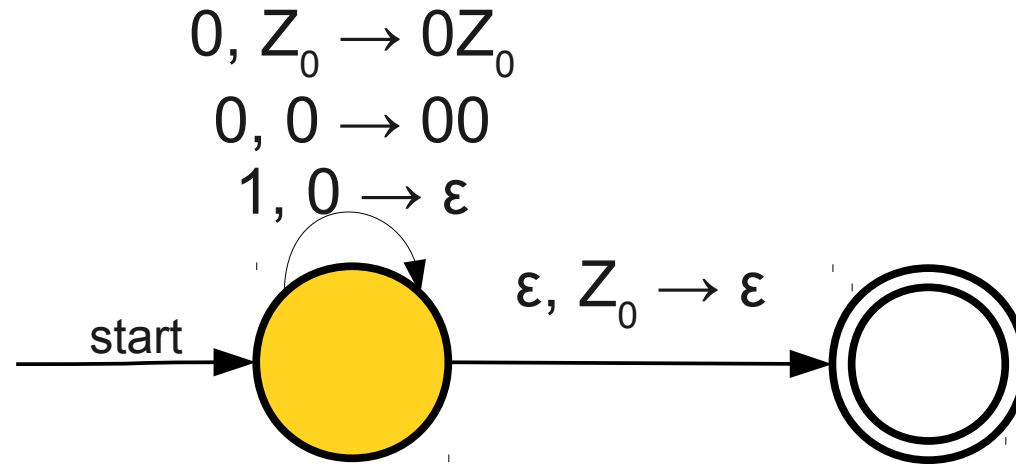
A Simple Pushdown Automaton



Z_0

0 0 0 1 1 1

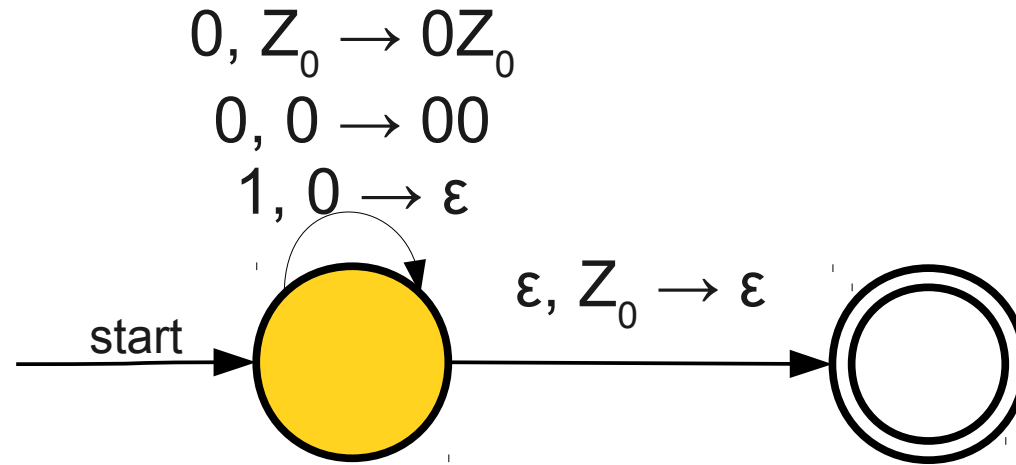
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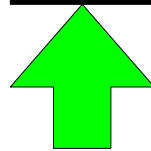
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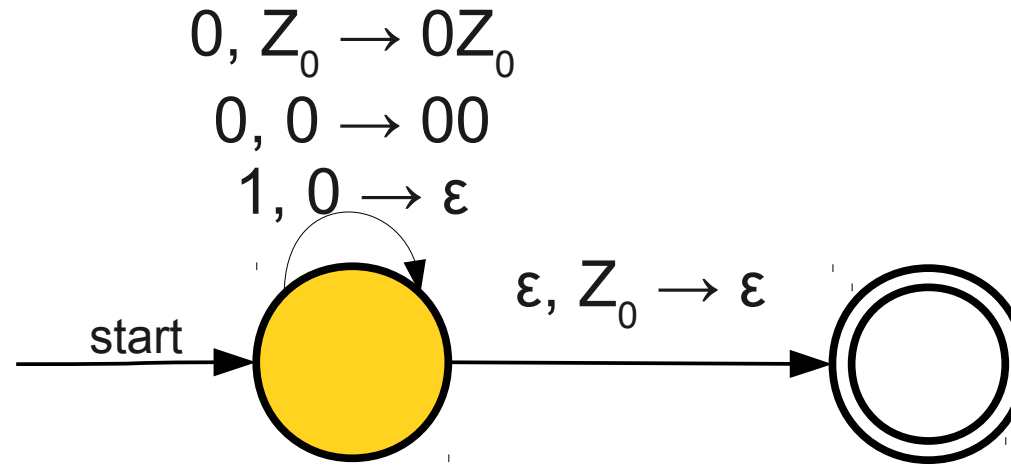


Z_0

0 0 0 1 1 1



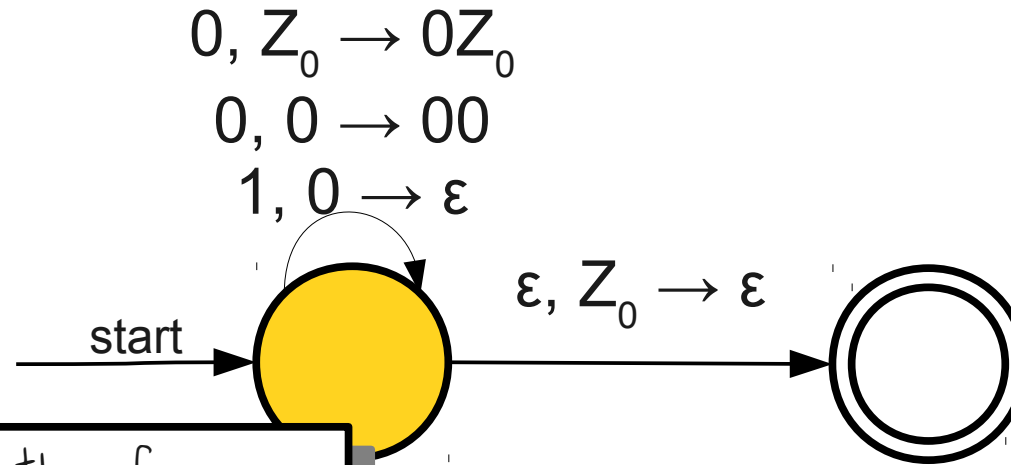
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Z_0



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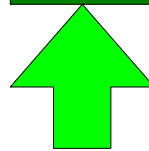
A transition of the form

$$\mathbf{a, b \rightarrow z}$$

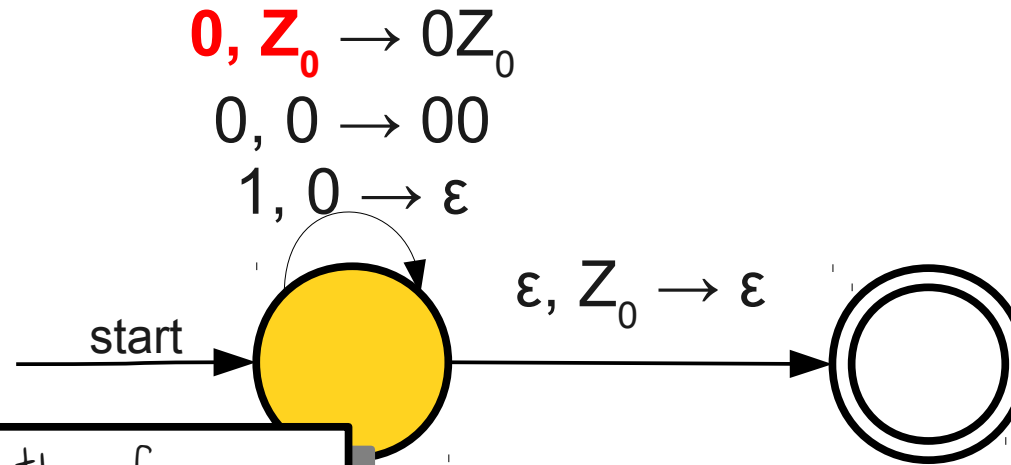
Means "If the current **input symbol** is a and the current **stack symbol** is b, then follow this transition, pop b, and push the string z.

Z_0

0 0 0 1 1 1



A Simple Pushdown Automaton



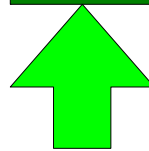
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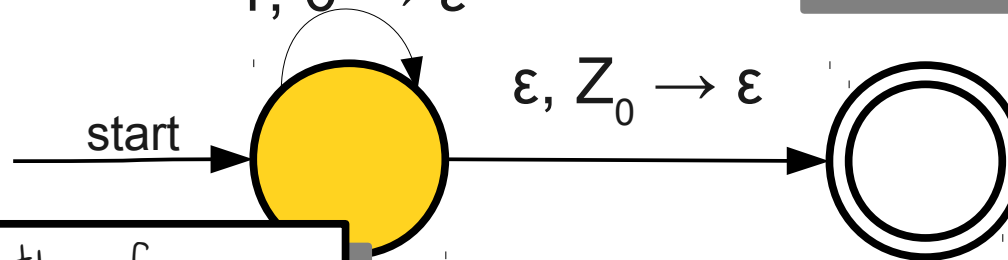
0 0 0 1 1 1



A Simple Pushdown Automaton

$0, Z_0 \rightarrow 0Z_0$
 $0, 0 \rightarrow 00$
 $1, 0 \rightarrow \epsilon$

To find an applicable transition, match the current input/stack pair.



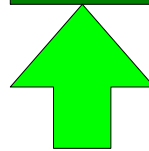
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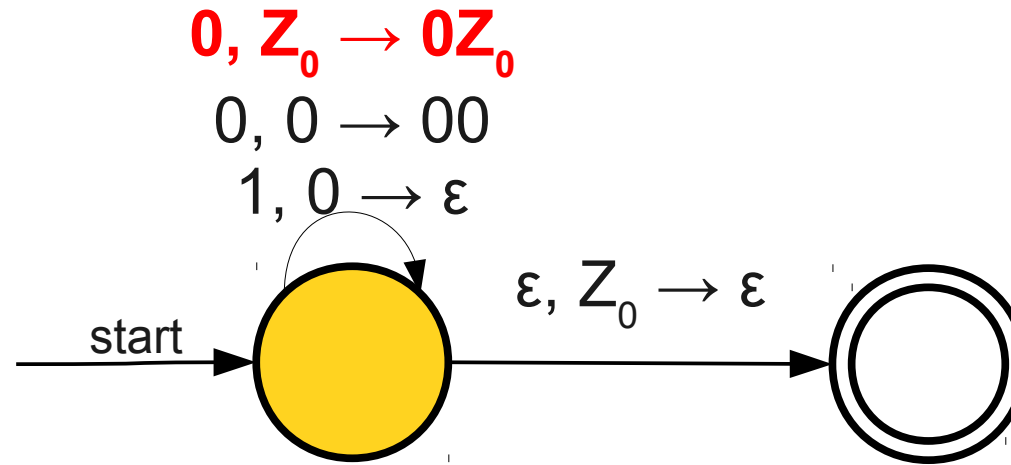
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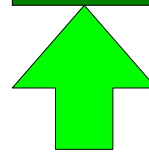


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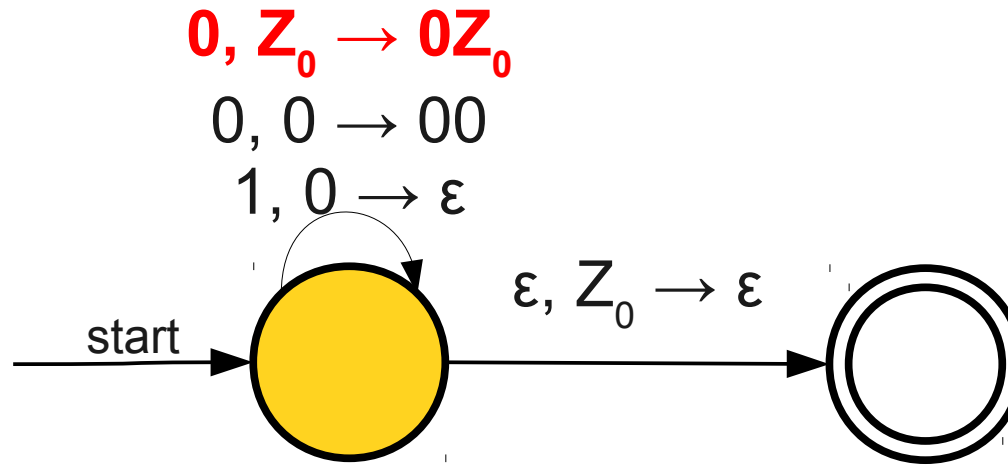


Z_0

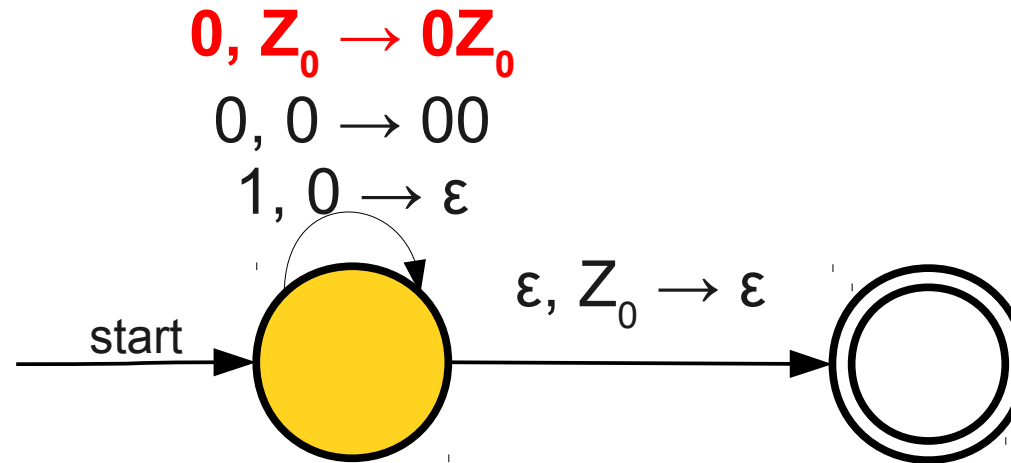
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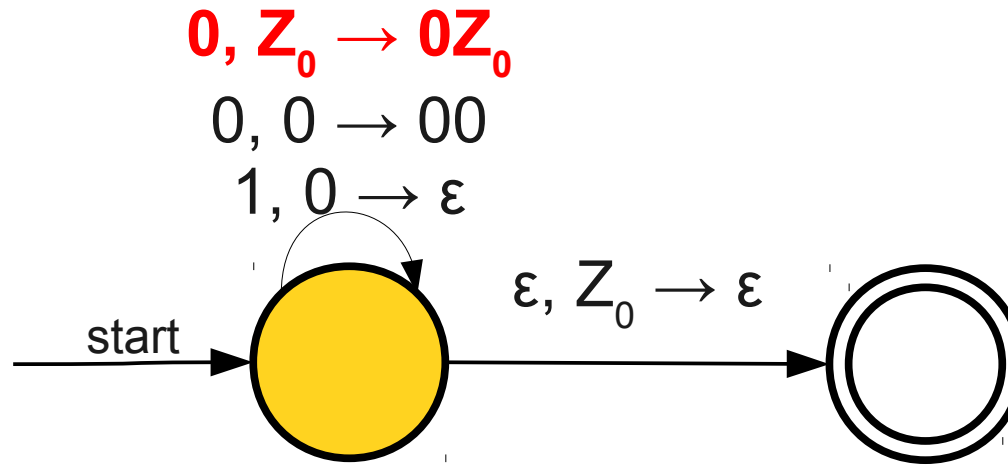
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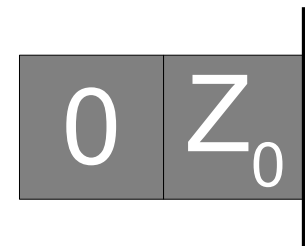
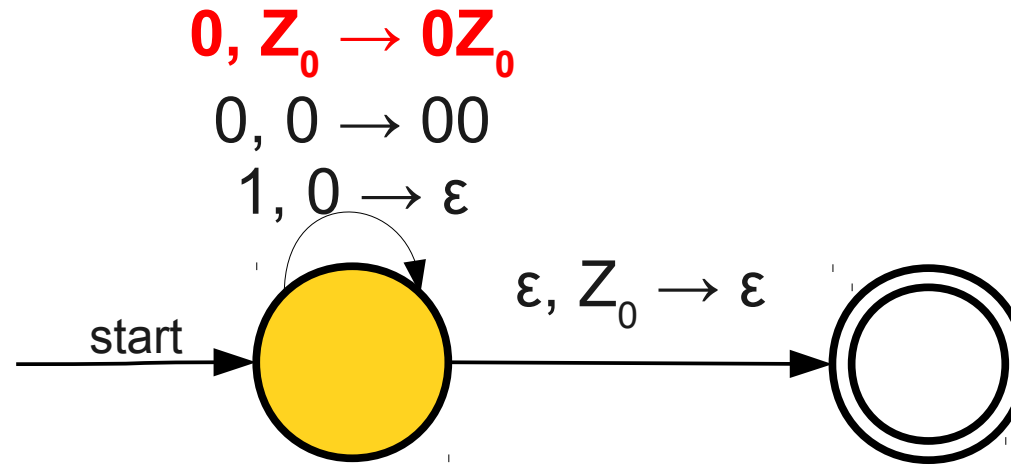
If a transition reads the top symbol of the stack, it always pops that symbol (though it might replace it)



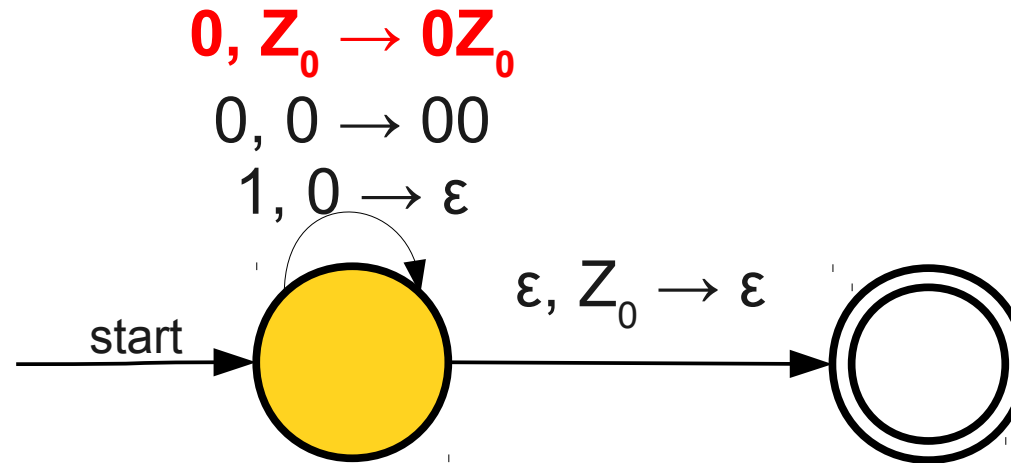
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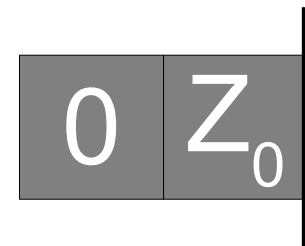
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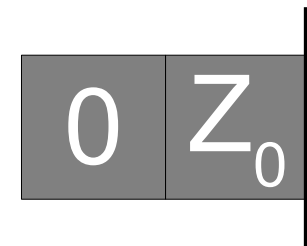
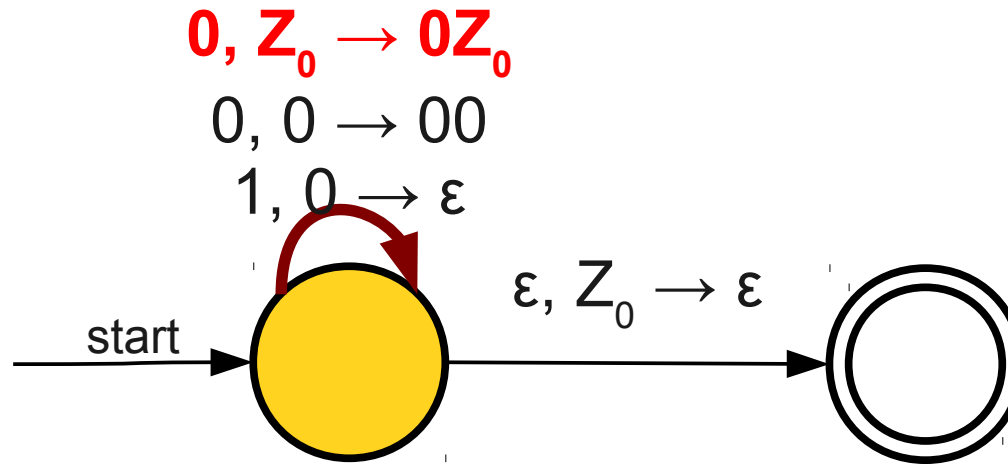
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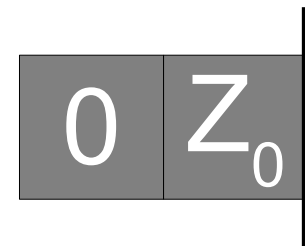
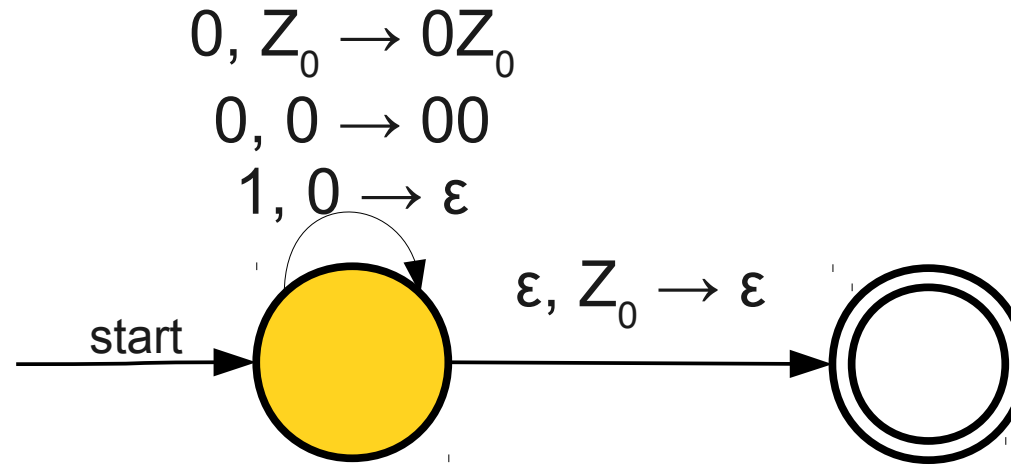
Each transition then pushes some (possibly empty) string back onto the stack. Notice that the leftmost symbol is pushed onto the top.



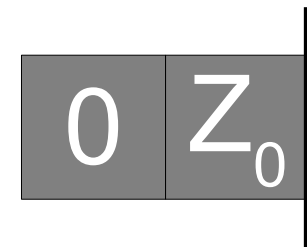
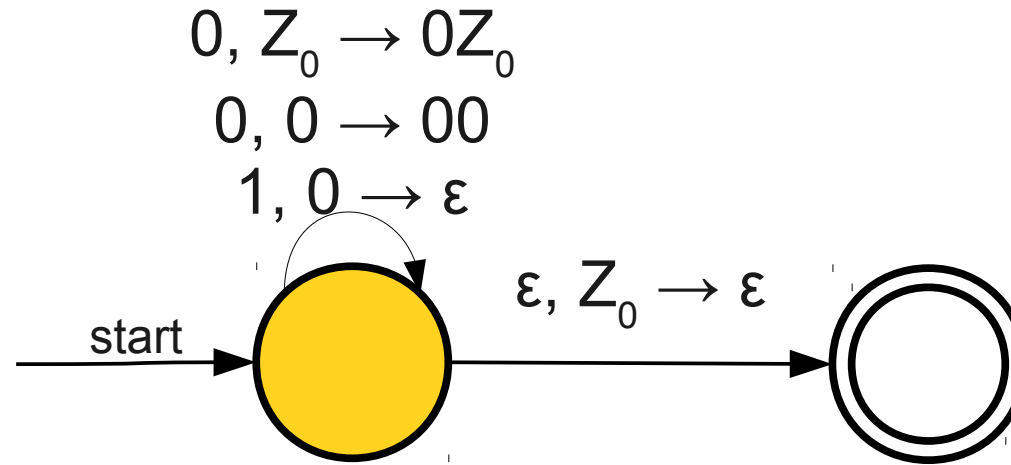
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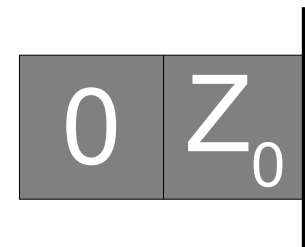
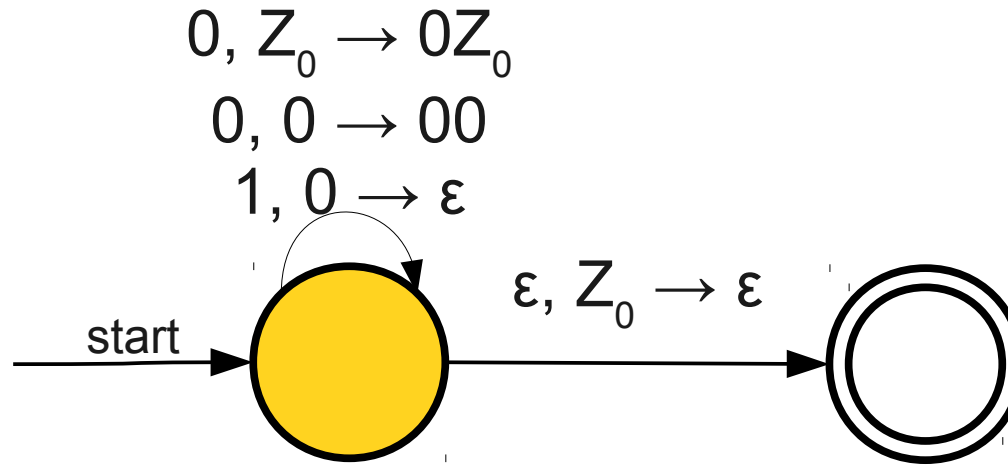
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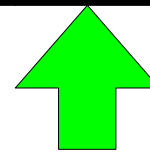
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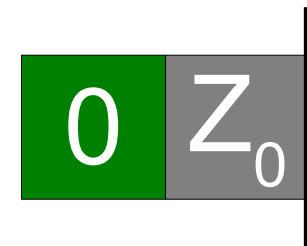
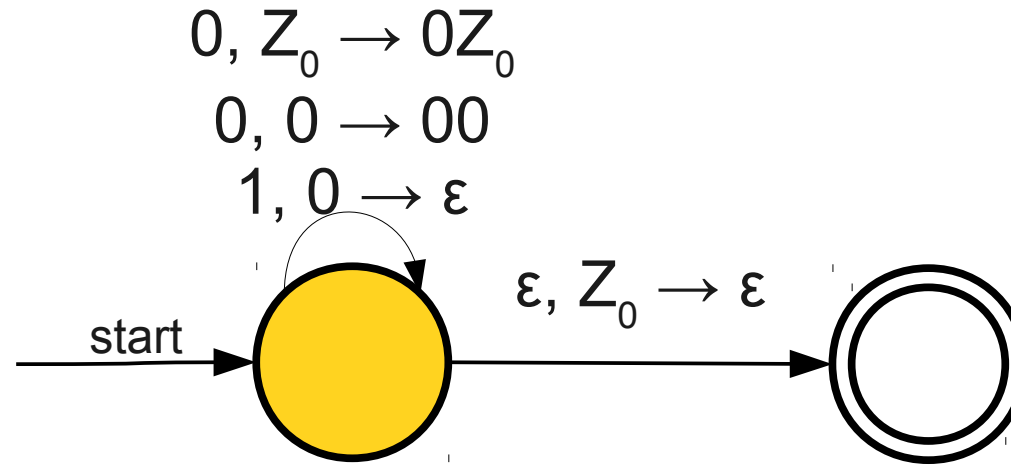
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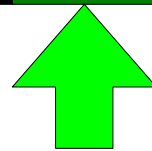
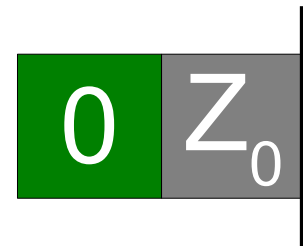
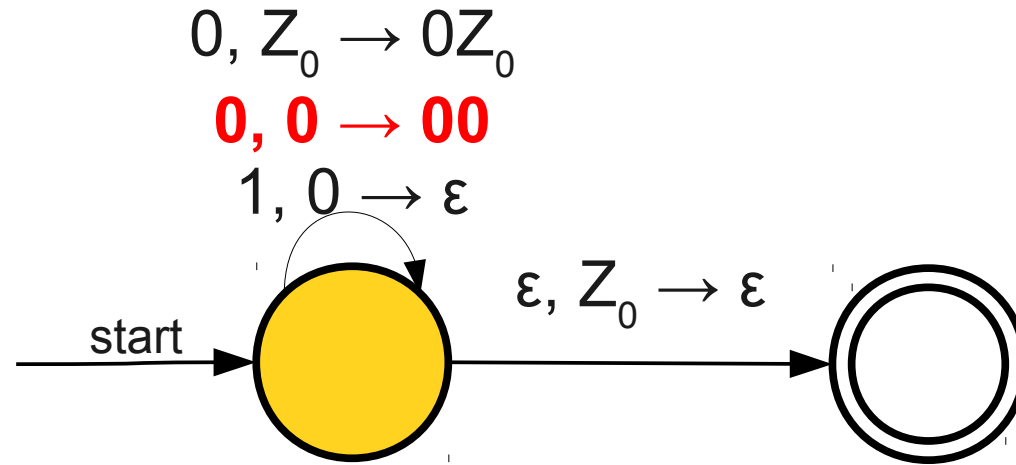
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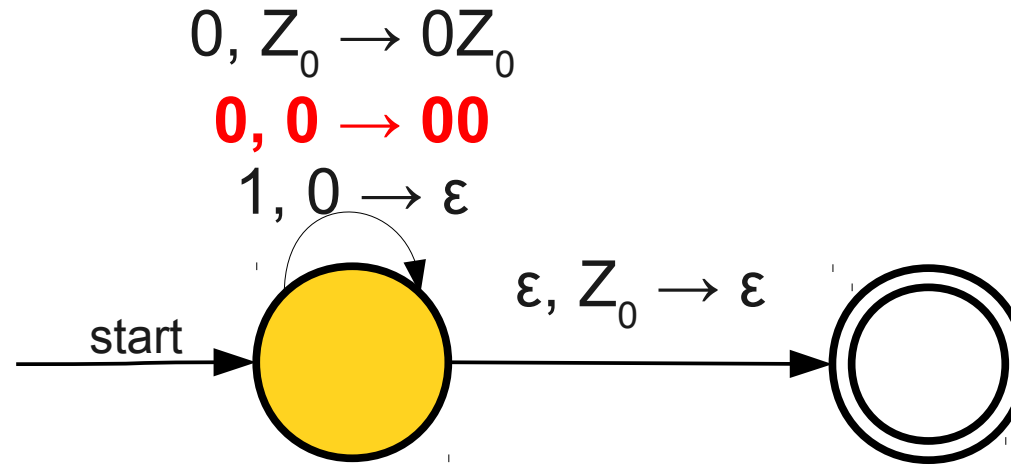
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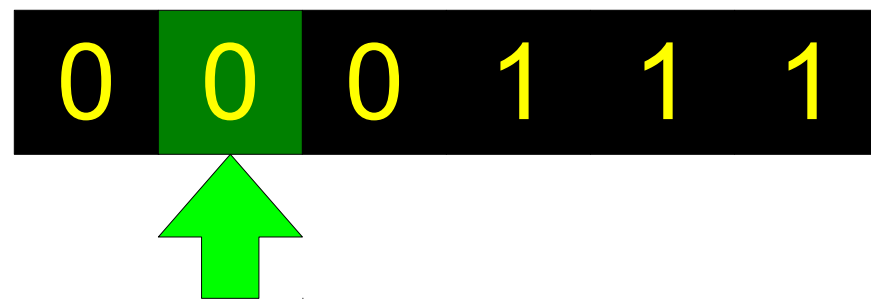
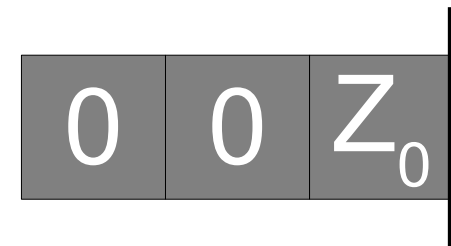
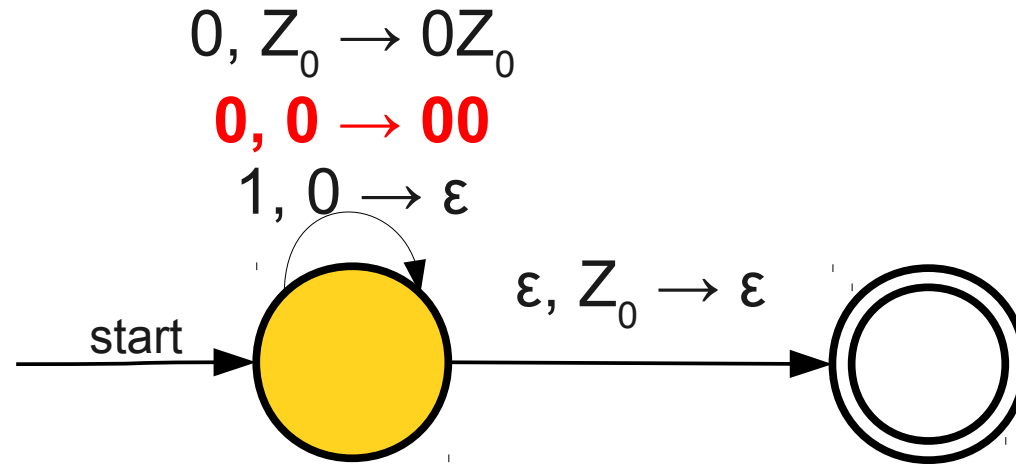


Z_0

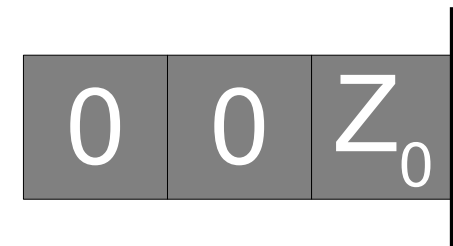
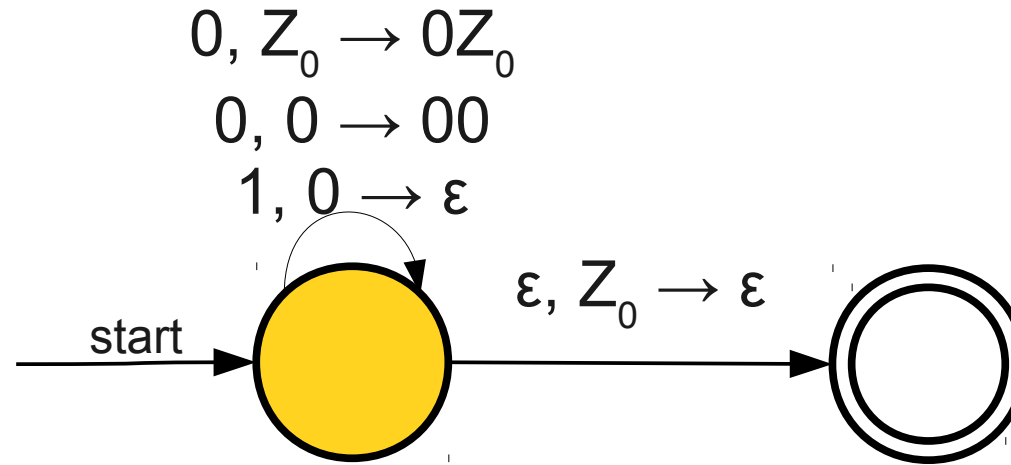
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A Simple Pushdown Automaton



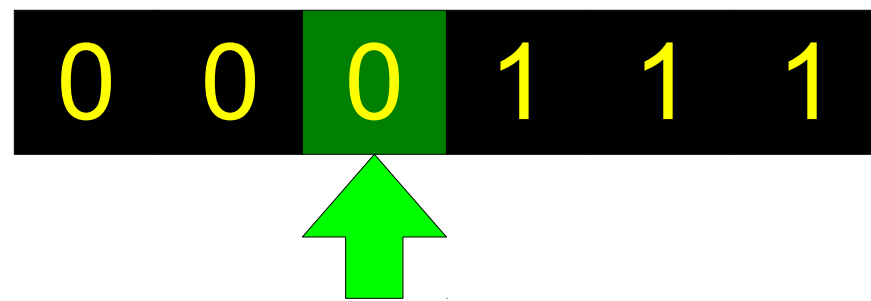
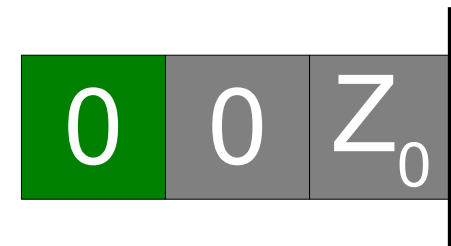
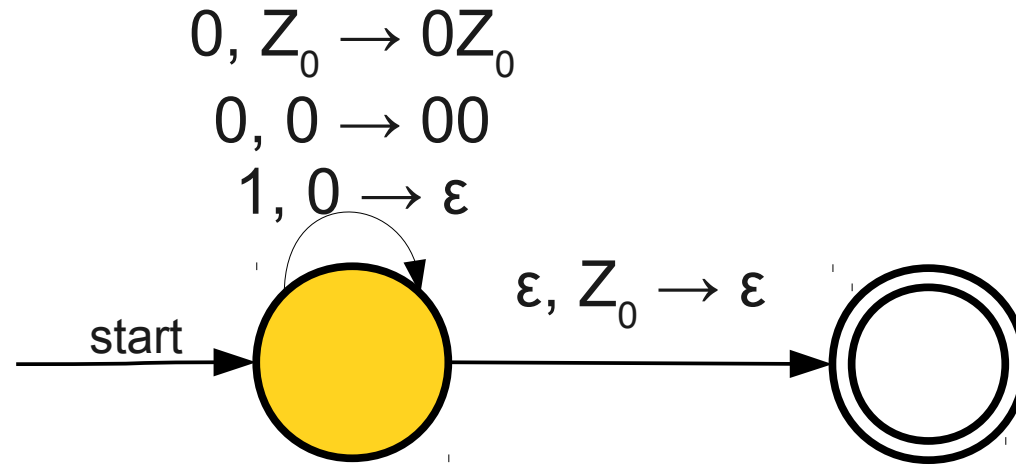
A Simple Pushdown Automaton



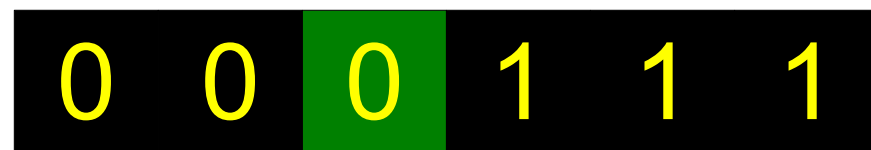
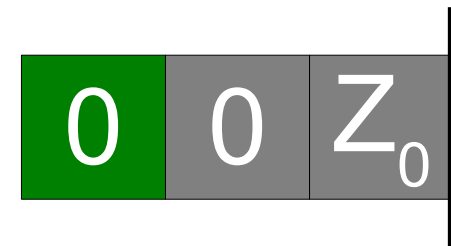
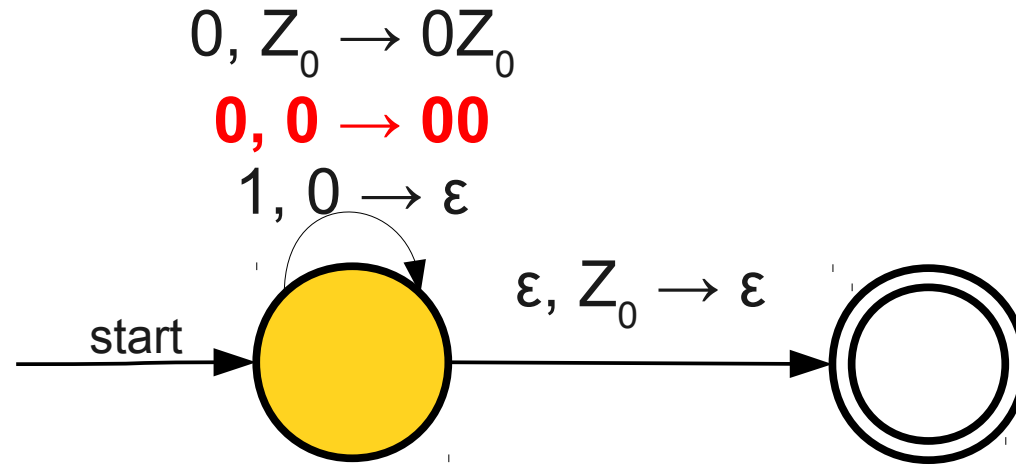
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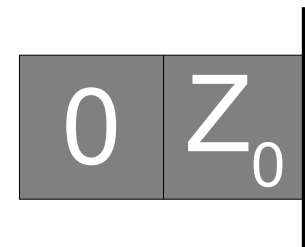
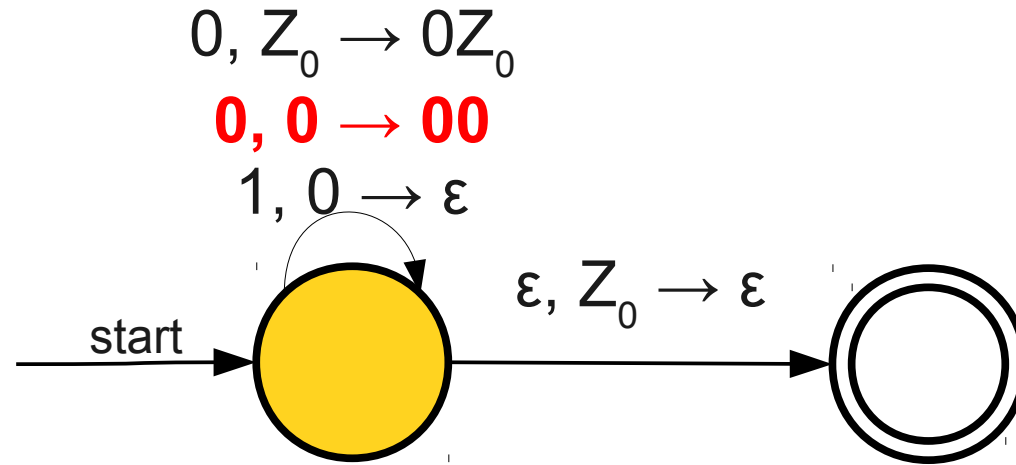
A Simple Pushdown Automaton



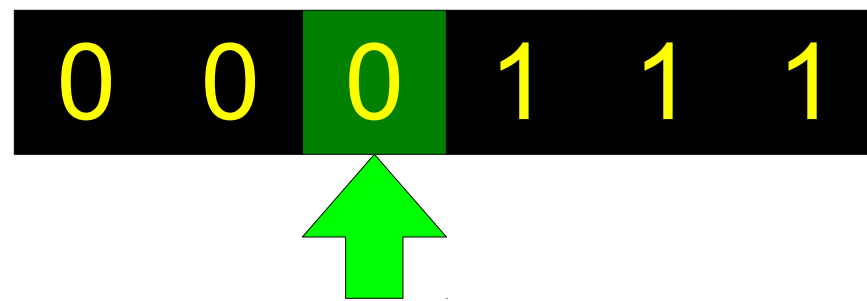
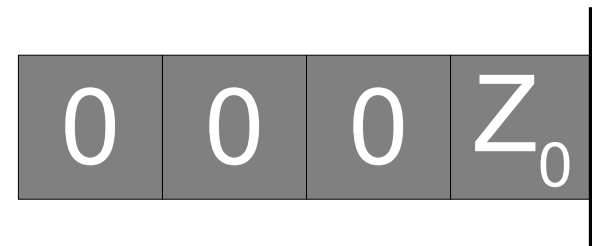
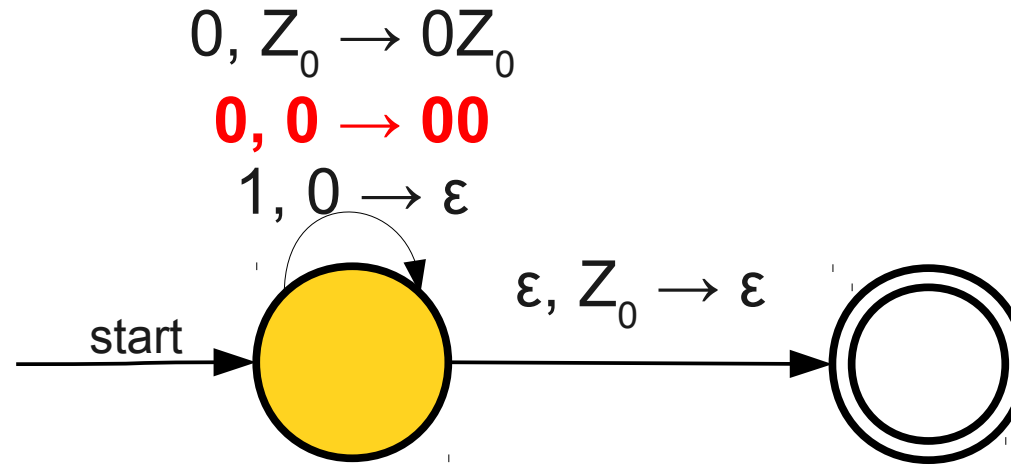
A Simple Pushdown Automaton



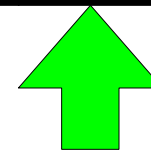
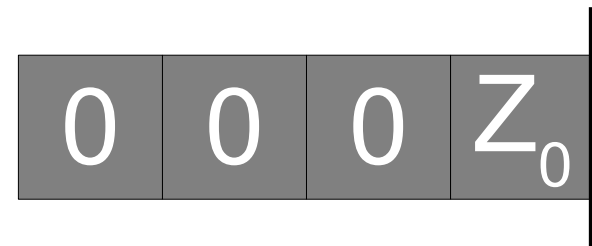
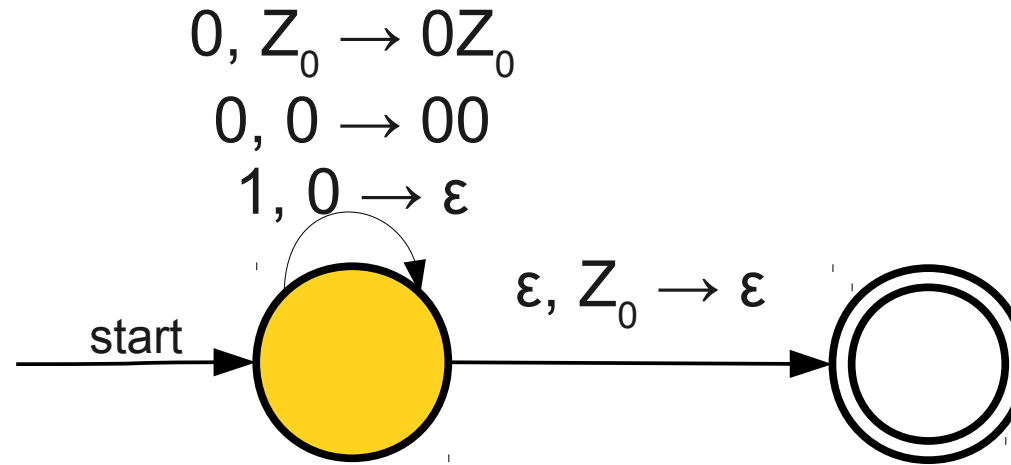
A Simple Pushdown Automaton



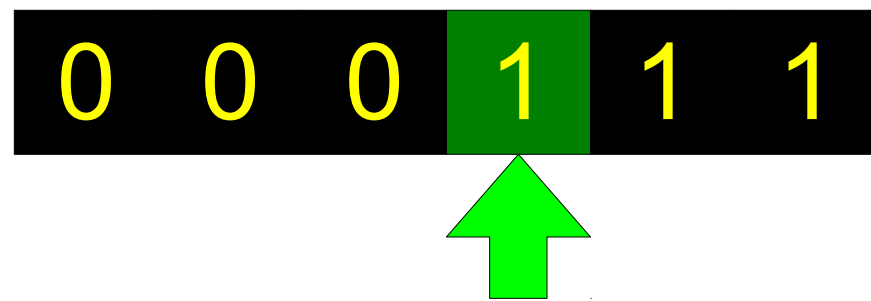
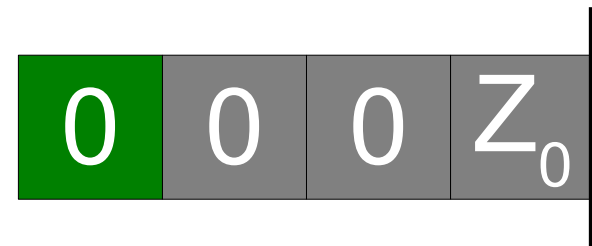
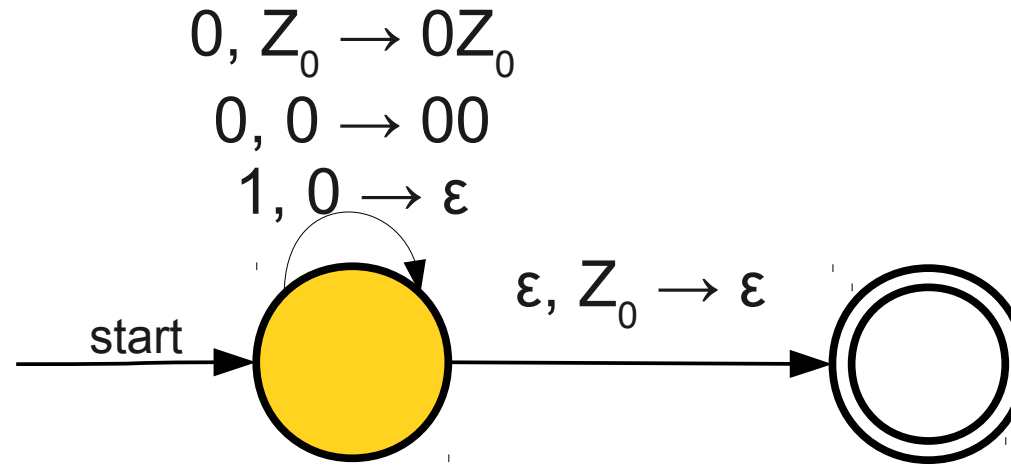
A Simple Pushdown Automaton



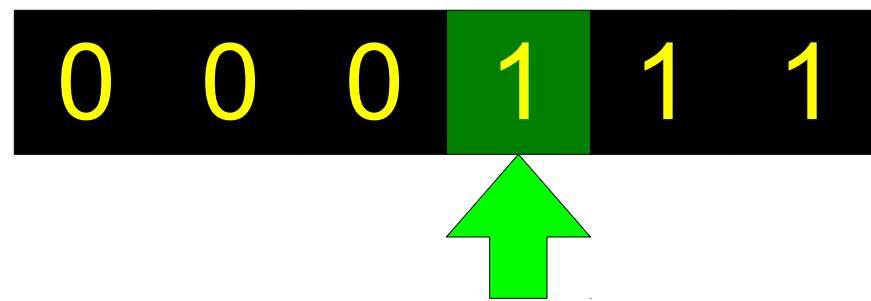
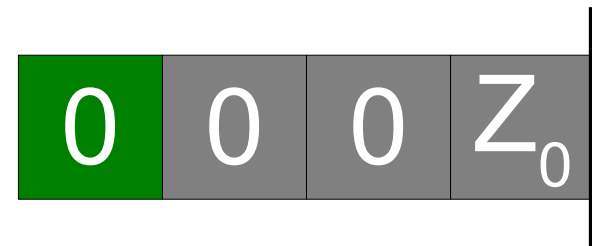
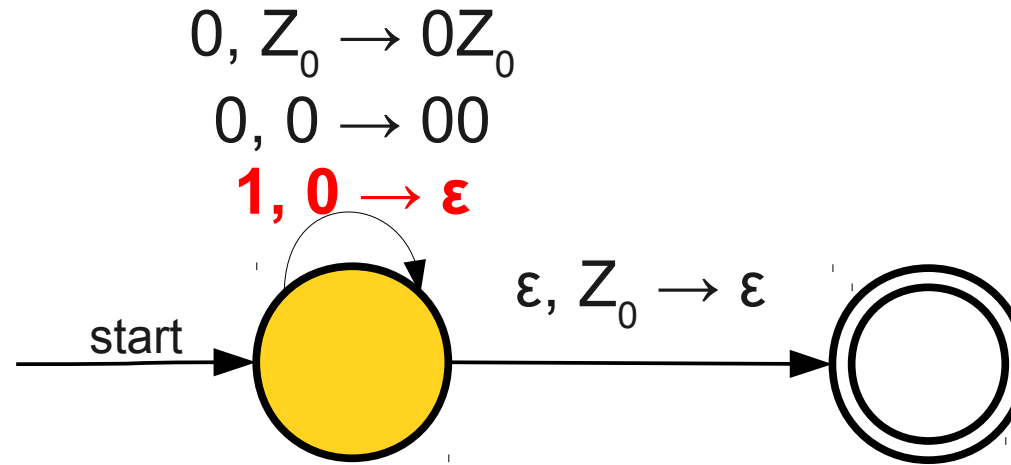
A Simple Pushdown Automaton



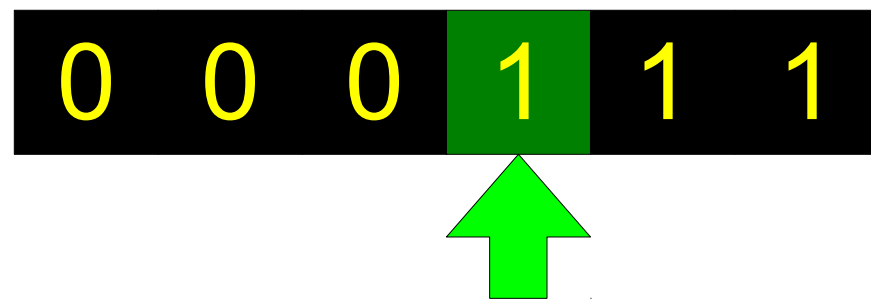
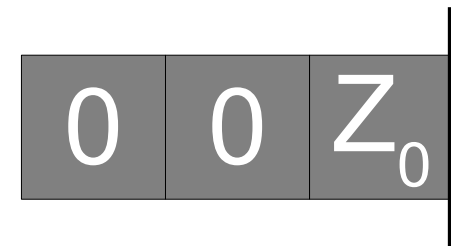
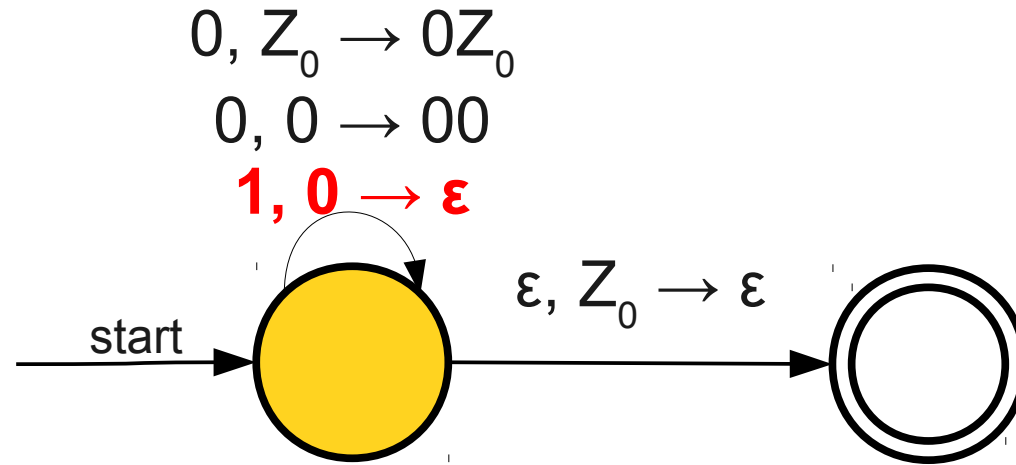
A Simple Pushdown Automaton



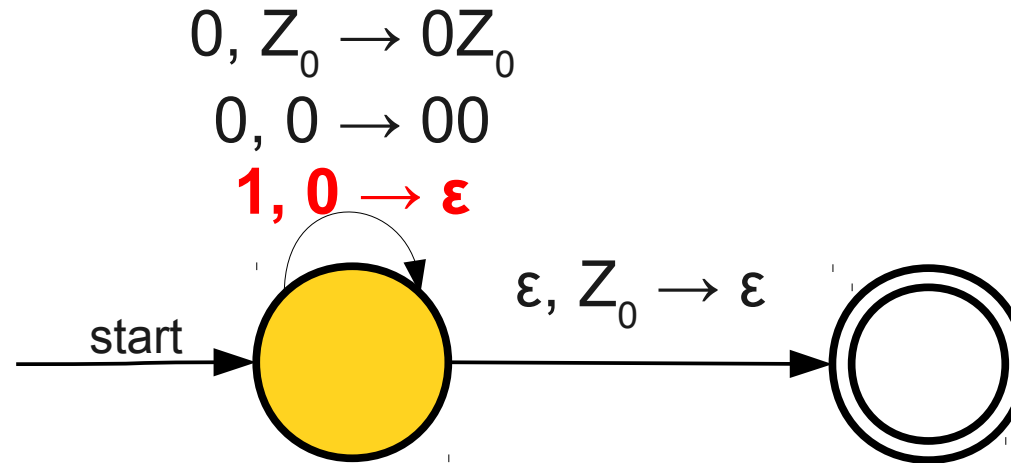
A Simple Pushdown Automaton



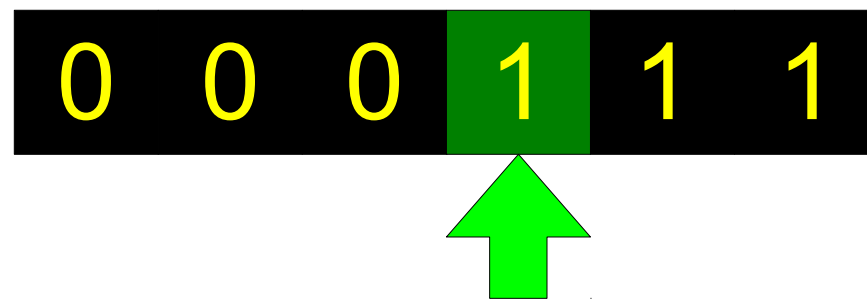
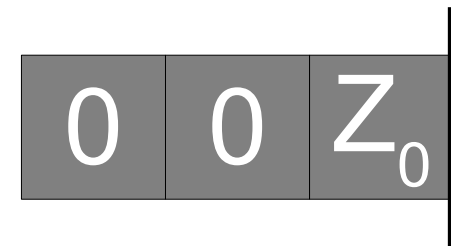
A Simple Pushdown Automaton



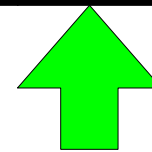
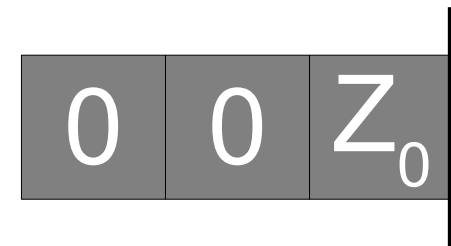
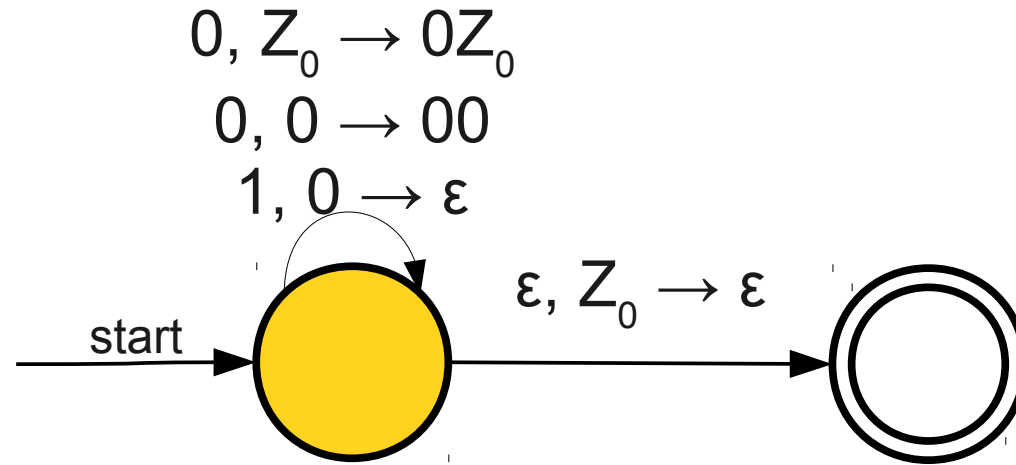
A Simple Pushdown Automaton



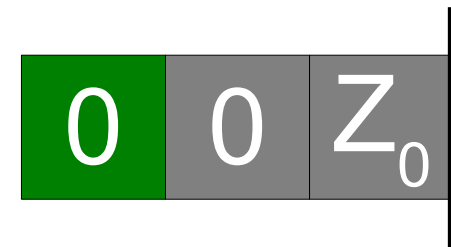
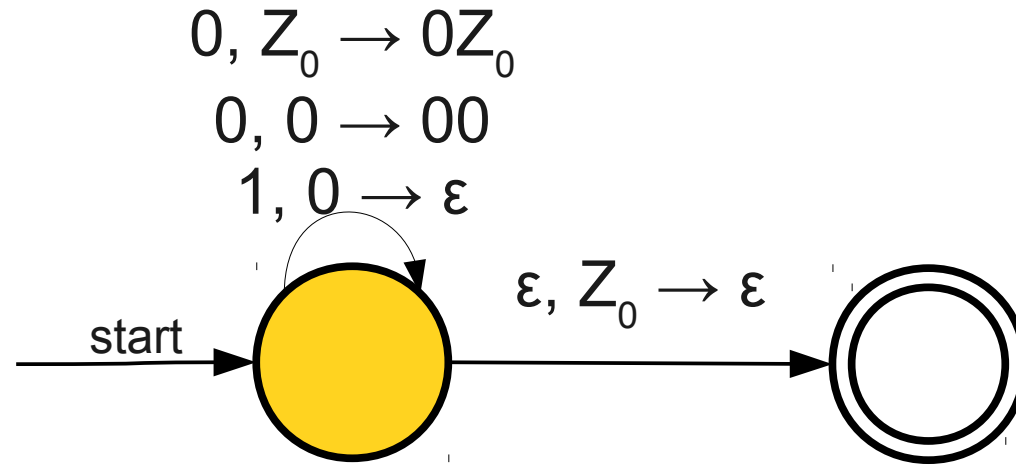
We now push the string ϵ onto the stack, which adds no new characters. This essentially means "pop the stack."



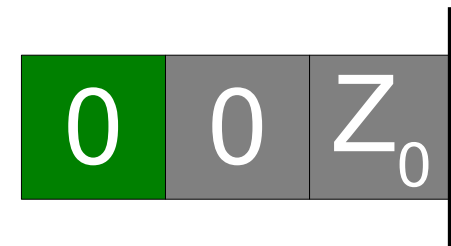
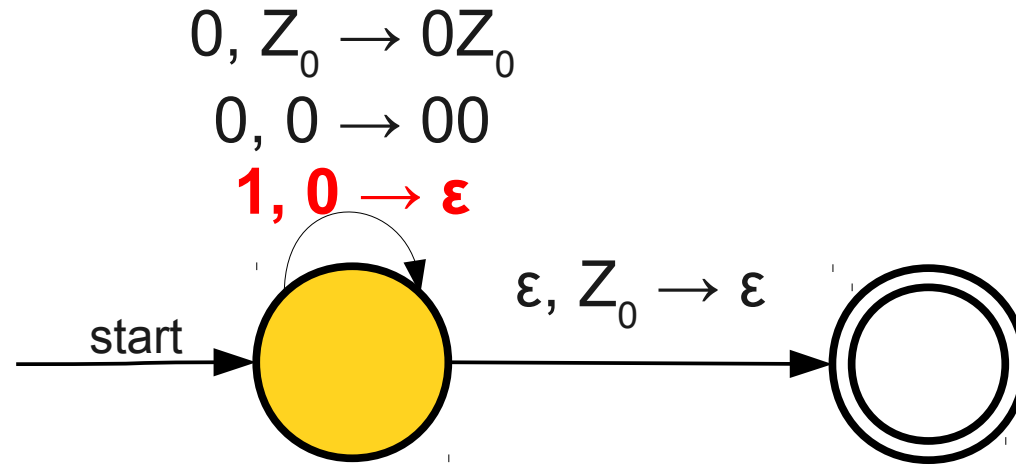
A Simple Pushdown Automaton



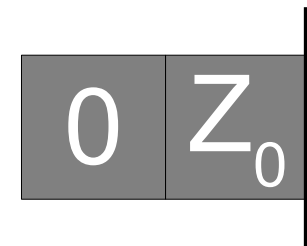
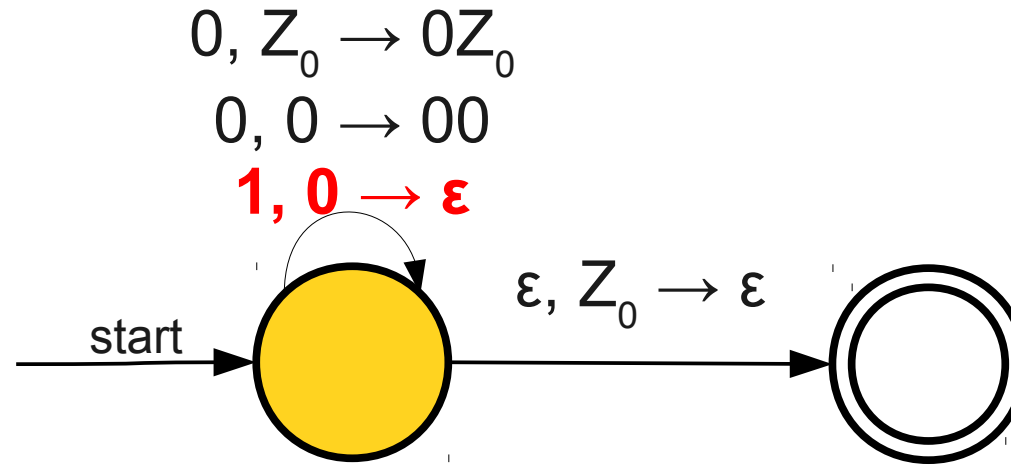
A Simple Pushdown Automaton



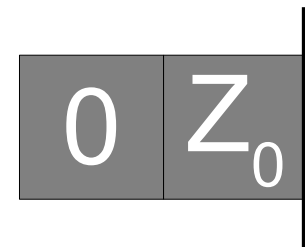
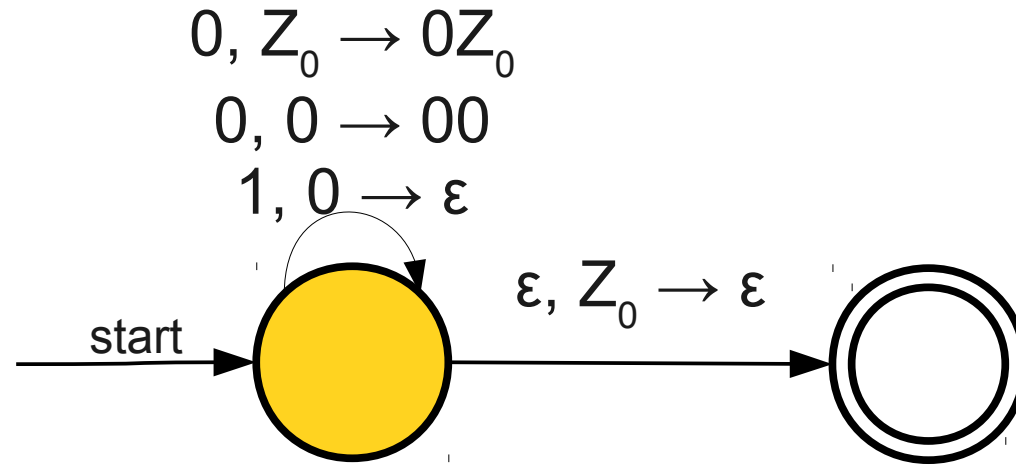
A Simple Pushdown Automaton



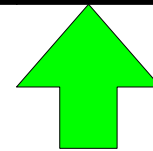
A Simple Pushdown Automaton



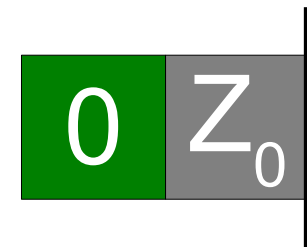
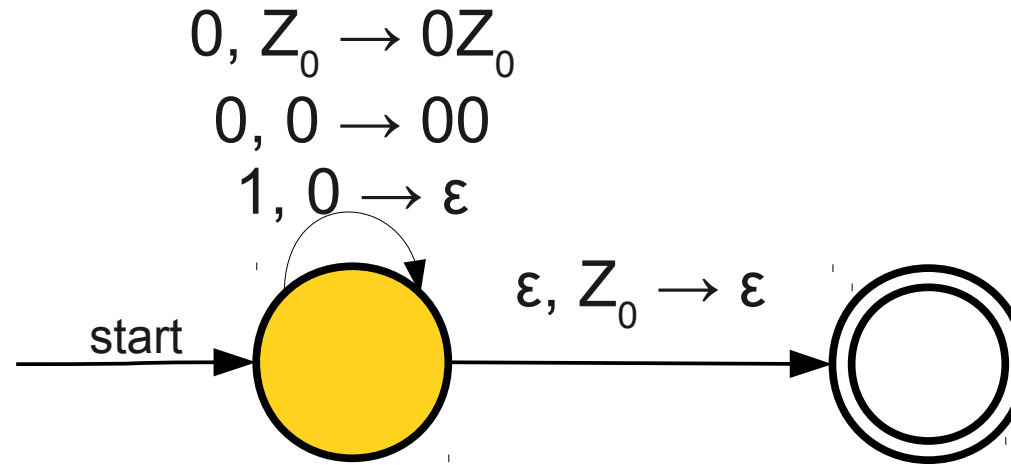
A Simple Pushdown Automaton



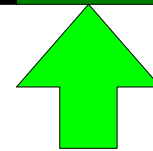
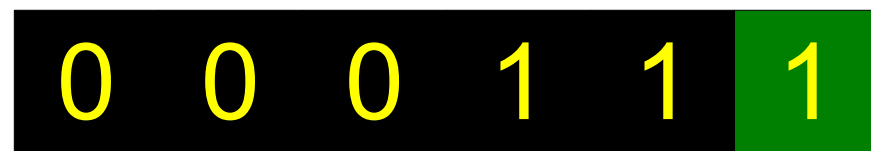
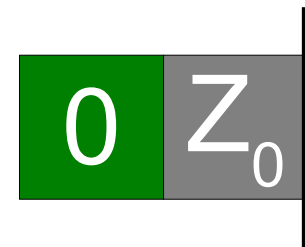
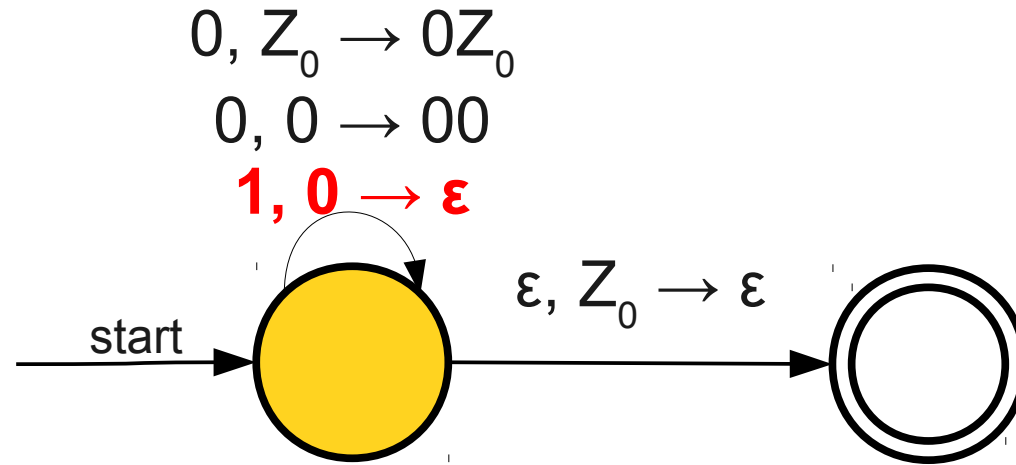
0 0 0 1 1 1



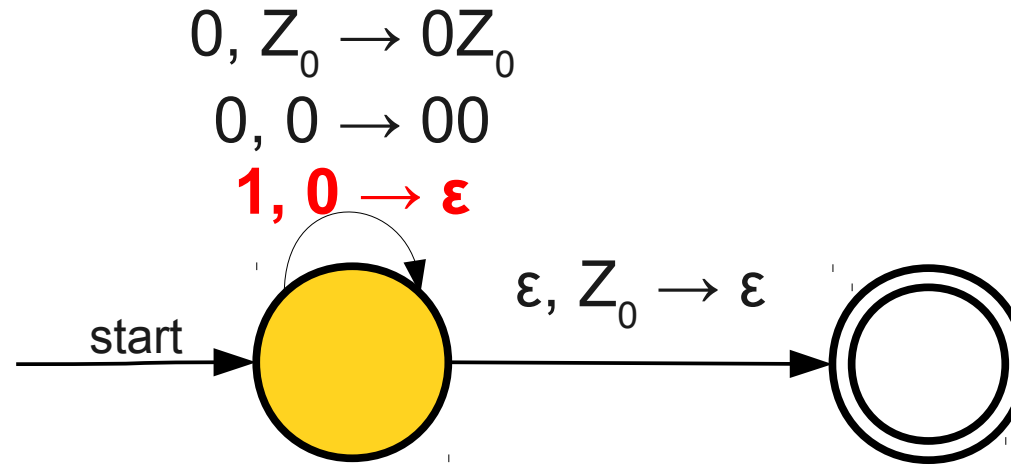
A Simple Pushdown Automaton



A Simple Pushdown Automaton



A Simple Pushdown Automaton

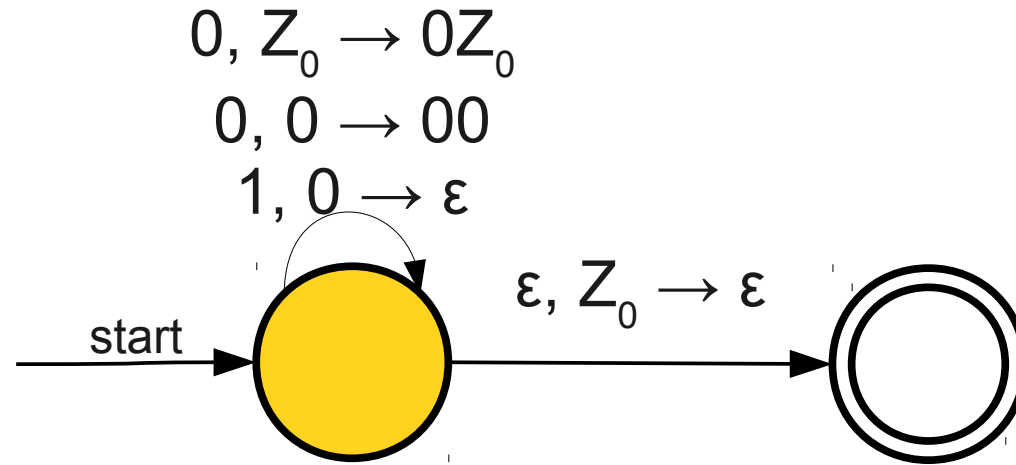


Z_0

0 0 0 1 1 1

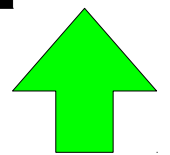


A Simple Pushdown Automaton

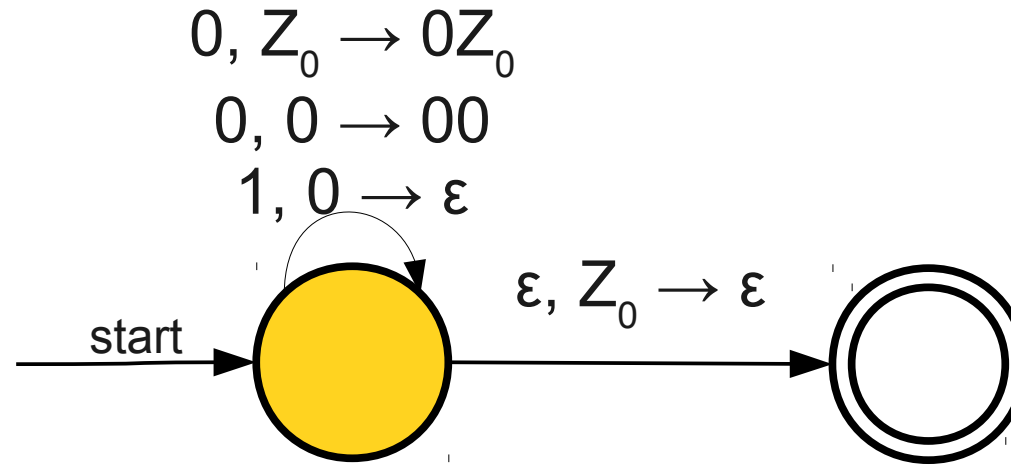


Z_0

0 0 0 1 1 1



A Simple Pushdown Automaton

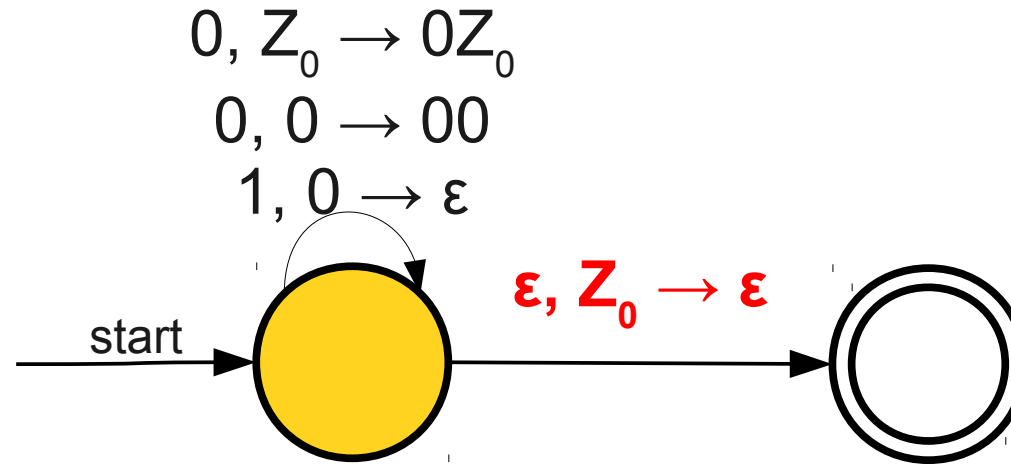


Z_0

0 0 0 1 1 1



A Simple Pushdown Automaton

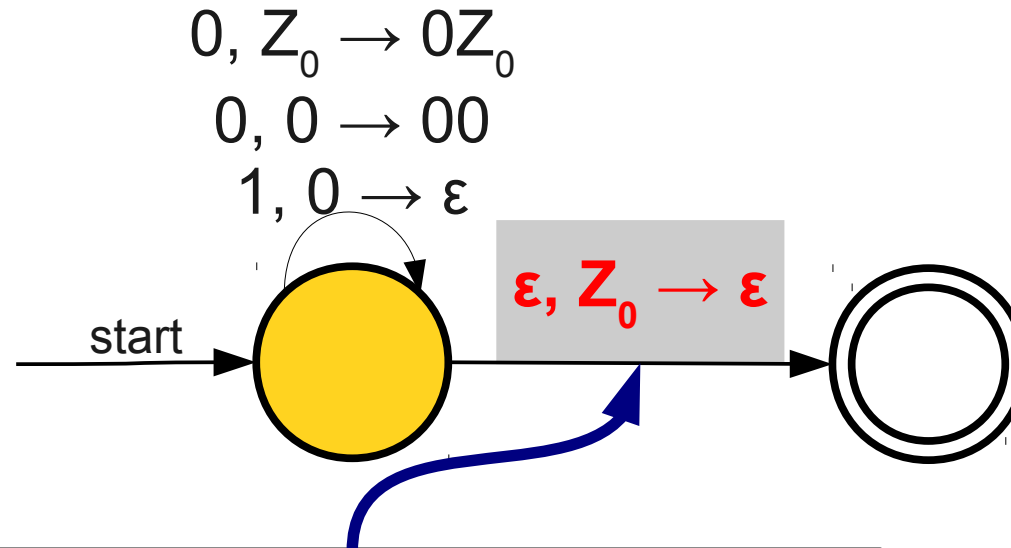


Z_0

0 0 0 1 1 1



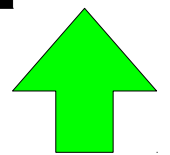
A Simple Pushdown Automaton



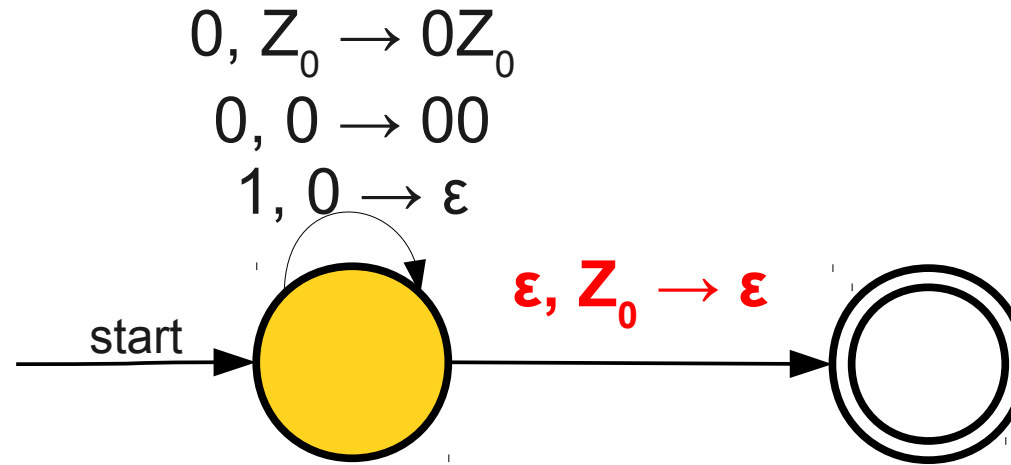
This transition can be taken at any time z_0 is atop the stack, but we've nondeterministically guessed that this would be a good time to take it.

Z_0

0 0 0 1 1 1



A Simple Pushdown Automaton

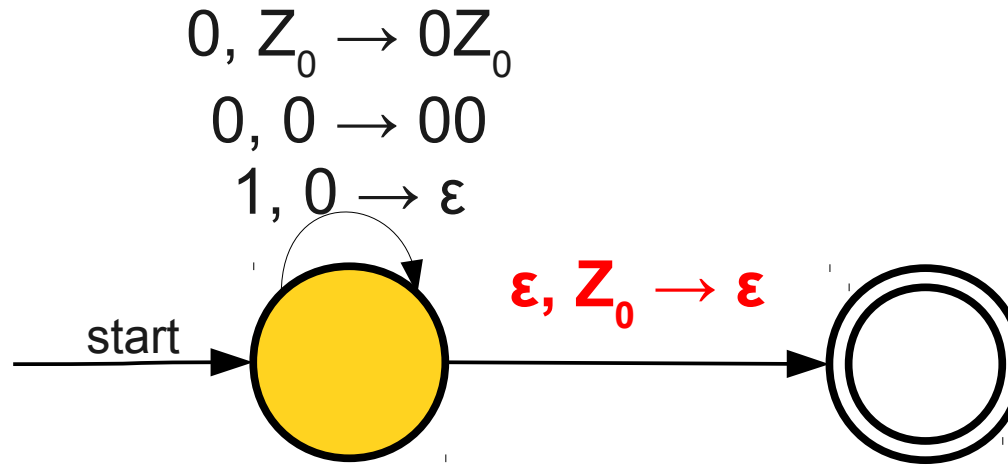


Z_0

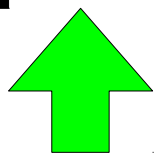
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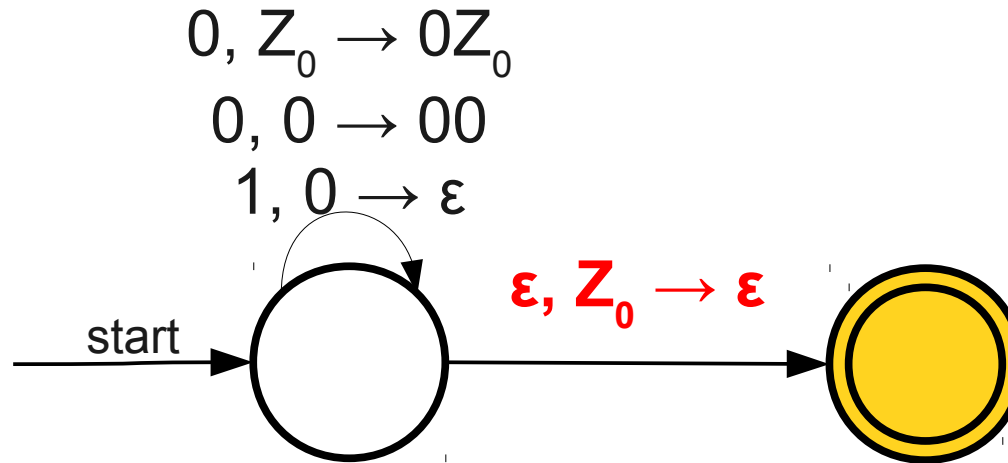
A Simple Pushdown Automaton



0 0 0 1 1 1



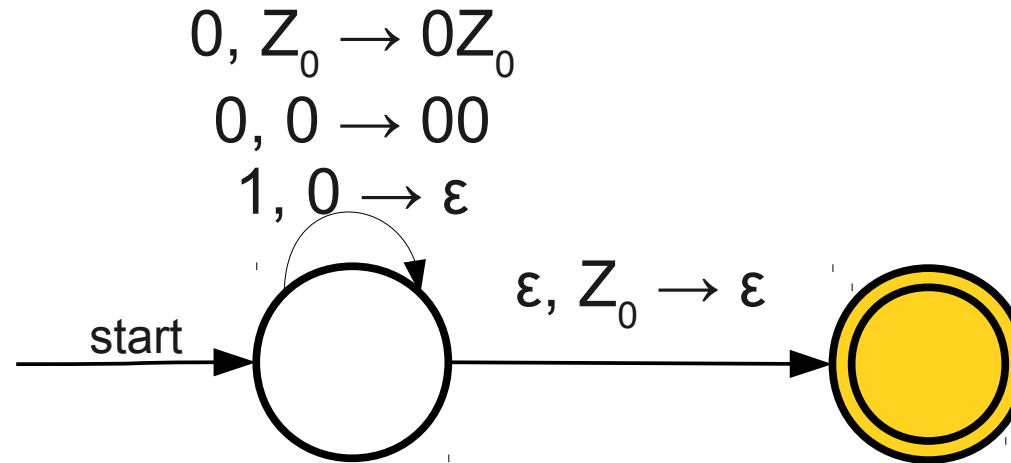
A Simple Pushdown Automaton



0 0 0 1 1 1



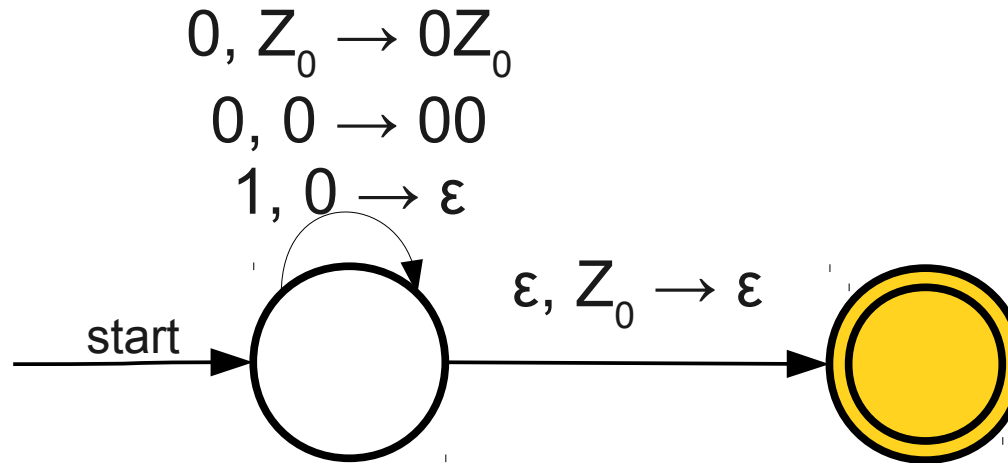
A Simple Pushdown Automaton



0 0 0 1 1 1

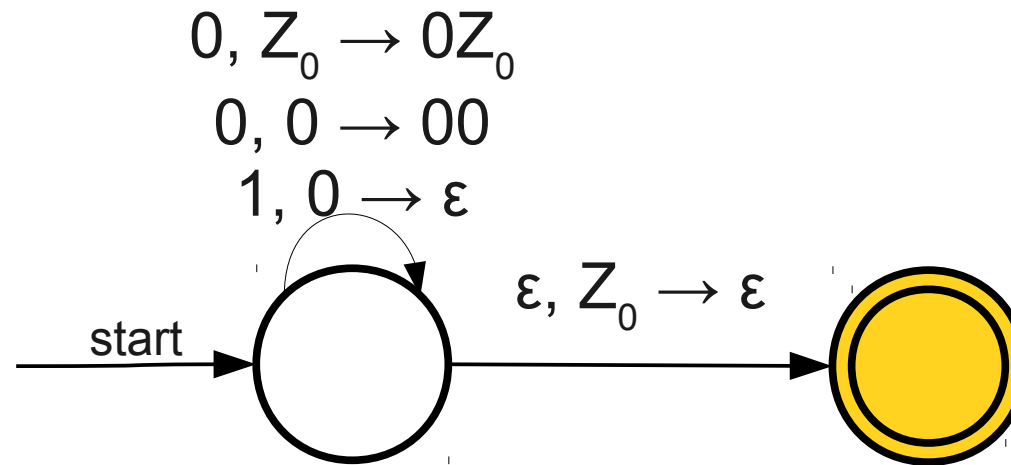


A Simple Pushdown Automaton



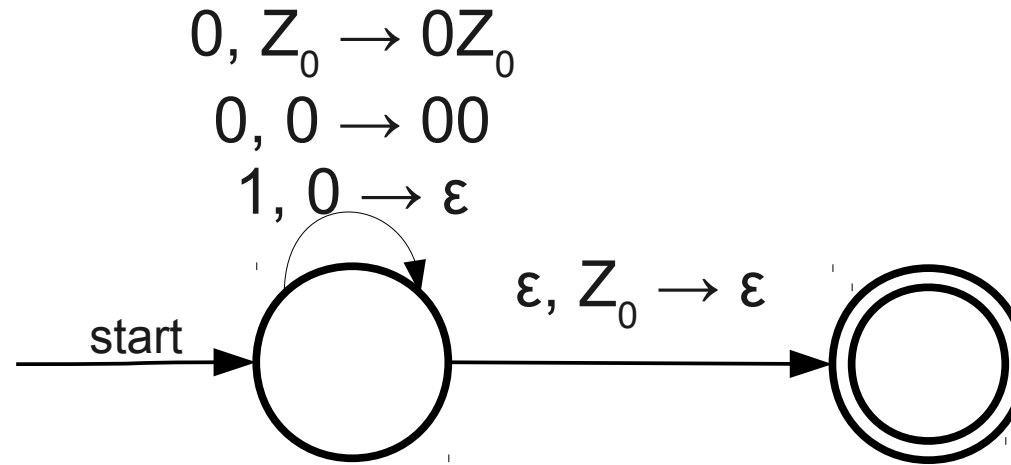
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A Simple Pushdown Automaton

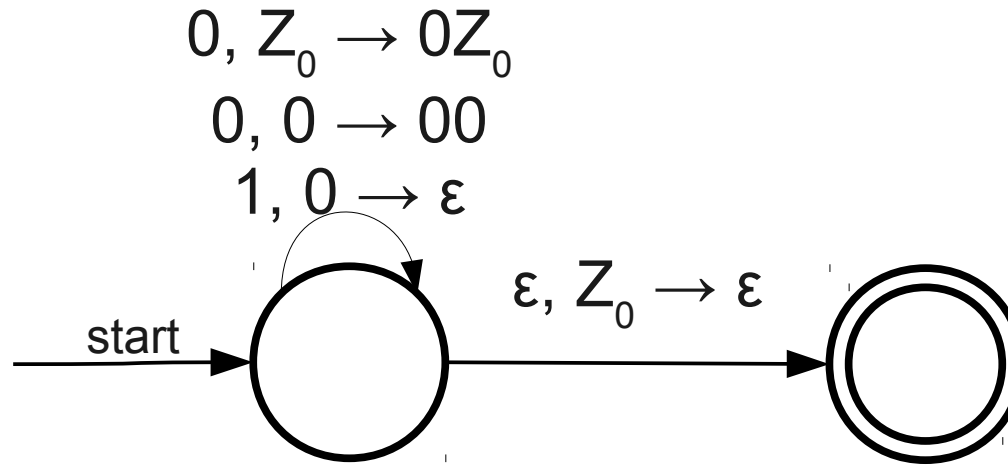


0 0 0 1 1 1

A Simple Pushdown Automaton

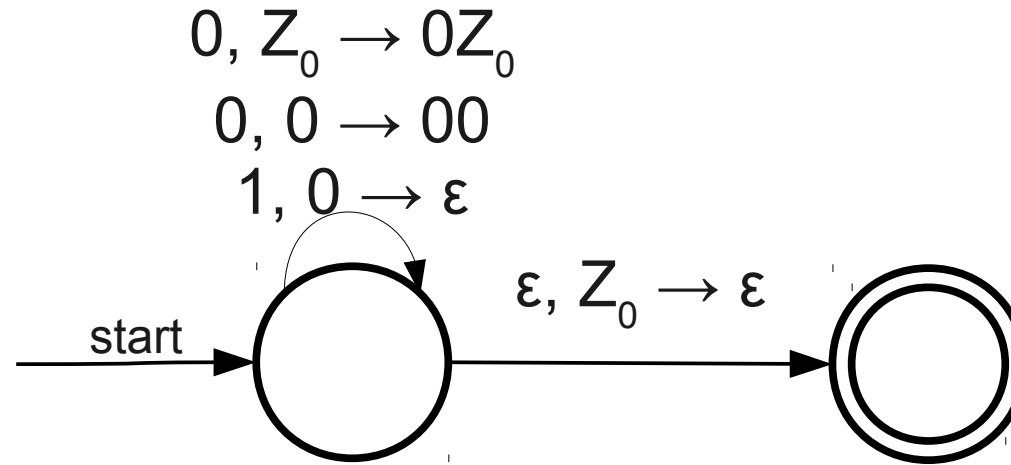


A Simple Pushdown Automaton



0 1 1 0 0 1

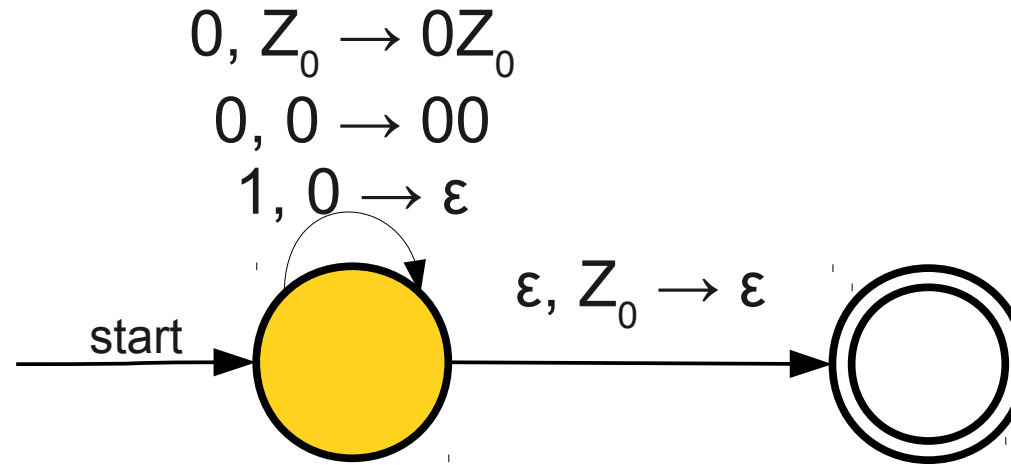
A Simple Pushdown Automaton



Z_0

0 1 1 0 0 1

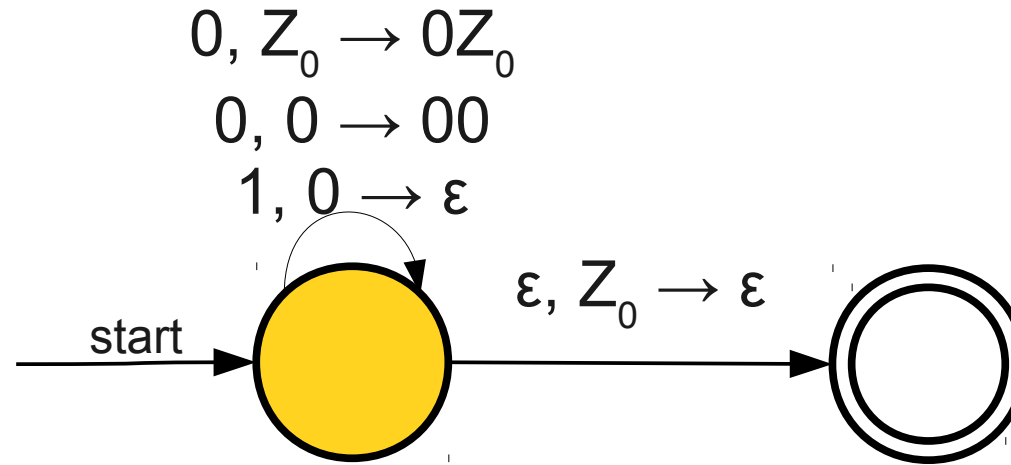
A Simple Pushdown Automaton



Z_0

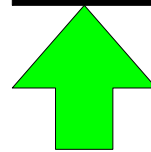
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A Simple Pushdown Automaton

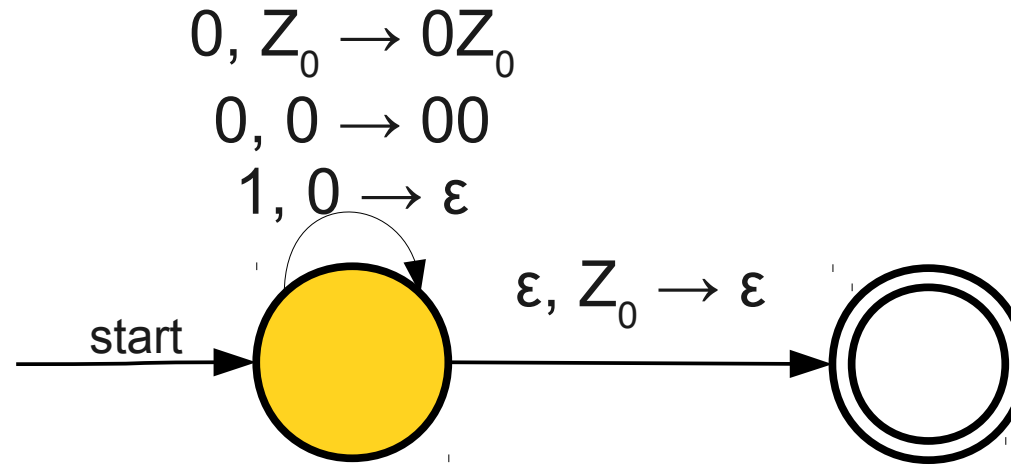


Z_0

0 1 1 0 0 1



A Simple Pushdown Automaton

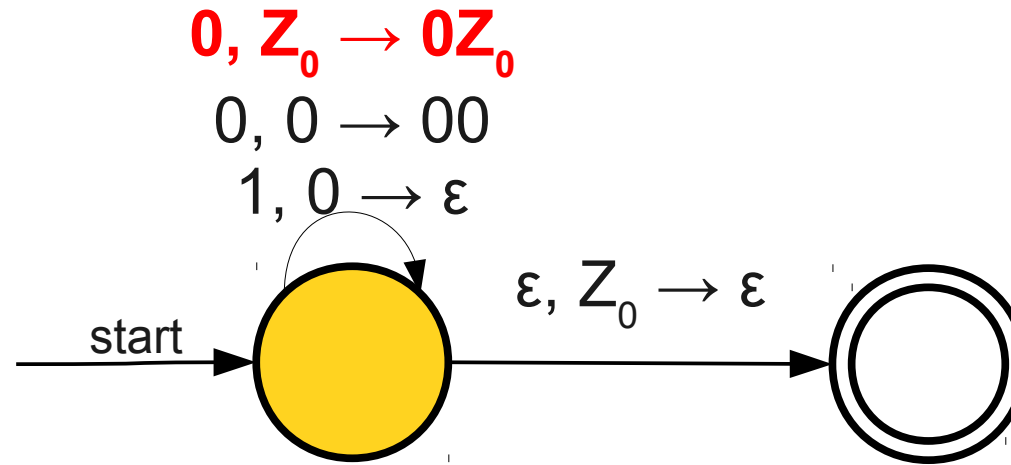


Z_0

0 1 1 0 0 1

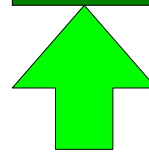


A Simple Pushdown Automaton

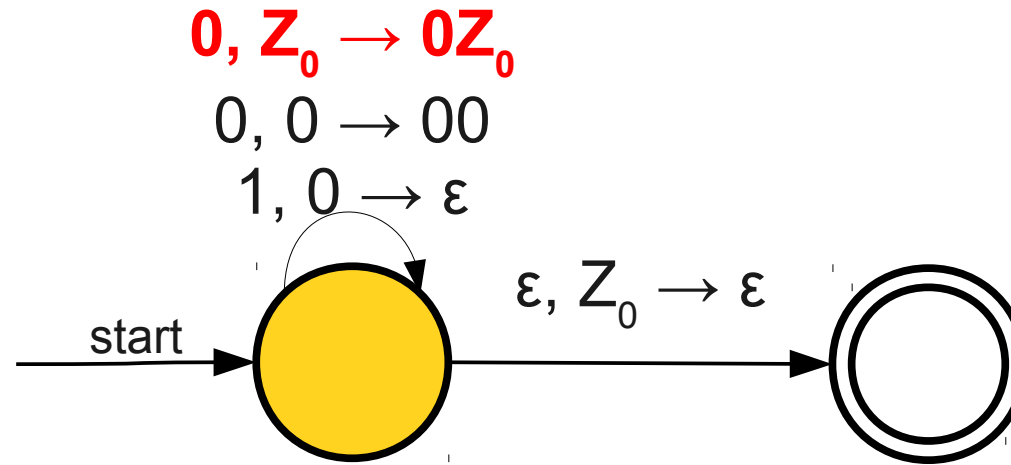


Z_0

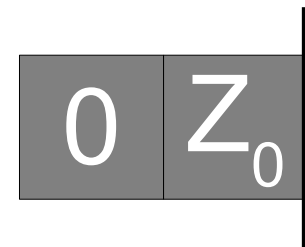
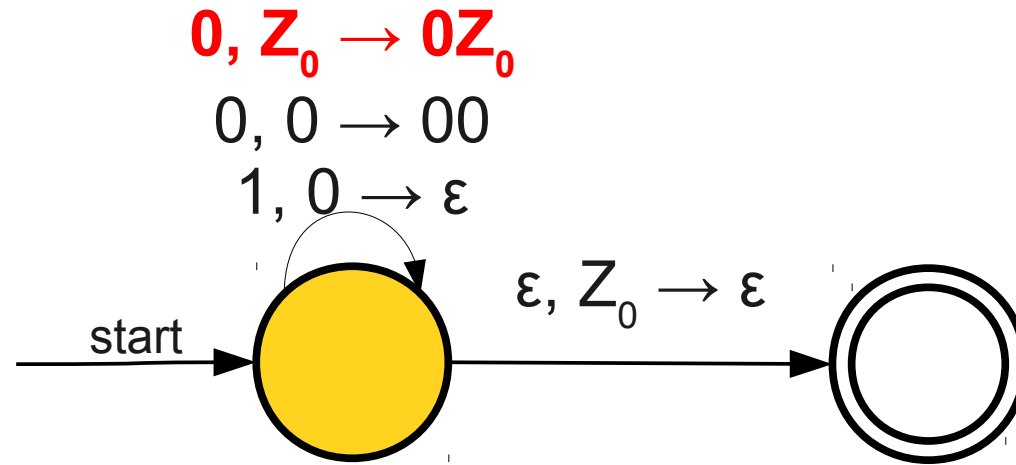
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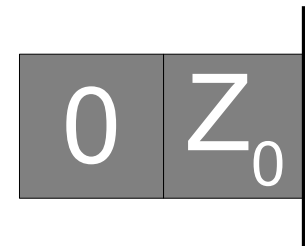
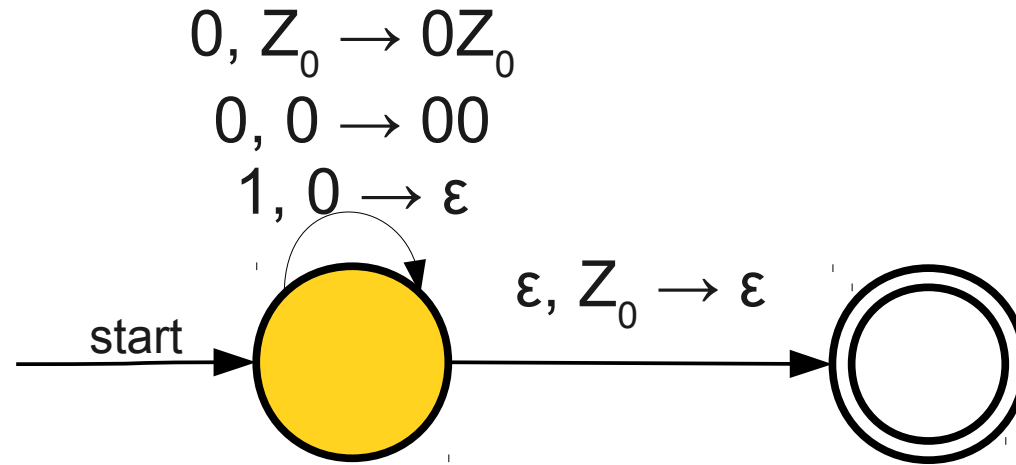
A Simple Pushdown Automaton



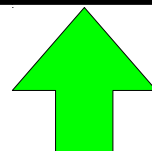
A Simple Pushdown Automaton



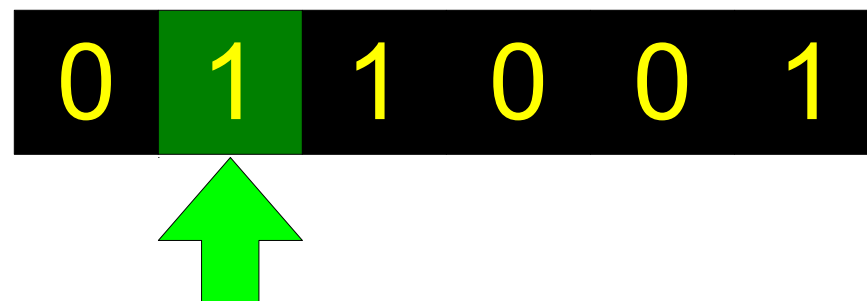
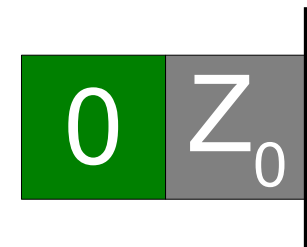
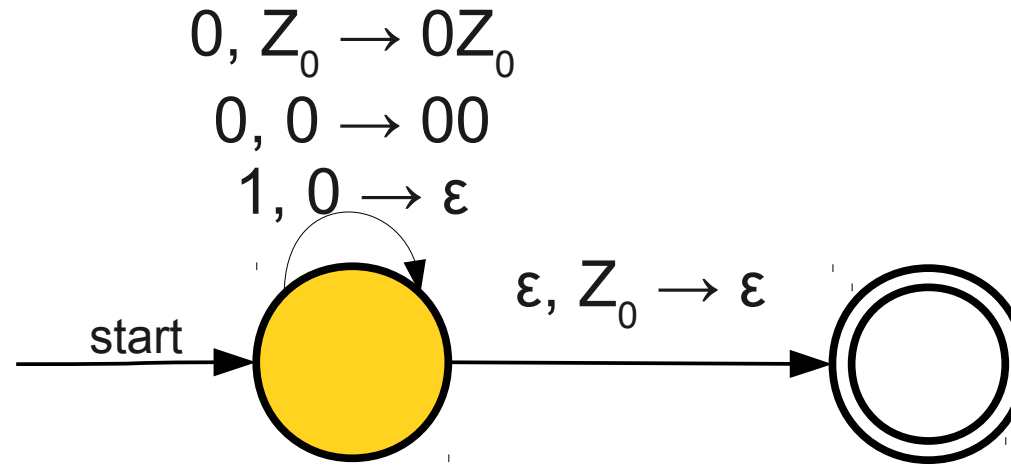
A Simple Pushdown Automaton



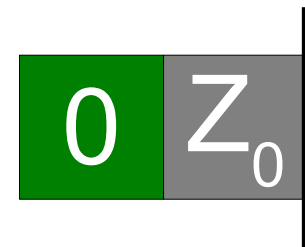
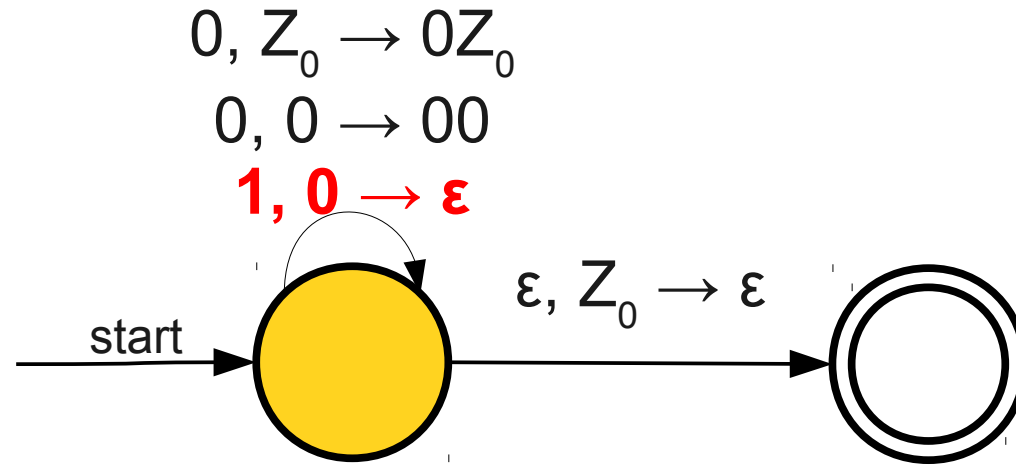
0 1 1 0 0 1



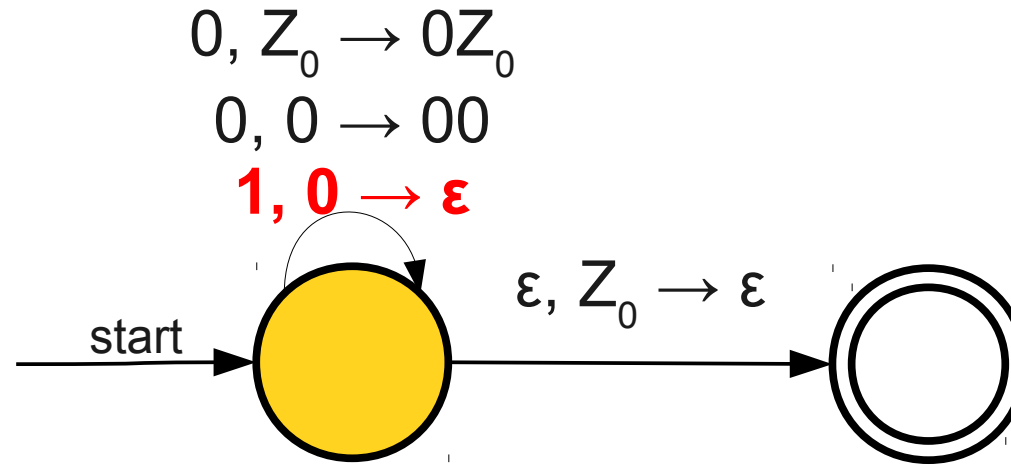
A Simple Pushdown Automaton



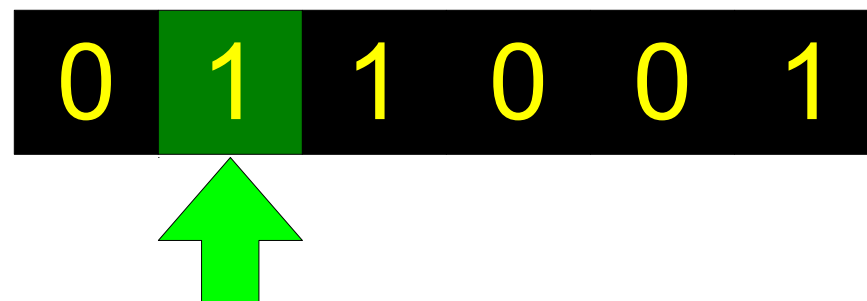
A Simple Pushdown Automaton



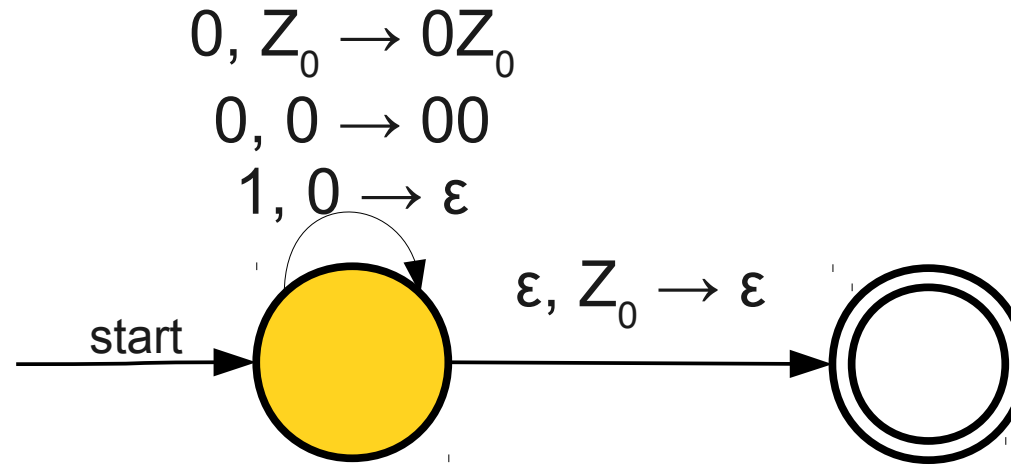
A Simple Pushdown Automaton



Z_0



A Simple Pushdown Automaton

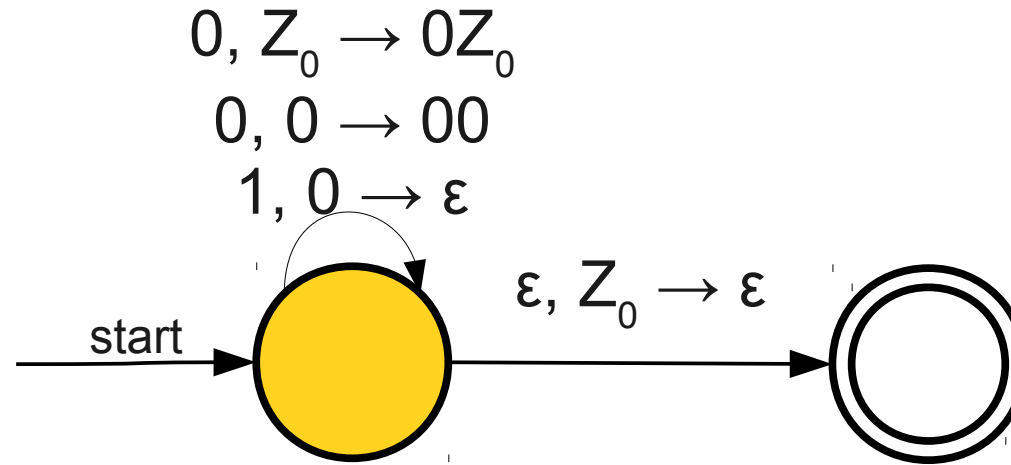


Z_0

0 1 1 0 0 1



A Simple Pushdown Automaton

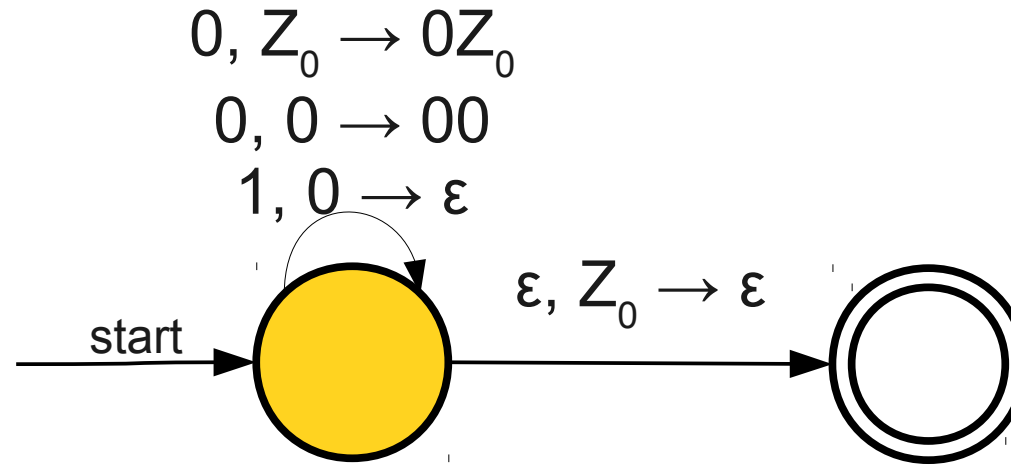


Z_0

0 1 1 0 0 1



A Simple Pushdown Automaton

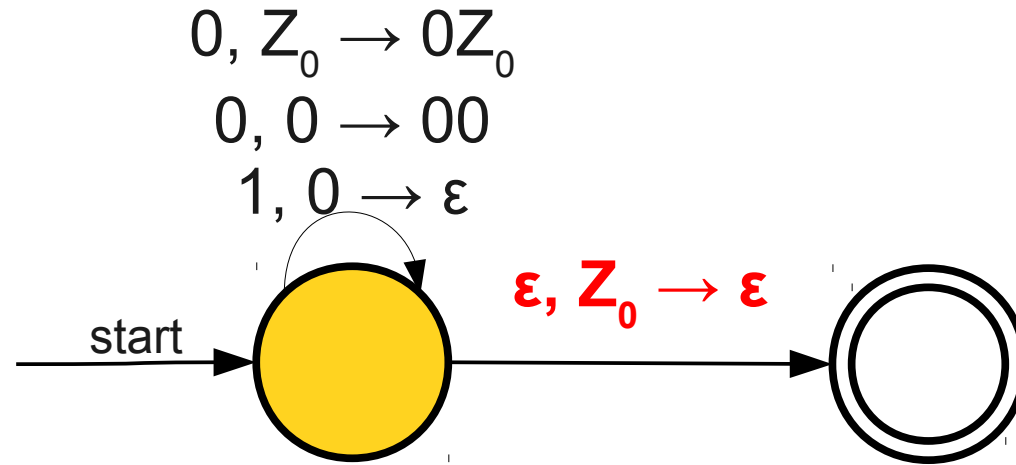


Z_0

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A Simple Pushdown Automaton

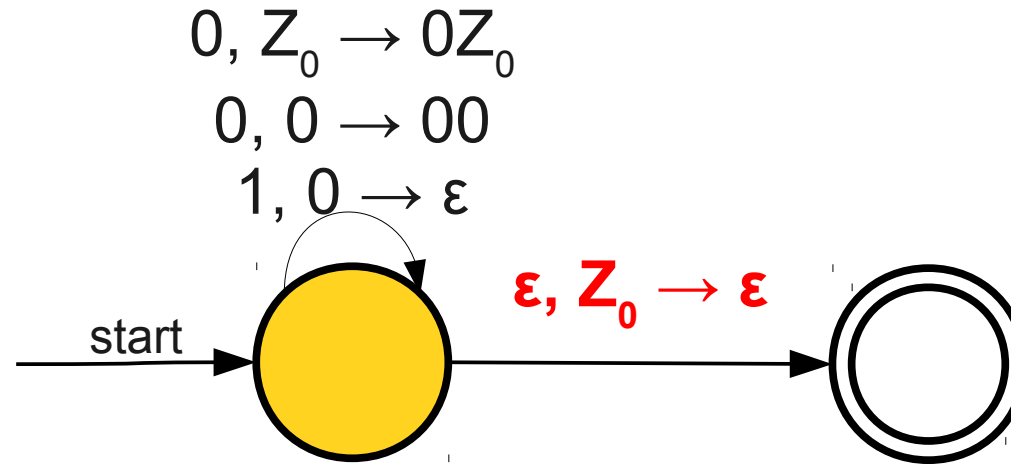


Z_0

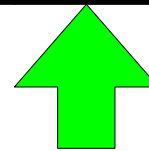
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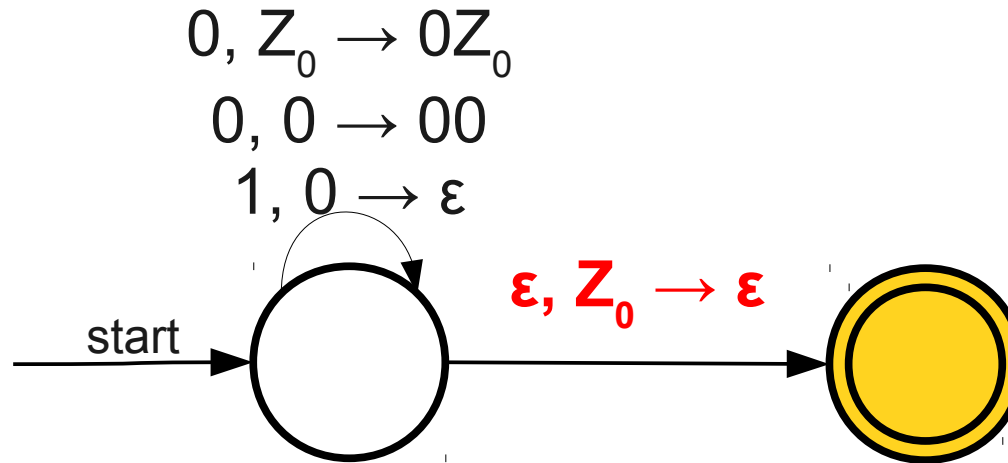
A Simple Pushdown Automaton



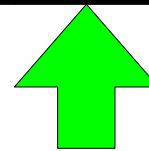
0 1 1 0 0 1



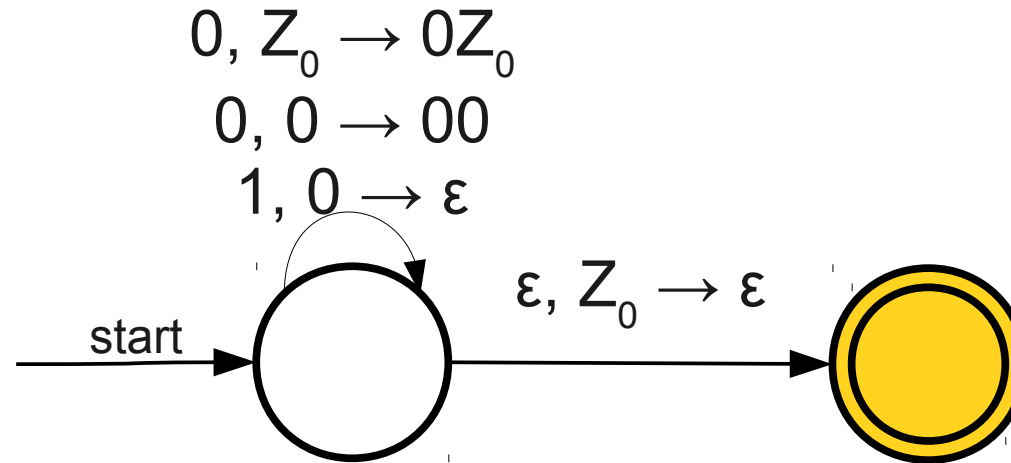
A Simple Pushdown Automaton



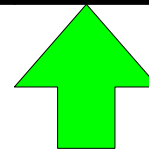
0 1 1 0 0 1



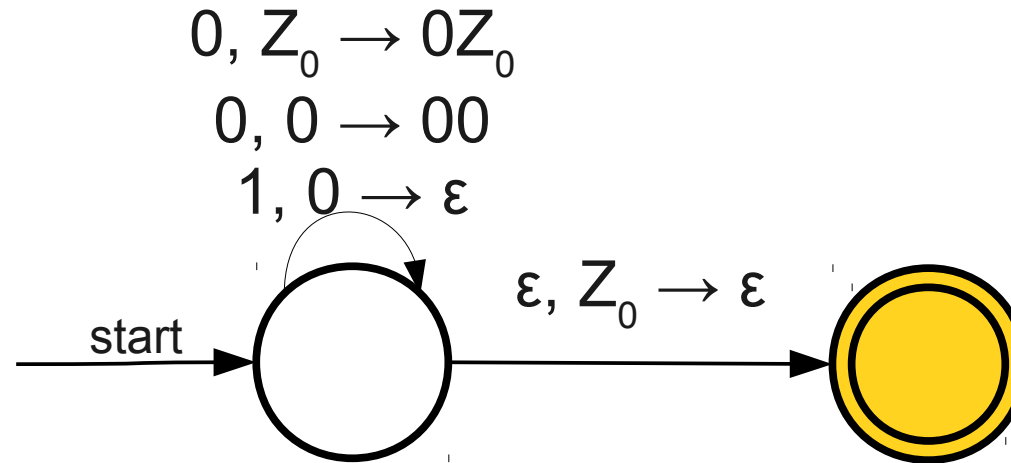
A Simple Pushdown Automaton



0 1 1 0 0 1



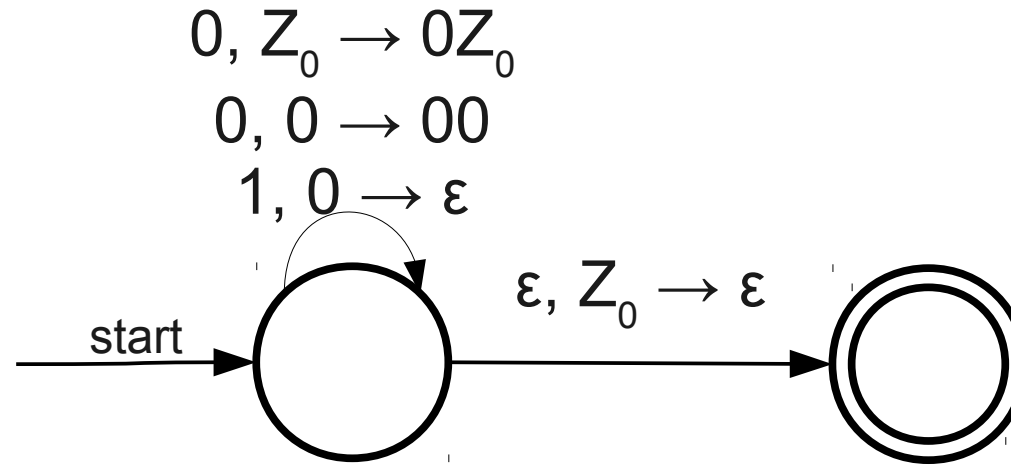
A Simple Pushdown Automaton



0 1 1 0 0 1



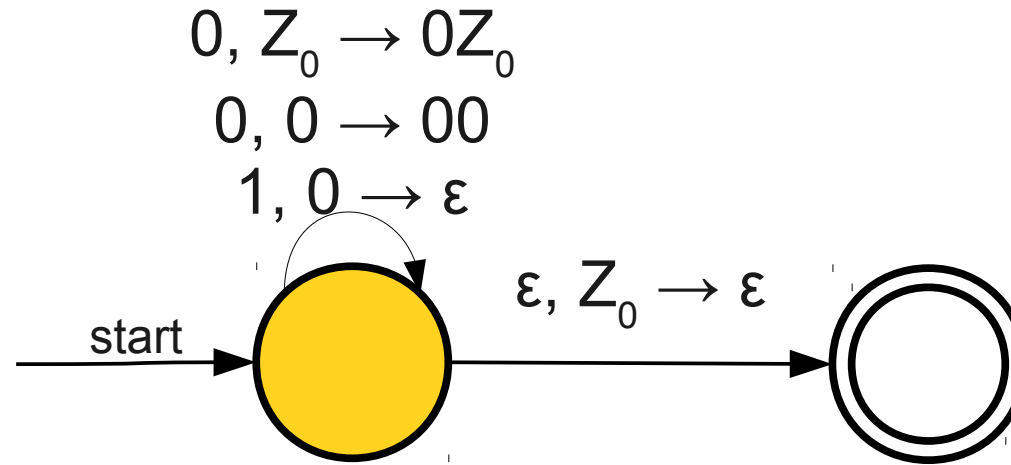
A Simple Pushdown Automaton



0 1 1 0 0 1



A Simple Pushdown Automaton

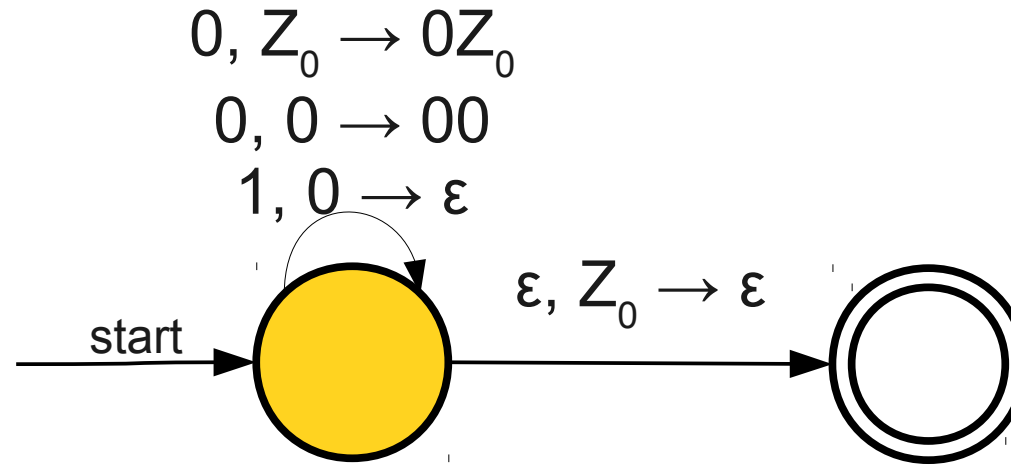


Z_0

0 1 1 0 0 1

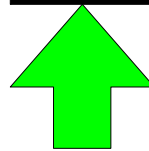


A Simple Pushdown Automaton

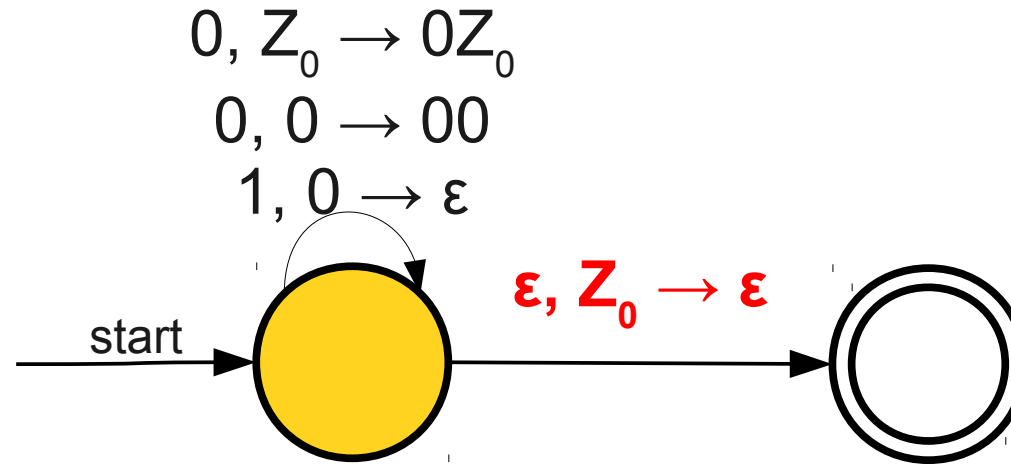


Z_0

0 1 1 0 0 1



A Simple Pushdown Automaton

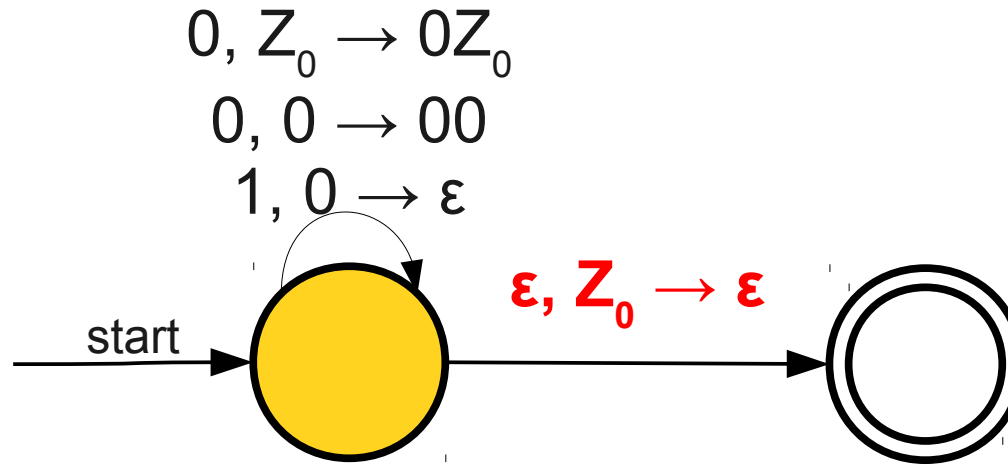


Z_0

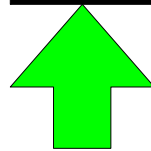
0 1 1 0 0 1



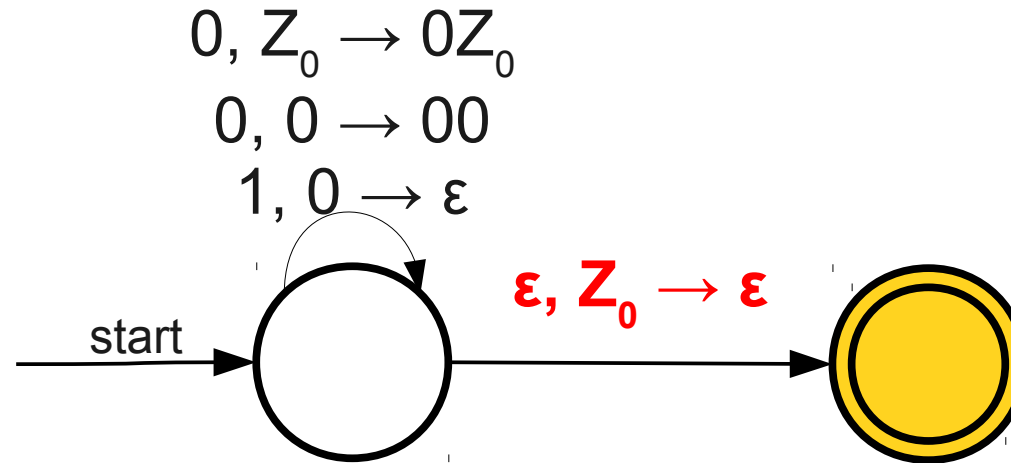
A Simple Pushdown Automaton



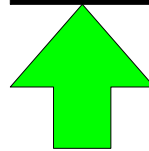
0 1 1 0 0 1



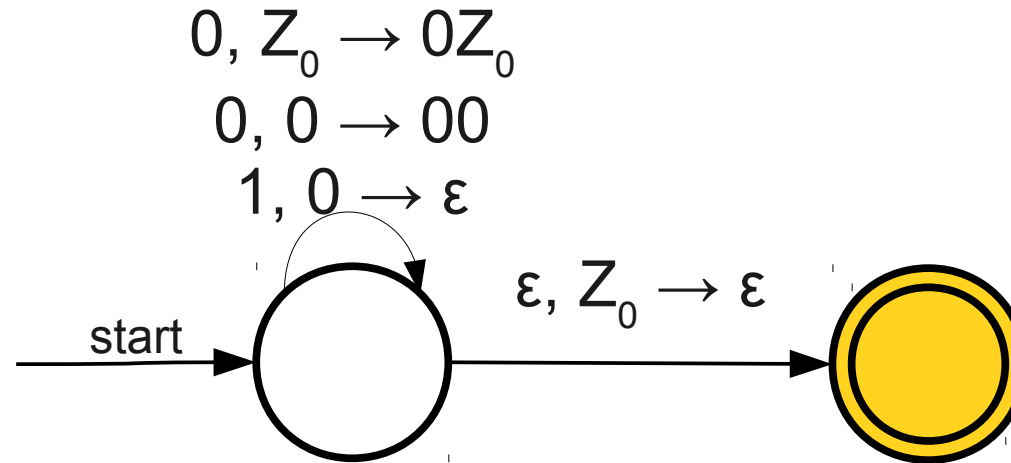
A Simple Pushdown Automaton



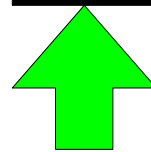
0 1 1 0 0 1



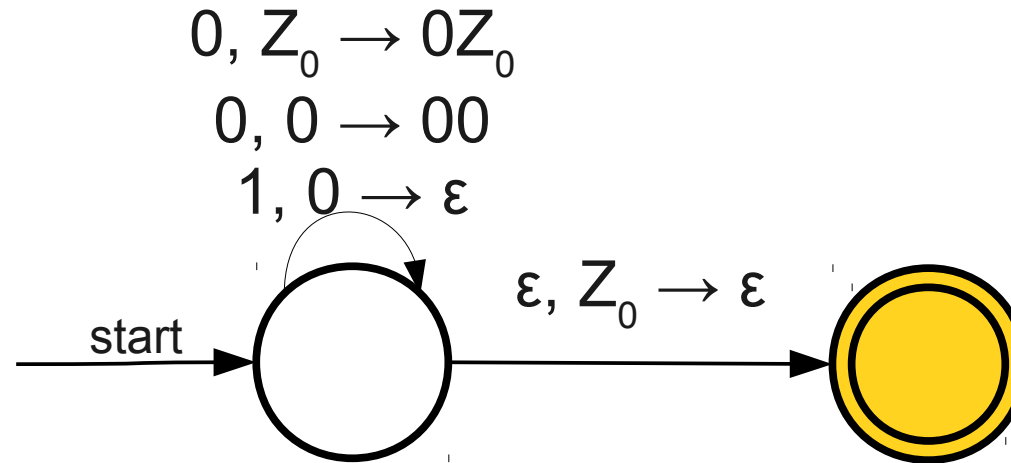
A Simple Pushdown Automaton



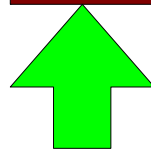
0 1 1 0 0 1



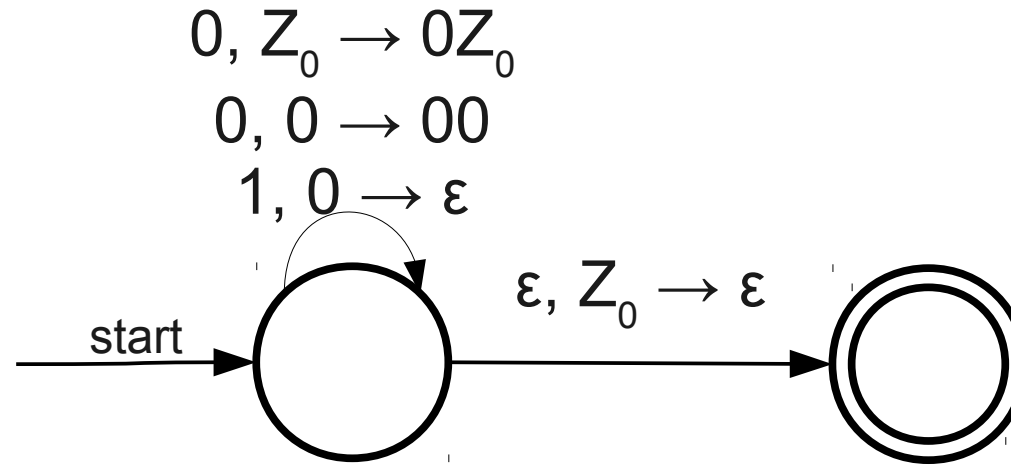
A Simple Pushdown Automaton



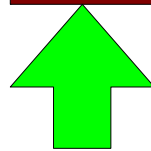
0 1 1 0 0 1



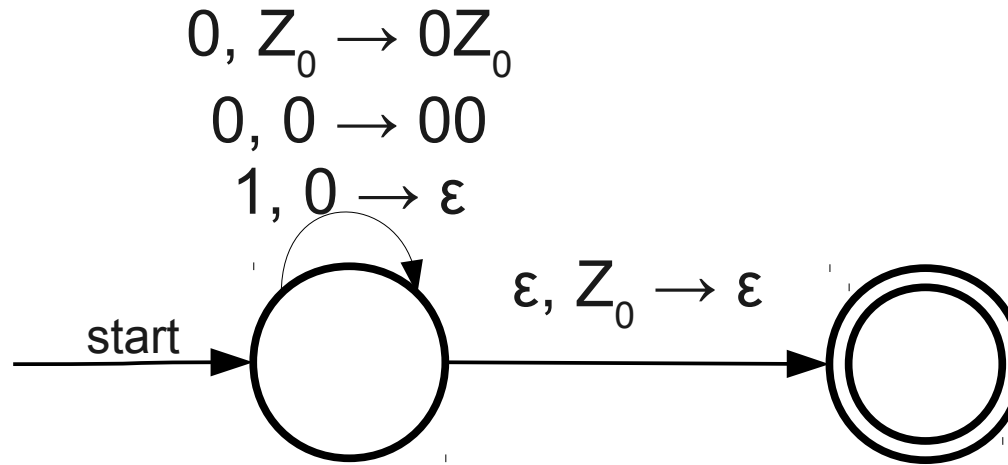
A Simple Pushdown Automaton



0 1 1 0 0 1

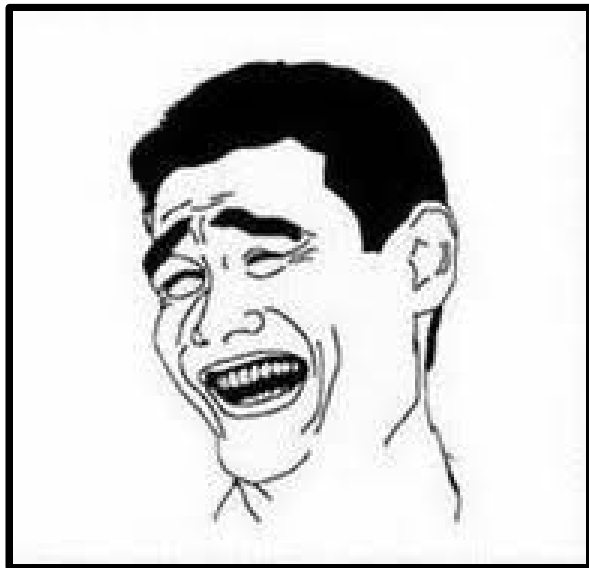
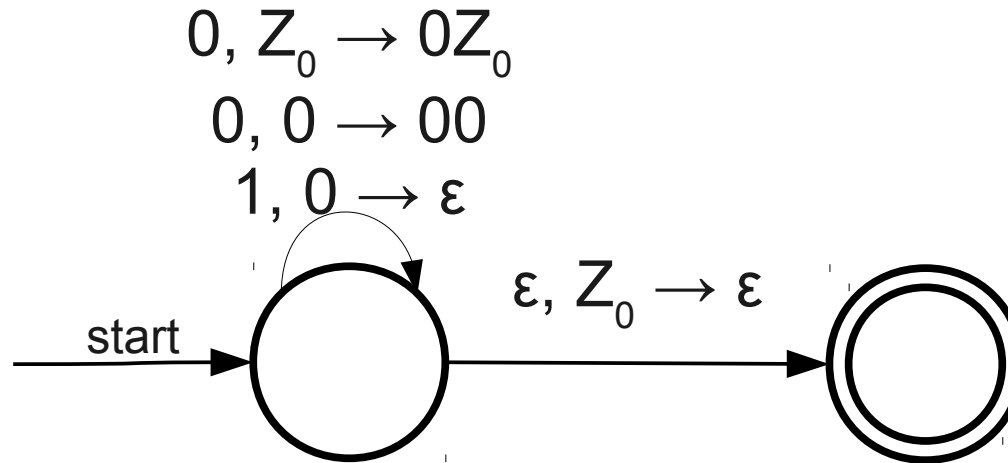


A Simple Pushdown Automaton



0 1 1 0 0 1

A Simple Pushdown Automaton



0 1 1 0 0 1

Exemplu de parser LL cu automat push-down

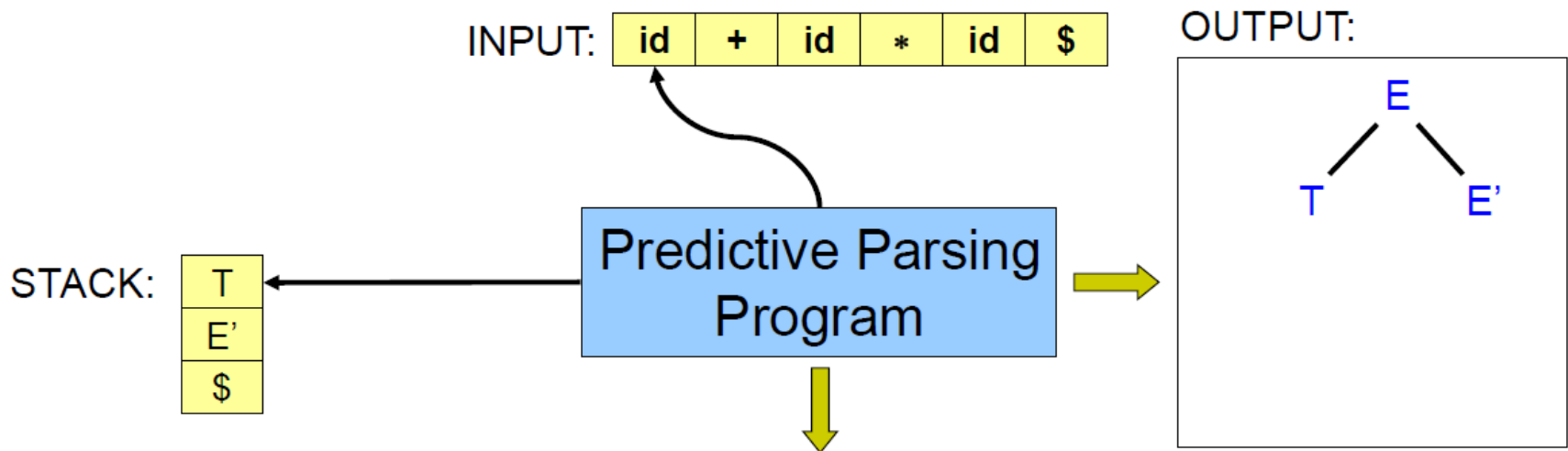
Gramatica:

$$\begin{aligned}
 E &\rightarrow T E' \\
 E' &\rightarrow + T E' \mid \epsilon \\
 T &\rightarrow F T' \\
 T' &\rightarrow * F T' \mid \epsilon \\
 F &\rightarrow (E) \mid \mathbf{id}
 \end{aligned}$$

Tabelul de parsare:

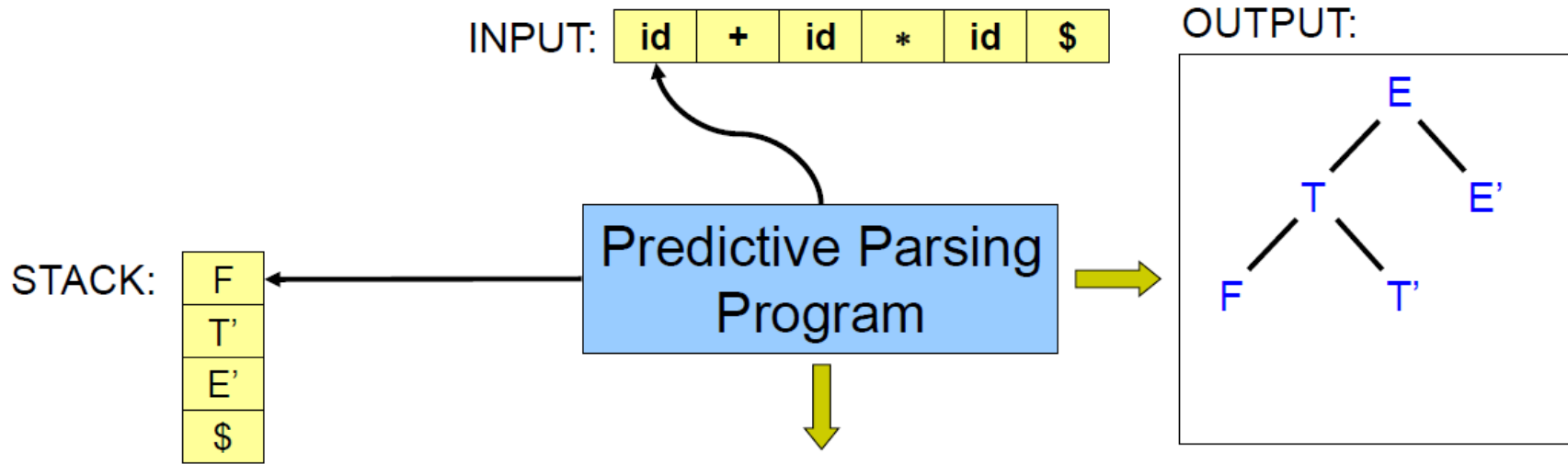
NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow T E'$			$E \rightarrow T E'$		
E'		$E' \rightarrow + T E'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow F T'$			$T \rightarrow F T'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow * F T'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \mathbf{id}$			$F \rightarrow (E)$		

Exemplu de parser LL cu automat push-down



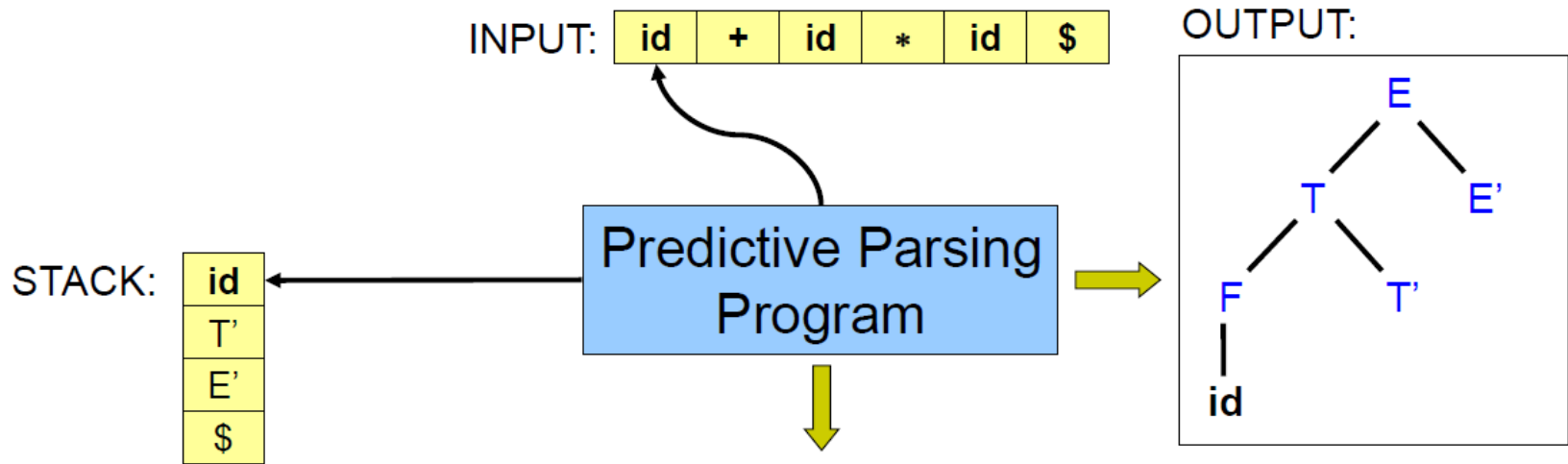
NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

Exemplu de parser LL cu automat push-down



NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
<i>E</i>	$E \rightarrow TE'$			$E \rightarrow TE'$		
<i>E'</i>		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
<i>T</i>	$T \rightarrow FT'$			$T \rightarrow FT'$		
<i>T'</i>		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
<i>F</i>	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

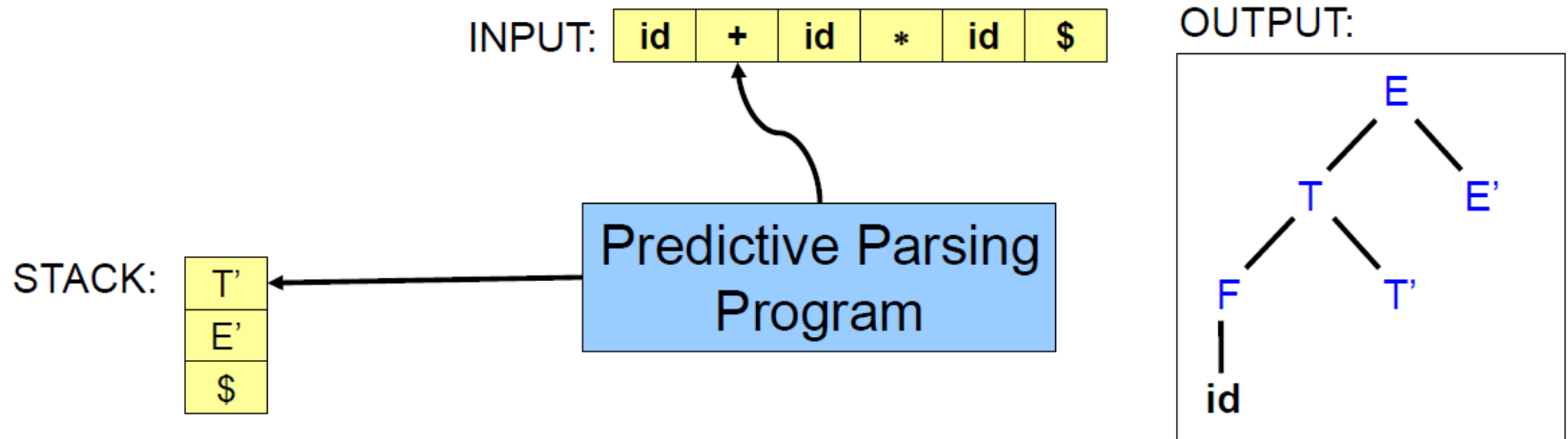
Exemplu de parser LL cu automat push-down



NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

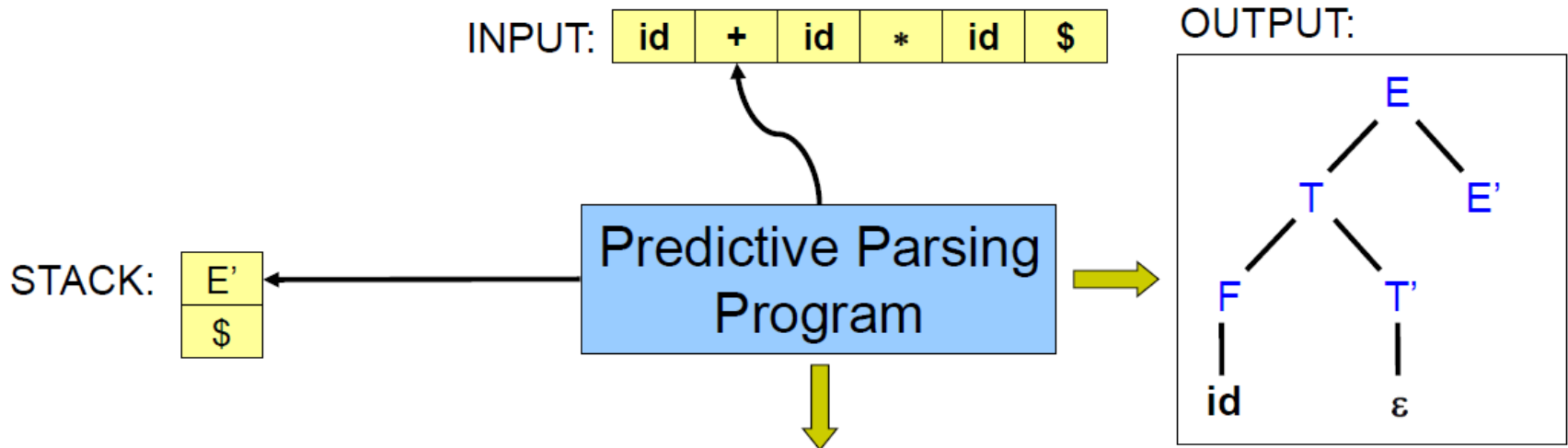
Exemplu de parser LL cu automat push-down

Actiunea cand $\text{Top}(\text{Stack}) = \text{input} \neq \$$: 'Pop' din stiva, avanseaza pe banda de intrare.



NON - TERMINAL	INPUT SYMBOL					
	id	$+$	$*$	$($	$)$	$\$$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

Exemplu de parser LL cu automat push-down



NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

Exemplu de parser LL cu automat push-down

Si tot asa, se construiesc urmatorul arbore de derivare:

$E' \rightarrow +TE'$

$T \rightarrow FT'$

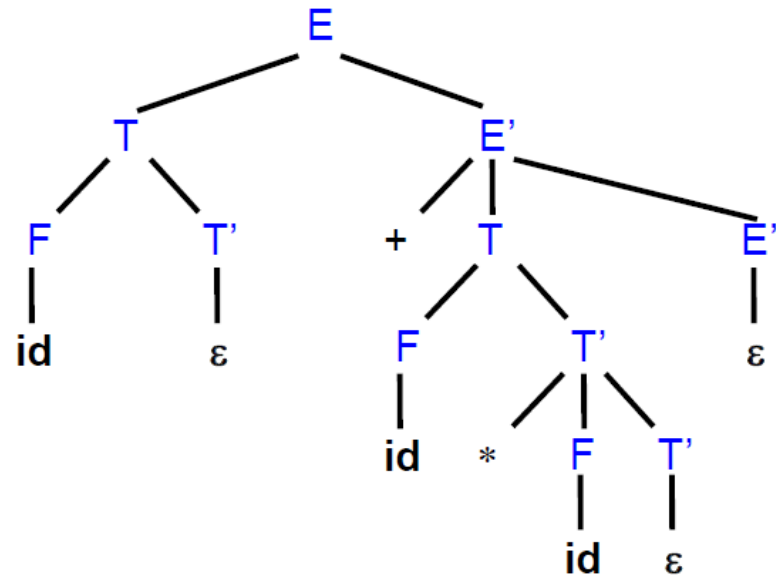
$F \rightarrow id$

$T' \rightarrow *FT'$

$F \rightarrow id$

$T' \rightarrow \varepsilon$

$E' \rightarrow \varepsilon$



Cand $\text{Top}(\text{Stack}) = \text{input} = \$$

Parserul se opreste si accepta intrarea.

(Aho, Sethi,
Ullman,
pp. 188)

Terminologie: LL vs LR

- LL(k)
 - Scaneaza intrarea "Left-to-right"
 - "Left-most derivation" – deriveaza mereu cel mai din stanga neterminal
 - k simboluri de lookahead
 - Face o traversare in pre-ordine a arborelui de parsare
- LR(k)
 - Scaneaza intrarea "Left-to-right"
 - "Right-most derivation" – 'deriveaza' cel mai din dreapta neterminal
 - k simboluri de lookahead
 - Face o traversare in post-ordine a arborelui de parsare

Parserul ascendent

Un parser ascendent, sau “parser shift-reduce”, incepe de la ‘frunze’ si construiește spre varf arborele de derivare

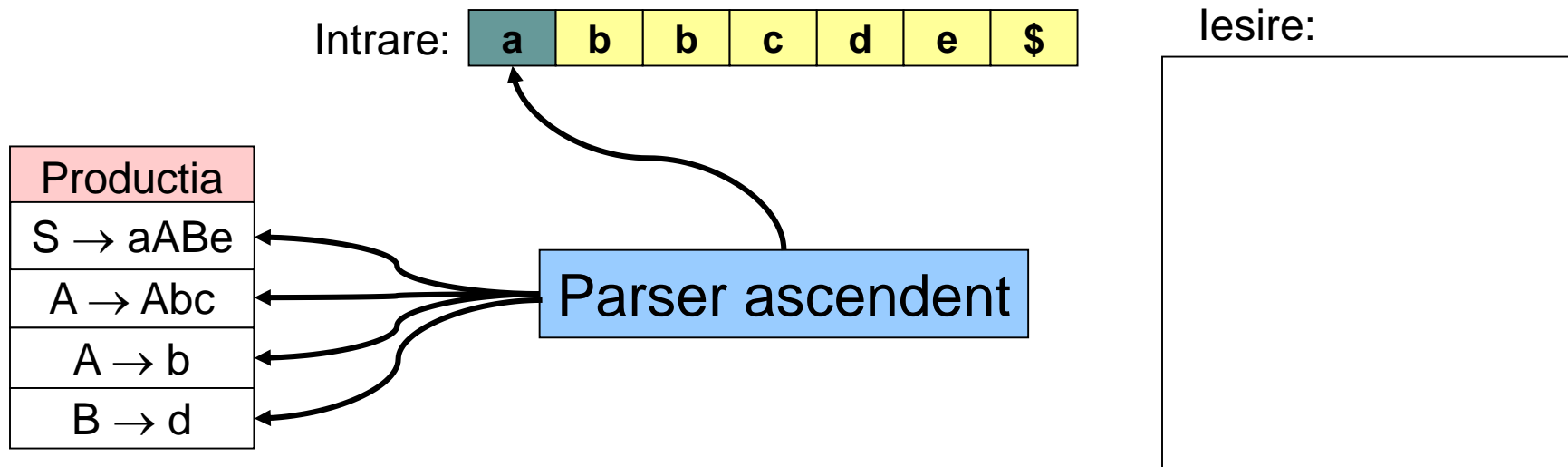
Pasii de reducere urmaresc o derivare dreapta in ordine inversa

Sa consideram GRAMATICA:

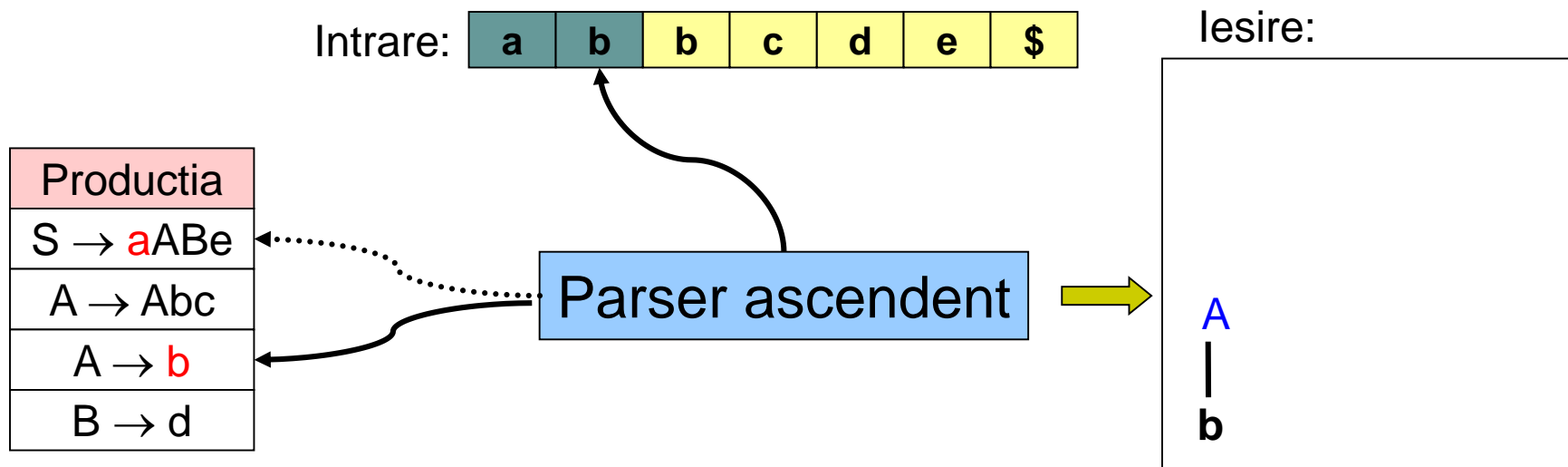
$S \rightarrow aABe$
$A \rightarrow Abc \mid b$
$B \rightarrow d$

Vrem sa parsam sirul de Intrare **abbcd**e.

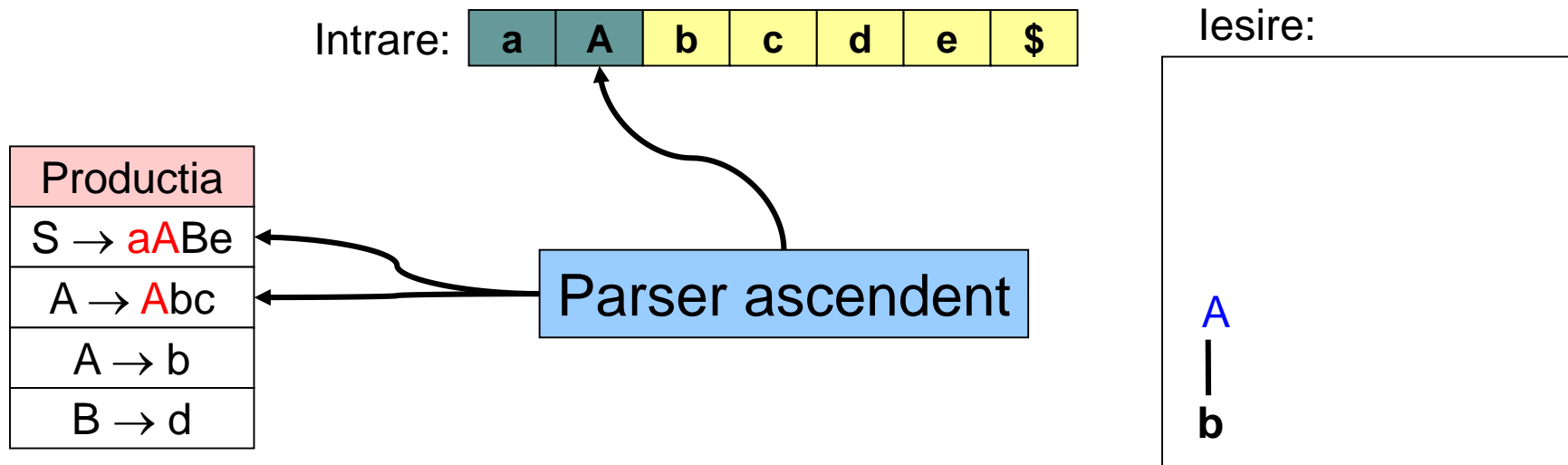
Exemplu de parser ascendent



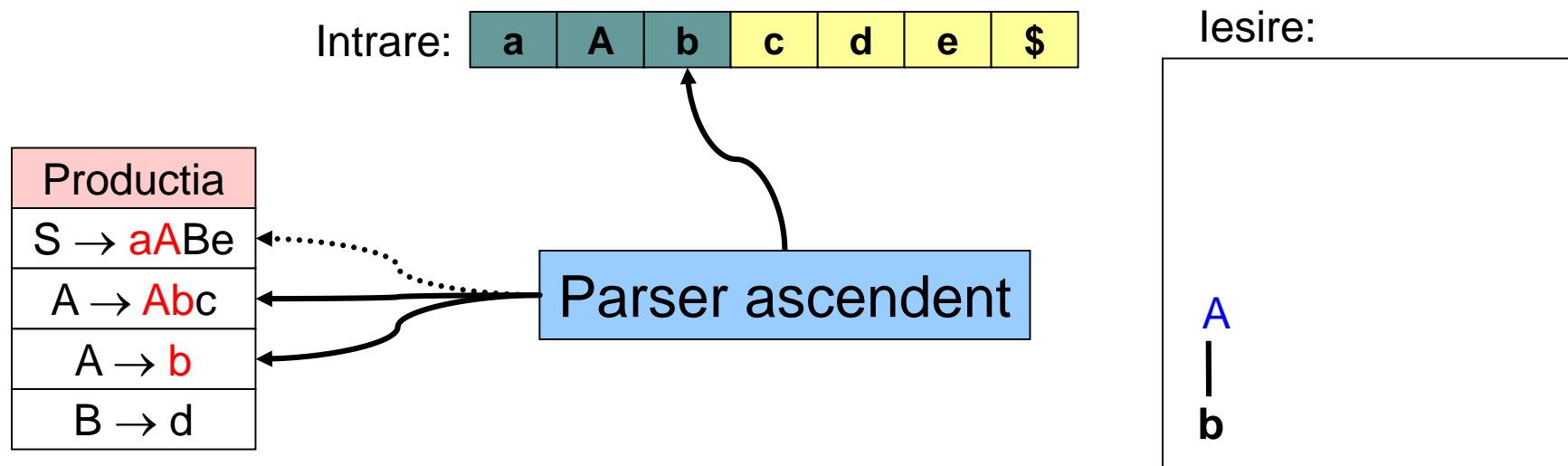
Exemplu de parser ascendent



Exemplu de parser ascendent

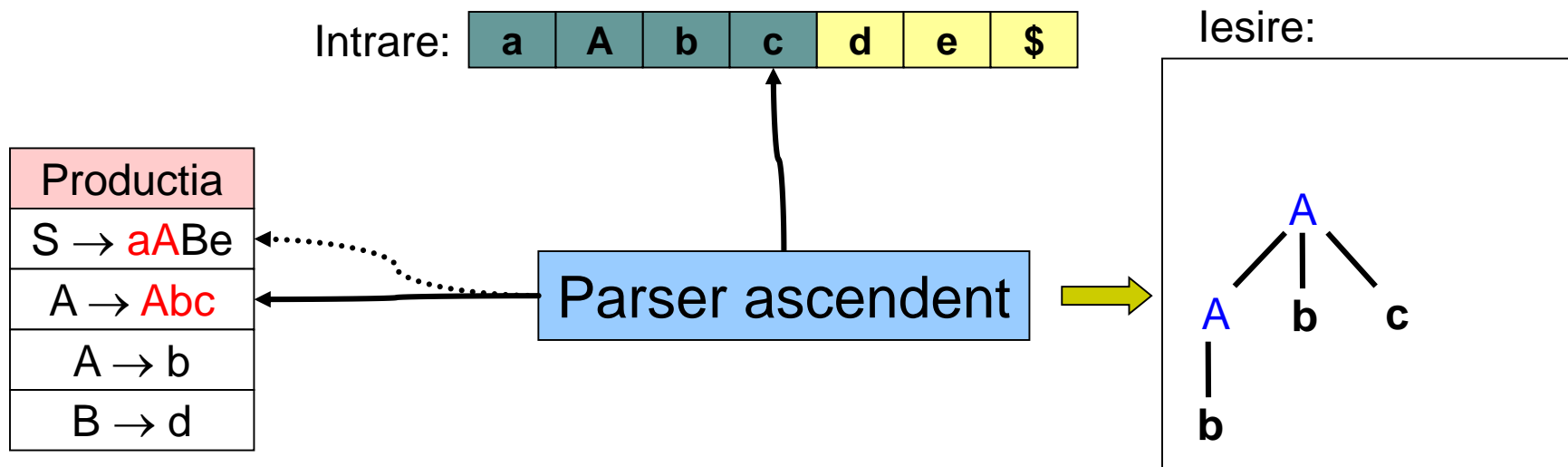


Exemplu de parser ascendent

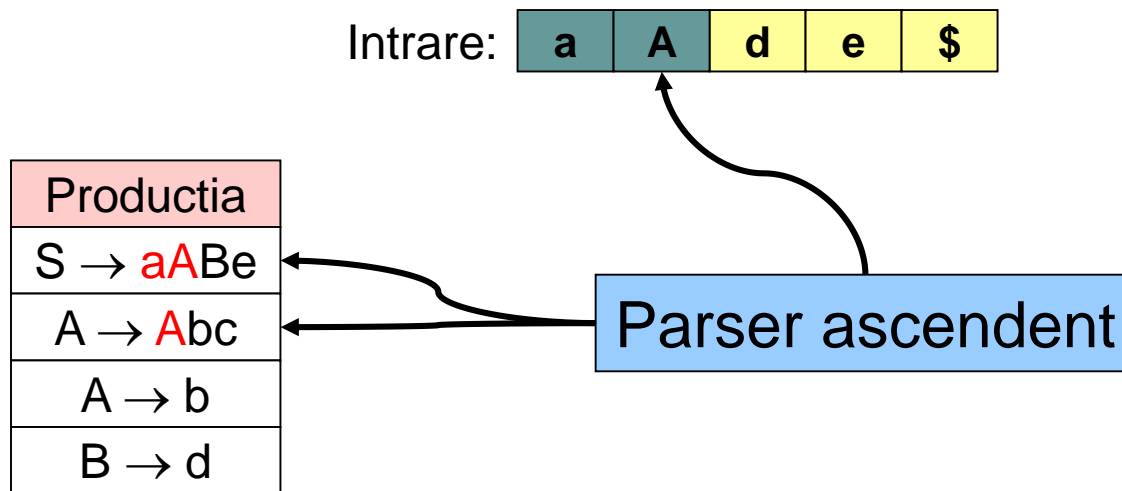


Nu reducem in acest exemplu. Un parser ar reduce, s-ar impotmoli si ar trebui sa faca backtracking!

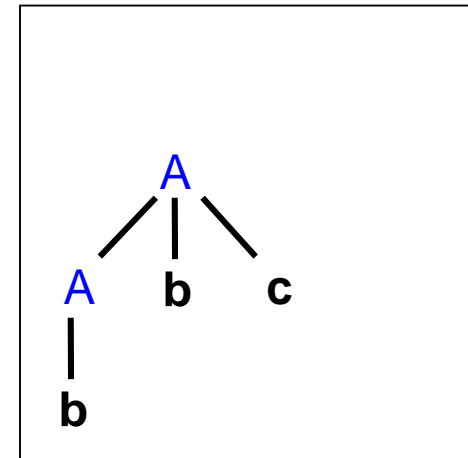
Exemplu de parser ascendent



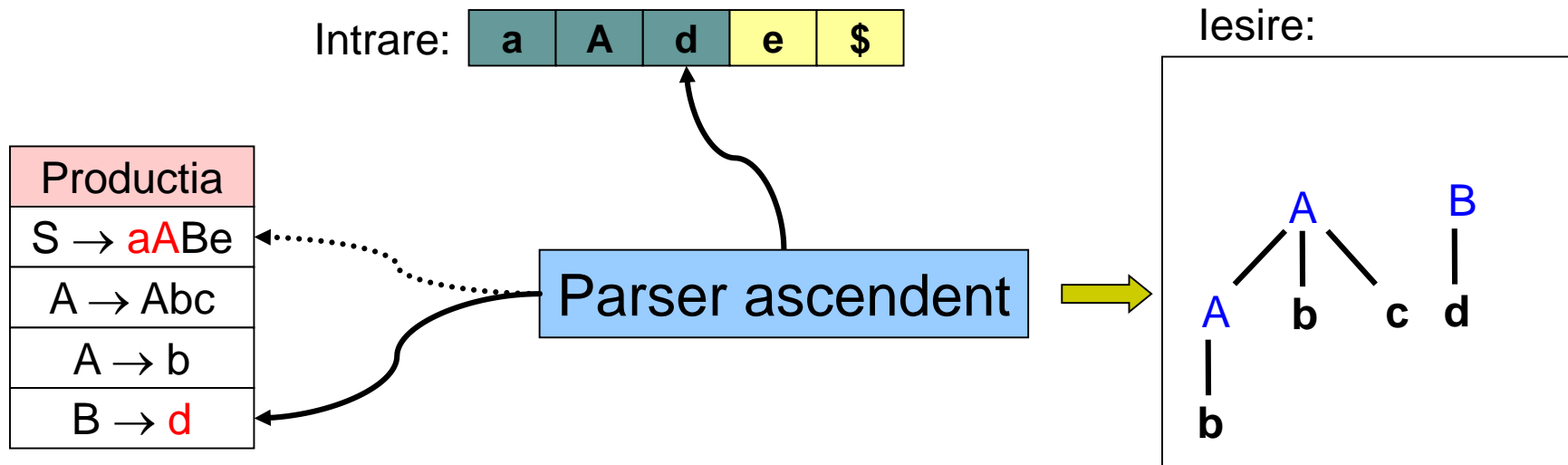
Exemplu de parser ascendent



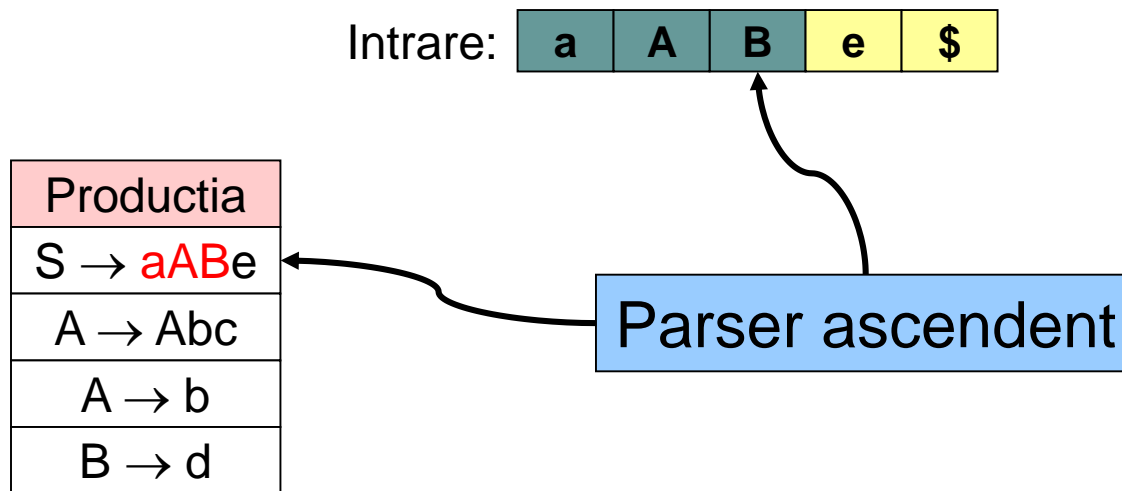
lesire:



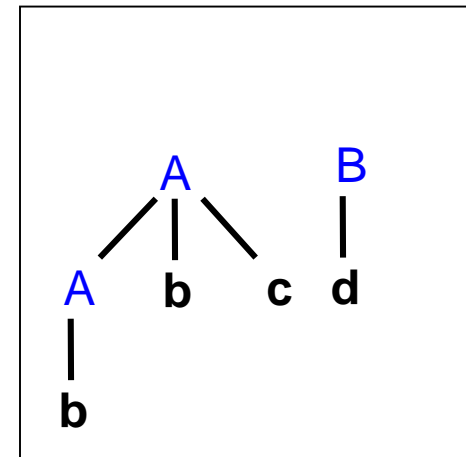
Exemplu de parser ascendent



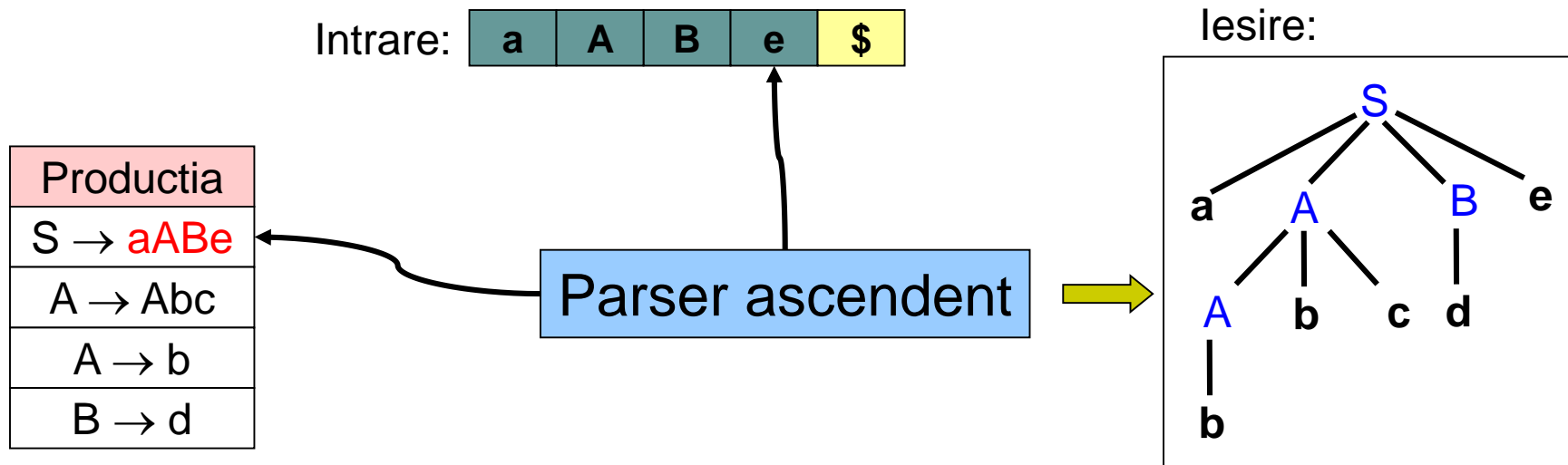
Exemplu de parser ascendent



lesire:

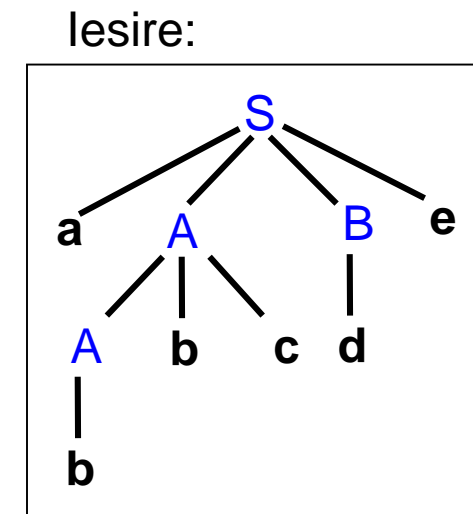
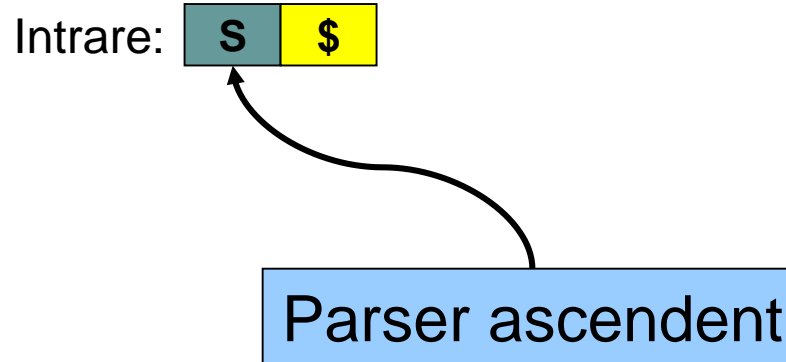


Exemplu de parser ascendent



Exemplu de parser ascendent

Productia
$S \rightarrow aABe$
$A \rightarrow Abc$
$A \rightarrow b$
$B \rightarrow d$



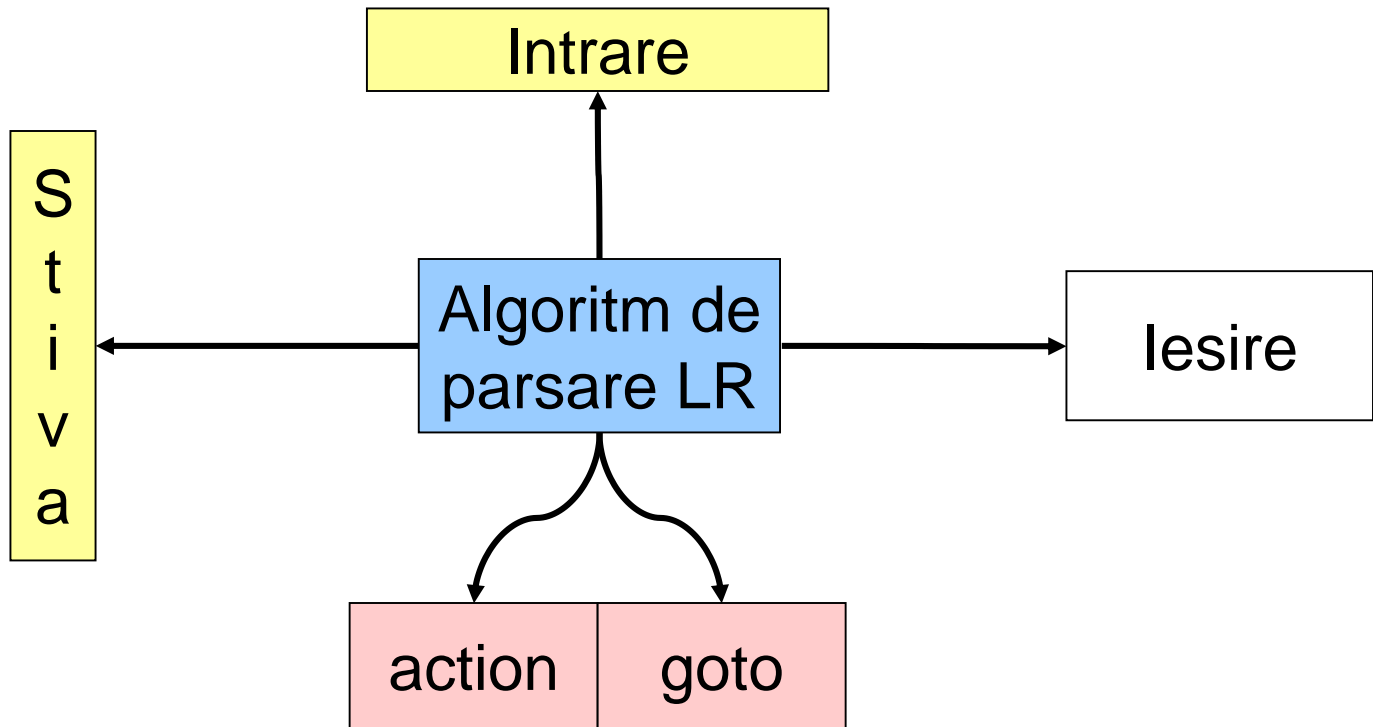
Acest parser este cunoscut ca **Parser LR** fiindca scaneaza Intrarea “**Left to right**”, si construieste “**Rightmost derivation**” in ordine inversa.

Exemplu de parser ascendent

Scanarea Productiilor pentru a detecta potrivirea cu subsiruri din Intrare, si backtrackingul face metoda din exemplul precedent foarte ineficienta.

Se poate mai bine?

Exemplu de parser LR



Exemplu de parser LR

Urmatoarea GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Poate fi parsata cu urmatoarele
tabele 'action' si 'goto'

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	+	id	*	id	\$
----	---	----	---	----	----

Iesire:

Stiva:

0

LR Parsing Program



State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare: id * id + id \$

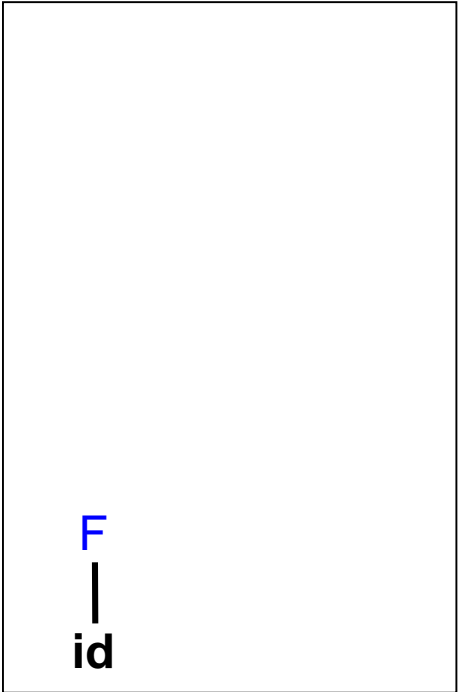
Iesire:

Stiva:

5
id
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



GRAMATICA:

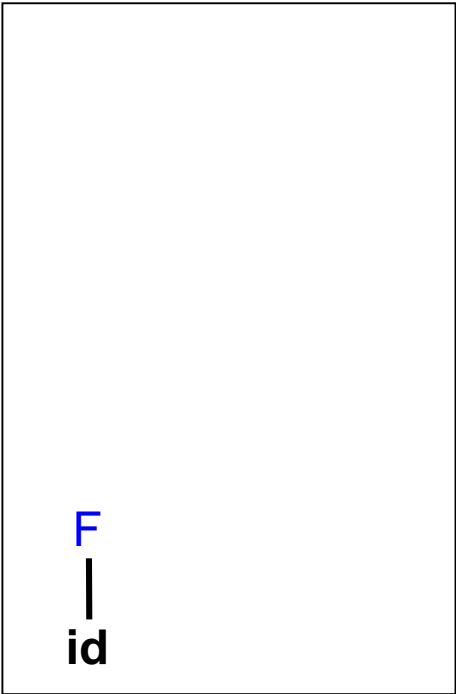
- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

Iesire:



Stiva:

0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare: id * id + id \$

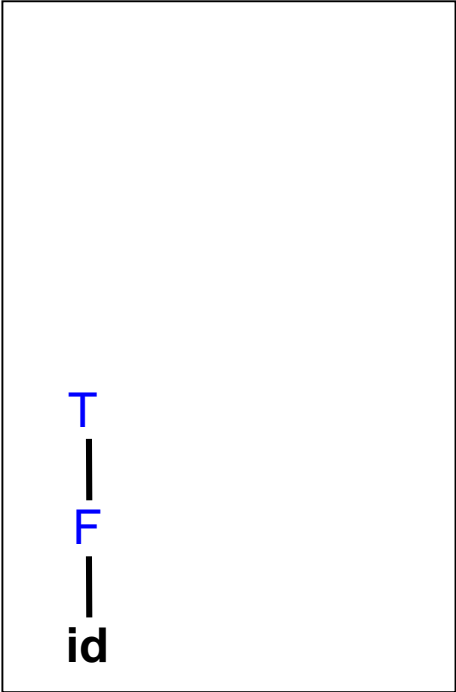
Iesire:

Stiva:

3
F
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

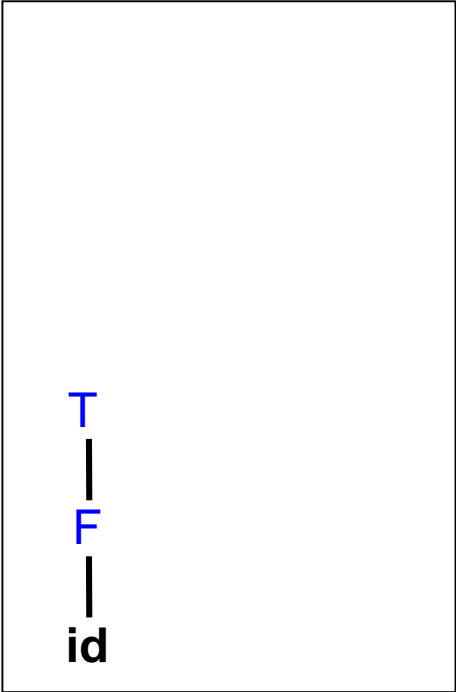
id	*	id	+	id	\$
----	---	----	---	----	----

Stiva:

0

LR Parsing Program

Iesire:



State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

lesire:

Stiva:

2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

T
|
F
|
id

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

Iesire:

Stiva:

7
*
2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

T
|
F
|
id

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow \mathbf{id}$

Exemple de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

lesire:

Stiva:

5
id
7
*
2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

T
|
F
|
id

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow \mathbf{id}$

Exemple de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

lesire:

Stiva:

7
*
2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

T
|
F
|
id

(Aho,Sethi,Ullman, pp. 220)

GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

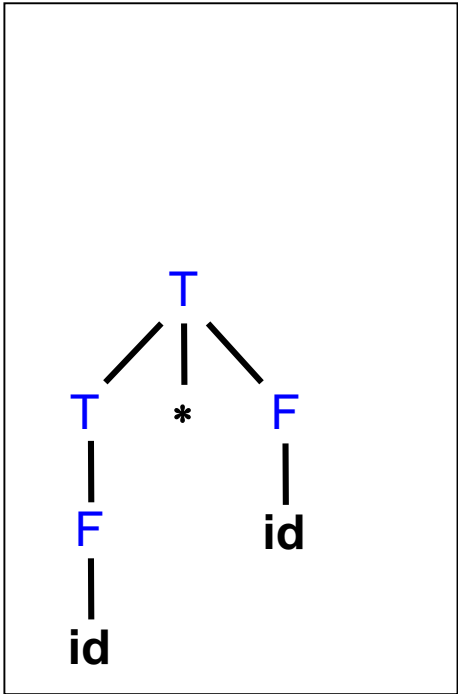
Stiva:

10
F
7
*
2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

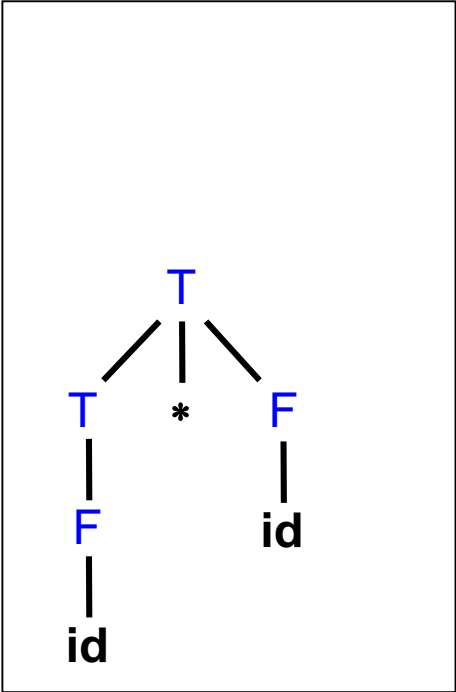
Stiva:

0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

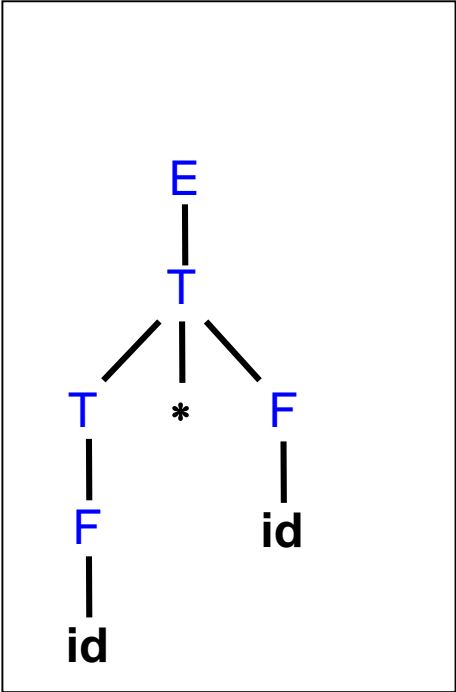
Stiva:

2
T
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

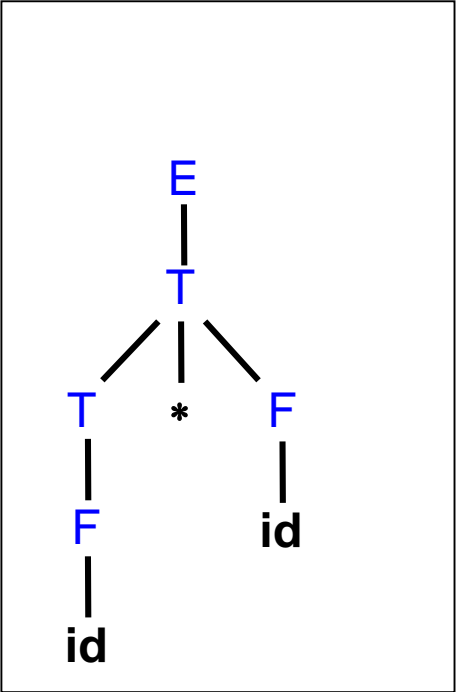
Iesire:

Stiva:

0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

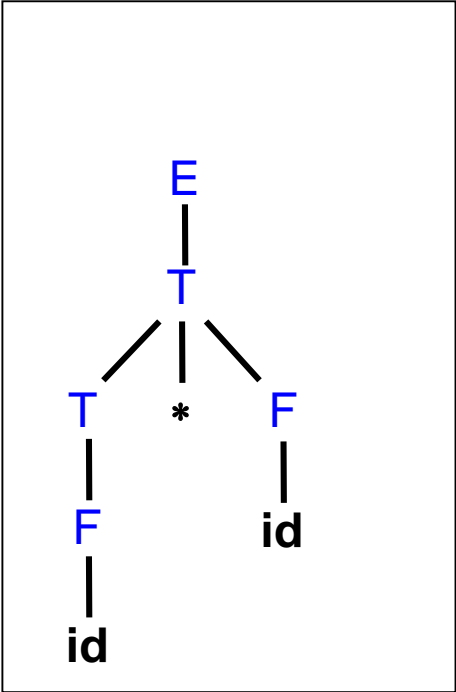
Stiva:

1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

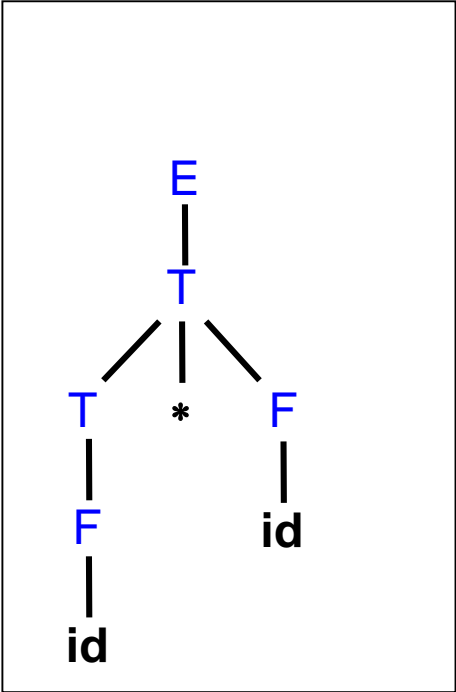
Stiva:

6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

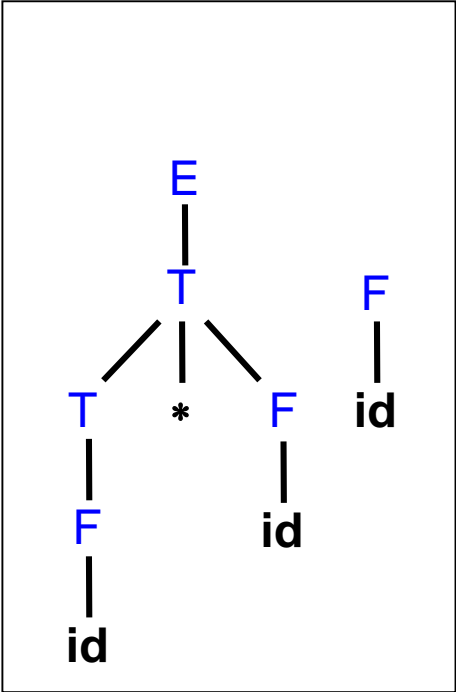
Iesire:

Stiva:

5
id
6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

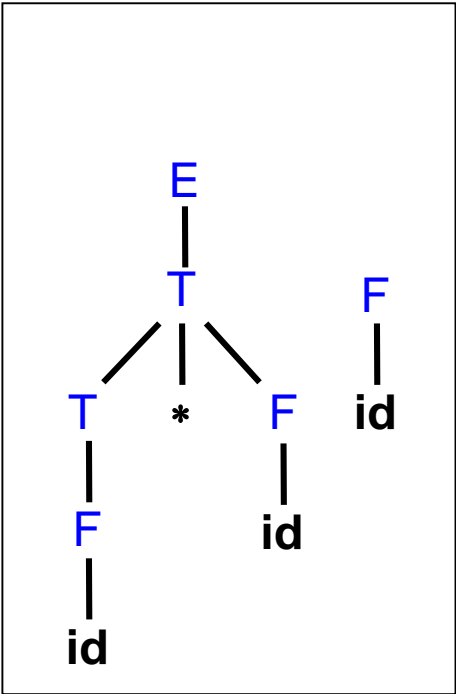
Iesire:

Stiva:

6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow \mathbf{id}$

Exemple de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

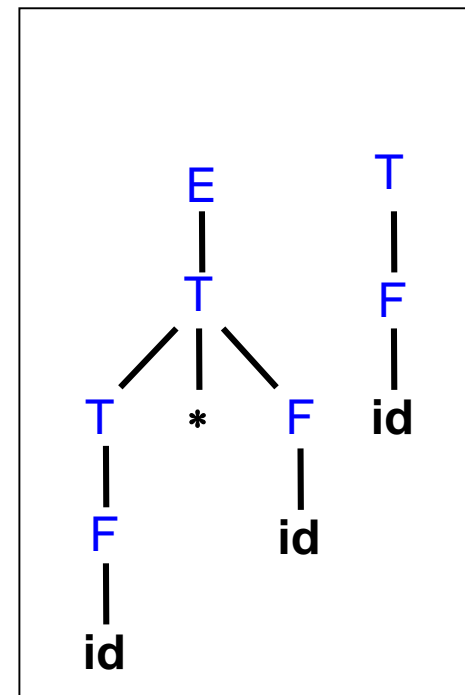
Stiva:

3
F
6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

lesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

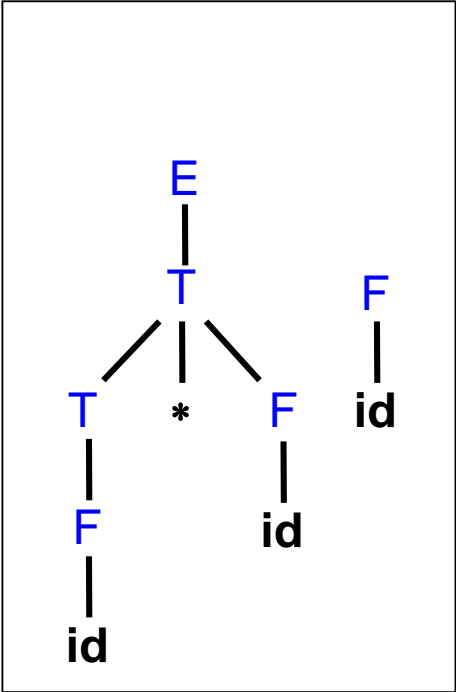
Stiva:

6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

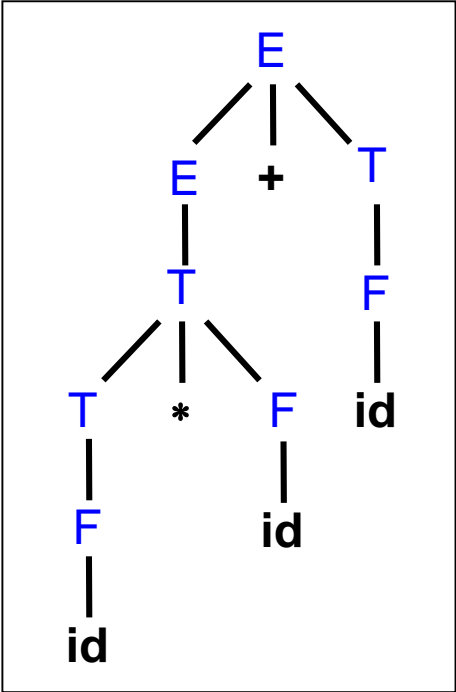
Stiva:

9
T
6
+
1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

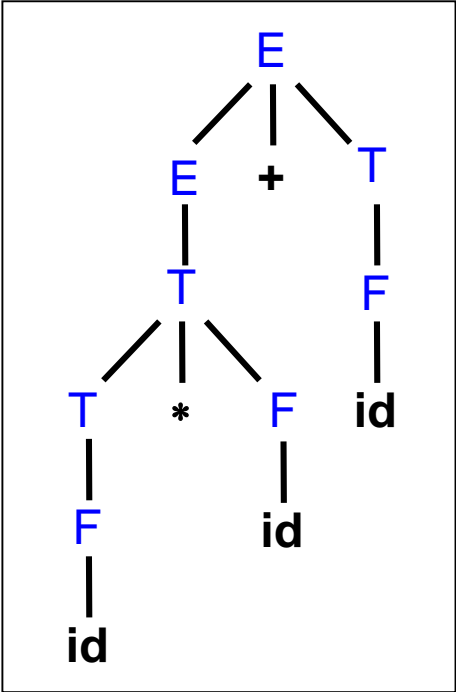
Stiva:

0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



GRAMATICA:

- (1) $E \rightarrow E + T$
- (2) $E' \rightarrow T$
- (3) $T \rightarrow T * F$
- (4) $T \rightarrow F$
- (5) $F \rightarrow (E)$
- (6) $F \rightarrow id$

Exemplu de parser LR

Intrare:

id	*	id	+	id	\$
----	---	----	---	----	----

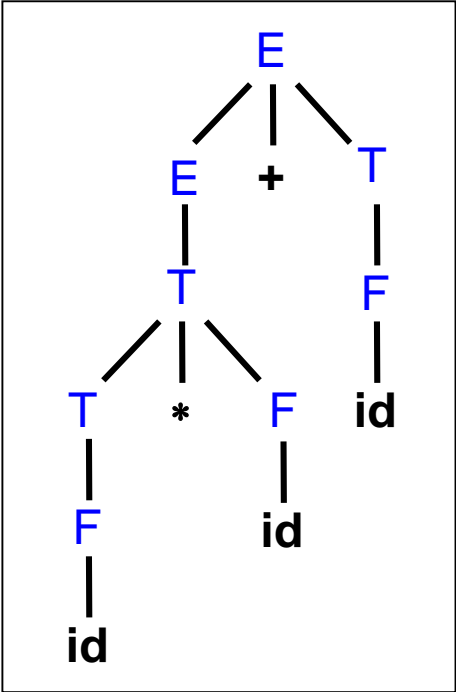
Stiva:

1
E
0

LR Parsing Program

State	action						goto		
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Iesire:



Construirea tabelelor de parsare

Toate parserele LR folosesc acelasi algoritm pe care l-am aratat in slide-urile precedente.

Diferentierea intre ele se face prin tabelele action si goto

Simple LR (SLR): merge pe cele mai putine GRAMATICI, dar e cel mai usor de implementat (AhoSethiUllman pp. 221-230).

Canonical LR: merge pe cele mai multe GRAMATICI, dar e cel mai greu de implementat. Imparte starile cand e necesar pentru a preveni reduceri care ar bloca parserul. (AhoSethiUllman pp. 230-236).

Lookahead LR (LALR): merge pe majoritatea constructiilor sintactice folosite in limbajele de programare, dar produce tabele mult mai mici decat Canonical LR.

(AhoSethiUllman pp. 236-247).

Analiza sintactica Shift-Reduce

- Actiunile analizorului : o secventa de operatii **shift** si **reduce**
- Starea analizorului : O stiva de terminali si neterminali, si o stiva de stari
- Pasul curent in analiza e dat atat de stiva cat si de banda de intrare

Actiuni Shift-Reduce

- Parsarea e o secventa de actiuni shift si reduce
- Shift: muta token-ul de look-ahead pe stiva

stiva	intrare	actiune
(1+2+(3+4))+5	shift 1
(1	+2+(3+4))+5	

- Reduce: Inlocuieste simbolurile β din varful stivei cu simbolul neterminal X din partea stanga a productiei $X \rightarrow \beta$ (adica: pop β , push X)

stiva	intrare	actiune
(<u>S+E</u>	+(3+4))+5	reduce $S \rightarrow S + E$
(S	+(3+4))+5	

Analiza Shift-Reduce

$$\begin{array}{l} S \rightarrow S + E \mid E \\ E \rightarrow \text{num} \mid (S) \end{array}$$

derivarea

(1+2+(3+4))+5
 (1+2+(3+4))+5
 (1+2+(3+4))+5
 (E+2+(3+4))+5
 (S+2+(3+4))+5
 (S+2+(3+4))+5
 (S+2+(3+4))+5
 (S+E+(3+4))+5
 (S+(3+4))+5
 (S+(3+4))+5
 (S+(3+4))+5
 (S+(3+4))+5

...

stiva

(
 (1
 (E
 (S
 (S+
 (S+2
 (S+E
 (S
 (S+
 (S+(
 (S+(3

sir de intrare

(1+2+(3+4))+5
 1+2+(3+4))+5
 +2+(3+4))+5
 +2+(3+4))+5
 +2+(3+4))+5
 2+(3+4))+5
 +(3+4))+5
 +(3+4))+5
 +(3+4))+5
 (3+4))+5
 3+4))+5
 +4))+5

actiune

shift
 shift
 reduce $E \rightarrow \text{num}$
 reduce $S \rightarrow E$
 shift
 shift
 reduce $E \rightarrow \text{num}$
 reduce $S \rightarrow S+E$
 shift
 shift
 shift
 reduce $E \rightarrow \text{num}$

Probleme (selectarea actiunii)

- De unde stim ce actiune sa aplicam: shift sau reduce? Si cu ce regula sa reducem?
 - Uneori putem reduce dar nu e bine sa o facem – am ajunge cu analiza intr-un punct mort (sau nu am respecta precedenta operatorilor)
 - Uneori putem reduce stiva in mai multe feluri, nu intr-un singur fel

Selectarea actiunii

- Starea curenta:
 - stiva β
 - simbolul look-ahead b
 - exista productia $X \rightarrow \gamma$, si stiva e de forma $\beta = \alpha\gamma$
- Ar trebui analizorul sa:
 - Shifteze b pe stiva, transformand-o in βb ?
 - Reduca aplicand productia $X \rightarrow \gamma$, presupunand ca stiva e de forma $\beta = \alpha\gamma$ - si sa o transforme astfel in αX ?
- Decizie in functie de b și de prefixul α
 - α e diferit pentru productii diferite, deoarece partea dreapta a productiilor(γ -urile) poate avea lungimi diferite

Algoritmul de parsare LR

- Mecanismul de baza
 - Folosim un set de stari ale parser-ului
 - Folosim o stiva de stari (eventual, alternam simboluri cu stari)
 - De ex., 1 (6 S 10 + 5 (verde = stari)
 - Folosim tabela de parsare pentru:
 - A determina ce actiune se aplica (shift/reduce)
 - A determina starea urmatoare
- Actiunile analizatorului pot fi determinate cu exactitate din tabellele de parsare

Tabela de parsare LR

	Terminali	Non-terminali
Stare	Actiunea si starea urmatoare	Starea urmatoare
	Tabela 'action'	Tabela 'Goto'

- Algoritm: ne uitam la starea curenta S si terminalul C de la intrare
 - Daca $Action[S, C] = s(S')$ atunci 'shift' si trece in S' :
 - push(C), push(S')
 - Daca $Action[S, C] = X \rightarrow \alpha$ atunci 'reduce':
 - pop($2 * |\alpha|$), $S' = top()$, push(X), push($Goto[S', X]$)

Gramatici LR(k)

- LR(k) = Left-to-right scanning, right-most derivation, k lookahead tokens
- Cazurile principale
 - LR(0), LR(1)
 - Variante: SLR and LALR(1)
- Analizările pt. gramatici LR(0):
 - Aleg shift/reduce fara sa se uite la lookahead
 - Incepem cu ele, caci ne vor ajuta sa intelegem parsarea shift-reduce

Cursul viitor:

- Analiza semantică

Întrebări?

