

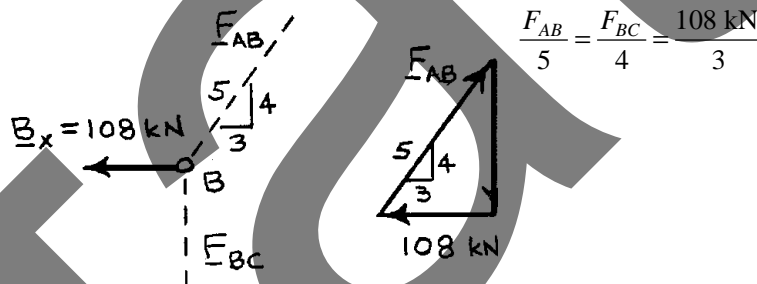
Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Entire truss:

$$\begin{aligned}
 +\uparrow \Sigma F_y = 0: & \quad B_y = 0 \quad \mathbf{B_y = 0} \\
 +\curvearrowright \Sigma M_C = 0: & \quad -B_x(3.2 \text{ m}) - (48 \text{ kN})(7.2 \text{ m}) = 0 \\
 & \quad B_x = -108 \text{ kN} \quad \mathbf{B_x = 108 \text{ kN} \leftarrow} \\
 +\rightarrow \Sigma F_x = 0: & \quad C - 108 \text{ kN} + 48 \text{ kN} = 0 \\
 & \quad C = 60 \text{ kN} \quad \mathbf{C = 60 \text{ kN} \rightarrow}
 \end{aligned}$$

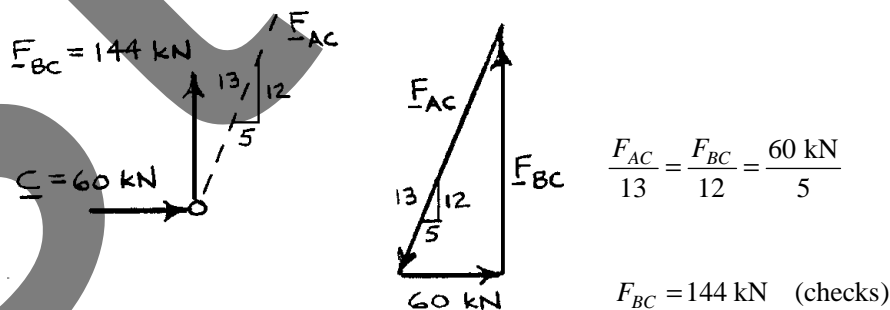
Free body: Joint B:



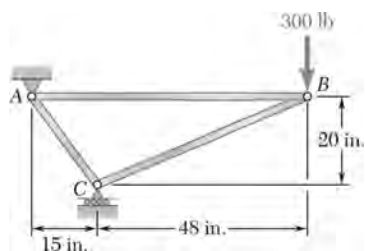
$$F_{AB} = 180.0 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{BC} = 144.0 \text{ kN} \quad T \quad \blacktriangleleft$$

Free body: Joint C:



$$F_{AC} = 156.0 \text{ kN} \quad C \quad \blacktriangleleft$$



Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

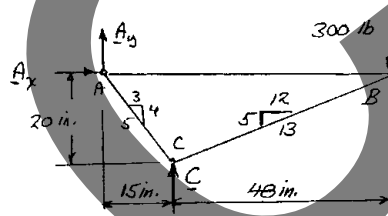
SOLUTION

Reactions:

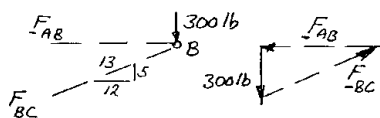
$$\Sigma M_A = 0: C = 1260 \text{ lb} \uparrow$$

$$\Sigma F_x = 0: A_x = 0$$

$$\Sigma F_y = 0: A_y = 960 \text{ lb} \downarrow$$



Joint B:

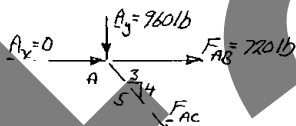


$$\frac{F_{AB}}{12} = \frac{F_{BC}}{13} = \frac{300 \text{ lb}}{5}$$

$$F_{AB} = 720 \text{ lb} \quad T \quad \blacktriangleleft$$

$$F_{BC} = 780 \text{ lb} \quad C \quad \blacktriangleleft$$

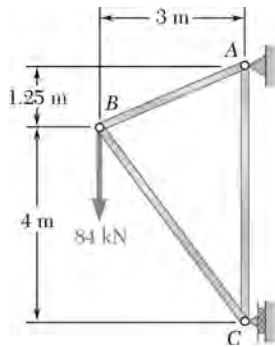
Joint A:



$$+\uparrow \Sigma F_y = 0: -960 \text{ lb} - \frac{4}{5} F_{AC} = 0$$

$$F_{AC} = 1200 \text{ lb} \quad F_{AC} = 1200 \text{ lb} \quad C \quad \blacktriangleleft$$

$$+\rightarrow \Sigma F_x = 0: 720 \text{ lb} - (1200 \text{ lb}) \frac{3}{5} = 0 \quad (\text{checks})$$



Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION

Reactions:

$$+\circlearrowleft \Sigma M_A = 0: (84 \text{ kN})(3 \text{ m}) - C(5.25 \text{ m}) = 0$$

$$C = 48 \text{ kN} \leftarrow$$

$$+\rightarrow \Sigma F_x = 0: A_x - C = 0$$

$$A_x = 48 \text{ kN} \rightarrow$$

$$+\uparrow \Sigma F_y = 0: A_y - 84 \text{ kN} = 0$$

$$A_y = 84 \text{ kN} \uparrow$$

Joint A:

$$+\rightarrow \Sigma F_x = 0: 48 \text{ kN} - \frac{12}{13} F_{AB} = 0$$

$$F_{AB} = +52 \text{ kN}$$

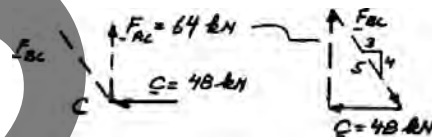
$$F_{AB} = 52.0 \text{ kN} \quad T \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: 84 \text{ kN} - \frac{5}{13} (52 \text{ kN}) - F_{AC} = 0$$

$$F_{AC} = +64.0 \text{ kN}$$

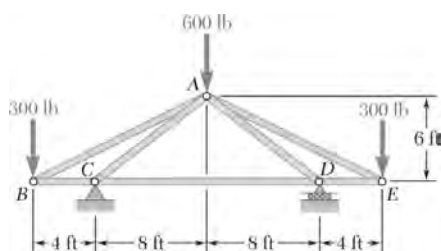
$$F_{AC} = 64.0 \text{ kN} \quad T \quad \blacktriangleleft$$

Joint C:



$$\frac{F_{BC}}{5} = \frac{48 \text{ kN}}{3}$$

$$F_{BC} = 80.0 \text{ kN} \quad C \quad \blacktriangleleft$$



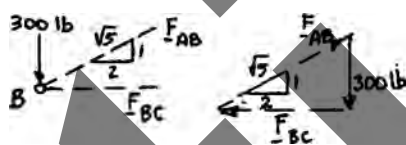
Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Truss:

From the symmetry of the truss and loading, we find

$$C = D = 600 \text{ lb} \uparrow$$

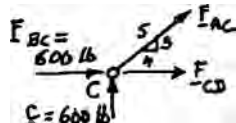


Free body: Joint B:

$$\frac{F_{AB}}{\sqrt{5}} = \frac{F_{BC}}{2} = \frac{300 \text{ lb}}{1}$$

$$F_{AB} = 671 \text{ lb } T \quad F_{BC} = 600 \text{ lb } C \blacktriangleleft$$

Free body: Joint C:



$$+\uparrow \Sigma F_y = 0: \frac{3}{5} F_{AC} + 600 \text{ lb} = 0$$

$$F_{AC} = -1000 \text{ lb}$$

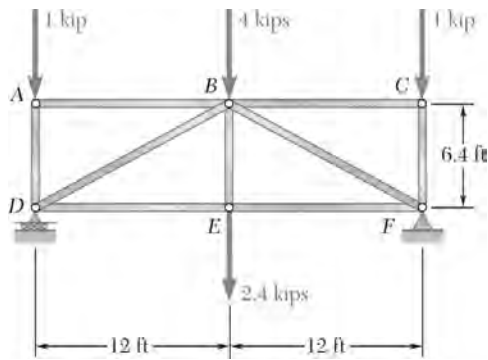
$$F_{AC} = 1000 \text{ lb } C \blacktriangleleft$$

$$+\rightarrow \Sigma F_x = 0: \frac{4}{5} (-1000 \text{ lb}) + 600 \text{ lb} + F_{CD} = 0$$

$$F_{CD} = 200 \text{ lb } T \blacktriangleleft$$

From symmetry:

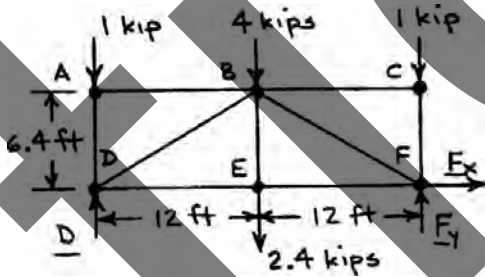
$$F_{AD} = F_{AC} = 1000 \text{ lb } C, \quad F_{AE} = F_{AB} = 671 \text{ lb } T, \quad F_{DE} = F_{BC} = 600 \text{ lb } C \blacktriangleleft$$



Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION

Reactions:



$$+\circlearrowleft \sum M_D = 0: F_y(24) - (4 + 2.4)(12) - (1)(24) = 0$$

$$F_y = 4.2 \text{ kips} \uparrow$$

$$\sum F_x = 0: F_x = 0$$

$$+\uparrow \sum F_y = 0: D - (1 + 4 + 1 + 2.4) + 4.2 = 0$$

$$D = 4.2 \text{ kips} \uparrow$$

Joint A:



$$\sum F_x = 0: F_{AB} = 0$$

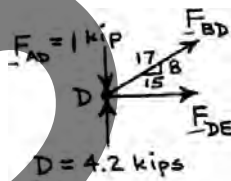
$$F_{AB} = 0 \quad \blacktriangleleft$$

$$+\uparrow \sum F_y = 0: -1 - F_{AD} = 0$$

$$F_{AD} = -1 \text{ kip}$$

$$F_{AD} = 1.000 \text{ kip} \quad C \quad \blacktriangleleft$$

Joint D:



$$+\uparrow \sum F_y = 0: -1 + 4.2 + \frac{8}{17} F_{BD} = 0$$

$$F_{BD} = -6.8 \text{ kips}$$

$$F_{BD} = 6.80 \text{ kips} \quad C \quad \blacktriangleleft$$

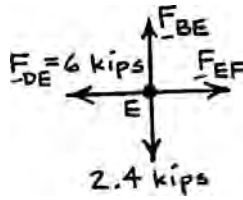
$$\rightarrow \sum F_x = 0: \frac{15}{17}(-6.8) + F_{DE} = 0$$

$$F_{DE} = +6 \text{ kips}$$

$$F_{DE} = 6.00 \text{ kips} \quad T \quad \blacktriangleleft$$

PROBLEM (Continued)

Joint E:

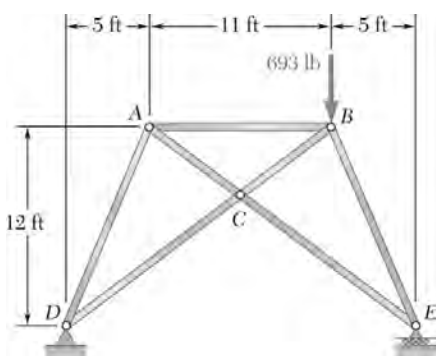


$$+\uparrow \Sigma F_y = 0: F_{BE} - 2.4 = 0$$

$$F_{BE} = +2.4 \text{ kips}$$

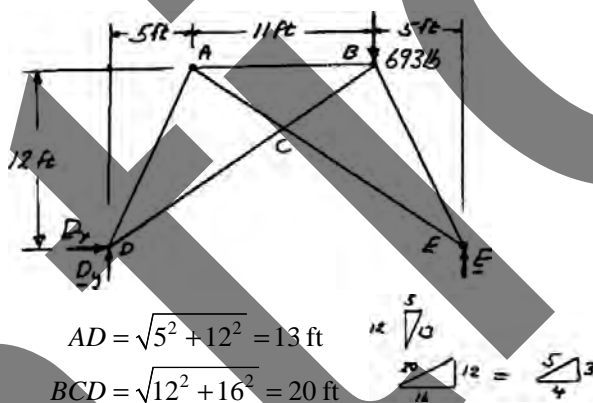
$$F_{BE} = 2.40 \text{ kips } T \quad \blacktriangleleft$$

Truss and loading symmetrical about C .



Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION



Reactions:

$$\Sigma F_x = 0: D_x = 0$$

$$+\circlearrowleft \Sigma M_E = 0: D_y(21 \text{ ft}) - (693 \text{ lb})(5 \text{ ft}) = 0$$

$$D_y = 165 \text{ lb} \uparrow$$

$$+\uparrow \Sigma F_y = 0: 165 \text{ lb} - 693 \text{ lb} + E = 0$$

$$E = 528 \text{ lb} \uparrow$$

Joint D:

$$+\leftarrow \Sigma F_x = 0: \frac{5}{13} F_{AD} + \frac{4}{5} F_{DC} = 0 \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \frac{12}{13} F_{AD} + \frac{3}{5} F_{DC} + 165 \text{ lb} = 0 \quad (2)$$

Solving Eqs. (1) and (2) simultaneously,

$$F_{AD} = -260 \text{ lb}$$

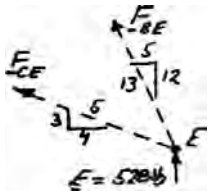
$$F_{AD} = 260 \text{ lb} \quad C \blacktriangleleft$$

$$F_{DC} = +125 \text{ lb}$$

$$F_{DC} = 125 \text{ lb} \quad T \blacktriangleleft$$

PROBLEM (Continued)

Joint E:



$$\rightarrow + \Sigma F_x = 0: \quad \frac{5}{13} F_{BE} + \frac{4}{5} F_{CE} = 0 \quad (3)$$

$$\uparrow + \Sigma F_y = 0: \quad \frac{12}{13} F_{BE} + \frac{3}{5} F_{CE} + 528 \text{ lb} = 0 \quad (4)$$

Solving Eqs. (3) and (4) simultaneously,

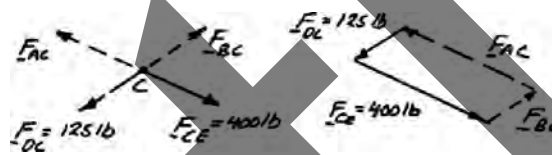
$$F_{BE} = -832 \text{ lb}$$

$$F_{CE} = +400 \text{ lb}$$

$$F_{BE} = 832 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{CE} = 400 \text{ lb} \quad T \quad \blacktriangleleft$$

Joint C:

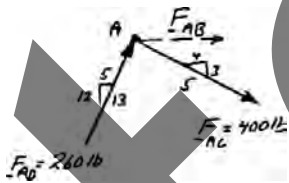


Force polygon is a parallelogram (see Fig. 6.11, p. 209).

$$F_{AC} = 400 \text{ lb} \quad T \quad \blacktriangleleft$$

$$F_{BC} = 125.0 \text{ lb} \quad T \quad \blacktriangleleft$$

Joint A:



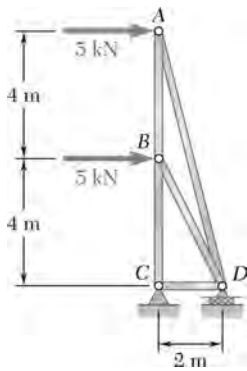
$$\rightarrow + \Sigma F_x = 0: \quad \frac{5}{13} (260 \text{ lb}) + \frac{4}{5} (400 \text{ lb}) + F_{AB} = 0$$

$$F_{AB} = -420 \text{ lb}$$

$$F_{AB} = 420 \text{ lb} \quad C \quad \blacktriangleleft$$

$$\uparrow + \Sigma F_y = 0: \quad \frac{12}{13} (260 \text{ lb}) - \frac{3}{5} (400 \text{ lb}) = 0$$

$$0 = 0 \quad (\text{Checks})$$



Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Entire truss:

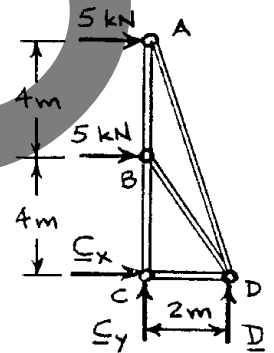
$$\rightarrow \Sigma F_x = 0: C_x + 2(5 \text{ kN}) = 0$$

$$C_x = -10 \text{ kN} \quad \bar{C}_x = 10 \text{ kN} \leftarrow$$

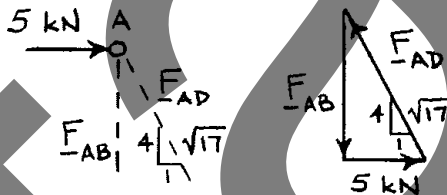
$$+\circlearrowleft \Sigma M_C = 0: D(2 \text{ m}) - (5 \text{ kN})(8 \text{ m}) - (5 \text{ kN})(4 \text{ m}) = 0$$

$$D = +30 \text{ kN} \quad \bar{D} = 30 \text{ kN} \uparrow$$

$$+\uparrow \Sigma F_y = 0: C_y + 30 \text{ kN} = 0 \quad C_y = -30 \text{ kN} \quad \bar{C}_y = 30 \text{ kN} \downarrow$$



Free body: Joint A:

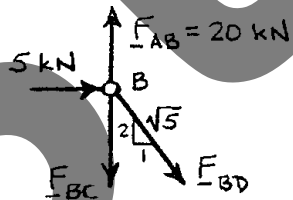


$$\frac{F_{AB}}{4} = \frac{F_{AD}}{\sqrt{17}} = \frac{5 \text{ kN}}{1}$$

$$F_{AB} = 20.0 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{AD} = 20.6 \text{ kN} \quad C \quad \blacktriangleleft$$

Free body: Joint B:



$$\rightarrow \Sigma F_x = 0: 5 \text{ kN} + \frac{1}{\sqrt{5}} F_{BD} = 0$$

$$F_{BD} = -5\sqrt{5} \text{ kN}$$

$$F_{BD} = 11.18 \text{ kN} \quad C \quad \blacktriangleleft$$

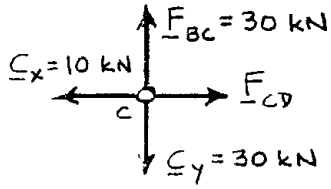
$$+\uparrow \Sigma F_y = 0: 20 \text{ kN} - F_{BC} - \frac{2}{\sqrt{5}} (-5\sqrt{5} \text{ kN}) = 0$$

$$F_{BC} = +30 \text{ kN}$$

$$F_{BC} = 30.0 \text{ kN} \quad T \quad \blacktriangleleft$$

PROBLEM(Continued)

Free body: Joint C:

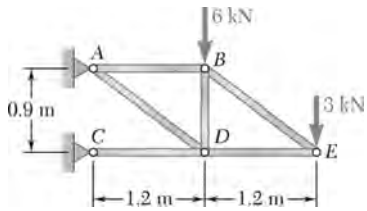


$$\rightarrow \Sigma F_x = 0: F_{CD} - 10 \text{ kN} = 0$$

$$F_{CD} = +10 \text{ kN}$$

$$F_{CD} = 10.00 \text{ kN } T \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: 30 \text{ kN} - 30 \text{ kN} = 0 \quad (\text{checks})$$



PROBLEM 6.8

Using the method of joints, determine the force in each member of the truss shown. State whether each member is in tension or compression.

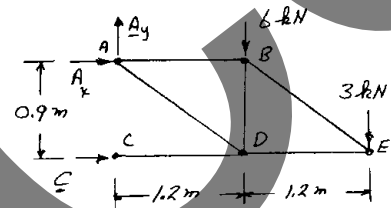
SOLUTION

Reactions:

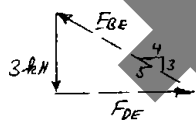
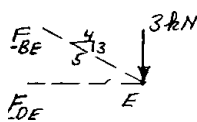
$$\Sigma M_C = 0: A_x = 16 \text{ kN} \leftarrow$$

$$\Sigma F_y = 0: A_y = 9 \text{ kN} \uparrow$$

$$\Sigma F_x = 0: C = 16 \text{ kN} \rightarrow$$



Joint E:

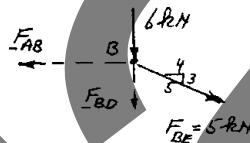


$$\frac{F_{BE}}{5} = \frac{F_{DE}}{4} = \frac{3 \text{ kN}}{3}$$

$$F_{BE} = 5.00 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{DE} = 4.00 \text{ kN} \quad C \quad \blacktriangleleft$$

Joint B:



$$\rightarrow \Sigma F_x = 0: \frac{4}{5}(5 \text{ kN}) - F_{AB} = 0$$

$$F_{AB} = +4 \text{ kN}$$

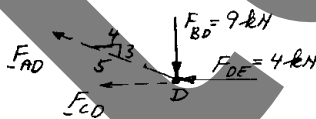
$$F_{AB} = 4.00 \text{ kN} \quad T \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -6 \text{ kN} - \frac{3}{5}(5 \text{ kN}) - F_{BD} = 0$$

$$F_{BD} = -9 \text{ kN}$$

$$F_{BD} = 9.00 \text{ kN} \quad C \quad \blacktriangleleft$$

Joint D:



$$+\uparrow \Sigma F_y = 0: -9 \text{ kN} + \frac{3}{5}F_{AD} = 0$$

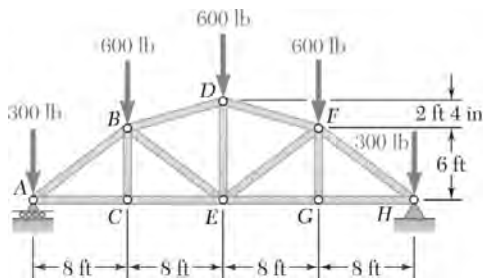
$$F_{AD} = +15 \text{ kN}$$

$$F_{AD} = 15.00 \text{ kN} \quad T \quad \blacktriangleleft$$

$$\rightarrow \Sigma F_x = 0: -4 \text{ kN} - \frac{4}{5}(15 \text{ kN}) - F_{CD} = 0$$

$$F_{CD} = -16 \text{ kN}$$

$$F_{CD} = 16.00 \text{ kN} \quad C \quad \blacktriangleleft$$



Determine the force in each member of the Gambrel roof truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Truss:

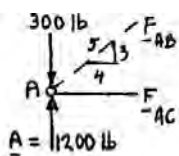
$$\Sigma F_x = 0: H_x = 0$$

Because of the symmetry of the truss and loading,

$$A = H_y = \frac{1}{2} \text{ total load}$$

$$A = H_y = 1200 \text{ lb} \uparrow$$

Free body: Joint A:



$$\frac{F_{AB}}{5} = \frac{F_{AC}}{4} = \frac{900 \text{ lb}}{3}$$

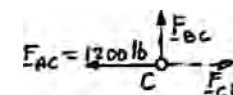
$$F_{AB} = 1500 \text{ lb} \quad C \blacktriangleleft$$

$$F_{AC} = 1200 \text{ lb} \quad T \blacktriangleleft$$

Free body: Joint C:

BC is a zero-force member.

$$F_{BC} = 0$$



$$F_{CE} = 1200 \text{ lb} \quad T \blacktriangleleft$$

Free body: Joint B:

$$+\rightarrow \Sigma F_x = 0: \frac{24}{25} F_{BD} + \frac{4}{5} F_{BE} + \frac{4}{5} (1500 \text{ lb}) = 0$$

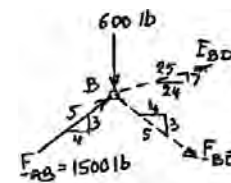
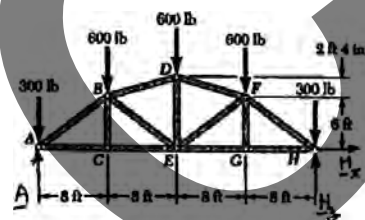
or

$$24F_{BD} + 20F_{BE} = -30,000 \text{ lb} \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \frac{7}{25} F_{BD} - \frac{3}{5} F_{BE} + \frac{3}{5} (1500) - 600 = 0$$

or

$$7F_{BD} - 15F_{BE} = -7,500 \text{ lb} \quad (2)$$



PROBLEM 6.9 (Continued)

Multiply Eq. (1) by 3, Eq. (2) by 4, and add:

$$100F_{BD} = -120,000 \text{ lb}$$

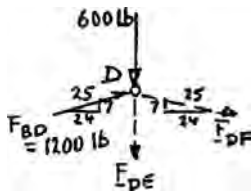
$$F_{BD} = 1200 \text{ lb} \quad C \quad \blacktriangleleft$$

Multiply Eq. (1) by 7, Eq. (2) by -24 , and add:

$$500F_{BE} = -30,000 \text{ lb}$$

$$F_{BE} = 60.0 \text{ lb} \quad C \quad \blacktriangleleft$$

Free body: Joint D:



$$+\rightarrow \Sigma F_x = 0: \quad \frac{24}{25}(1200 \text{ lb}) + \frac{24}{25}F_{DF} = 0$$

$$F_{DF} = -1200 \text{ lb}$$

$$F_{DF} = 1200 \text{ lb} \quad C \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: \quad \frac{7}{25}(1200 \text{ lb}) - \frac{7}{25}(-1200 \text{ lb}) - 600 \text{ lb} - F_{DE} = 0$$

$$F_{DE} = 72.0 \text{ lb}$$

$$F_{DE} = 72.0 \text{ lb} \quad T \quad \blacktriangleleft$$

Because of the symmetry of the truss and loading, we deduce that

$$F_{EF} = F_{BE}$$

$$F_{EF} = 60.0 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{EG} = F_{CE}$$

$$F_{EG} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$

$$F_{FG} = F_{BC}$$

$$F_{FG} = 0 \quad \blacktriangleleft$$

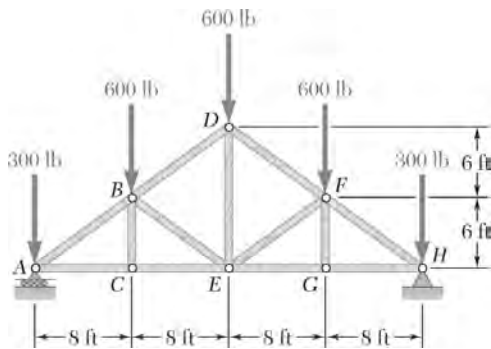
$$F_{FH} = F_{AB}$$

$$F_{FH} = 1500 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{GH} = F_{AC}$$

$$F_{GH} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$

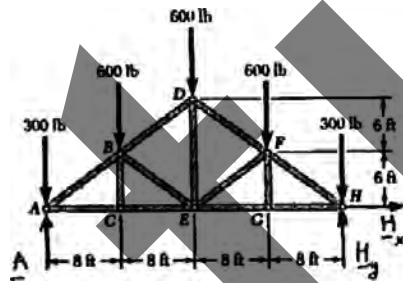
Note: Compare results with those of Problem 6.11.



Determine the force in each member of the Howe roof truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Truss:



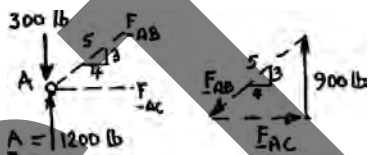
$$\Sigma F_x = 0: H_x = 0$$

Because of the symmetry of the truss and loading,

$$A = H_y = \frac{1}{2} \text{ total load}$$

$$A = H_y = 1200 \text{ lb} \uparrow$$

Free body: Joint A:



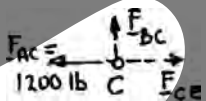
$$\frac{F_{AB}}{5} = \frac{F_{AC}}{4} = \frac{900 \text{ lb}}{3}$$

$$F_{AB} = 1500 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{AC} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$

Free body: Joint C:

BC is a zero-force member.



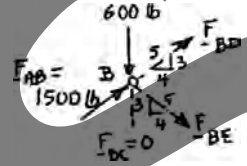
$$F_{BC} = 0$$

$$F_{CE} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$

PROBLEM 6.10 (Continued)

Free body: Joint B:

$$+\rightarrow \Sigma F_x = 0: \quad \frac{4}{5} F_{BD} + \frac{4}{5} F_{BC} + \frac{4}{5} (1500 \text{ lb}) = 0$$



or

$$F_{BD} + F_{BE} = -1500 \text{ lb} \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \quad \frac{3}{5} F_{BD} - \frac{3}{5} F_{BE} + \frac{3}{5} (1500 \text{ lb}) - 600 \text{ lb} = 0$$

or

$$F_{BD} - F_{BE} = -500 \text{ lb} \quad (2)$$

Add Eqs. (1) and (2):

$$2F_{BD} = -2000 \text{ lb}$$

$$F_{BD} = 1000 \text{ lb} \quad C \quad \blacktriangleleft$$

Subtract Eq. (2) from Eq. (1):

$$2F_{BE} = -1000 \text{ lb}$$

$$F_{BE} = 500 \text{ lb} \quad C \quad \blacktriangleleft$$

Free Body: Joint D:

$$+\rightarrow \Sigma F_x = 0: \quad \frac{4}{5} (1000 \text{ lb}) + \frac{4}{5} F_{DF} = 0$$

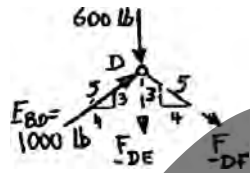
$$F_{DF} = -1000 \text{ lb}$$

$$F_{DF} = 1000 \text{ lb} \quad C \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: \quad \frac{3}{5} (1000 \text{ lb}) - \frac{3}{5} (-1000 \text{ lb}) - 600 \text{ lb} - F_{DE} = 0$$

$$F_{DE} = +600 \text{ lb}$$

$$F_{DE} = 600 \text{ lb} \quad T \quad \blacktriangleleft$$



Because of the symmetry of the truss and loading, we deduce that

$$F_{EF} = F_{BE}$$

$$F_{EF} = 500 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{EG} = F_{CE}$$

$$F_{EG} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$

$$F_{FG} = F_{BC}$$

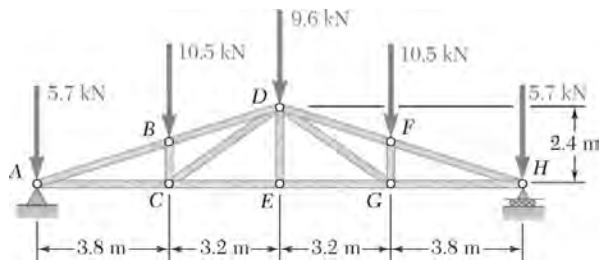
$$F_{FG} = 0 \quad \blacktriangleleft$$

$$F_{FH} = F_{AB}$$

$$F_{FH} = 1500 \text{ lb} \quad C \quad \blacktriangleleft$$

$$F_{GH} = F_{AC}$$

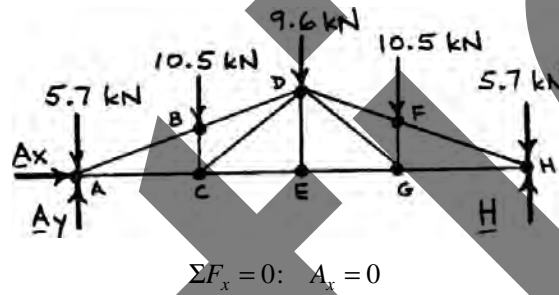
$$F_{GH} = 1200 \text{ lb} \quad T \quad \blacktriangleleft$$



Determine the force in each member of the Pratt roof truss shown. State whether each member is in tension or compression.

SOLUTION

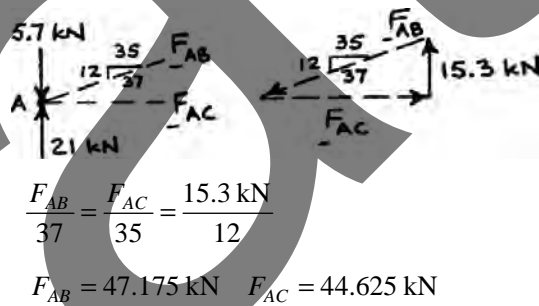
Free body: Truss:



Due to symmetry of truss and load,

$$A_y = H = \frac{1}{2} \text{ total load} = 21 \text{ kN} \uparrow$$

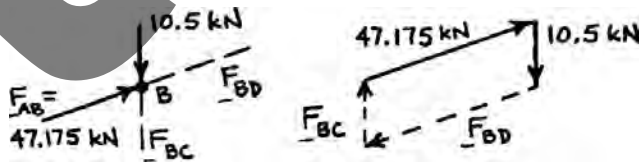
Free body: Joint A:



$$F_{AB} = 47.2 \text{ kN} \quad C \blacktriangleleft$$

$$F_{AC} = 44.6 \text{ kN} \quad T \blacktriangleleft$$

Free body: Joint B:



From force polygon:

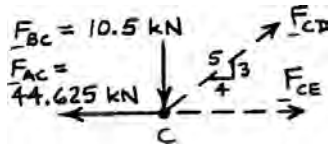
$$F_{BD} = 47.175 \text{ kN}, \quad F_{BC} = 10.5 \text{ kN}$$

$$F_{BC} = 10.50 \text{ kN} \quad C \blacktriangleleft$$

$$F_{BD} = 47.2 \text{ kN} \quad C \blacktriangleleft$$

PROBLEM 6.11 (Continued)

Free body: Joint C:



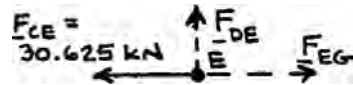
$$+\uparrow \Sigma F_y = 0: \frac{3}{5} F_{CD} - 10.5 = 0$$

$$+\rightarrow \Sigma F_x = 0: F_{CE} + \frac{4}{5}(17.50) - 44.625 = 0$$

$$F_{CD} = 17.50 \text{ kN } T \quad \blacktriangleleft$$

$$F_{CE} = 30.625 \text{ kN} \quad F_{CE} = 30.6 \text{ kN } T \quad \blacktriangleleft$$

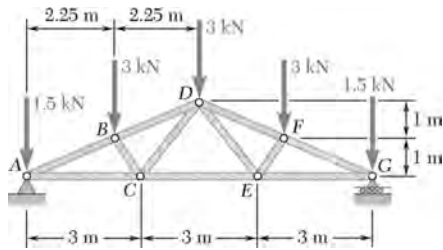
Free body: Joint E:



DE is a zero-force member.

$$F_{DE} = 0 \quad \blacktriangleleft$$

Truss and loading symmetrical about \bar{C} .



Determine the force in each member of the Fink roof truss shown.
State whether each member is in tension or compression.

SOLUTION

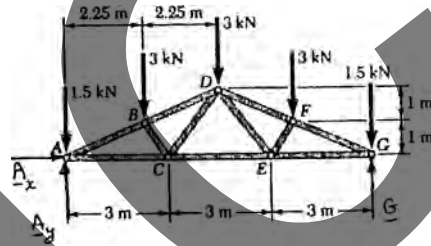
Free body: Truss:

$$\Sigma F_x = 0: A_x = 0$$

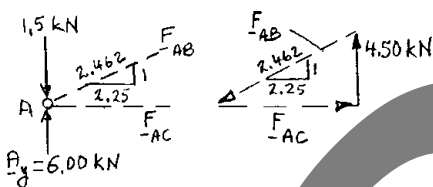
Because of the symmetry of the truss and loading,

$$A_y = G = \frac{1}{2} \text{ total load}$$

$$A_y = G = 6.00 \text{ kN} \uparrow$$



Free body: Joint A:



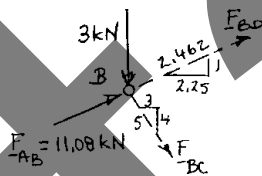
$$\frac{F_{AB}}{2.462} = \frac{F_{AC}}{2.25} = \frac{4.50 \text{ kN}}{1}$$

$$F_{AB} = 11.08 \text{ kN} \quad C \blacktriangleleft$$

$$F_{AC} = 10.125 \text{ kN}$$

$$F_{AC} = 10.13 \text{ kN} \quad T \blacktriangleleft$$

Free body: Joint B:



$$+\rightarrow \Sigma F_x = 0: \frac{3}{5} F_{BC} + \frac{2.25}{2.462} F_{BD} + \frac{2.25}{2.462} (11.08 \text{ kN}) = 0 \quad (1)$$

$$+\uparrow \Sigma F_y = 0: -\frac{4}{5} F_{BC} + \frac{F_{BD}}{2.462} + \frac{11.08 \text{ kN}}{2.462} - 3 \text{ kN} = 0 \quad (2)$$

Multiply Eq. (2) by -2.25 and add to Eq. (1):

$$\frac{12}{5} F_{BC} + 6.75 \text{ kN} = 0 \quad F_{BC} = -2.8125 \quad F_{BC} = 2.81 \text{ kN} \quad C \blacktriangleleft$$

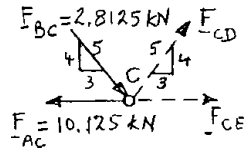
Multiply Eq. (1) by 4, Eq. (2) by 3, and add:

$$\frac{12}{2.462} F_{BD} + \frac{12}{2.462} (11.08 \text{ kN}) - 9 \text{ kN} = 0$$

$$F_{BD} = -9.2335 \text{ kN} \quad F_{BD} = 9.23 \text{ kN} \quad C \blacktriangleleft$$

PROBLEM (Continued)

Free body: Joint C:



$$+\uparrow \Sigma F_y = 0: \frac{4}{5} F_{CD} - \frac{4}{5} (2.8125 \text{ kN}) = 0$$

$$F_{CD} = 2.8125 \text{ kN},$$

$$F_{CD} = 2.81 \text{ kN} \quad T \quad \blacktriangleleft$$

$$+\rightarrow \Sigma F_x = 0: F_{CE} - 10.125 \text{ kN} + \frac{3}{5} (2.8125 \text{ kN}) + \frac{3}{5} (2.8125 \text{ kN}) = 0$$

$$F_{CE} = +6.7500 \text{ kN}$$

$$F_{CE} = 6.75 \text{ kN} \quad T \quad \blacktriangleleft$$

Because of the symmetry of the truss and loading, we deduce that

$$F_{DE} = F_{CD}$$

$$F_{CD} = 2.81 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{DF} = F_{BD}$$

$$F_{DF} = 9.23 \text{ kN} \quad C \quad \blacktriangleleft$$

$$F_{EF} = F_{BC}$$

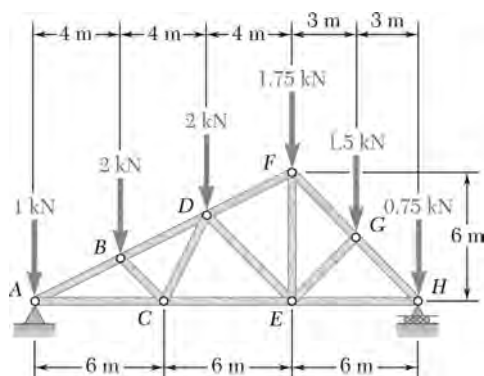
$$F_{EF} = 2.81 \text{ kN} \quad C \quad \blacktriangleleft$$

$$F_{EG} = F_{AC}$$

$$F_{EG} = 10.13 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{FG} = F_{AB}$$

$$F_{FG} = 11.08 \text{ kN} \quad C \quad \blacktriangleleft$$

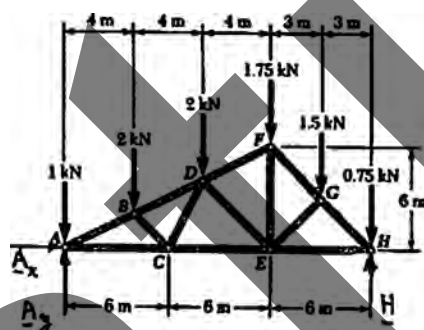


PROBLEM 6.13

Using the method of joints, determine the force in each member of the double-pitch roof truss shown. State whether each member is in tension or compression.

SOLUTION

Free body: Truss:



$$+\circlearrowleft \Sigma M_A = 0: H(18 \text{ m}) - (2 \text{ kN})(4 \text{ m}) - (2 \text{ kN})(8 \text{ m}) - (1.75 \text{ kN})(12 \text{ m}) - (1.5 \text{ kN})(15 \text{ m}) - (0.75 \text{ kN})(18 \text{ m}) = 0$$

$$H = 4.50 \text{ kN} \uparrow$$

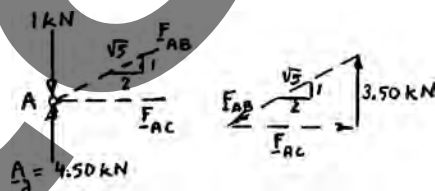
$$\Sigma F_x = 0: A_x = 0$$

$$\Sigma F_y = 0: A_y + H - 9 = 0$$

$$A_y = 9 - 4.50$$

$$A_y = 4.50 \text{ kN} \uparrow$$

Free body: Joint A:



$$\frac{F_{AB}}{\sqrt{5}} = \frac{F_{AC}}{2} = \frac{3.50 \text{ kN}}{1}$$

$$F_{AB} = 7.8262 \text{ kN} \quad C$$

$$F_{AB} = 7.83 \text{ kN} \quad C \quad \blacktriangleleft$$

$$F_{AC} = 7.00 \text{ kN} \quad T \quad \blacktriangleleft$$

PROBLEM 6.13 (Continued)

Free body: Joint B:

$$+\rightarrow \Sigma F_x = 0: \frac{2}{\sqrt{5}} F_{BD} + \frac{2}{\sqrt{5}} (7.8262 \text{ kN}) + \frac{1}{\sqrt{2}} F_{BC} = 0$$

or

$$F_{BD} + 0.79057 F_{BC} = -7.8262 \text{ kN}$$

$$+\uparrow \Sigma F_y = 0: \frac{1}{\sqrt{5}} F_{BD} + \frac{1}{\sqrt{5}} (7.8262 \text{ kN}) - \frac{1}{\sqrt{2}} F_{BC} - 2 \text{ kN} = 0$$

or

$$F_{BD} - 1.58114 F_{BC} = -3.3541$$

Multiply Eq. (1) by 2 and add Eq. (2):

$$3F_{BD} = -19.0065$$

$$F_{BD} = -6.3355 \text{ kN}$$

$$F_{BD} = 6.34 \text{ kN} \quad C \blacktriangleleft$$

Subtract Eq. (2) from Eq. (1):

$$2.37111 F_{BC} = -4.4721$$

$$F_{BC} = -1.8861 \text{ kN}$$

$$F_{BC} = 1.886 \text{ kN} \quad C \blacktriangleleft$$

Free body: Joint C:

$$+\uparrow \Sigma F_y = 0: \frac{2}{\sqrt{5}} F_{CD} - \frac{1}{\sqrt{2}} (1.8861 \text{ kN}) = 0$$

$$F_{CD} = +1.4911 \text{ kN}$$

$$F_{CD} = 1.491 \text{ kN} \quad T \blacktriangleleft$$

$$+\rightarrow \Sigma F_x = 0: F_{CE} - 7.00 \text{ kN} + \frac{1}{\sqrt{2}} (1.8861 \text{ kN}) + \frac{1}{\sqrt{5}} (1.4911 \text{ kN}) = 0$$

$$F_{CE} = +5.000 \text{ kN}$$

$$F_{CE} = 5.00 \text{ kN} \quad T \blacktriangleleft$$

Free body: Joint D:

$$+\rightarrow \Sigma F_x = 0: \frac{2}{\sqrt{5}} F_{DF} + \frac{1}{\sqrt{2}} F_{DE} + \frac{2}{\sqrt{5}} (6.3355 \text{ kN}) - \frac{1}{\sqrt{5}} (1.4911 \text{ kN}) = 0$$

or

$$F_{DF} + 0.79057 F_{DE} = -5.5900 \text{ kN}$$

(1)

$$+\uparrow \Sigma F_y = 0: \frac{1}{\sqrt{5}} F_{DF} - \frac{1}{\sqrt{2}} F_{DE} + \frac{1}{\sqrt{5}} (6.3355 \text{ kN}) - \frac{2}{\sqrt{5}} (1.4911 \text{ kN}) - 2 \text{ kN} = 0$$

or

$$F_{DF} - 0.79057 F_{DE} = -1.1188 \text{ kN}$$

(2)

Add Eqs. (1) and (2):

$$2F_{DF} = -6.7088 \text{ kN}$$

$$F_{DF} = -3.3544 \text{ kN}$$

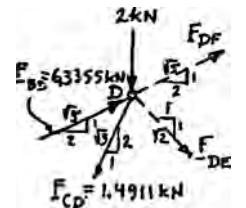
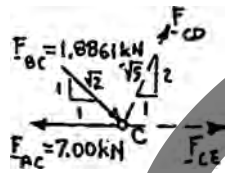
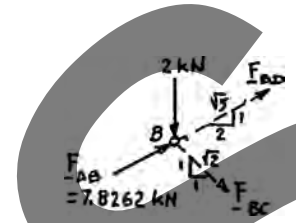
$$F_{DF} = 3.35 \text{ kN} \quad C \blacktriangleleft$$

Subtract Eq. (2) from Eq. (1):

$$1.58114 F_{DE} = -4.4712 \text{ kN}$$

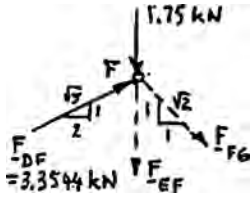
$$F_{DE} = -2.8278 \text{ kN}$$

$$F_{DE} = 2.83 \text{ kN} \quad C \blacktriangleleft$$



PROBLEM 6.13 (Continued)

Free body: Joint F:



$$+\rightarrow \Sigma F_x = 0: \quad \frac{1}{\sqrt{2}} F_{FG} + \frac{2}{\sqrt{5}} (3.3544 \text{ kN}) = 0$$

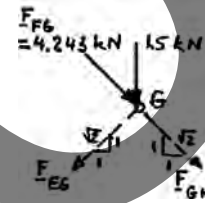
$$F_{FG} = -4.243 \text{ kN}$$

$$F_{FG} = 4.24 \text{ kN} \quad C \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: \quad -F_{EF} - 1.75 \text{ kN} + \frac{1}{\sqrt{5}} (3.3544 \text{ kN}) - \frac{1}{\sqrt{2}} (-4.243 \text{ kN}) = 0$$

$$F_{EF} = 2.750 \text{ kN}$$

$$F_{EF} = 2.75 \text{ kN} \quad T \blacktriangleleft$$



Free body: Joint G:

$$+\rightarrow \Sigma F_x = 0: \quad \frac{1}{\sqrt{2}} F_{GH} - \frac{1}{\sqrt{2}} F_{EG} + \frac{1}{\sqrt{2}} (4.243 \text{ kN}) = 0$$

or

$$F_{GH} - F_{EG} = -4.243 \text{ kN} \quad (1)$$

$$+\uparrow \Sigma F_y = 0: \quad -\frac{1}{\sqrt{2}} F_{GH} - \frac{1}{\sqrt{2}} F_{EG} - \frac{1}{\sqrt{2}} (4.243 \text{ kN}) - 1.5 \text{ kN} = 0$$

or

$$F_{GH} + F_{EG} = -6.364 \text{ kN} \quad (2)$$

Add Eqs. (1) and (2):

$$2F_{GH} = -10.607$$

$$F_{GH} = -5.303$$

$$F_{GH} = 5.30 \text{ kN} \quad C \blacktriangleleft$$

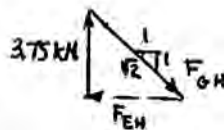
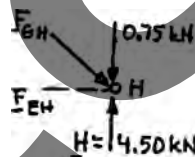
Subtract Eq. (1) from Eq. (2):

$$2F_{EG} = -2.121 \text{ kN}$$

$$F_{EG} = -1.0605 \text{ kN}$$

$$F_{EG} = 1.061 \text{ kN} \quad C \blacktriangleleft$$

Free body: Joint H:



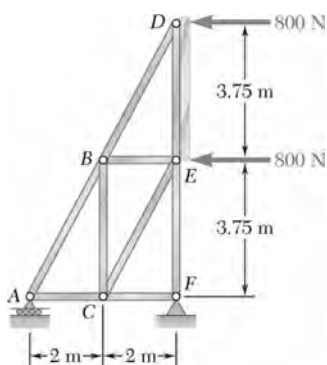
$$\frac{F_{EH}}{1} = \frac{3.75 \text{ kN}}{1}$$

$$F_{EH} = 3.75 \text{ kN} \quad T \blacktriangleleft$$

We can also write

$$\frac{F_{GH}}{\sqrt{2}} = \frac{3.75 \text{ kN}}{1}$$

$$F_{GH} = 5.30 \text{ kN} \quad C \quad (\text{Checks})$$

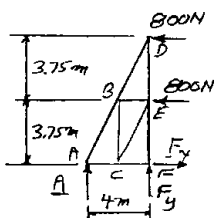


PROBLEM 6.14

The truss shown is one of several supporting an advertising panel. Determine the force in each member of the truss for a wind load equivalent to the two forces shown. State whether each member is in tension or compression.

SOLUTION

Free body: Entire truss:



$$+\circlearrowleft \Sigma M_F = 0: (800 \text{ N})(7.5 \text{ m}) + (800 \text{ N})(3.75 \text{ m}) - A(2 \text{ m}) = 0$$

$$A = +2250 \text{ N} \quad A = 2250 \text{ N} \uparrow$$

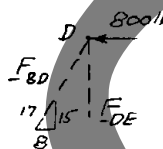
$$+\uparrow \Sigma F_y = 0: 2250 \text{ N} + F_y = 0$$

$$F_y = -2250 \text{ N} \quad F_y = 2250 \text{ N} \downarrow$$

$$+\rightarrow \Sigma F_x = 0: -800 \text{ N} - 800 \text{ N} + F_x = 0$$

$$F_x = +1600 \text{ N} \quad F_x = 1600 \text{ N} \rightarrow$$

Joint D:

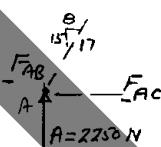


$$\frac{800 \text{ N}}{8} = \frac{F_{DE}}{15} = \frac{F_{BD}}{17}$$

$$F_{BD} = 1700 \text{ N} \quad C \quad \blacktriangleleft$$

$$F_{DE} = 1500 \text{ N} \quad T \quad \blacktriangleleft$$

Joint A:

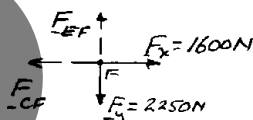


$$\frac{2250 \text{ N}}{15} = \frac{F_{AB}}{17} = \frac{F_{AC}}{8}$$

$$F_{AB} = 2250 \text{ N} \quad C \quad \blacktriangleleft$$

$$F_{AC} = 1200 \text{ N} \quad T \quad \blacktriangleleft$$

Joint F:



$$+\rightarrow \Sigma F_x = 0: 1600 \text{ N} - F_{CF} = 0$$

$$F_{CF} = +1600 \text{ N}$$

$$F_{CF} = 1600 \text{ N} \quad T \quad \blacktriangleleft$$

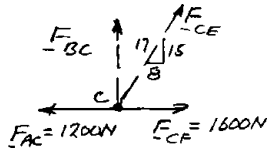
$$+\uparrow \Sigma F_y = 0: F_{EF} - 2250 \text{ N} = 0$$

$$F_{EF} = +2250 \text{ N}$$

$$F_{EF} = 2250 \text{ N} \quad T \quad \blacktriangleleft$$

PROBLEM 6.14 (Continued)

Joint C:



$$\rightarrow \Sigma F_x = 0: \frac{8}{17} F_{CE} - 1200 \text{ N} + 1600 \text{ N} = 0$$

$$F_{CE} = -850 \text{ N}$$

$$F_{CE} = 850 \text{ N} \quad C \leftarrow$$

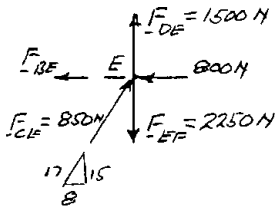
$$+\uparrow \Sigma F_y = 0: F_{BC} + \frac{15}{17} F_{CE} = 0$$

$$F_{BC} = -\frac{15}{17} F_{CE} = -\frac{15}{17} (-850 \text{ N})$$

$$F_{BC} = +750 \text{ N}$$

$$F_{BC} = 750 \text{ N} \quad T \leftarrow$$

Joint E:



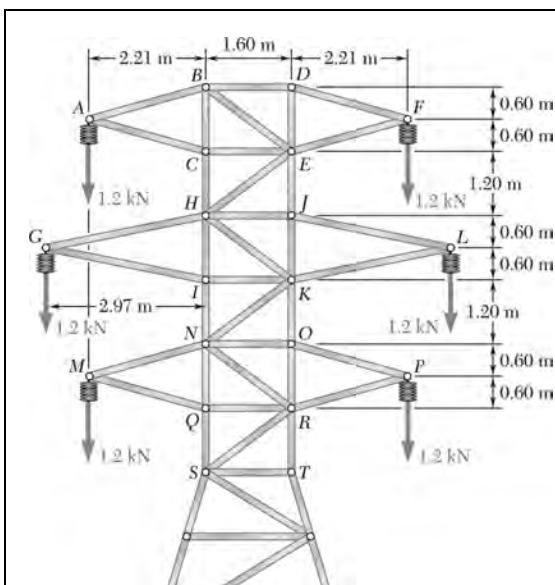
$$\rightarrow \Sigma F_x = 0: -F_{BE} - 800 \text{ N} + \frac{8}{17} (850 \text{ N}) = 0$$

$$F_{BE} = -400 \text{ N}$$

$$F_{BE} = 400 \text{ N} \quad C \leftarrow$$

$$+\uparrow \Sigma F_y = 0: 1500 \text{ N} - 2250 \text{ N} + \frac{15}{17} (850 \text{ N}) = 0$$

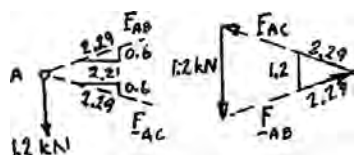
$$0 = 0 \quad (\text{checks})$$



PROBLEM 6.23

The portion of truss shown represents the upper part of a power transmission line tower. For the given loading, determine the force in each of the members located above HJ . State whether each member is in tension or compression.

SOLUTION

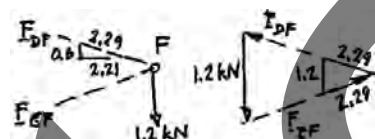


Free body: Joint A:

$$\frac{F_{AB}}{2.29} = \frac{F_{AC}}{2.29} = \frac{1.2 \text{ kN}}{1.2}$$

$$F_{AB} = 2.29 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{AC} = 2.29 \text{ kN} \quad C \quad \blacktriangleleft$$

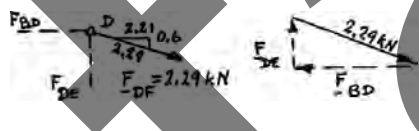


Free body: Joint F:

$$\frac{F_{DF}}{2.29} = \frac{F_{EF}}{2.29} = \frac{1.2 \text{ kN}}{2.1}$$

$$F_{DF} = 2.29 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{EF} = 2.29 \text{ kN} \quad C \quad \blacktriangleleft$$



Free body: Joint D:

$$\frac{F_{BD}}{2.21} = \frac{F_{DE}}{0.6} = \frac{2.29 \text{ kN}}{2.29}$$

$$F_{BD} = 2.21 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{DE} = 0.600 \text{ kN} \quad C \quad \blacktriangleleft$$

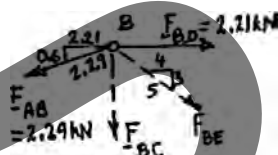
Free body: Joint B:

$$+\rightarrow \Sigma F_x = 0: \quad \frac{4}{5} F_{BE} + 2.21 \text{ kN} - \frac{2.21}{2.29} (2.29 \text{ kN}) = 0$$

$$F_{BE} = 0 \quad \blacktriangleleft$$

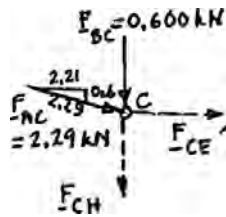
$$+\uparrow \Sigma F_y = 0: \quad -F_{BC} - \frac{3}{5} (0) - \frac{0.6}{2.29} (2.29 \text{ kN}) = 0$$

$$F_{BC} = -0.600 \text{ kN} \quad F_{BC} = 0.600 \text{ kN} \quad C \quad \blacktriangleleft$$



PROBLEM 6.23 (Continued)

Free body: Joint C:



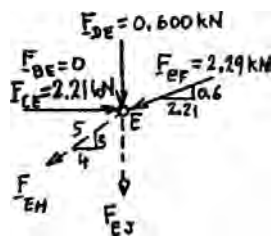
$$\rightarrow \Sigma F_x = 0: F_{CE} + \frac{2.21}{2.29}(2.29 \text{ kN}) = 0$$

$$F_{CE} = -2.21 \text{ kN} \quad F_{CE} = 2.21 \text{ kN} \quad C \leftarrow$$

$$+\uparrow \Sigma F_y = 0: -F_{CH} - 0.600 \text{ kN} - \frac{0.6}{2.29}(2.29 \text{ kN}) = 0$$

$$F_{CH} = -1.200 \text{ kN} \quad F_{CH} = 1.200 \text{ kN} \quad C \leftarrow$$

Free body: Joint E:

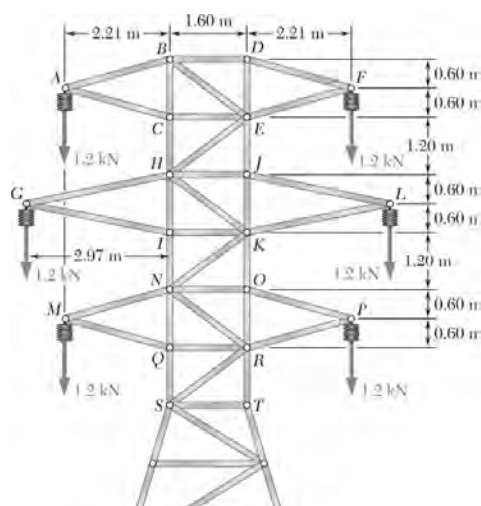


$$\rightarrow \Sigma F_x = 0: 2.21 \text{ kN} - \frac{2.21}{2.29}(2.29 \text{ kN}) - \frac{4}{5}F_{EH} = 0$$

$$F_{EH} = 0 \quad \leftarrow$$

$$+\uparrow \Sigma F_y = 0: -F_{EJ} - 0.600 \text{ kN} - \frac{0.6}{2.29}(2.29 \text{ kN}) - 0 = 0$$

$$F_{EJ} = -1.200 \text{ kN} \quad F_{EJ} = 1.200 \text{ kN} \quad C \leftarrow$$

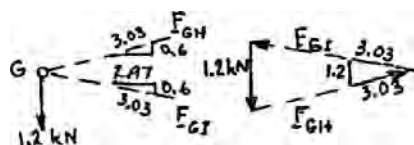


PROBLEM 6.24

For the tower and loading of Problem 6.23 and knowing that $F_{CH} = F_{EJ} = 1.2 \text{ kN}$ and $F_{EH} = 0$, determine the force in member HJ and in each of the members located between HJ and NO . State whether each member is in tension or compression.

PROBLEM 6.23 The portion of truss shown represents the upper part of a power transmission line tower. For the given loading, determine the force in each of the members located above HJ . State whether each member is in tension or compression.

SOLUTION

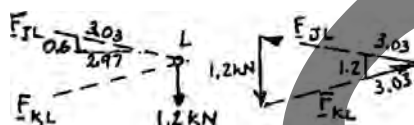


Free body: Joint G :

$$\frac{F_{GH}}{3.03} = \frac{F_{GI}}{3.03} = \frac{1.2 \text{ kN}}{1.2}$$

$$F_{GH} = 3.03 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{GI} = 3.03 \text{ kN} \quad C \quad \blacktriangleleft$$

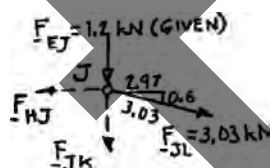


Free body: Joint L :

$$\frac{F_{JL}}{3.03} = \frac{F_{KL}}{3.03} = \frac{1.2 \text{ kN}}{1.2}$$

$$F_{JL} = 3.03 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{KL} = 3.03 \text{ kN} \quad C \quad \blacktriangleleft$$



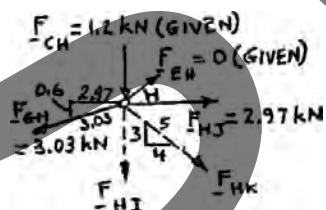
Free body: Joint J :

$$+\rightarrow \Sigma F_x = 0: -F_{HJ} + \frac{2.97}{3.03}(3.03 \text{ kN}) = 0$$

$$F_{HJ} = 2.97 \text{ kN} \quad T \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{JK} - 1.2 \text{ kN} - \frac{0.6}{3.03}(3.03 \text{ kN}) = 0$$

$$F_{JK} = -1.800 \text{ kN} \quad F_{JK} = 1.800 \text{ kN} \quad C \quad \blacktriangleleft$$



Free body: Joint H :

$$+\rightarrow \Sigma F_x = 0: \frac{4}{5}F_{HK} + 2.97 \text{ kN} - \frac{2.97}{3.03}(3.03 \text{ kN}) = 0$$

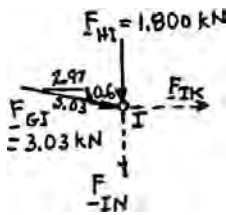
$$F_{HK} = 0 \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{HI} - 1.2 \text{ kN} - \frac{0.6}{3.03}(3.03 \text{ kN}) - \frac{3}{5}(0) = 0$$

$$F_{HI} = -1.800 \text{ kN} \quad F_{HI} = 1.800 \text{ kN} \quad C \quad \blacktriangleleft$$

PROBLEM 6.24 (Continued)

Free body: Joint I:



$$+\rightarrow \Sigma F_x = 0: F_{IK} + \frac{2.97}{3.03}(3.03 \text{ kN}) = 0$$

$$F_{IK} = -2.97 \text{ kN}$$

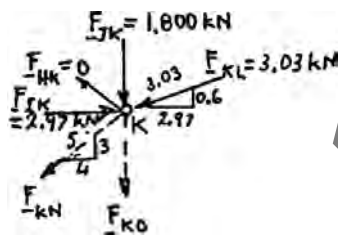
$$F_{IK} = 2.97 \text{ kN} \quad C \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{IN} - 1.800 \text{ kN} - \frac{0.6}{3.03}(3.03 \text{ kN}) = 0$$

$$F_{IN} = -2.40 \text{ kN}$$

$$F_{IN} = 2.40 \text{ kN} \quad C \quad \blacktriangleleft$$

Free body: Joint K:



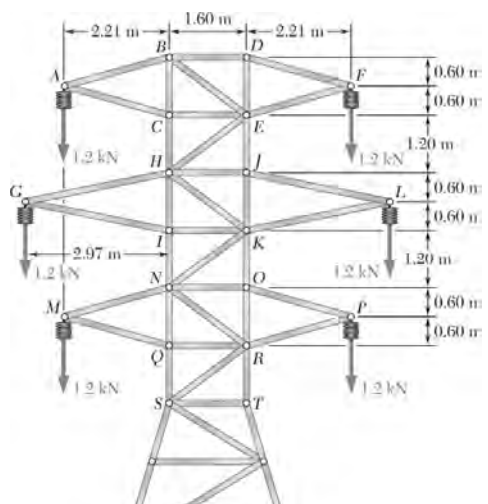
$$+\rightarrow \Sigma F_x = 0: -\frac{4}{5}F_{KN} + 2.97 \text{ kN} - \frac{2.97}{3.03}(3.03 \text{ kN}) = 0$$

$$F_{KN} = 0 \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{KO} - \frac{0.6}{3.03}(3.03 \text{ kN}) - 1.800 \text{ kN} - \frac{3}{5}(0) = 0$$

$$F_{KO} = -2.40 \text{ kN}$$

$$F_{KO} = 2.40 \text{ kN} \quad C \quad \blacktriangleleft$$

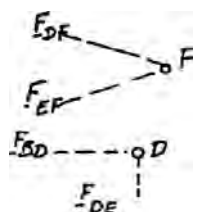


PROBLEM 6.25

Solve Problem 6.23 assuming that the cables hanging from the right side of the tower have fallen to the ground.

PROBLEM 6.23 The portion of truss shown represents the upper part of a power transmission line tower. For the given loading, determine the force in each of the members located above *HJ*. State whether each member is in tension or compression.

SOLUTION



Zero-Force Members:

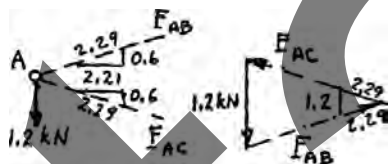
Considering joint *F*, we note that *DF* and *EF* are zero-force members:

$$F_{DF} = F_{EF} = 0 \quad \blacktriangleleft$$

Considering next joint *D*, we note that *BD* and *DE* are zero-force members:

$$F_{BD} = F_{DE} = 0 \quad \blacktriangleleft$$

Free body: Joint A:

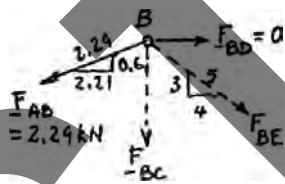


$$\frac{F_{AB}}{2.29} = \frac{F_{AC}}{2.29} = \frac{1.2 \text{ kN}}{1.2}$$

$$F_{AB} = 2.29 \text{ kN} \quad T \quad \blacktriangleleft$$

$$F_{AC} = 2.29 \text{ kN} \quad C \quad \blacktriangleleft$$

Free body: Joint B:



$$+\rightarrow \Sigma F_x = 0: \quad \frac{4}{5} F_{BE} - \frac{2.21}{2.29} (2.29 \text{ kN}) = 0$$

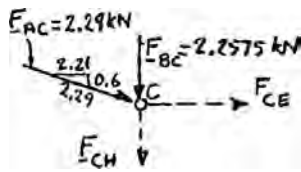
$$F_{BE} = 2.7625 \text{ kN} \quad F_{BE} = 2.76 \text{ kN} \quad T \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: \quad -F_{BC} - \frac{0.6}{2.29} (2.29 \text{ kN}) - \frac{3}{5} (2.7625 \text{ kN}) = 0$$

$$F_{BC} = -2.2575 \text{ kN} \quad F_{BC} = 2.26 \text{ kN} \quad C \quad \blacktriangleleft$$

PROBLEM 6.25 (Continued)

Free body: Joint C:



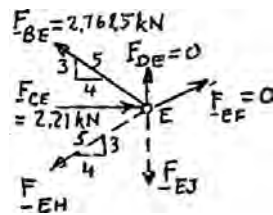
$$+\rightarrow \Sigma F_x = 0: F_{CE} + \frac{2.21}{2.29}(2.29 \text{ kN}) = 0$$

$$F_{CE} = 2.21 \text{ kN} \quad C \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{CH} - 2.2575 \text{ kN} - \frac{0.6}{2.29}(2.29 \text{ kN}) = 0$$

$$F_{CH} = -2.8575 \text{ kN} \quad F_{CH} = 2.86 \text{ kN} \quad C \blacktriangleleft$$

Free body: Joint E:



$$+\rightarrow \Sigma F_x = 0: -\frac{4}{5}F_{EH} - \frac{4}{5}(2.7625 \text{ kN}) + 2.21 \text{ kN} = 0$$

$$F_{EH} = 0 \quad \blacktriangleleft$$

$$+\uparrow \Sigma F_y = 0: -F_{EJ} + \frac{3}{5}(2.7625 \text{ kN}) - \frac{3}{5}(0) = 0$$

$$F_{EJ} = +1.6575 \text{ kN} \quad F_{EJ} = 1.658 \text{ kN} \quad T \blacktriangleleft$$