

# Assignment 10

Parvez Alam : AI21RESCH01005

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Git Hub Link : <https://github.com/ParvezAlam123/Assignment-10>

## 1 Gate 21 :

Consider two identically distributed zero mean random variables  $U$  and  $V$ . Let the cumulative distribution function of  $U$  and  $2V$  be  $F(x)$  and  $G(x)$  respectively. Then for all value of  $x$

- (a)  $F(x)-G(x) \leq 0$  (b)  $(F(x)-G(x)) \leq 0$   
(c)  $F(x)-G(x) \geq 0$  (d)  $(F(x)-G(x))x \geq 0$

**Solution:**

Let  $X$  be a random variable having zero mean.  $X, U, V$  have the same distribution.

Since  $U$  and  $V$  are identically distributed. So

$$\begin{aligned} F(x) &= P(X \leq x) \\ G(x) &= P(2X \leq x) \\ &= P(X \leq x/2) \end{aligned}$$

1. if  $X > 0$  then

$$F(x) - G(x) > 0$$

2. if  $X < 0$  then

$$\begin{aligned} F(x) - G(x) &< 0 \\ \Rightarrow (F(x) - G(x))x &\geq 0 \end{aligned}$$

