

⇒ Practicing is the key.

⇒ " Able to solve the problem
but not getting confidence of
solving a new question if faced."

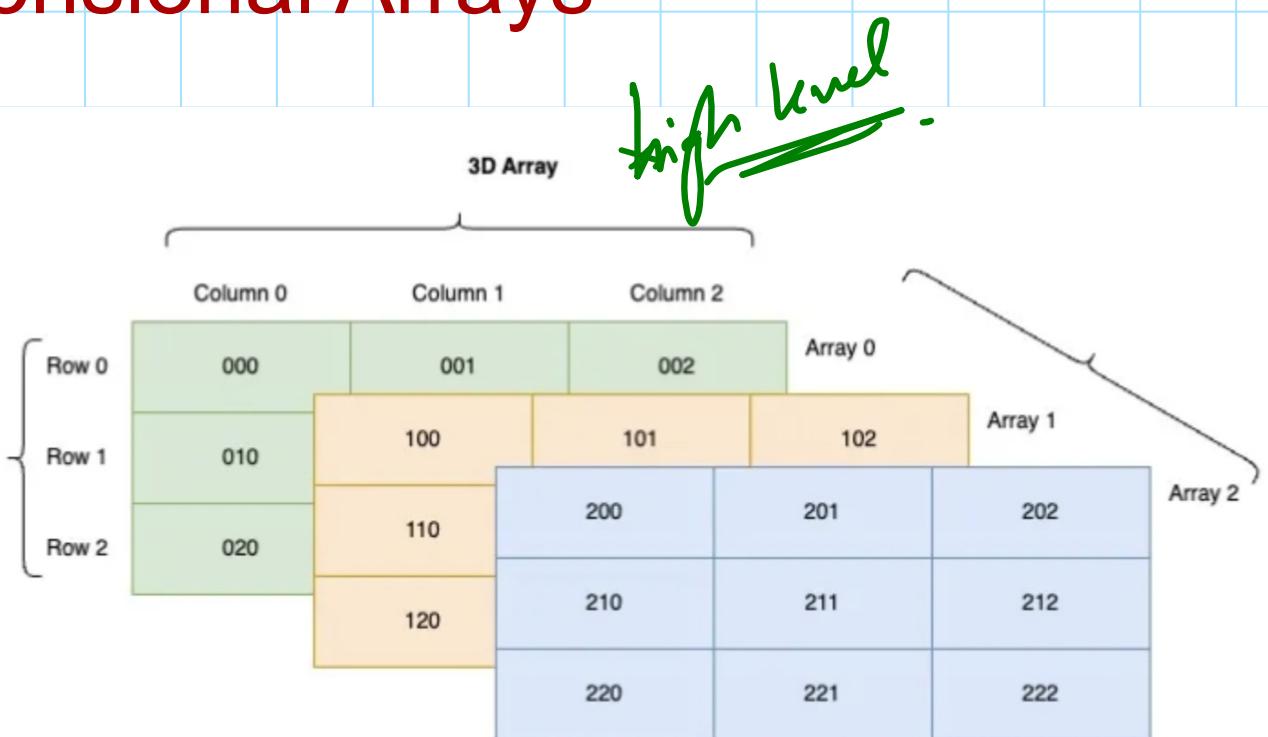
the better you
become.

Introduction to Multi-dimensional Arrays

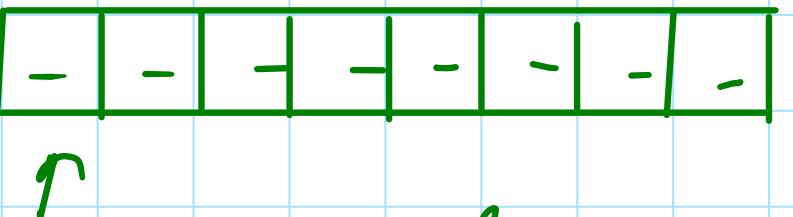
2D Array ✓

	Column 0	Column 1	Column 2
Row 0	X[0][0]	X[0][1]	X[0][2]
Row 1	X[1][0]	X[1][1]	X[1][2]
Row 2	X[2][0]	X[2][1]	X[2][2]

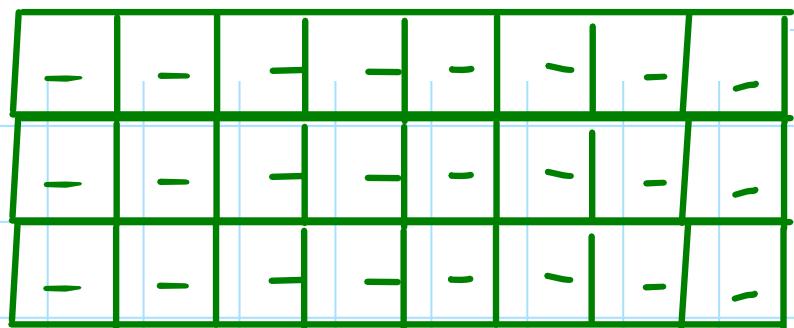
2D.
Array
Multi-Dimensional



1-D →



same type of data stored.



2-D Array :

How ? ← I will tell.
Why ??

Problem Statement : I want to store distances between some cities

Kanpur → K → B → 100 km

Bokaro → B → L → 200 km

Lucknow → L → C → 50 km

Chennai → C → L → 150 km

Jodhpur → J → K → 300 km

Appr. 1 → Dictionary.

Kanpur → K → B → 100 km

Bokaro → B → L → 200 km

Lucknow → L → C → 50 km

Chennai → C → B → 150 km

Jodhpur → J → K → 300 km

{ K-B : 100,
B-L : 200,
L-C : 50,
C-B : 150
J-K : 300

→ Advantages
easy to fetch; no duplicates.

Appx 2 : 2D Array .

Kanpur → K → B → 100 km

Bokaro → B → L → 200 km

Lucknow → L → C → 50 km

Chennai → C → B → 150 km

Jodhpur → J → K → 300 km

K	0	100	0	0	300
B	100	0	200	150	0
L	0	200	0	50	0
C	0	150	50	0	0
J	300	0	0	0	0

Approach 1 : using Dictionary

```
# Creating a dictionary to store distances between cities
distances = {
    "CityA_CityB": 100,
    "CityA_CityC": 150,
    "CityA_CityD": 200,
    "CityB_CityC": 50,
    "CityB_CityD": 250,
    "CityC_CityD": 100,
}
# Accessing the distance between City A and City D
print("Distance between City A and City D:", distances["CityA_CityD"],
      "km")
```

Pros:

- Direct mapping between two cities and their distance.
- Easy to access the distance between any two given cities.

Cons:

- Can become cumbersome as the number of cities grows, leading to a significant increase in dictionary keys.
- Not the most space-efficient if many distances are the same or zero.

Approach 2 : 2D Array

→ A more structured way to represent such data is by using 2D arrays (lists of lists in Python), where each row and column represent a city, and the intersection represents the distance between those cities.

	Column 0	Column 1	Column 2
Row 0	x[0][0]	x[0][1]	x[0][2]
Row 1	x[1][0]	x[1][1]	x[1][2]
Row 2	x[2][0]	x[2][1]	x[2][2]

Kanpur → K → B → 100 km
Bokaro → B → L → 200 km
Lucknow → L → C → 50 km
Chennai → C → B → 150 km
Jodhpur → J → K → 300 km

	K	B	L	C	J
K	0	100	0	0	300
B	100	0	200	150	0
L	0	200	0	50	0
C	0	150	50	0	0
J	300	0	0	0	0

Approach 2 : 2D Array

A more structured way to represent such data is by using 2D arrays (lists of lists in Python), where each row and column represent a city, and the intersection represents the distance between those cities.

```
# Creating a 2D array to store distances between cities  
# Assume CityA=0, CityB=1, CityC=2, CityD=3 for indexing purposes  
distances = [
```

```
    [0, 100, 150, 200], # Distances from City A  
    [100, 0, 50, 250], # Distances from City B  
    [150, 50, 0, 100], # Distances from City C  
    [200, 250, 100, 0] # Distances from City D
```

```
]
```

```
# Accessing the distance between City A and City D  
print("Distance between City A and City D:", distances[0][3], "km")
```

0	1	2	3	
A	B	C	D	
0	A	0	100	150
1	B			
2	C			
3	D			

Approach 2 : 2D Array

A more structured way to represent such data is by using 2D arrays (lists of lists in Python), where each row and column represent a city, and the intersection represents the distance between those cities.

```
# Creating a 2D array to store distances between cities
# Assume CityA=0, CityB=1, CityC=2, CityD=3 for indexing purposes
distances = [
    [0, 100, 150, 200], # Distances from City A
    [100, 0, 50, 250], # Distances from City B
    [150, 50, 0, 100], # Distances from City C
    [200, 250, 100, 0] # Distances from City D
]
# Accessing the distance between City A and City D
print("Distance between City A and City D:", distances[0][3], "km")
```

Pros:

- Offers a structured, tabular form of data representation.
- Efficiently stores distances, especially when the number of cities is fixed and known.

Cons:

- Can require a significant amount of space, particularly if there are many cities with zero or the same distances.

	0	1	2	3
0	0	100	150	200
1	100	0	50	250
2	150	50	0	100
3	200	250	100	0

Dictionary Vs 2D Array :

Both dictionaries and 2D arrays offer viable methods for storing distances between cities.

The choice between them depends on the specific requirements of your problem and your preference for space efficiency versus ease of data access.

Beginners might find dictionaries more straightforward for smaller sets of data, while 2D arrays offer a more scalable solution for larger datasets.

Visualizing Report Cards :

Math → M

Biology → B

Economics → E

100 students in
a class learning
above subjects.

→ What would be the
efficient way of
storing/representing
their scores

Dictionary:

{Ram: {M: 50, B: 40, E: 60}, -----}

3

not efficient in
terms of space.
(keys)

Visualizing Report Cards :

Math → M

Biology → B

Economics → F

100 students in
a class learning
above subjects.

→ what would be the efficient way of storing / representing their scores

MSheet.

Diagram illustrating a beam segment O-B-E. The beam is divided into segments OB and BE by points B and E. A coordinate system is established at O with segments OB and BE as axes. A force vector M is applied at O along the OB axis. Points D, L, and 2 are marked above the beam. A circled 'stud 1' is at O, and a circled '9D' is at point 9D on the BE axis.

	O	L	2
stud 1	0	50	60
stud 2.1	30	80	9D
2	20	50	40
3	:	:	:
-	,	,	,
1	.	.	,
0	,	,	,

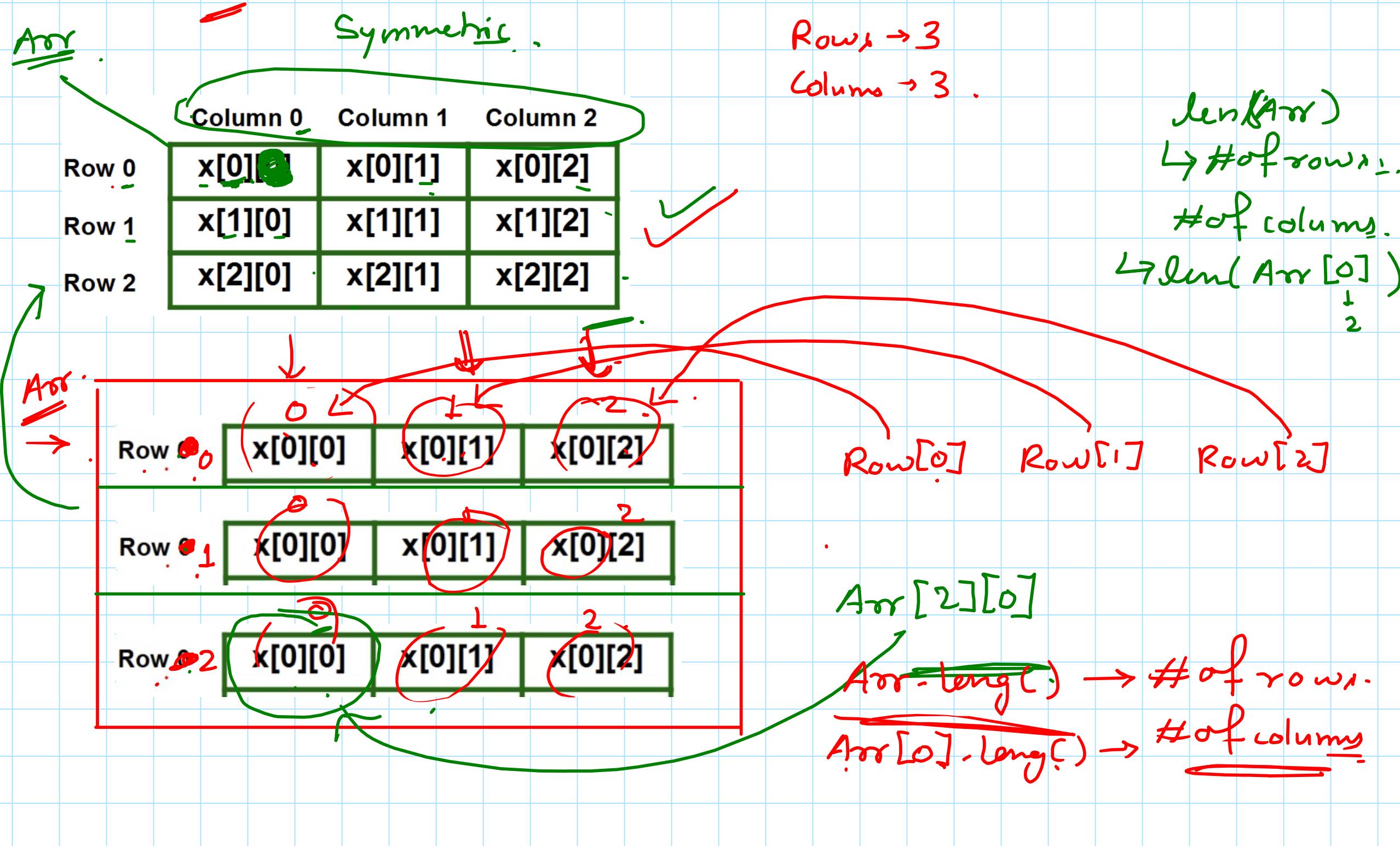
m sheet $[+][z]$ \rightarrow go,
=,

```
# Example 2D array  
grades = [  
    [90, 80, 70], # Grades for student 1  
    [85, 75, 65], # Grades for student 2  
    [88, 78, 68] # Grades for student 3  
]
```

Students Subjects

	Column 0	Column 1	Column 2
Row 0	$x[0][0]$	$x[0][1]$	$x[0][2]$
Row 1	$x[1][0]$	$x[1][1]$	$x[1][2]$
Row 2	$x[2][0]$	$x[2][1]$	$x[2][2]$

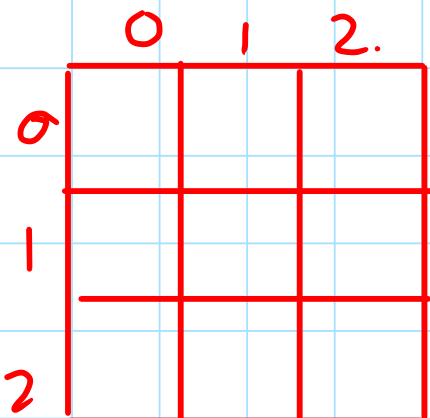
Indexing in 2D Arrays :



Finding the Length of Rows and Columns in 2D Arrays :

3×3

grades.



```
# Example 2D array  
grades = [  
    [90, 80, 70], # Grades for student 1  
    [85, 75, 65], # Grades for student 2  
    [88, 78, 68] # Grades for student 3  
]
```

Finding the number of rows

`num_rows = len(grades)` → # of rows or # of 1-D array.

```
print("Number of Rows:", num_rows)
```

3

Finding the number of columns

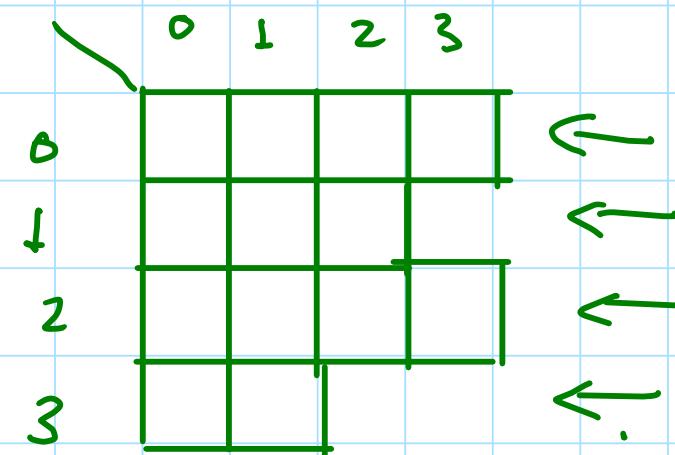
`num_columns = len(grades[0])` → # of col or length of 1-D array.

```
print("Number of Columns:", num_columns)
```

3

= .

Arr.



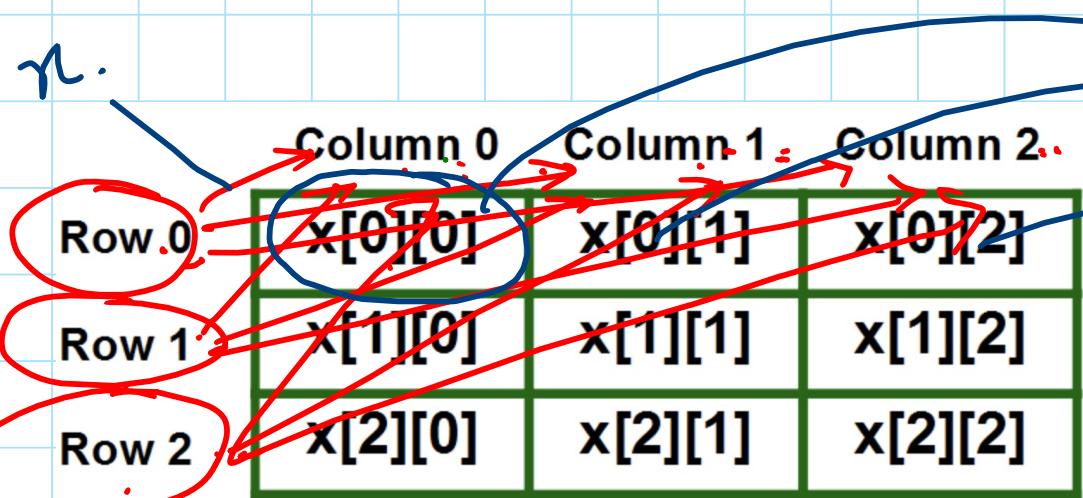
`len(Arr[0])` → 4

`len(Arr[1])` → 3

`len(Arr[2])` → 4

`len(Arr[3])` → 2

Traversing 2D Arrays :



now col.

$x[0][1]$

$x[0][2]$

rows.

\downarrow

$i < 3$ ✓

$\underline{i < \text{len}(x)}$

$2 < 3$ ✓

$3 < 3$ X

$0 < 3$ ✓

$\underline{\underline{\text{len}(x[0])}}$

$3 < 3$ X

for ($i = 0$; $i < \text{len}(x)$; $i++$)

{
for ($j = 0$; $j < \underline{\underline{\text{len}(x[0])}}$; $j++$)

{
print ($x[i][j]$)
}

outside → rows are repeating.
inside → columns are repeating.

0	5	10	50
1	20	70	40
2	100	90	80

O/P.

5. 10 50 4
20 70 100
90 80

$i = 0$, $j = 0, 1, 2, 3$ X = $x[0][0]$.
 $i = 1$, $j = 0, 1, 2, 3$ X
 $i = 2$, $j = 0, 1, 2, 3$ X
 $i = 3$ X

point all the items in array

Arr.	0	1	2	3
0	4	5	6	7
1	8	9	10	
2	4	5	11	12
3	3	1		

$\text{len}(\text{Arr}[0]) \rightarrow 4$

$\text{len}(\text{Arr}[1]) \rightarrow 3$

$\text{len}(\text{Arr}[2]) \rightarrow 4$

$\text{len}(\text{Arr}[3]) \rightarrow 2$

```
for( i=0 ; i< len(Arr) ; i++ )  
{   for( j=0 ; j< len(Arr[i]) ; j++ )  
}
```

}

5 minutes.

back at

1:05

~~1:05~~.

B to T & L to R.

	Column 0	Column 1	Column 2
Row 0	x[0][0]	x[0][1]	x[0][2]
Row 1	x[1][0]	x[1][1]	x[1][2]
Row 2	x[2][0]	x[2][1]	x[2][2]

T → B & L → R.

100 90 80
4. 20 70
5 10 50

π

0	1	2
5	10	50
4	20	70
100	90	80

T → B & L → R.

Nested Loop.

$i = 2$.

```
for ( i = len(n)-1 ; i >= 0 ; i-- ) // reverse loop
{
    for ( j = 0 ; j < len(n[0]) ; j++ )
    {
        print [ n[i][j] ]
    }
}
```

row → outer loop → reversed.

col → inner loop → forward.

α

	Column 0	Column 1	Column 2
Row 0	$x[0][0]$	$x[0][1]$	$x[0][2]$
Row 1	$x[1][0]$	$x[1][1]$	$x[1][2]$
Row 2	$x[2][0]$	$x[2][1]$	$x[2][2]$

$\alpha [row\ ind] [col\ ind]$

Column wise Traversal : (Reverse order)

	Column 0	Column 1	Column 2
Row 0	x[0][0]	x[0][1]	x[0][2]
Row 1	x[1][0]	x[1][1]	x[1][2]
Row 2	x[2][0]	x[2][1]	x[2][2]

Ans:

0	1	2
5	10	50
2	20	70
100	90	80

Very important.

- outer loop → columns → forward.
- inner loop → rows → reverse.

1.

O/p → 100 90 5

90 20 10

80 70 50

len(arr)-1

for($i=0$; $i < \text{len}(\text{arr}[0])$; $i++$) ✓

```
{
    for( $j = \text{len}(\text{arr}) - 1$ ;  $j \geq 0$ ;  $j--$ )
    {
        point( $\text{arr}[j][i]$ )
    }
}
```

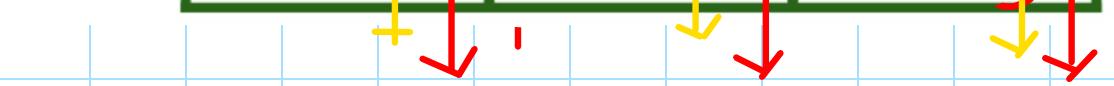
Hw: $i=0 \rightarrow j = \frac{\text{arr}[0][2]}{\text{arr}[0][0]}$

Column wise Traversal : [forward order]

$O/P \rightarrow 5 \ 4 \ 100$

$10 \ 20 \ 90$
 $50 \ 70 \ 80$

	Column 0	Column 1	Column 2
Row 0	$x[0][0]$	$x[0][1]$	$x[0][2]$
Row 1	$x[1][0]$	$x[1][1]$	$x[1][2]$
Row 2	$x[2][0]$	$x[2][1]$	$x[2][2]$



Code (n/w)

row	0	1	2
0	5	10	50
1	4	20	70
2	100	90	80

outer loop \rightarrow column \rightarrow forward.

inner loop \rightarrow row \rightarrow forward.

Finding a Target item in 2D array:-

arr

0	1	2	
0	5	10	50
1	15	20	70
2	100	90	80

key = 70.

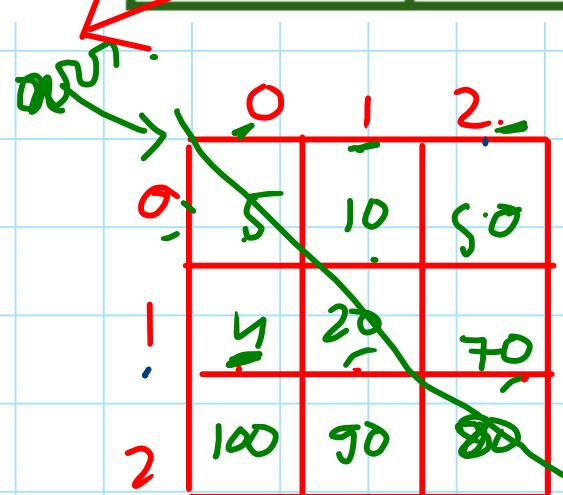
```
for (i=0; i< len(arr); i++)  
{  
    for (j=0; j < len(arr[0]); j++)  
        {  
            if (arr[i][j] == key)  
                return true;  
        }  
}
```

return false.

Pointing Diagonal items : .

L to R. ~~sq. matrix~~

	Column 0	Column 1	Column 2
Row 0	x[0][0]	x[0][1]	x[0][2]
Row 1	x[1][0]	x[1][1]	x[1][2]
Row 2	x[2][0]	x[2][1]	x[2][2]



Right to Left

o/p → 5 20 80

of loops = 2

for (; i=0 ; i<3 ; i++)

{ for (j=0 ; j < 3 ; j++)

{ if (i == j)

point arr[i][j] .

i = 0, 1, 2, 3
j = 0, 1, 2, 3

for (i=0, j=0 ; i < length ; i++, j++)

{ point (arr[i][j])

arr[0][0] ~
arr[1][1] ~
arr[2][2] ✓

5 → [0][0]

20 → [1][1]

80 → [2][2]

outer →

inner →

H.W

point

Right Diagonal.

L to R.

sq. mat.

	Column 0	Column 1	Column 2
Row 0	x[0][0]	x[0][1]	x[0][2]
Row 1	x[1][0]	x[1][1]	x[1][2]
Row 2	x[2][0]	x[2][1]	x[2][2]

Ans.

0	5	10	50
1	5	20	70
2	100	90	80

Can you do it using
single loop?

arr[0][2]

arr[1][1]

arr[2][0]

row → 0 to 2.

col → 2 to 1.

