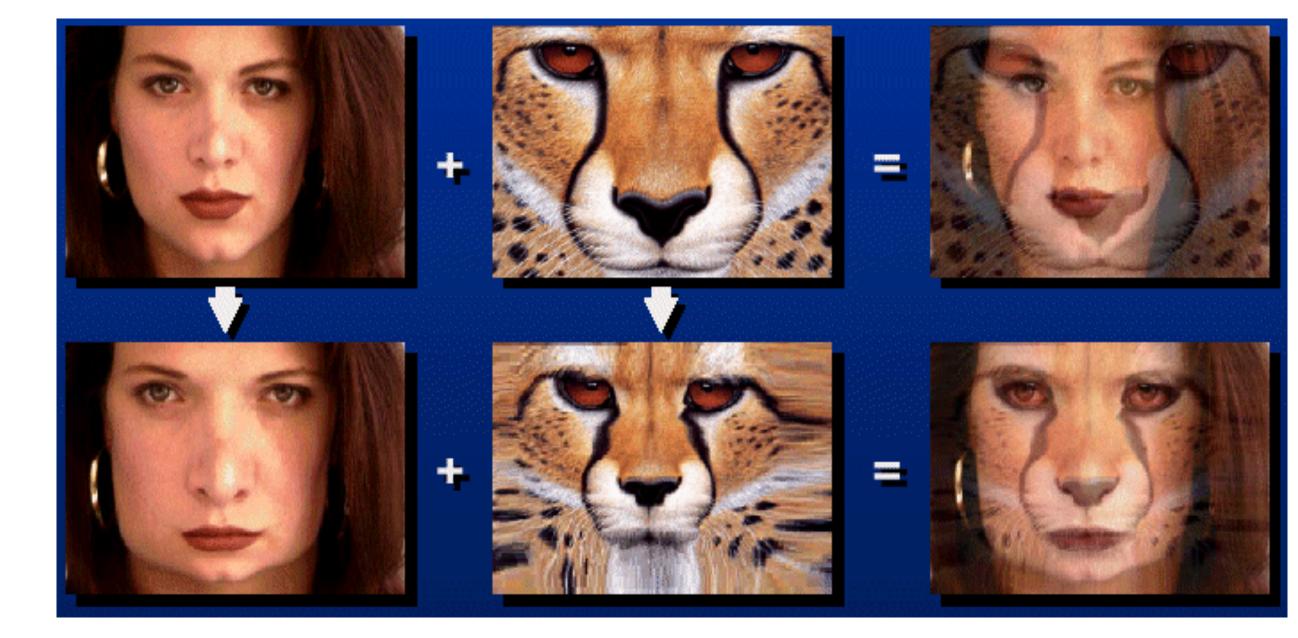
Morphing

For each intermediate frame It:

1. Interpolate feature locations

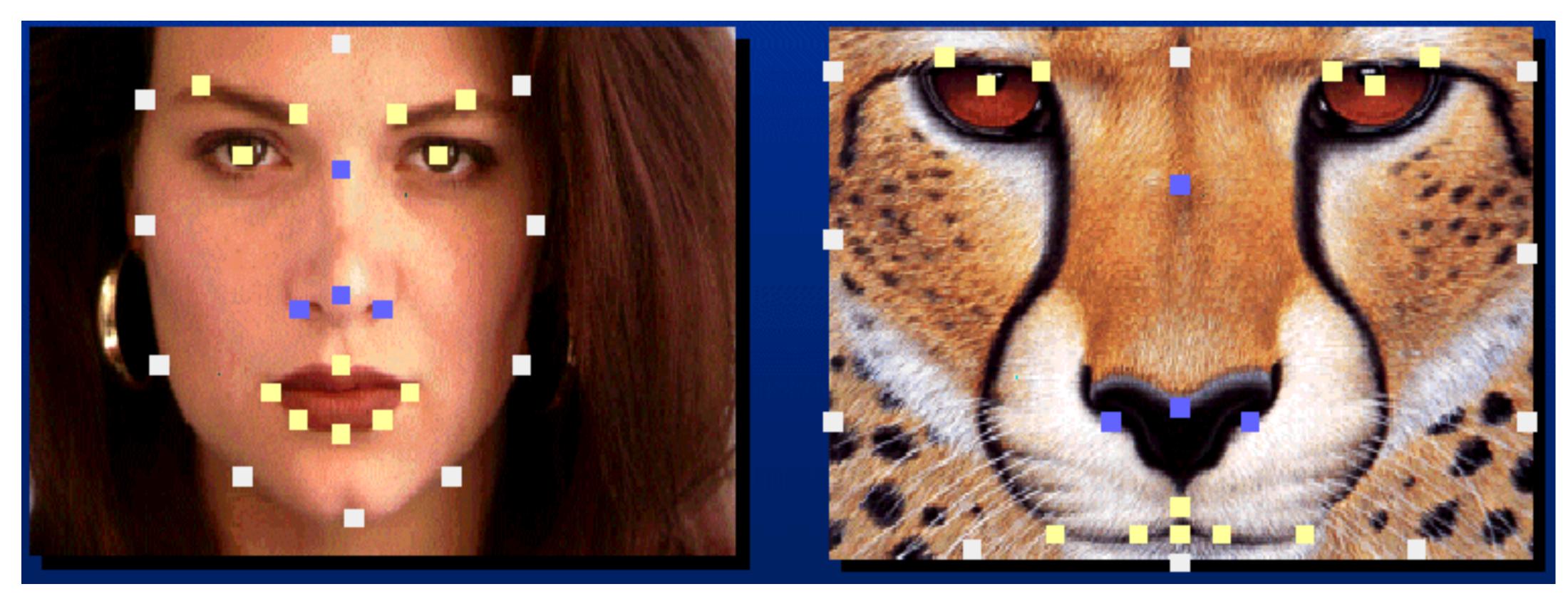
$$\mathbf{p}_i^t = (1 - \alpha)\mathbf{p}_i^0 + \alpha\mathbf{p}_i^1$$

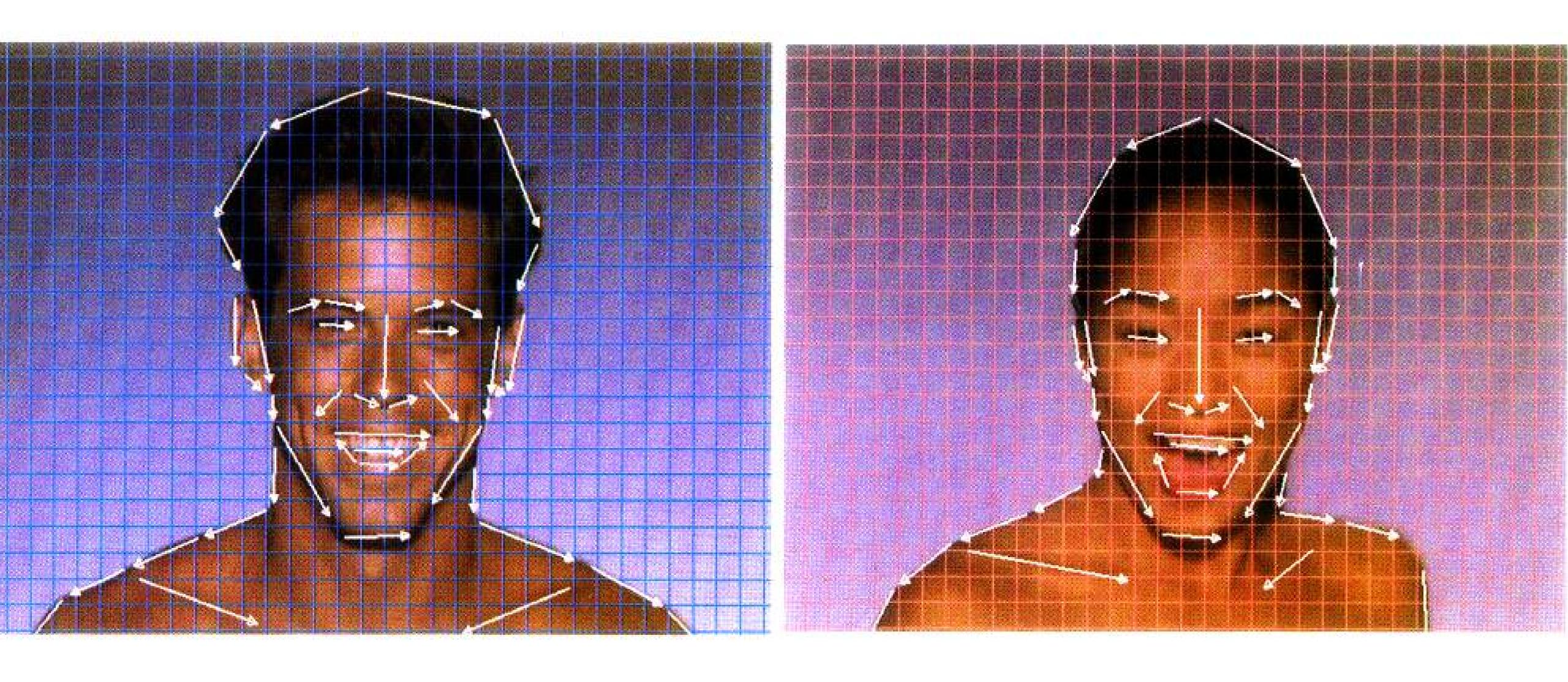
- 2. Perform two warps: one for I₀, one for I₁
 - Deduce a dense warp field from the pairs of features
 - Warp the pixels
- 3. Linearly interpolate the two warped images

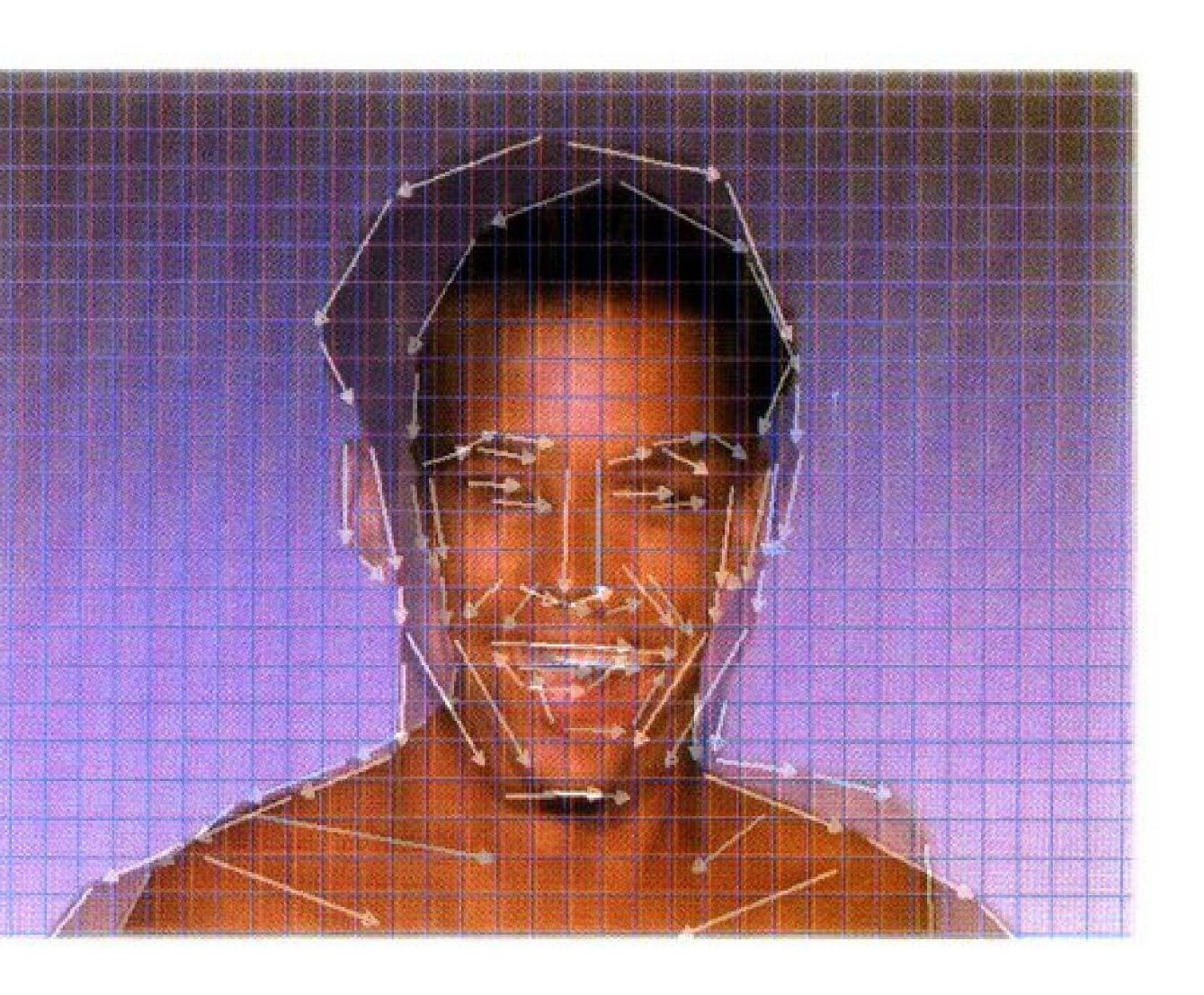


How can we specify the warp?

- Specify corresponding points
- interpolate to a complete warping function
- How do we do it?

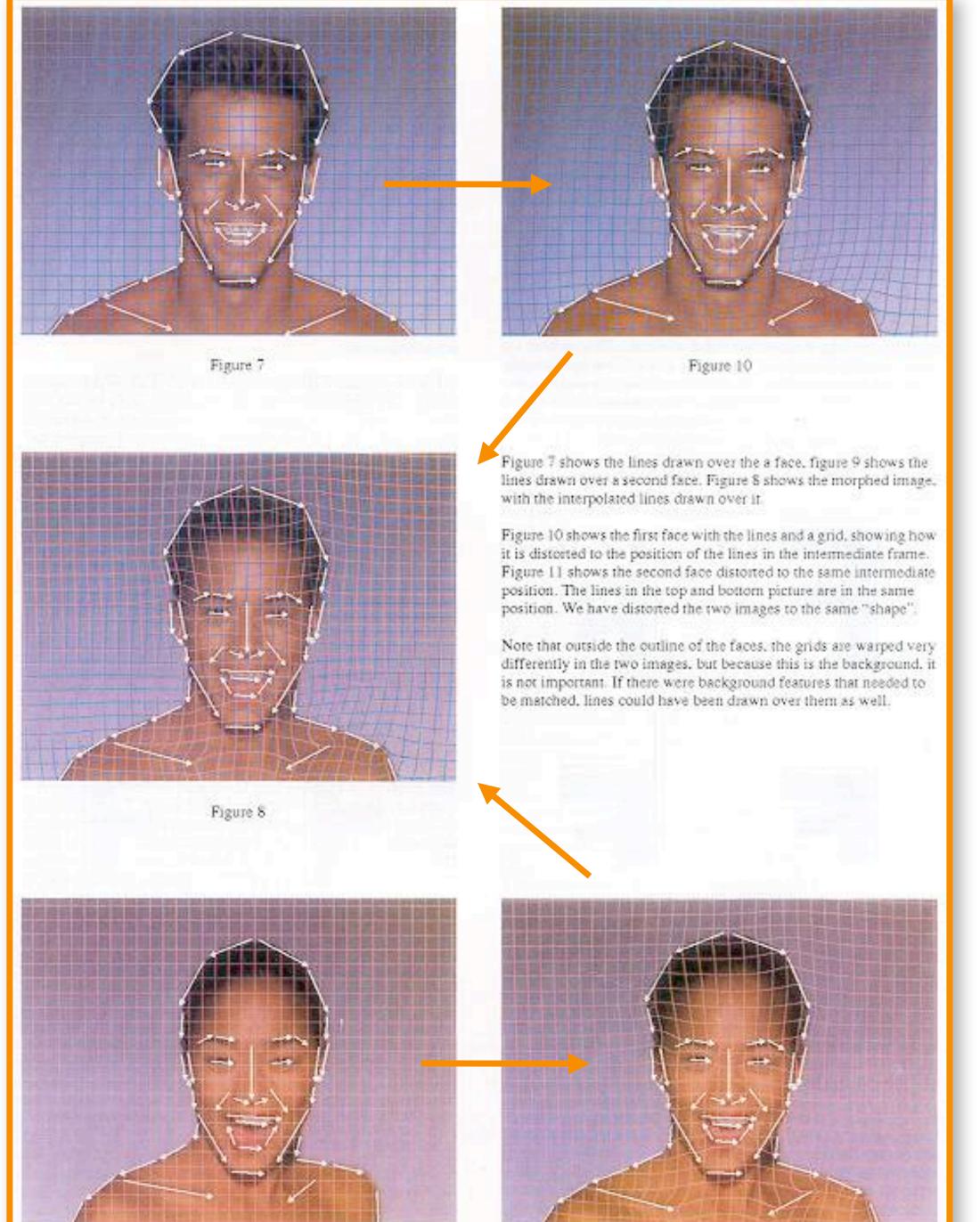






Image₀

Result



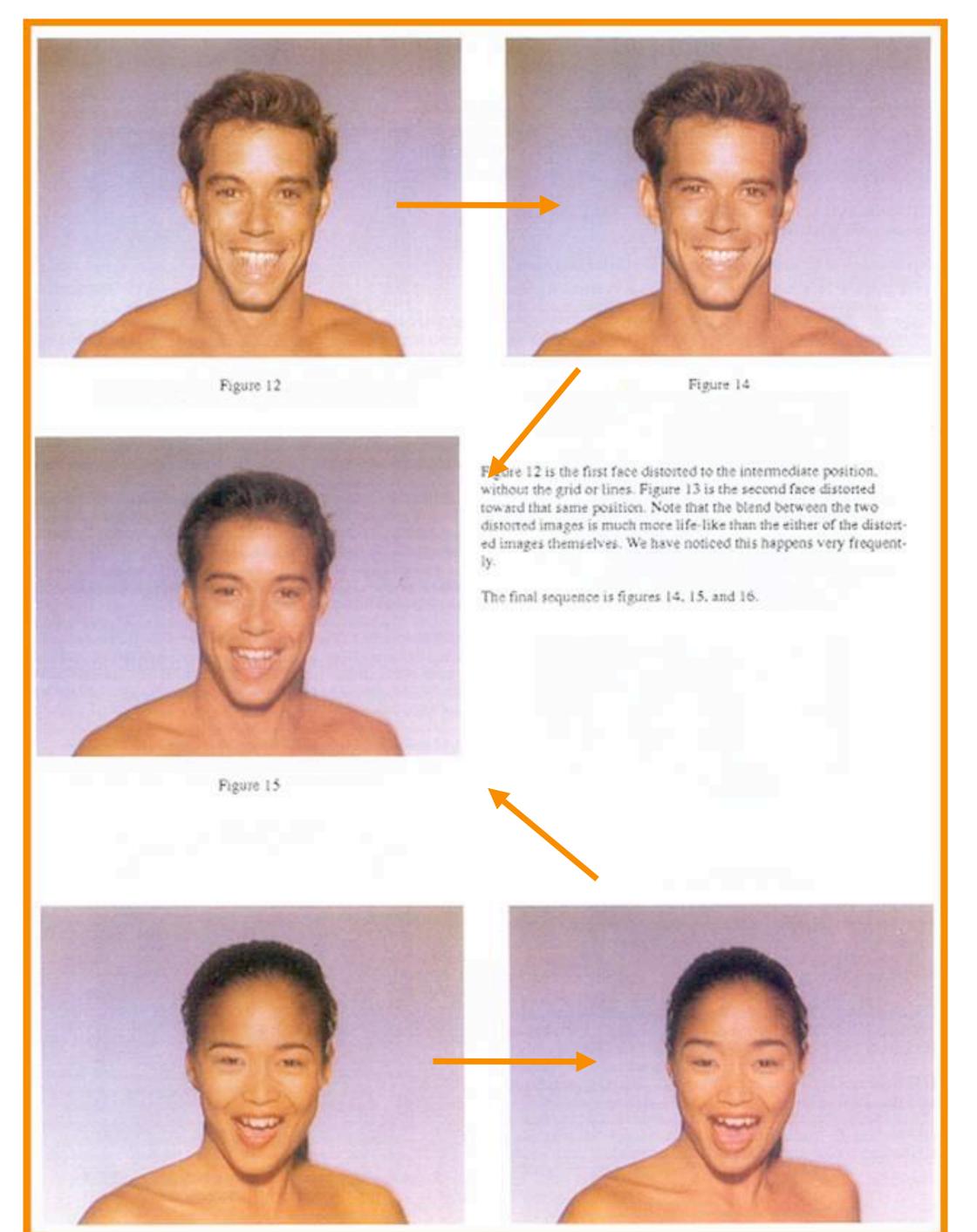
Warp₀

Image₁

Warp₁

Image₀

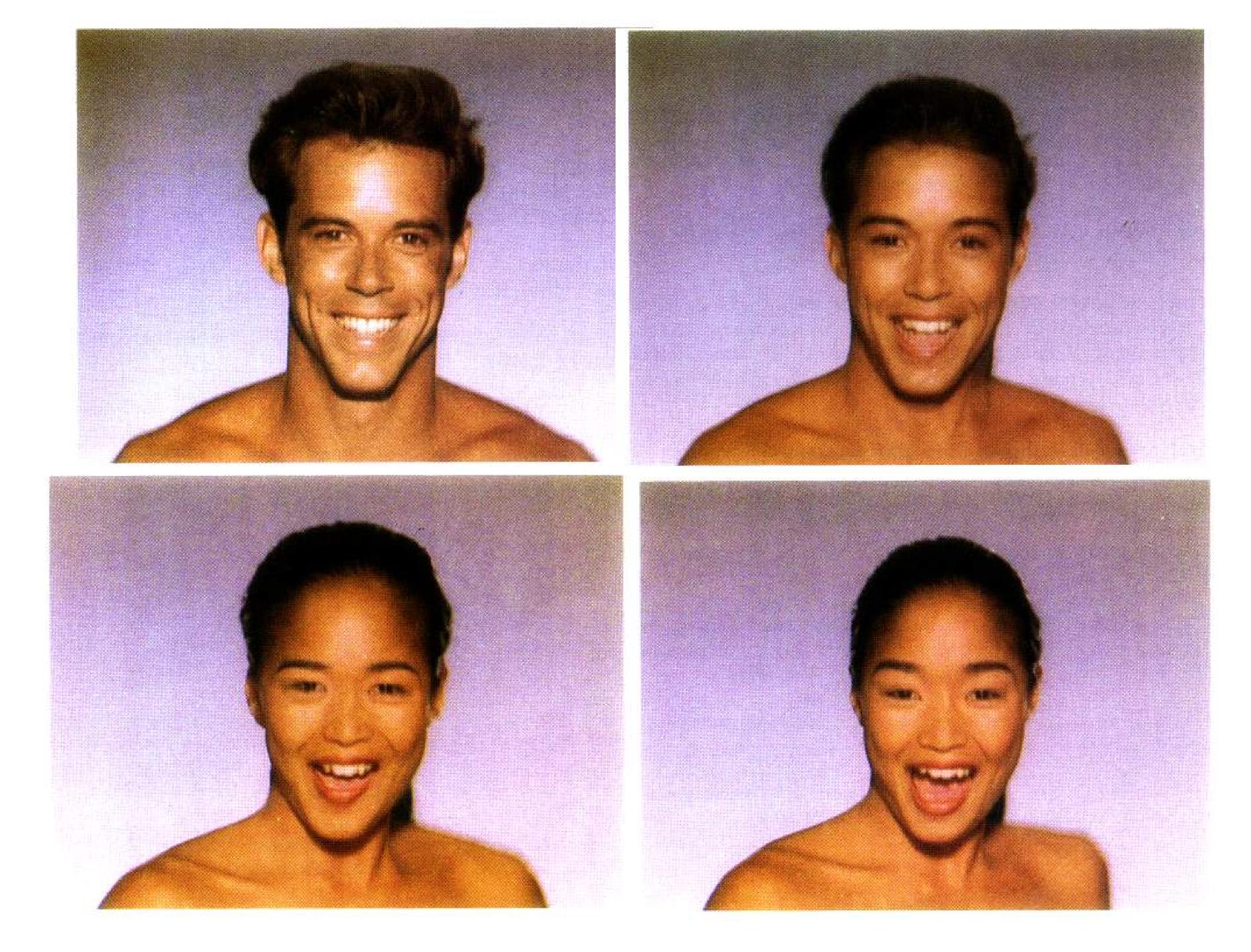
Result



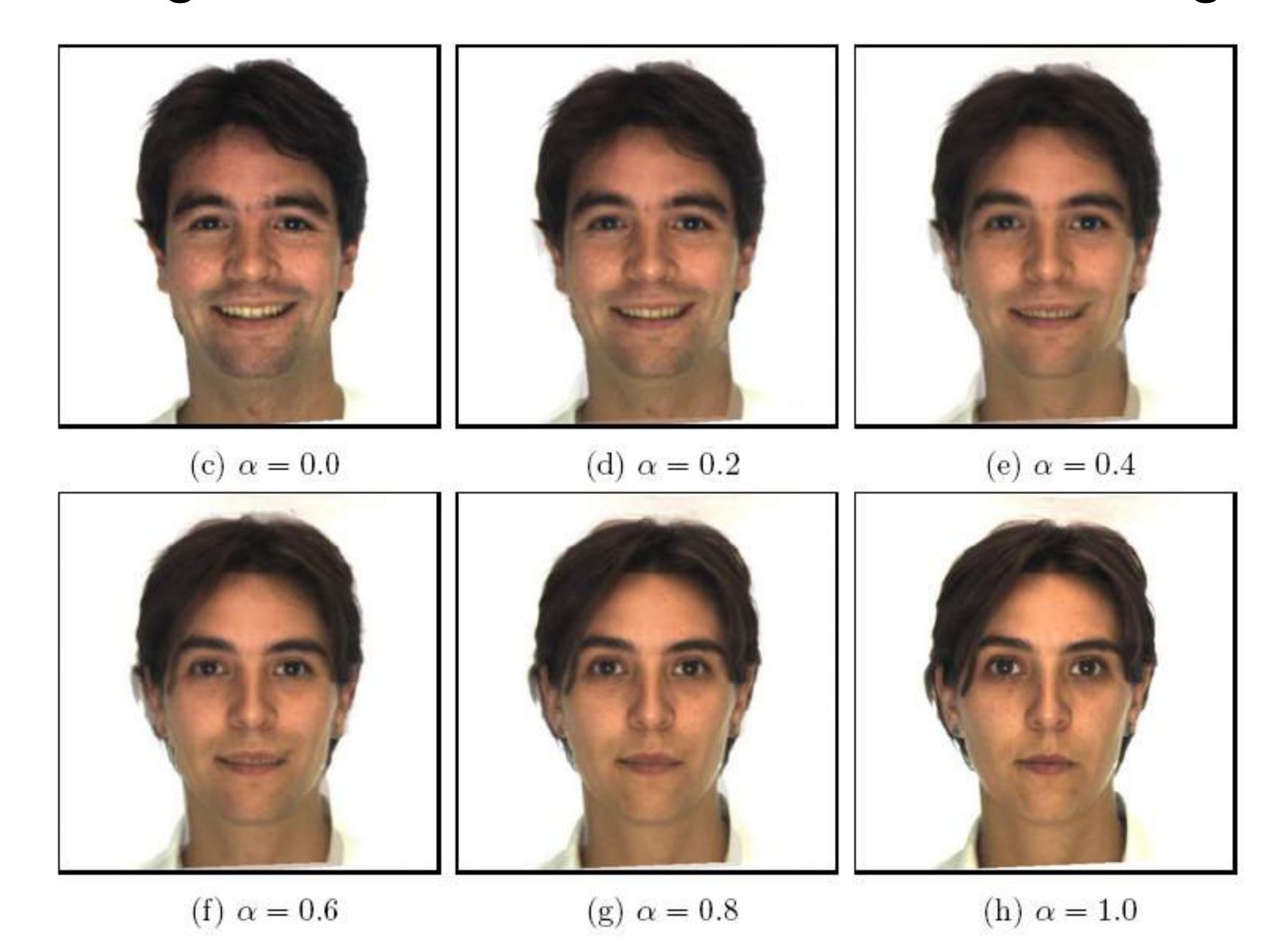
Warp₀

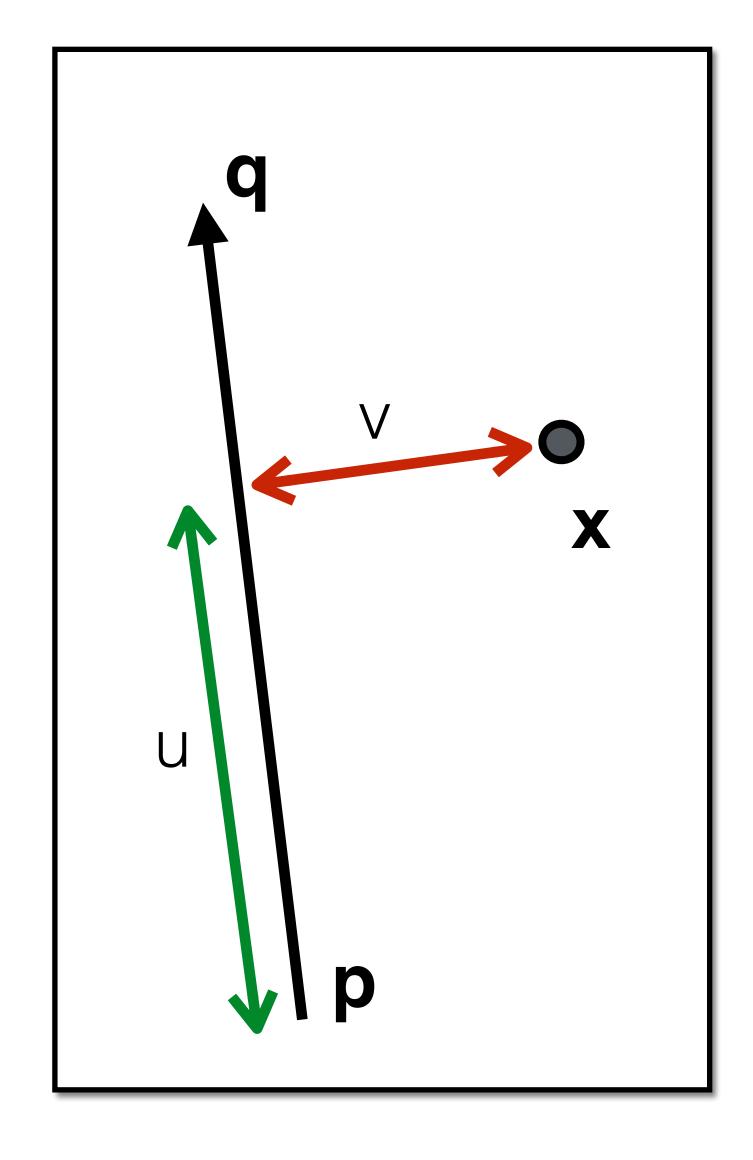
Image₁

Warp₁

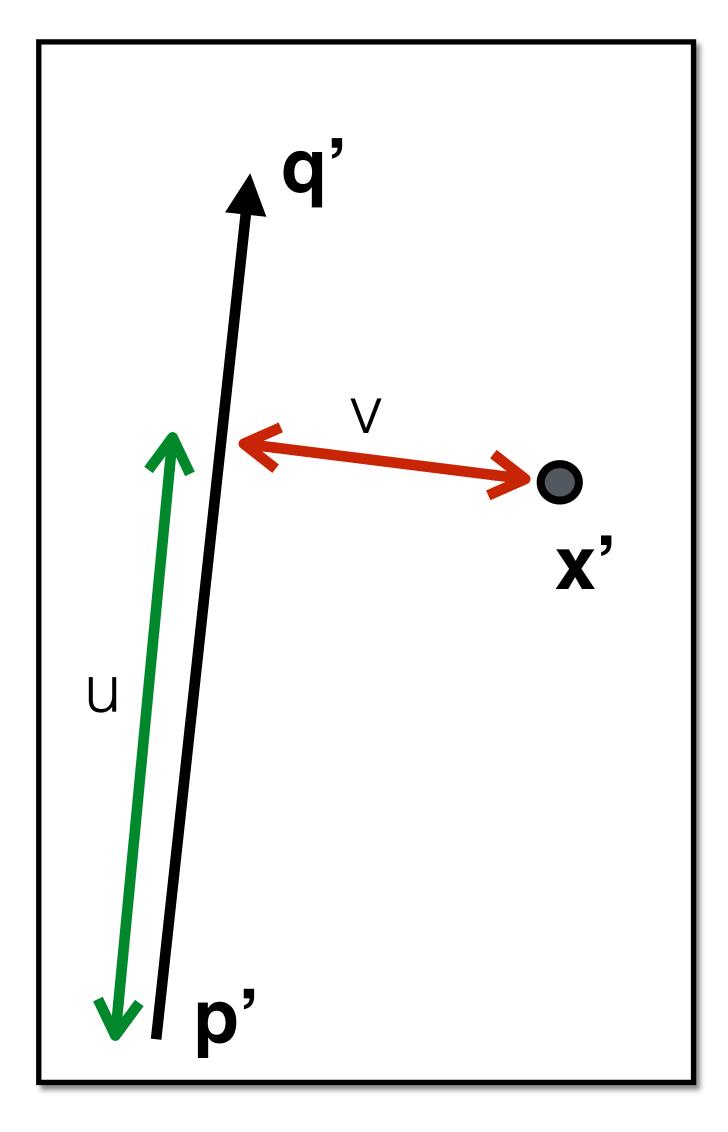


Extract foreground to avoid artifacts in the background



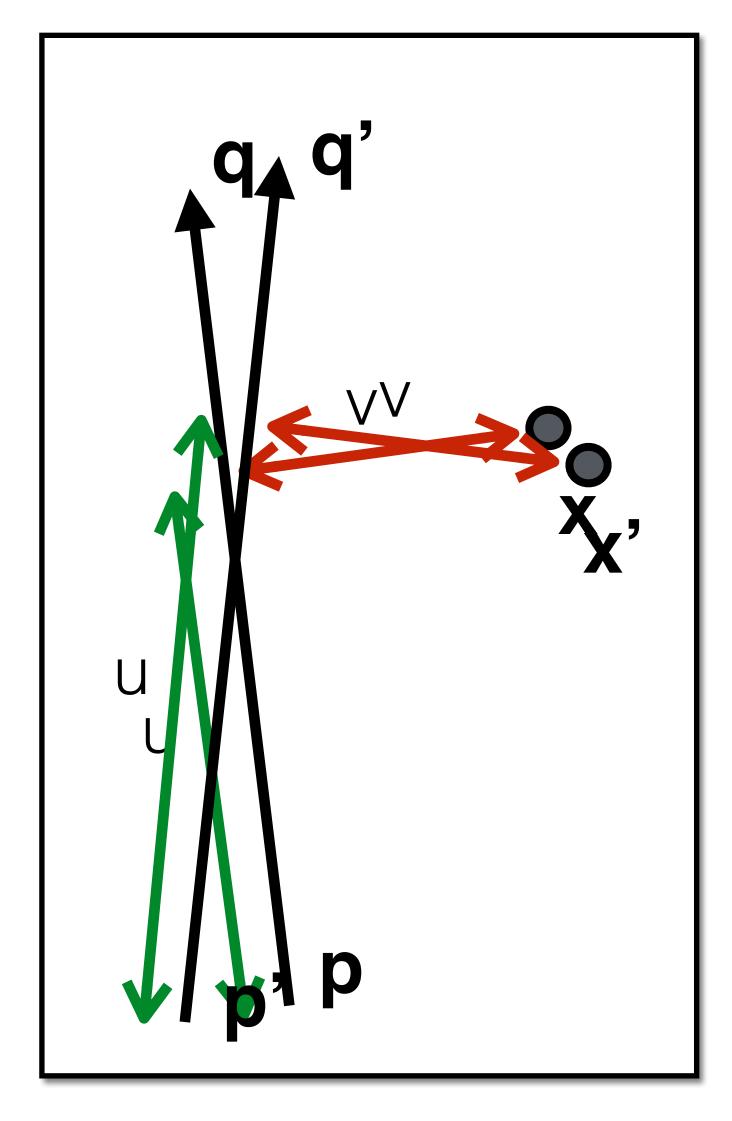


destination image



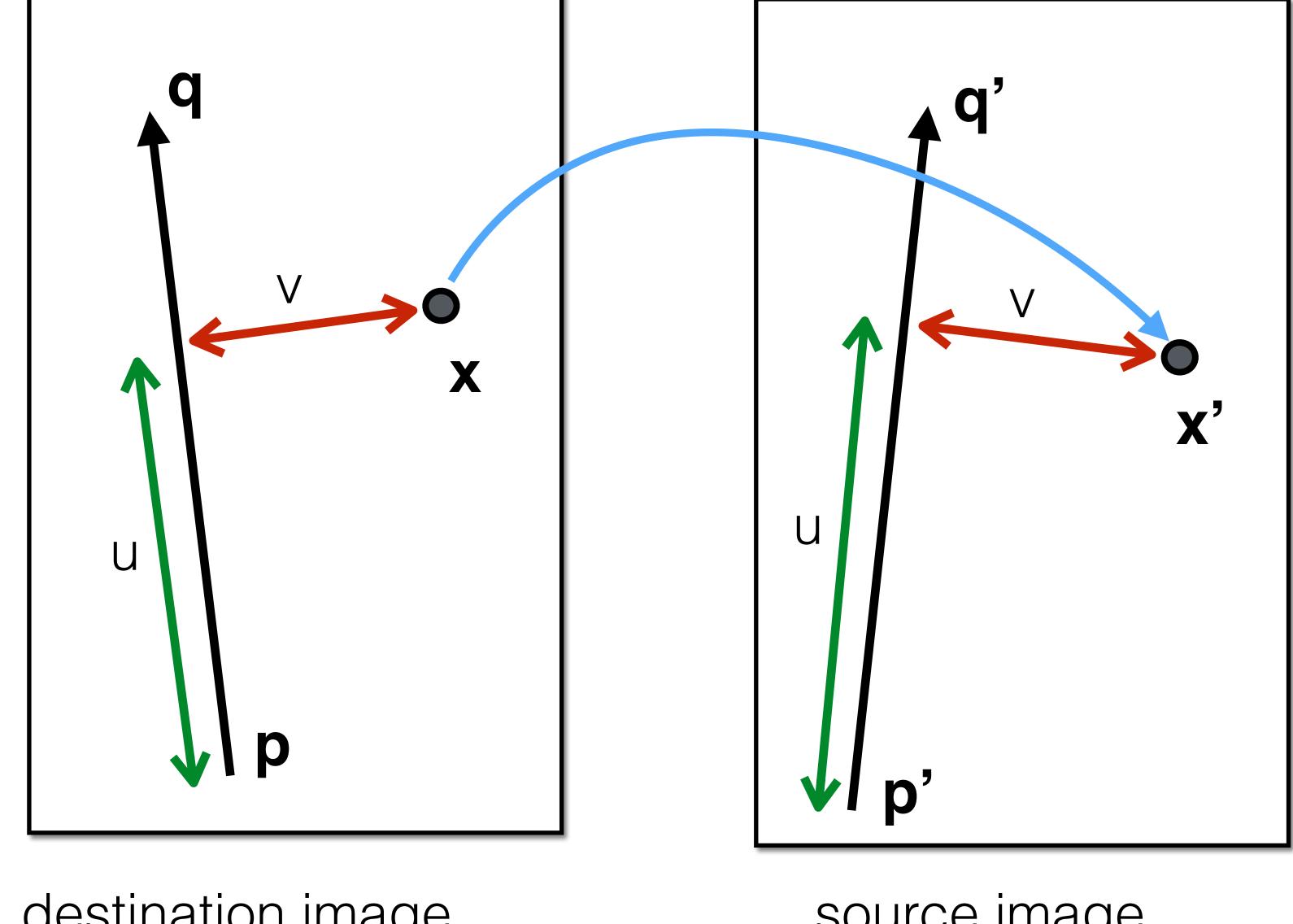
source image

u is a fraction v is a length (in pixels)



source image and destination image superimposed

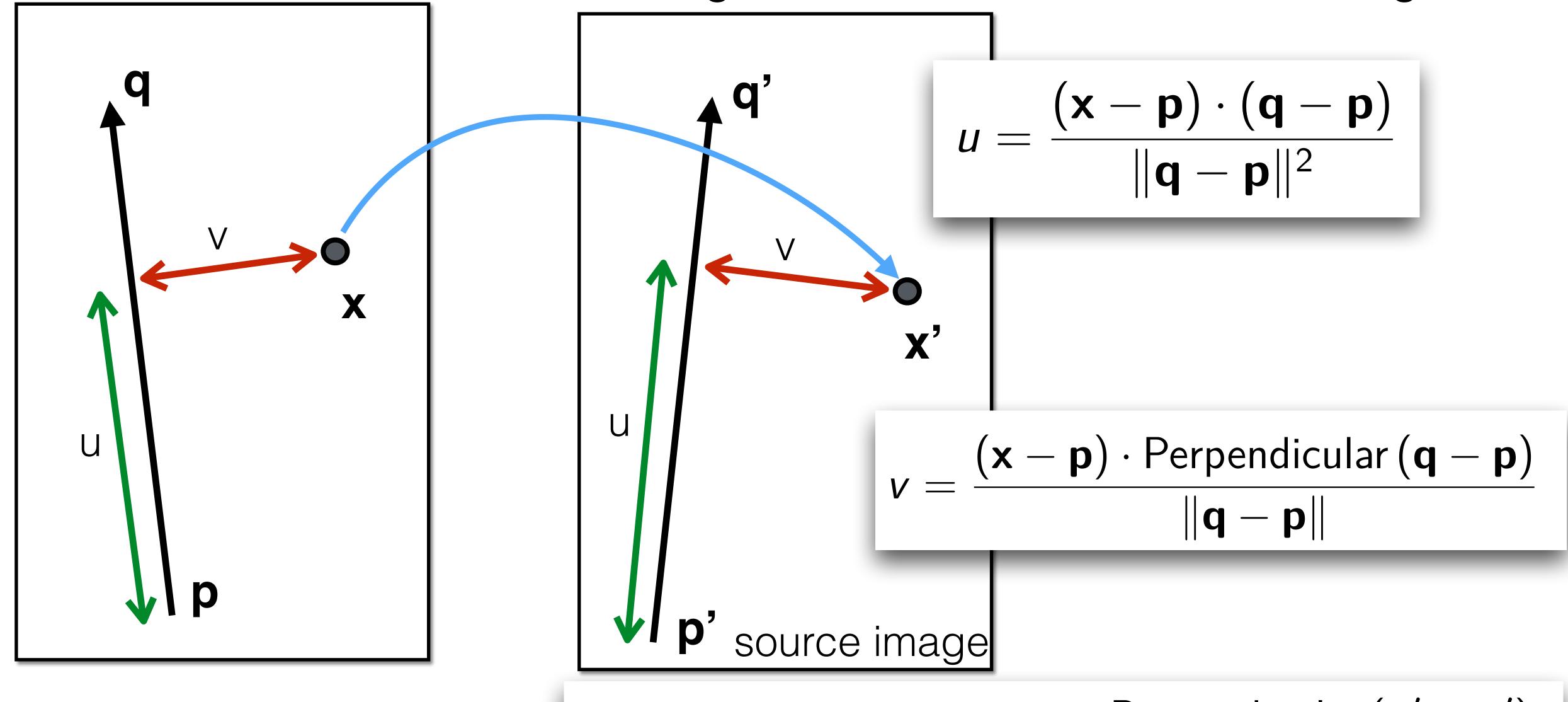
u is a fraction v is a length (in pixels) Given x in the destination image, where is x' in the source image?



destination image

source image

u is a fraction v is a length (in pixels) Given x in the destination image, where is x' in the source image?



destination image

$$x' = \mathbf{p}' + \mathbf{u} \cdot (\mathbf{q}' - \mathbf{p}') + \frac{\mathbf{v} \cdot \mathsf{Perpendicular}(\mathbf{q}' - \mathbf{p}')}{\|\mathbf{q}' - \mathbf{p}'\|}$$

$$u = \frac{(\mathbf{x} - \mathbf{p}) \cdot (\mathbf{q} - \mathbf{p})}{\|\mathbf{q} - \mathbf{p}\|^2}$$

$$v = \frac{(\mathbf{x} - \mathbf{p}) \cdot \text{Perpendicular}(\mathbf{q} - \mathbf{p})}{\|\mathbf{q} - \mathbf{p}\|}$$

$$x' = \mathbf{p}' + \mathbf{u} \cdot (\mathbf{q}' - \mathbf{p}') + \frac{\mathbf{v} \cdot \text{Perpendicular}(\mathbf{q}' - \mathbf{p}')}{\|\mathbf{q}' - \mathbf{p}'\|}$$

Weighting Effect of Each Line Pair

 To weight the contribution of each line pair, Beier & Neeley use:

$$weight[i] = \left(\frac{length[i]^p}{a + dist[i]}\right)^{\frac{b}{2}}$$

Where:

- length[i] is the length of L[i]
- dist[i] is the distance from X to L[i]
- a, b, p are constants that control the warp

Warping Pseudocode

```
WarpImage(Image, L'[...], L[...])
begin
   foreach destination pixel p do
       psum = (0,0)
       wsum = 0
       foreach line L[i] in destination do
           p'[i] = p transformed by (L[i],L'[i])
           psum = psum + p'[i] * weight[i]
           wsum += weight[i]
       end
        p' = psum / wsum
        Result(p) = Image(p')
   end
end
           slide from: http://www.cs.virginia.edu/~gfx/Courses/2010/IntroGraphics/Lectures/4-Image.pdf
```

Morphing Pseudocode

```
GenerateAnimation(Image<sub>0</sub>, L_0[...], Image<sub>1</sub>, L_1[...])
begin
    foreach intermediate frame time t do
        for i = 1 to number of line pairs do
            L[i] = line t-th of the way from <math>L_0[i] to L_1[i]
        end
        Warp_0 = WarpImage(Image_0, L_0, L)
        Warp_1 = WarpImage(Image_1, L_1, L)
        foreach pixel p in Finallmage do
            Result(p) = (1-t) Warp<sub>0</sub> + t Warp<sub>1</sub>
```

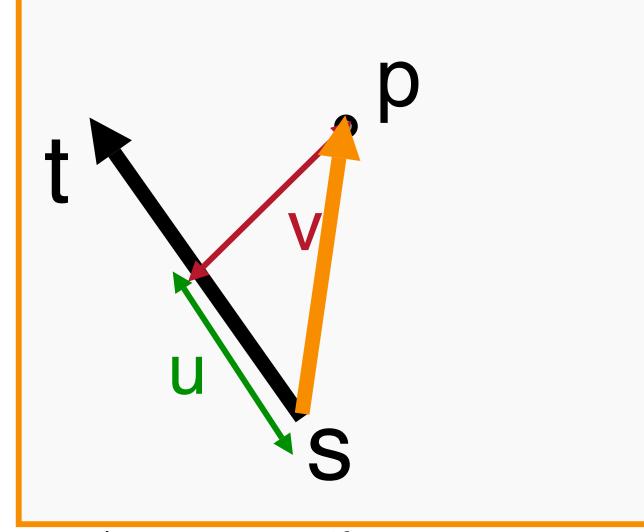
end end

Feature-Based Warping

How do I calculate dist? Dist is either...

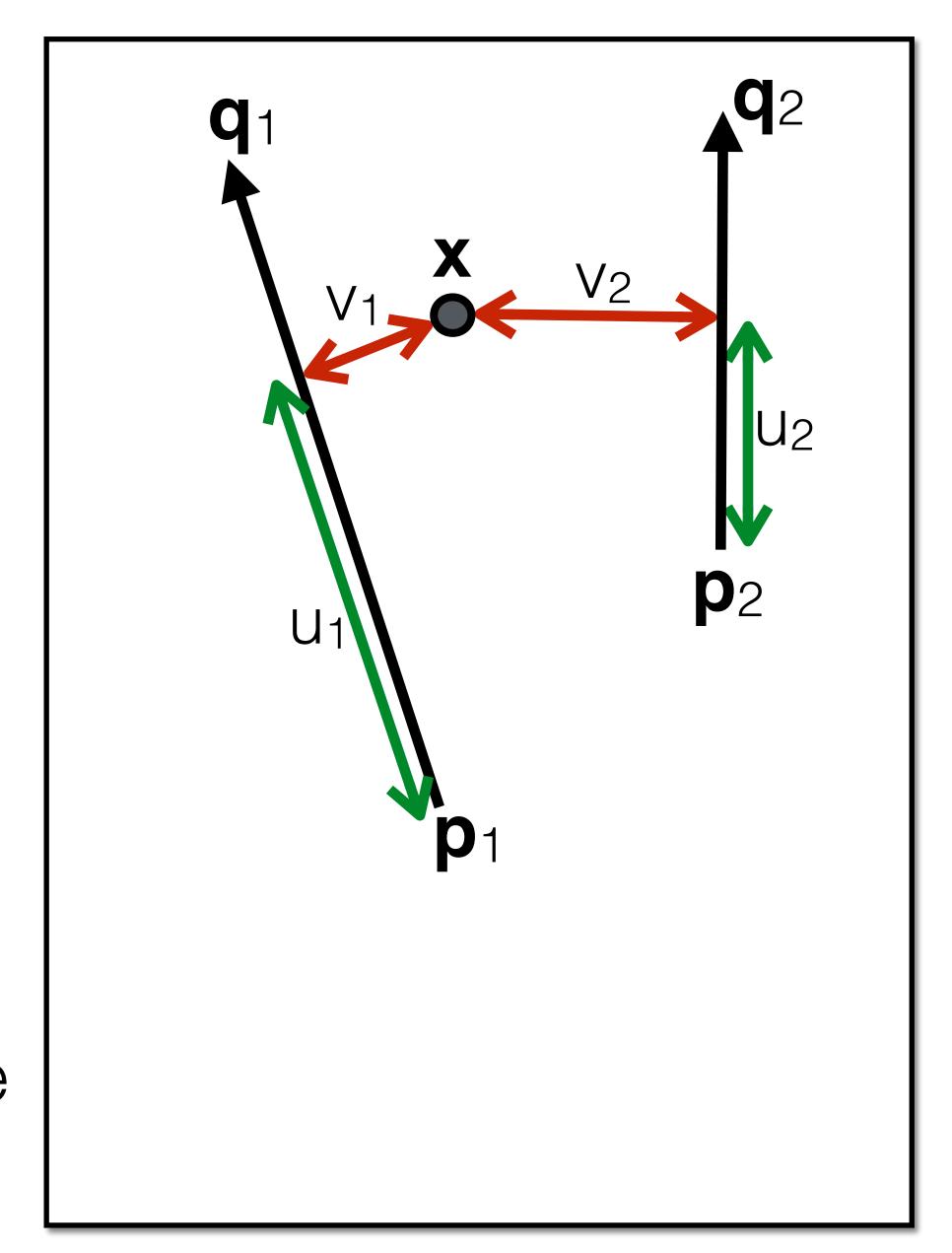
- abs(v) if u is >= 0 and <= 1
 OR
- distance to the closest endpoint i.e.

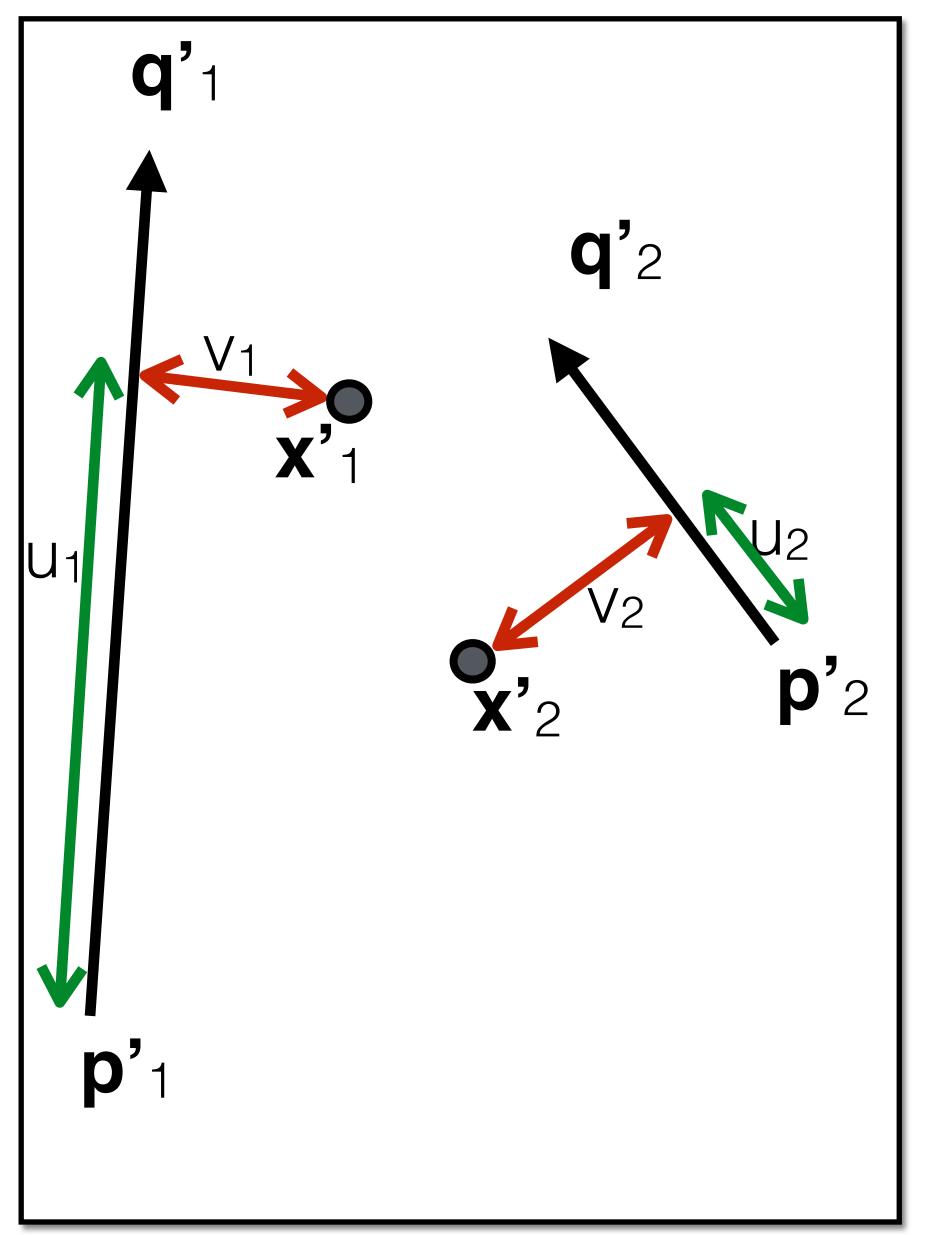
$$Min(||p-s||,||p-t||)$$



Pairs of lines

- Each line produces one mapping (i.e., warping) for a point **x**.
- As a result, two locations, \mathbf{x}'_1 and \mathbf{x}'_2 , are produced on the source image.



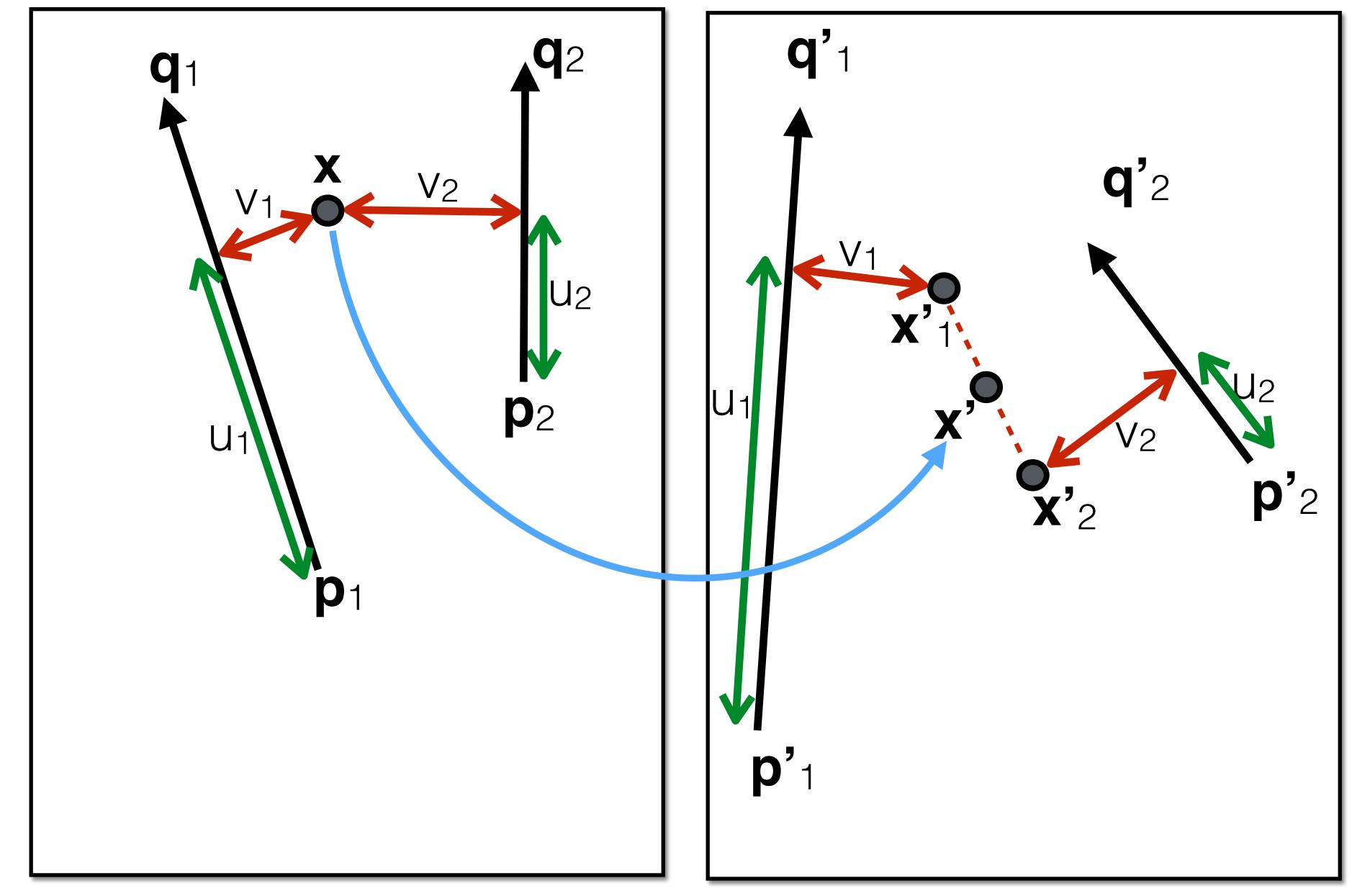


destination image

source image

Pairs of lines

- Select the mapped location, **x**', as an average of **x**'₁ and **x**'₂.

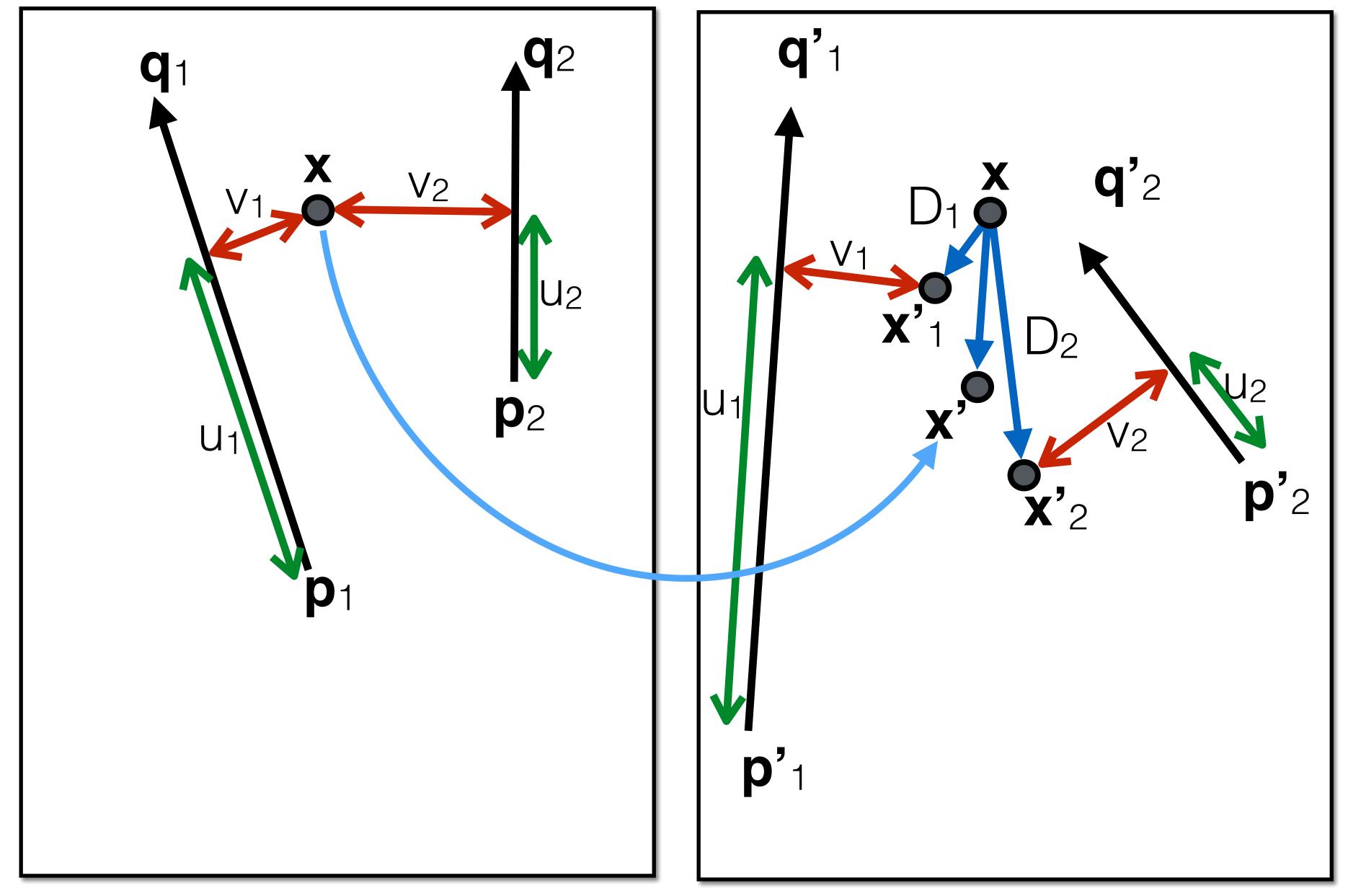


destination image

source image

Pairs of lines

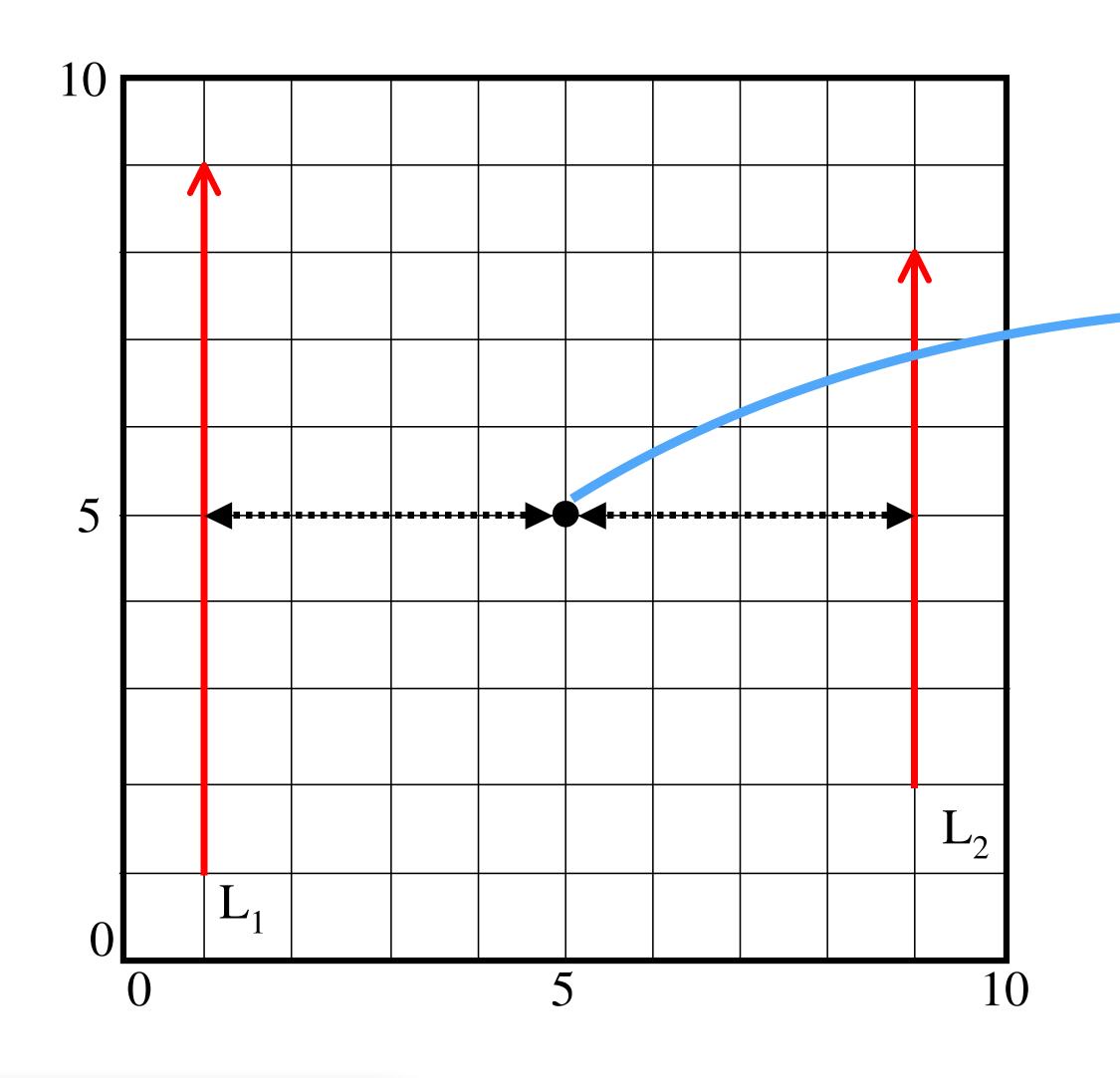
- Select the mapped location, **x**', as an average of **x**'₁ and **x**'₂.
- Use a weighted average, using the distance from the **x** to the lines.



destination image

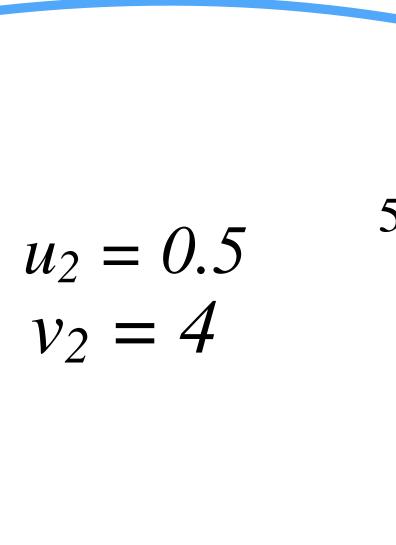
source image

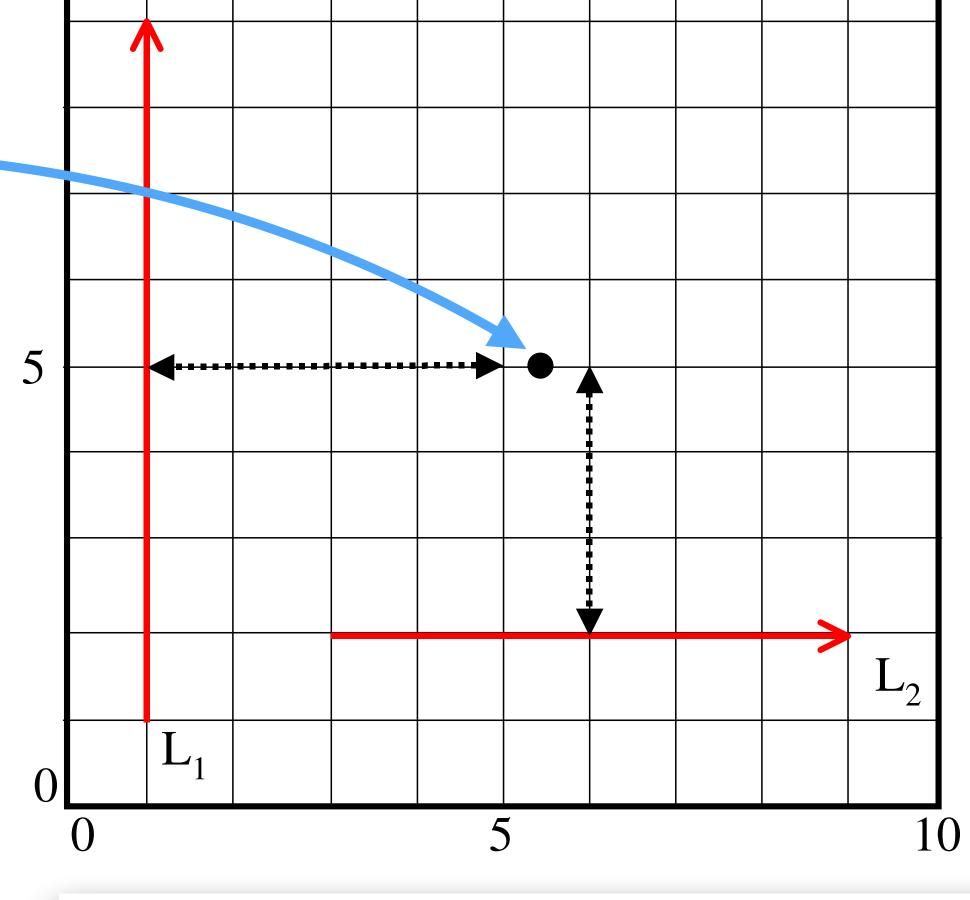
Assume that the constants controlling the warping are a = b = p = 1.



$$u_1 = 0.5$$

$$v_1 = 4$$





$$w_{i} = \left(\frac{length_{i}^{p}}{a + dist_{i}}\right)^{b}$$

 $\left(\frac{length_{i}^{p}}{a+dist_{i}}\right)^{b} \quad For L_{1}^{r} \text{ the weight } w_{1} = 8 / (1+4) = 1.6 \\ for L_{2}^{r} \text{ the weight } w_{2} = 6 / (1+3) = 1.5.$ $\mathbf{x'} = \frac{\sum_{i} w_{i} \mathbf{p}_{i}}{\sum w_{i}} = \frac{1.6 \cdot \binom{5}{5} + 1.5 \cdot \binom{6}{5}}{3.1}$

$$\mathbf{x'} = \frac{\sum_{i} w_{i} \mathbf{p}_{i}}{\sum_{i} w_{i}} = \frac{1.6 \cdot \binom{5}{5} + 1.5 \cdot \binom{6}{5}}{3.1} = \binom{5.48}{5}$$

Source: http://www.doc.ic.ac.uk/~dfg/graphics/graphics2010/GraphicsTutorialSolution09.pdf