





CSE3103 : Database

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Motivation

- To have dynamic indexing structures that can evolve when records are added and deleted
 - Not the case for static indexes
 - Would have to be completely rebuilt
- Optimized for searches on *block devices*
- Both B trees and B+ trees are not binary
 - Objective is to increase *branching factor* (*degree* or fan-out) to reduce the number of device accesses

Binary vs. Higher-Order Tree

- ***Binary trees:***

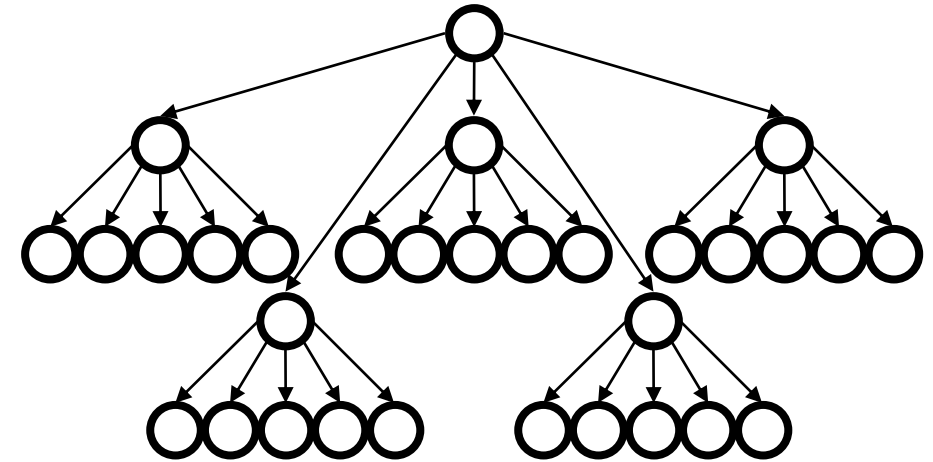
- Designed for in-memory searches.
- Try to minimize the number of memory accesses.

- ***Higher-order trees:***

- Designed for searching data on block devices.
- Try to minimize the number of device accesses.
 - Searching within a block is cheap.

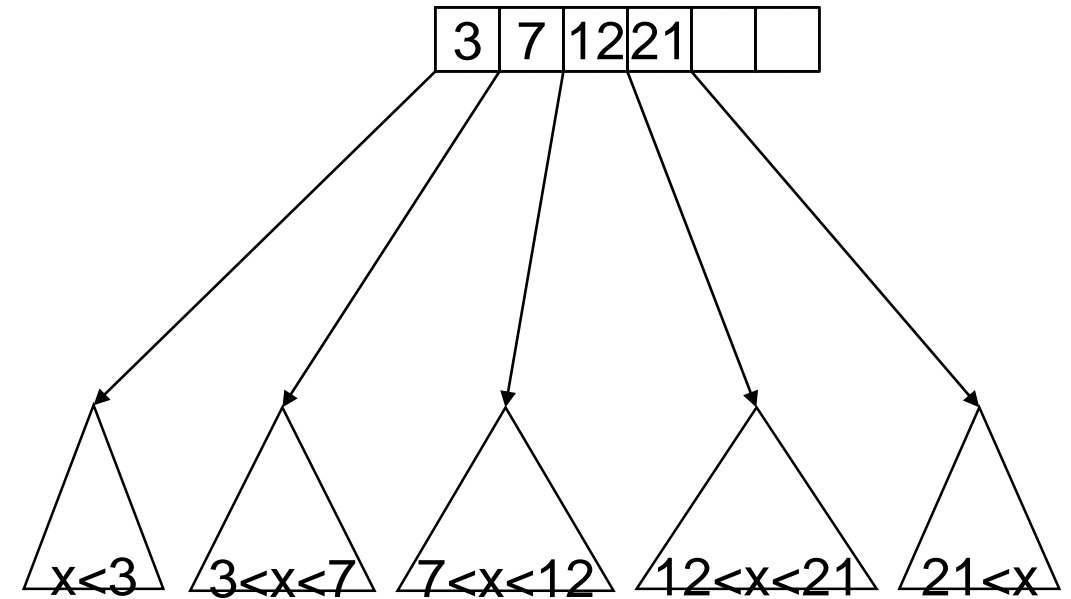
What is an M-ary Search Tree?

- ✓ Maximum branching factor of M
- ✓ Complete tree has depth = $\log_M N$
- ✓ Each internal node in a complete tree has $M - 1$ keys
- ✓ Binary search tree is a B Tree where M is 2



B Trees

- B-Trees are specialized M -ary search trees
- Each node has many keys
 - Sub-tree between two keys x and y contains values v such that $x \leq v < y$
 - binary search within a node to find correct sub-tree
- Each node takes one
 - full $\{page, block, line\}$ of memory (disk)



B-Tree Properties

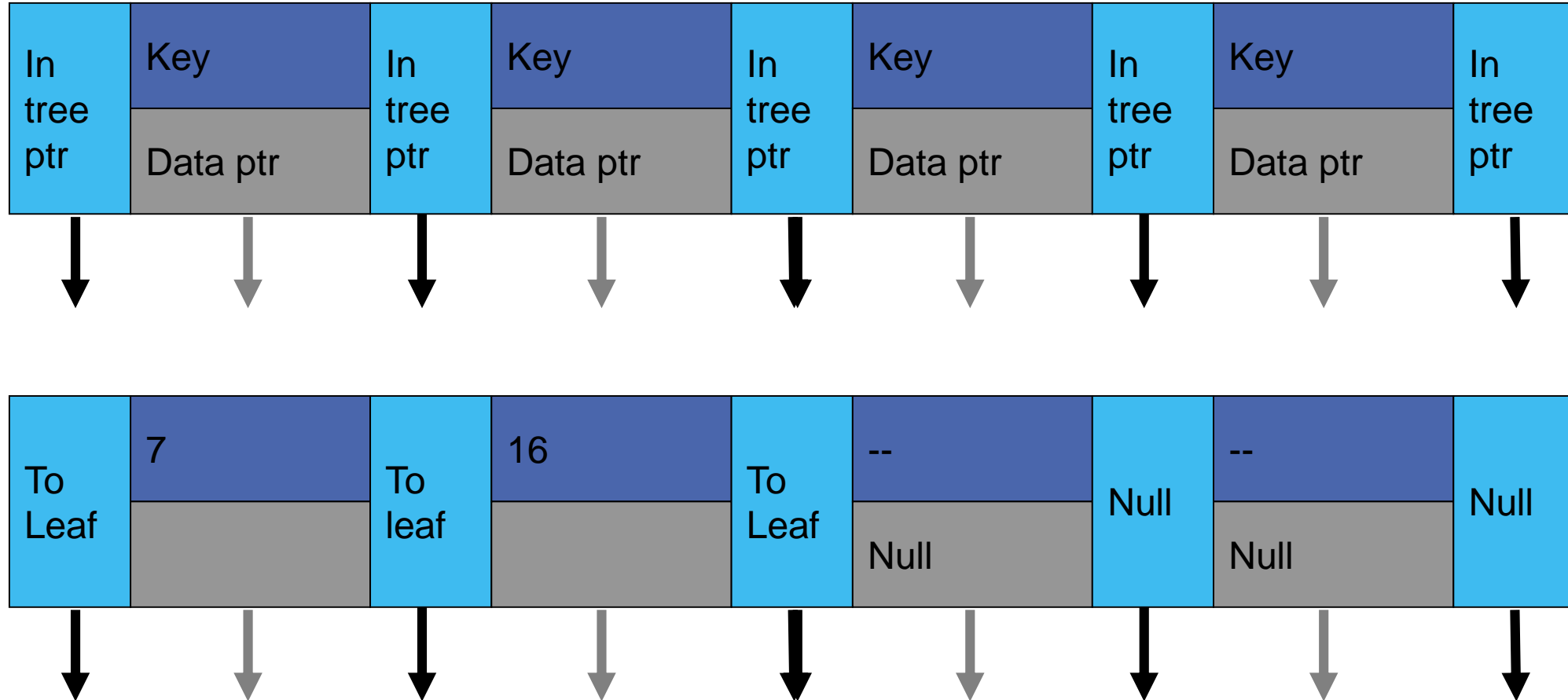
- Properties

- Maximum branching factor of M
- The root has between 2 and M children *or* at most $M-1$ keys
- All other nodes have between $\lceil M/2 \rceil$ and M record
- Keys + Data

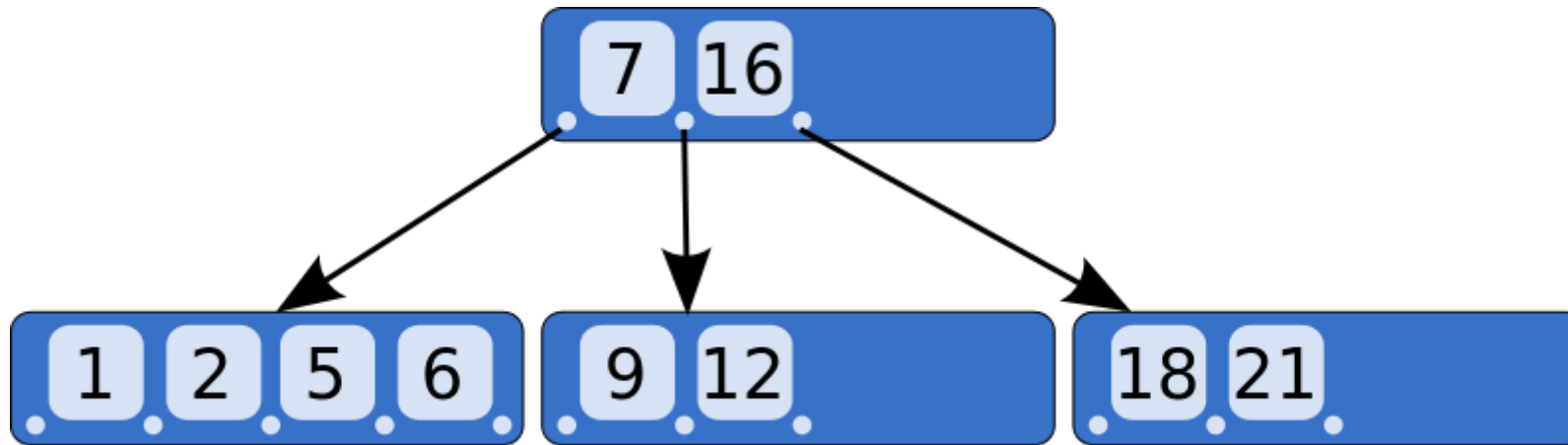
- Result

- tree is $O(\log M)$ deep
- all operations run in $O(\log M)$ time
- operations pull in about M items at a time

In Reality

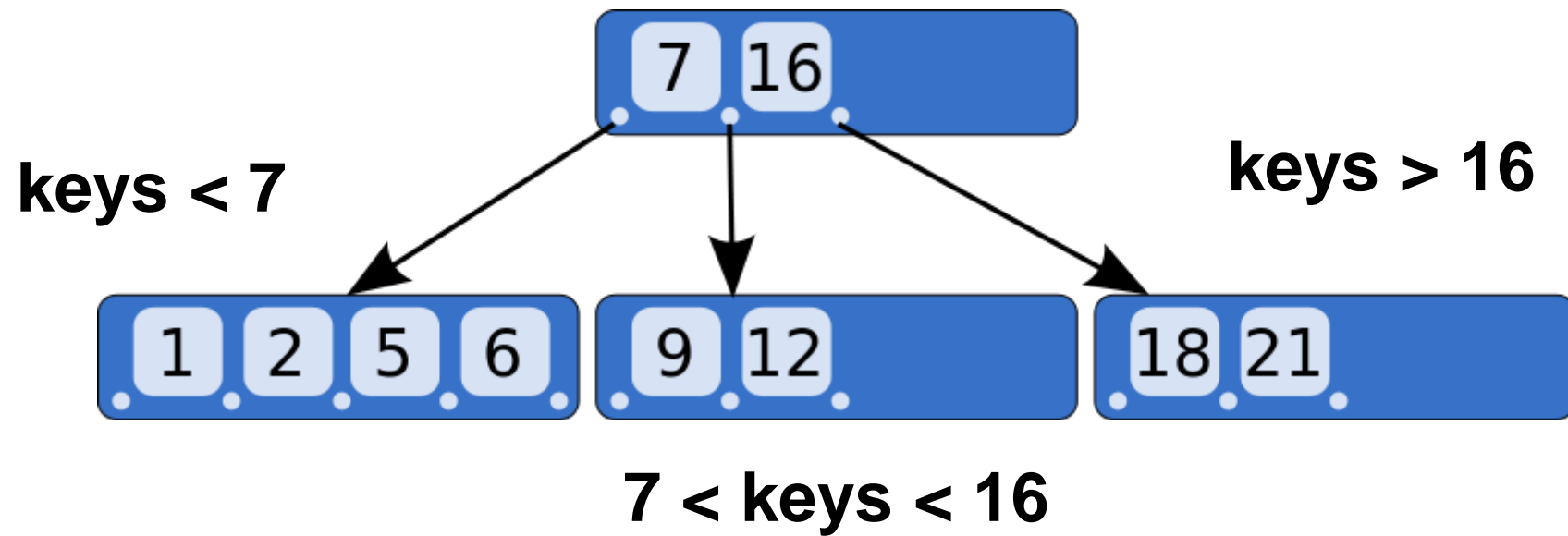


A very small B tree



Bottom nodes are leaf nodes: all their pointers are NULL

Searching the tree



B+ Tree

