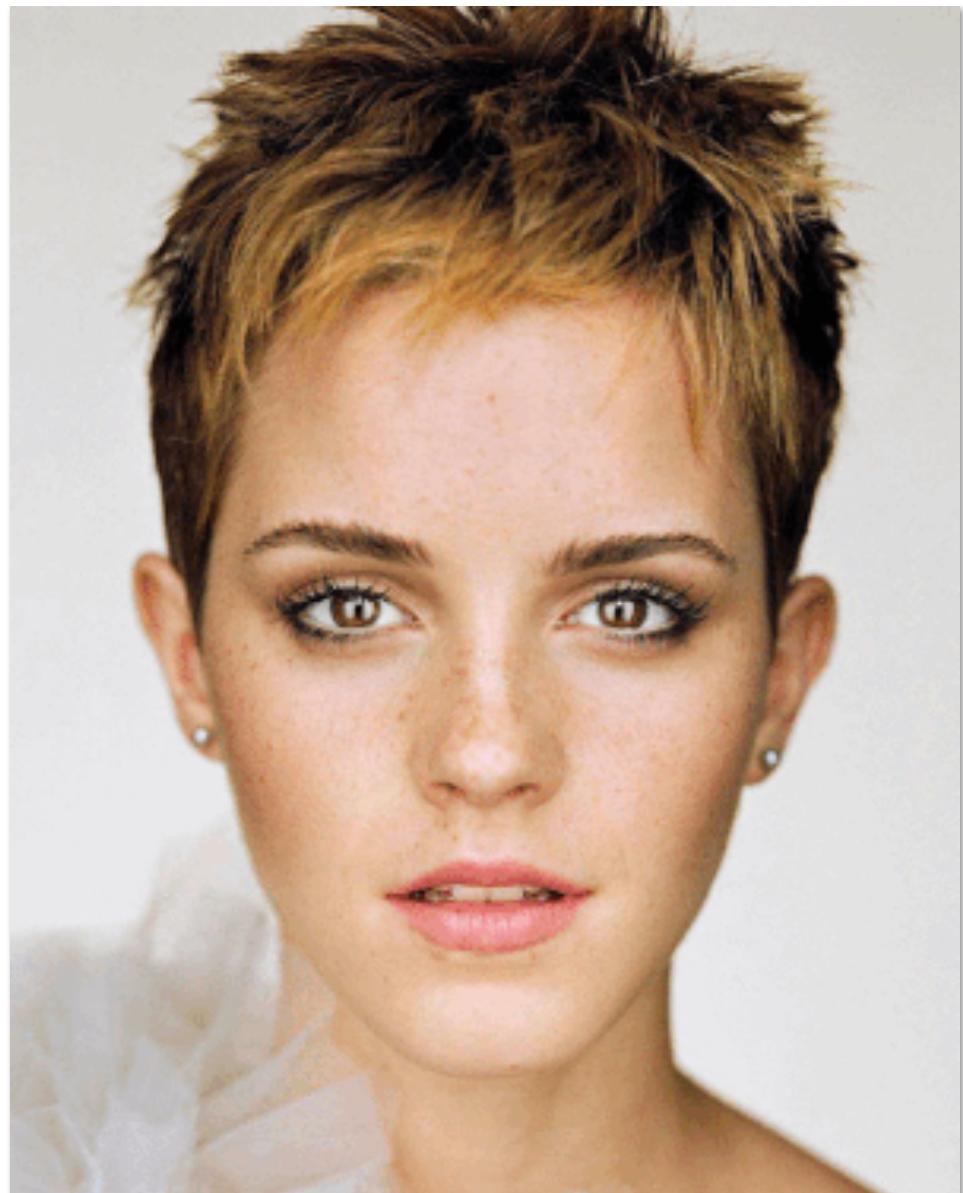


The image is a horizontal strip composed of five vertical panels. From left to right: 1. A portrait of a young woman with dark hair, wearing a light blue headband and a red necklace. 2. A woman's face that is partially obscured by a tiger's face, with the tiger's stripes visible on the forehead and around the eyes. 3. A tiger's face with its characteristic orange and black stripes. 4. A tiger's face where the stripes are becoming more prominent and defined. 5. A close-up of a tiger's face with intense yellow eyes and detailed stripes.

Morphing

CSE 5280



**Click on the link to see video:**

Source: <http://0e303c09b5d540ddca1ba32f9c73930f0077ec4cbda0c3141619.r85.cf2.rackcdn.com/project5.html>

# Examples



<https://youtu.be/nUDIoN-Hxs>

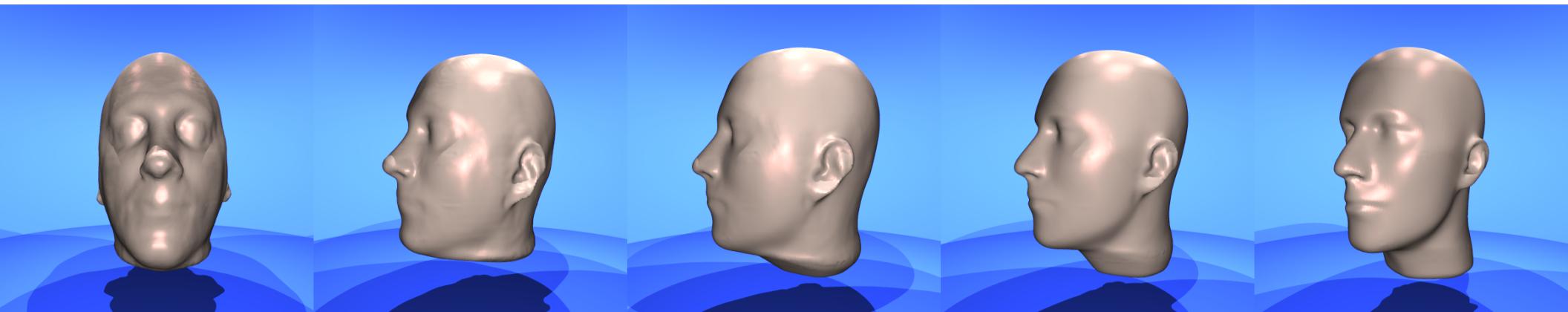


<https://youtu.be/-ZopSqeJOgo>

Click on the links to see videos:

# Examples

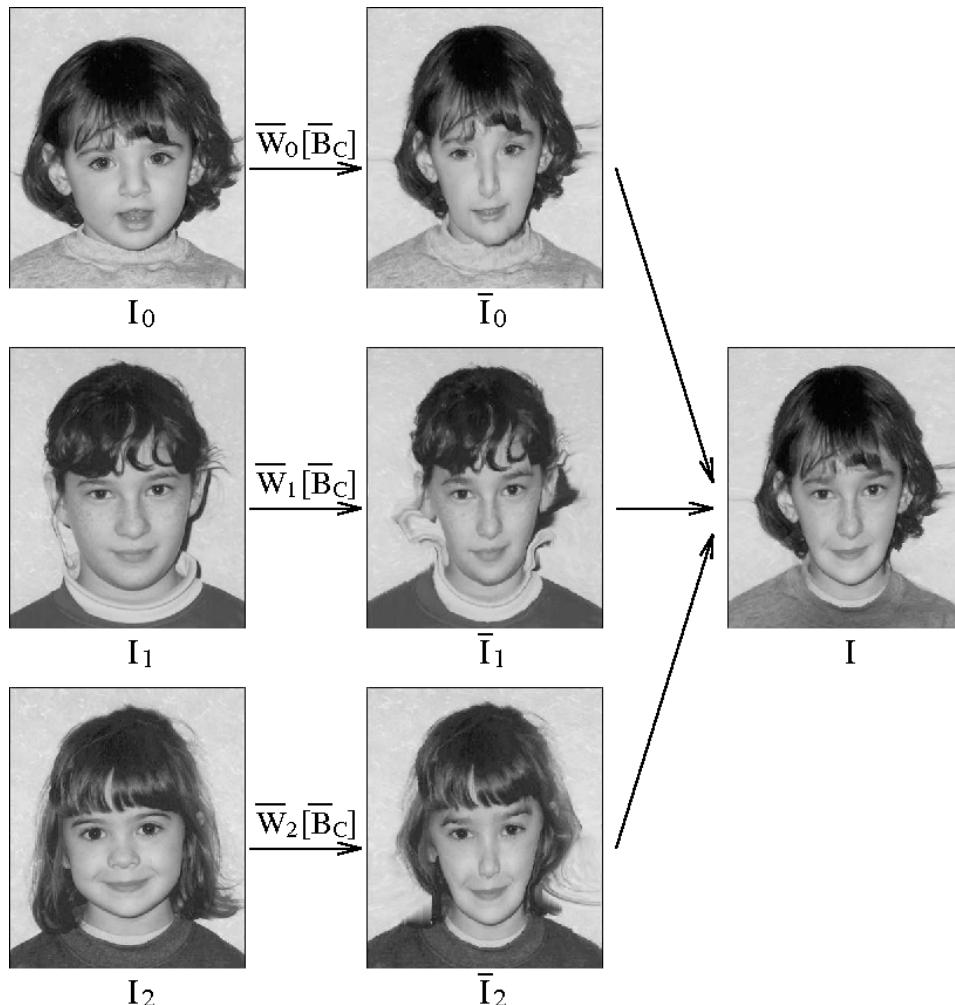
## 3-D morphing



<https://www.cs.drexel.edu/~david/Abstracts/morph-diff-mods-abs.html>

# Examples

Combining  
multiple faces to  
form a new one



**Paper:** Polymorph:  
Morphing Among Multiple Images by Lee et al. (1998)

<http://www-cs.ccny.cuny.edu/~wolberg/pub/cga98.pdf>

# Examples



Preview for  
plastic surgery

<https://www.businessinsider.com.au/visual-plastic-surgery-2014-2>

# Examples

OPEN

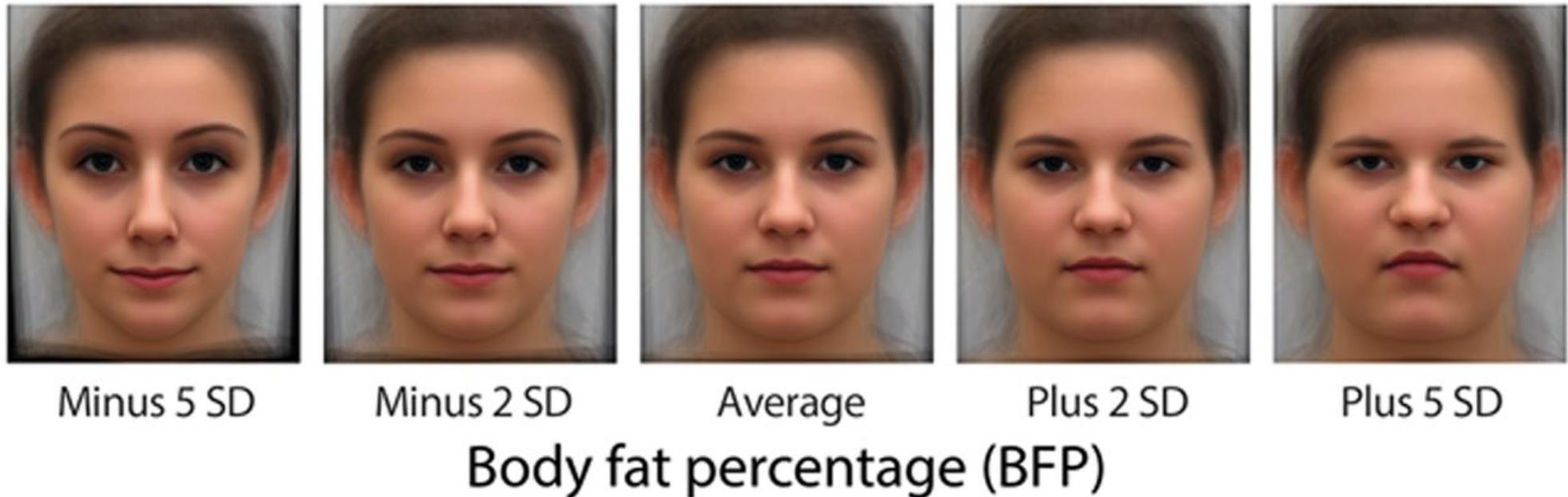
Calibrating facial morphs for use as stimuli in biological studies of social perception

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Published online: 27 April 2018

Sonja Windhager<sup>1</sup>, Fred L. Bookstein<sup>2,3</sup>, Hanna Mueller<sup>2</sup>, Elke Zunner<sup>2</sup>, Sylvia Kirchengast<sup>2</sup>  
& Katrin Schaefer<sup>3,2</sup>



<https://www.nature.com/articles/s41598-018-24911-0.pdf>

# Examples



Figure 2. (Left) Male average, (center) female average, and (right) generic, androgynous average. The sex-specific averages were made by morphing together 24 male and 24 female faces, respectively. The generic average was made by morphing all 48 faces (24 males, 24 females).

<https://www.semanticscholar.org/paper/Sex-specific-norms-code-face-identity.-Rhodes-Jaquet/8d95e11d78fbec0db4add7d8d64f6545ba640f3d>

## Sex-specific norms code face identity

Gillian Rhodes

FaceLab, School of Psychology, University of Western Australia, Crawley, Australia



Emma Jaquet

FaceLab, School of Psychology, University of Western Australia, Crawley, Australia, & University of Bristol, UK



Linda Jeffery

FaceLab, School of Psychology, University of Western Australia, Crawley, Australia



Emma Evangelista

FaceLab, School of Psychology, University of Western Australia, Crawley, Australia



Jill Keane

MRC Cognition and Brain Sciences Unit, Cambridge, UK



Andrew J. Calder

MRC Cognition and Brain Sciences Unit, Cambridge, UK



# Examples: playing with averages



German avg.

Finnish avg.

Irish avg.

American avg.

Mongolian avg.

# Examples: transferring morphings



My face

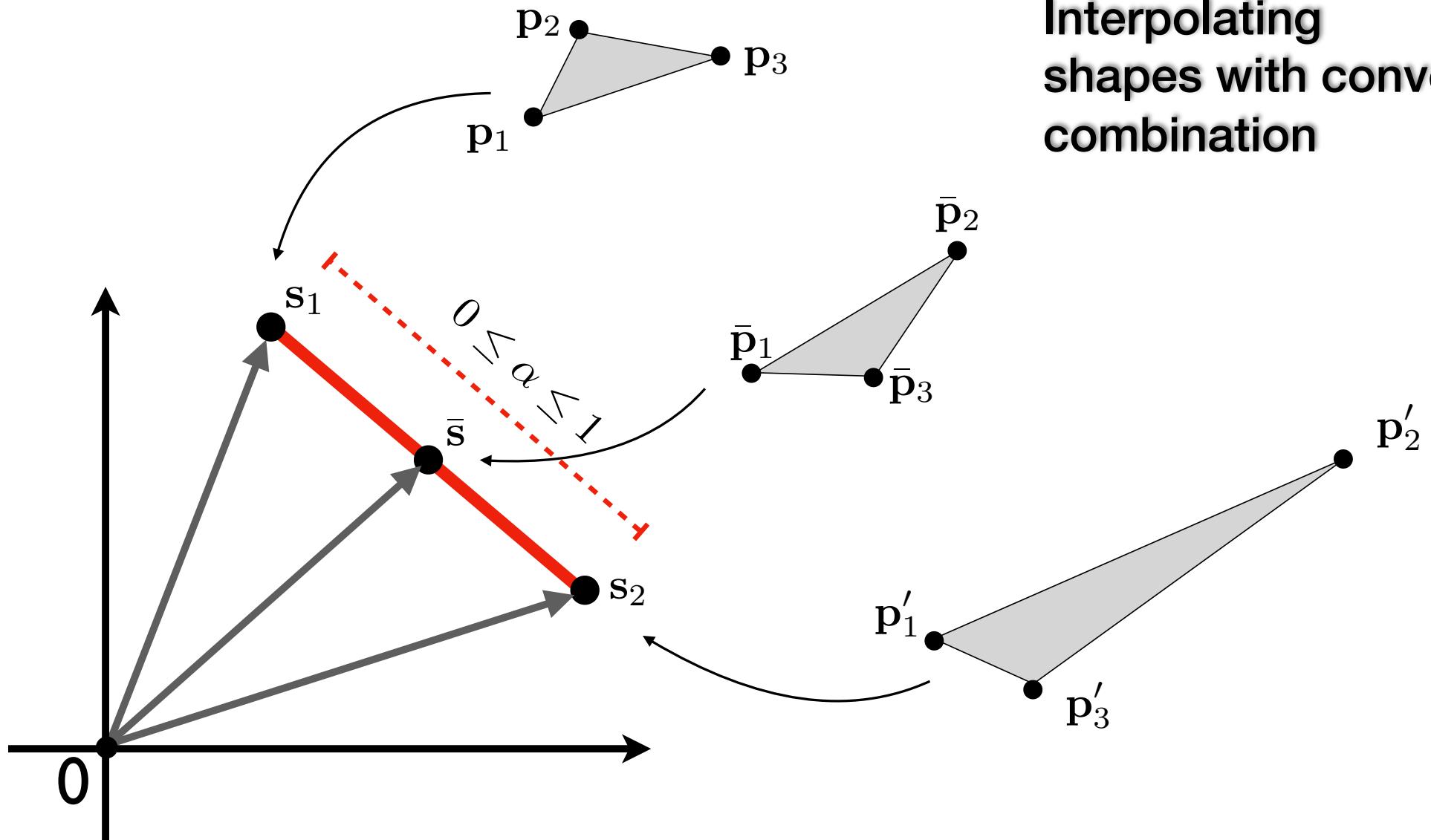


Show Efros' slides

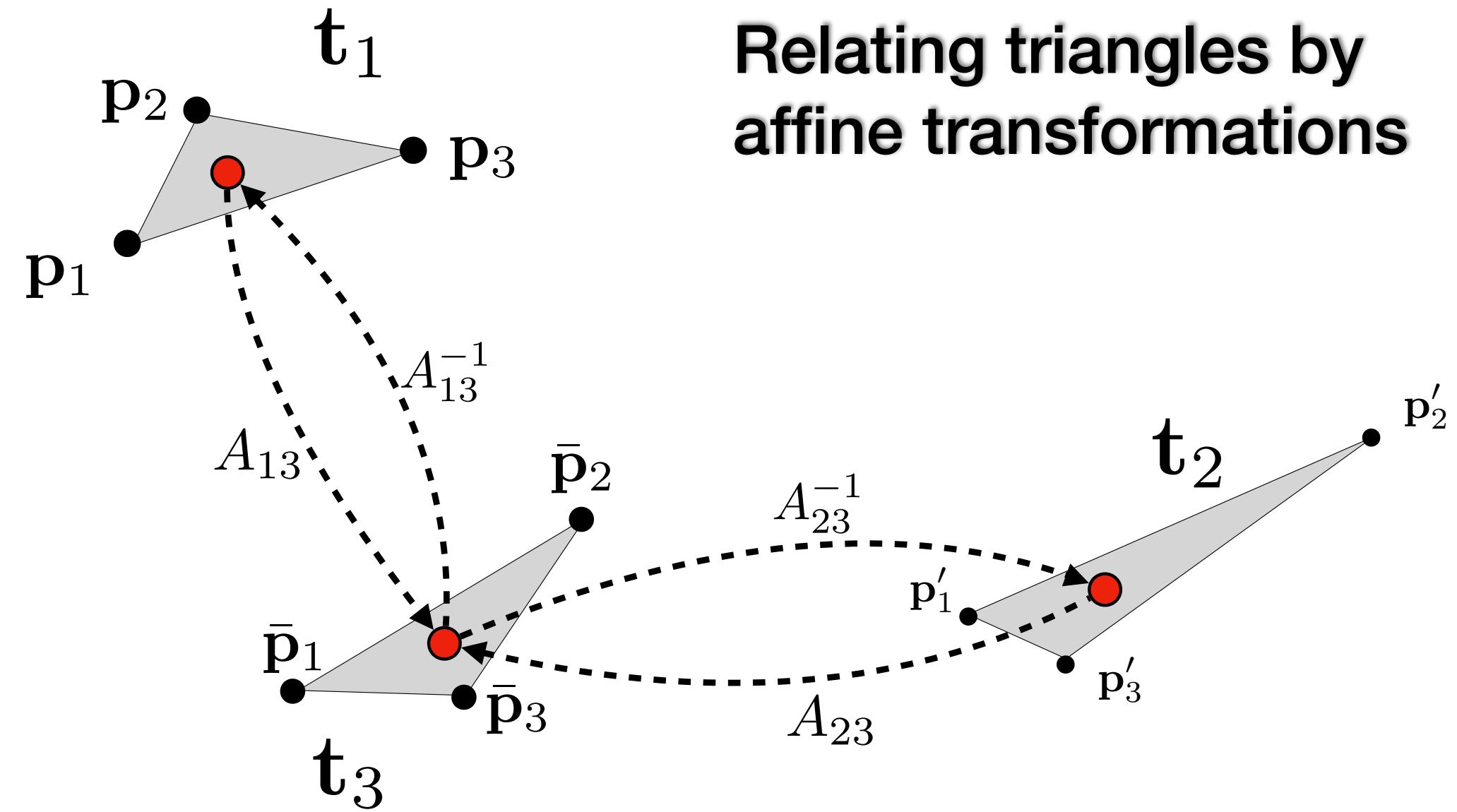
# What do you need to know?

- How to estimate an affine transformation given at least 3 pairs of corresponding points.
- How to use the inverse transformation (e.g., affine) to calculate the location of a pixel on the original (i.e., un-warped) image. This is the inverse mapping that you use to transfer pixel colors.
- How to calculate the average of a set of shapes described by ordered landmarks.
- How to transfer the edges (i.e., connections) from one triangulation to another.
- How to use convex combination to synthesize new shapes and also to blend colors.
- How to determine if points are inside or outside a triangle

## Interpolating shapes with convex combination



# Relating triangles by affine transformations



# Affine transformation and homogenous coordinates

**Function form:**

$$\vec{y} = f(\vec{x}) = A\vec{x} + \vec{b}.$$

**Homogeneous coordinates (augmented matrix form):**

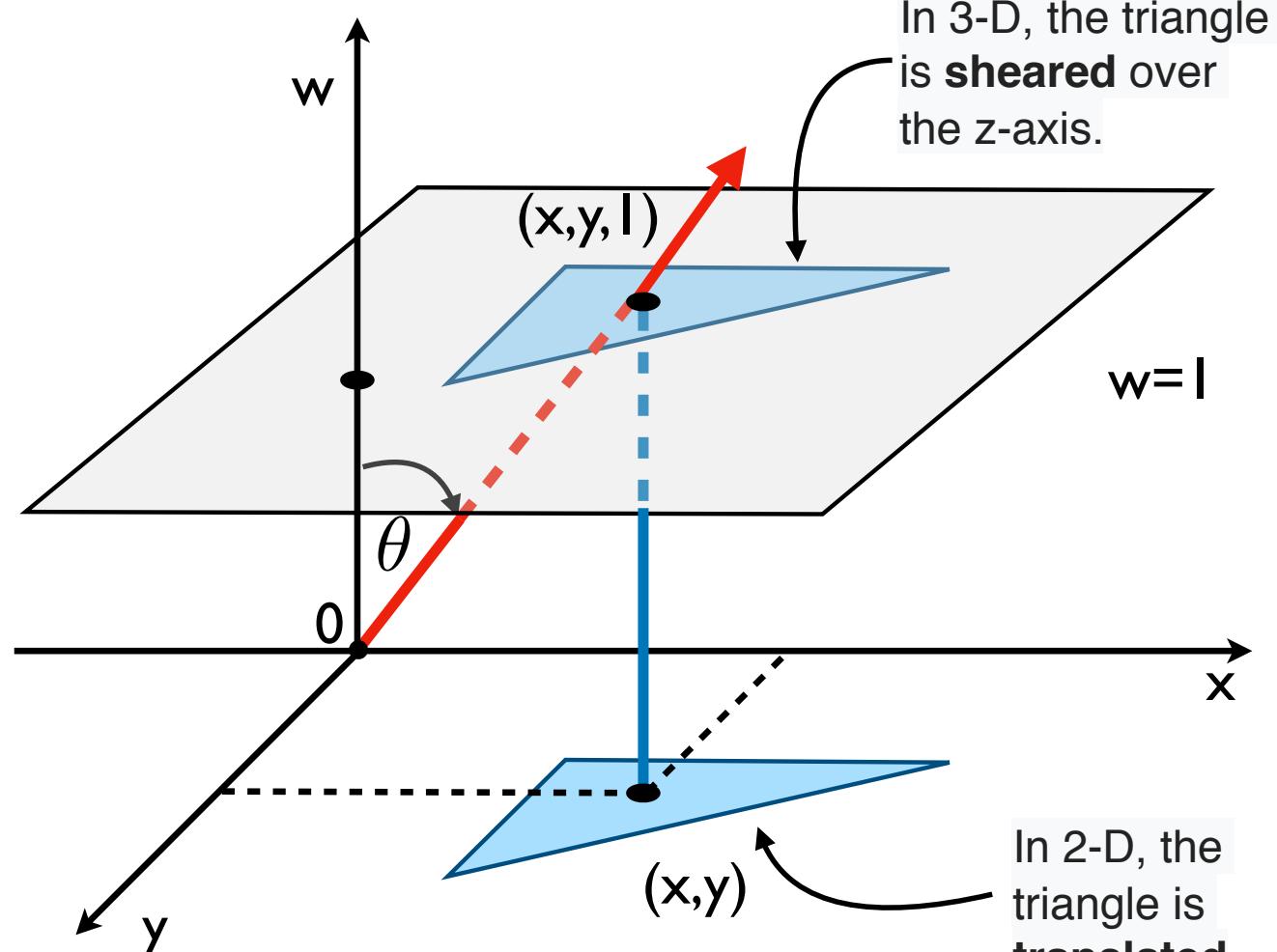
$$\begin{bmatrix} \vec{y} \\ 1 \end{bmatrix} = \left[ \begin{array}{ccc|c} & A & & \vec{b} \\ 0 & \dots & 0 & 1 \end{array} \right] \begin{bmatrix} \vec{x} \\ 1 \end{bmatrix}$$

# Affine transformation and homogenous coordinates

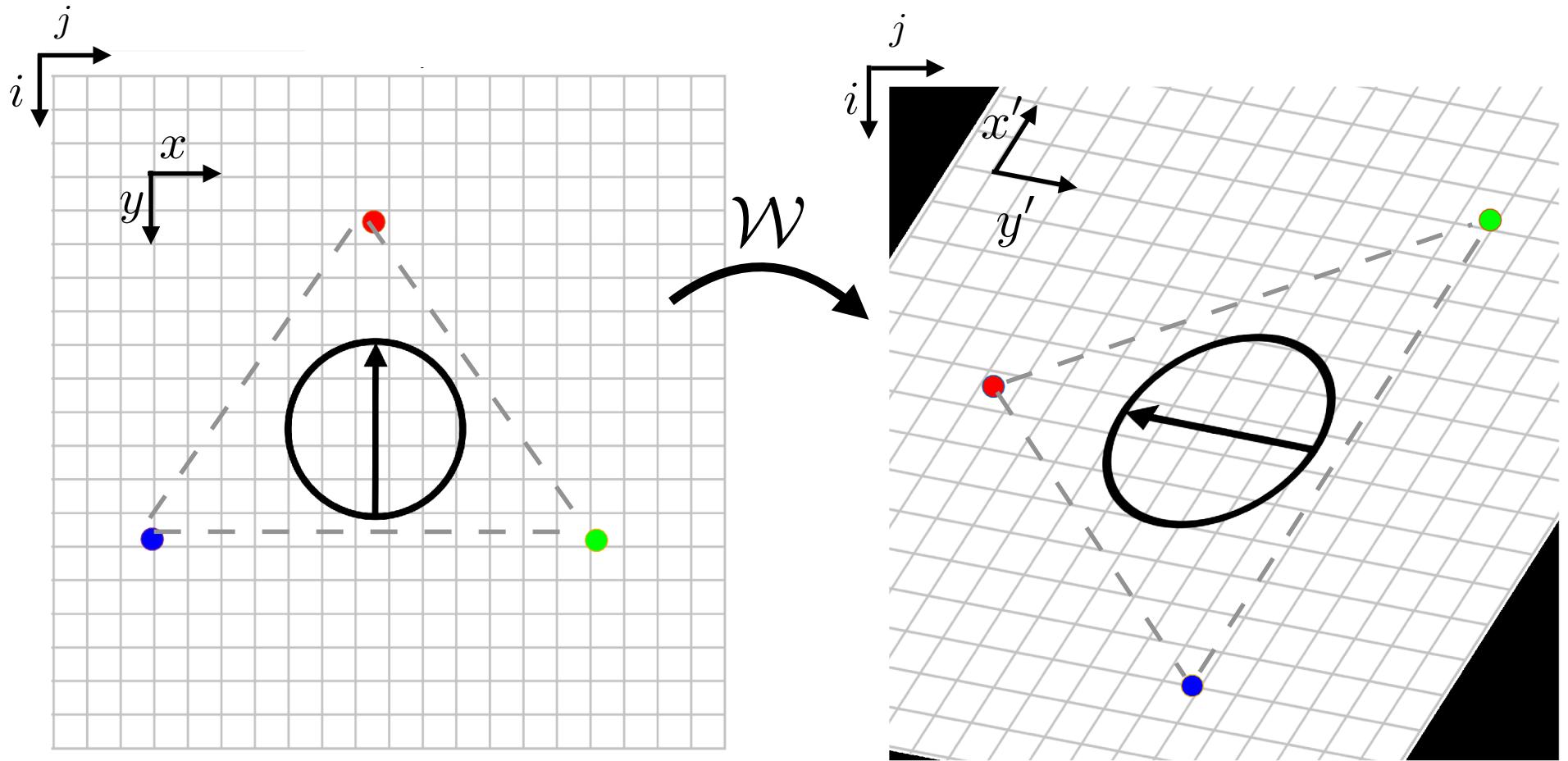
2-D affine transformations can be performed in 3-D.

Translation is done by shearing along over the z axis, and rotation is performed around the z axis.

Shear is a linear transformation (i.e., it has a matrix form). Translation is not a linear transformation in 2-D) as it moves the origin.

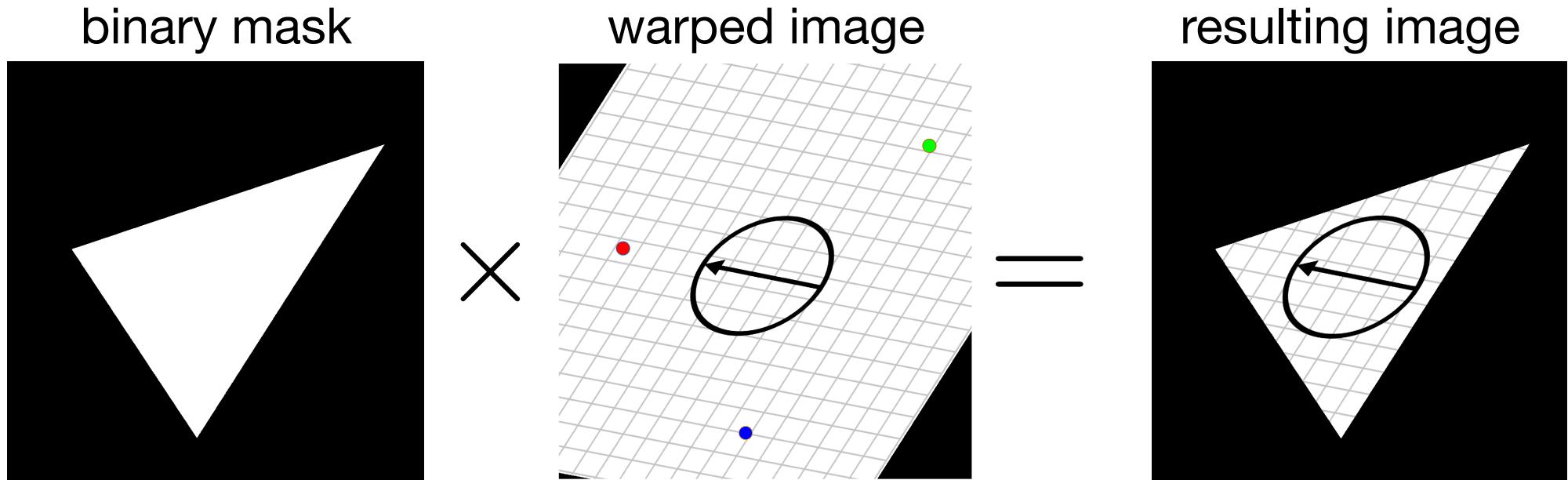


# Mapping only points that are inside a triangle

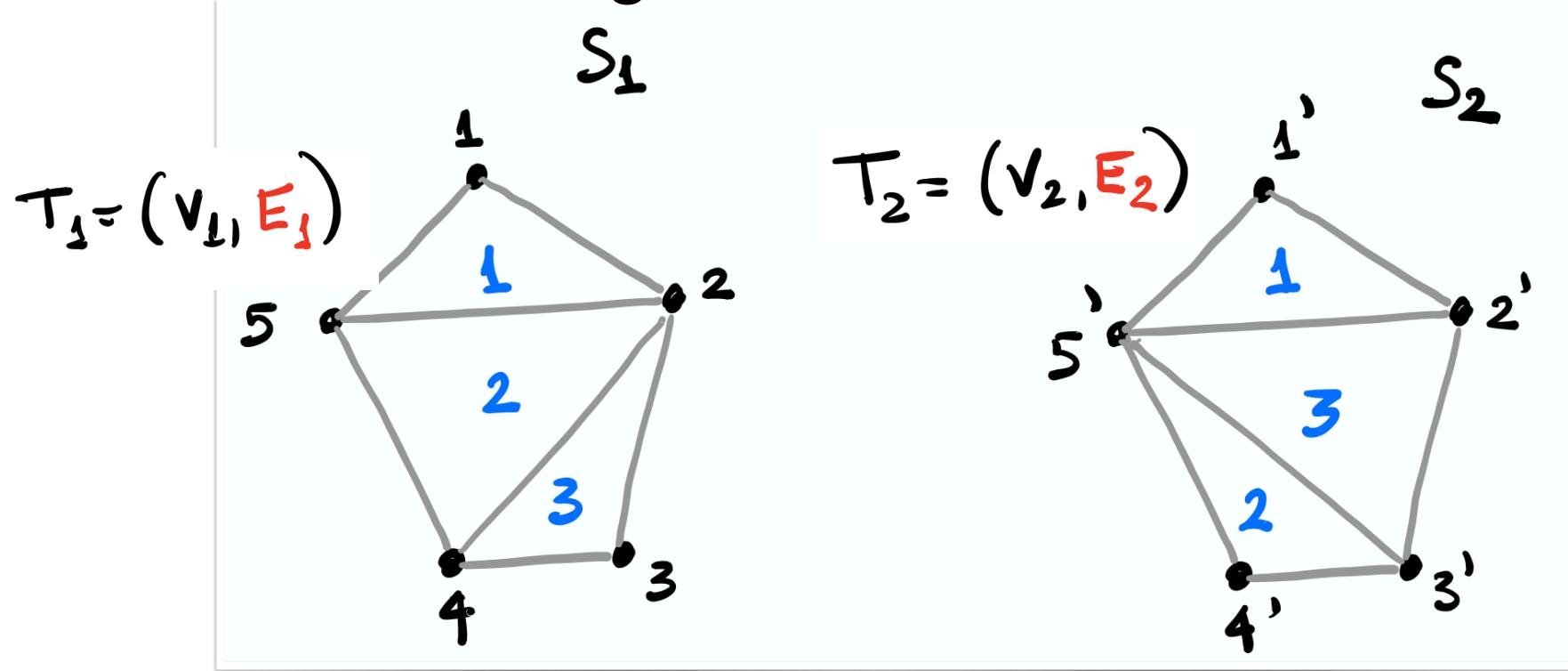


# Mapping only points that are inside a triangle

We can create a binary mask with pixels inside a triangle, then transfer only pixel colors from inside the mask. Or we can warp the whole image and then multiply it by the mask.

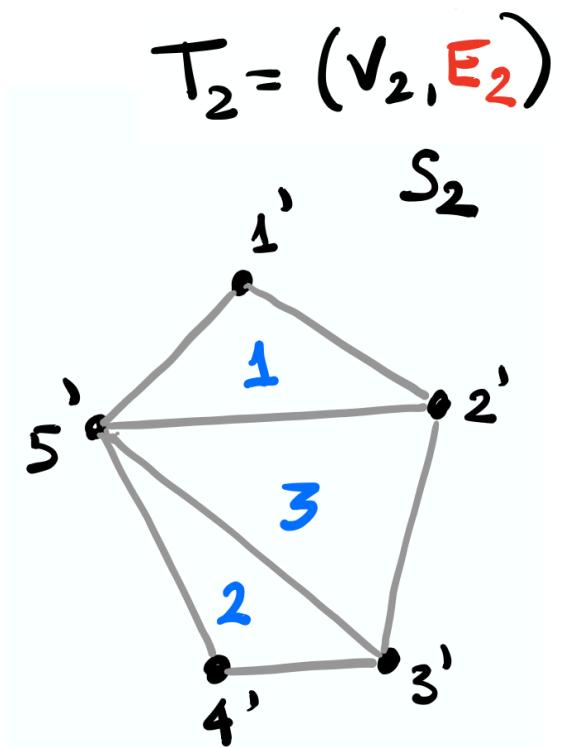
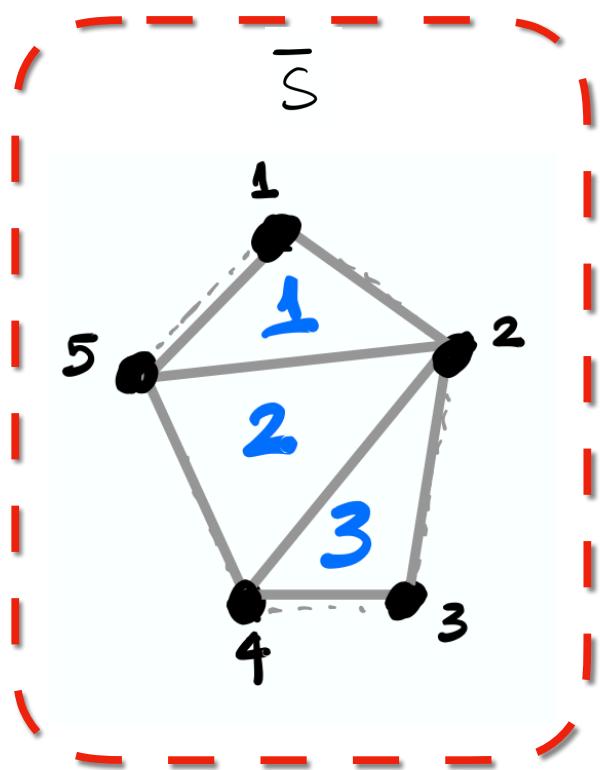
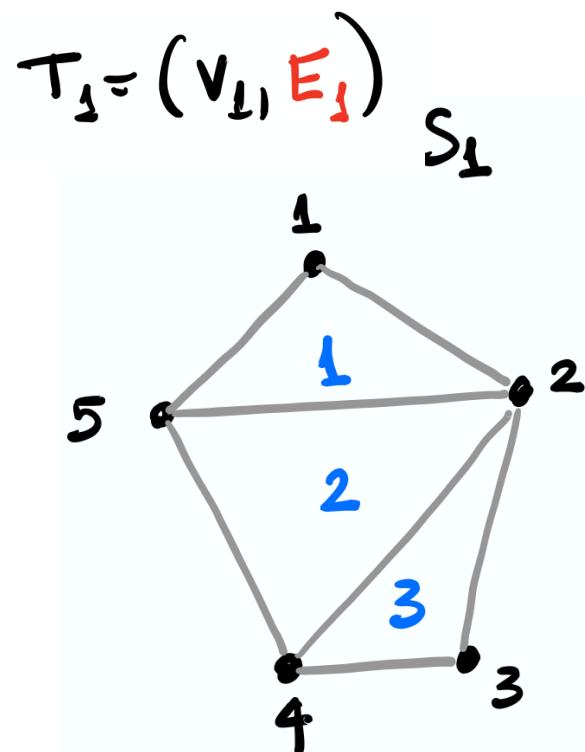


# Slightly different shapes can yield highly inconsistent triangulations



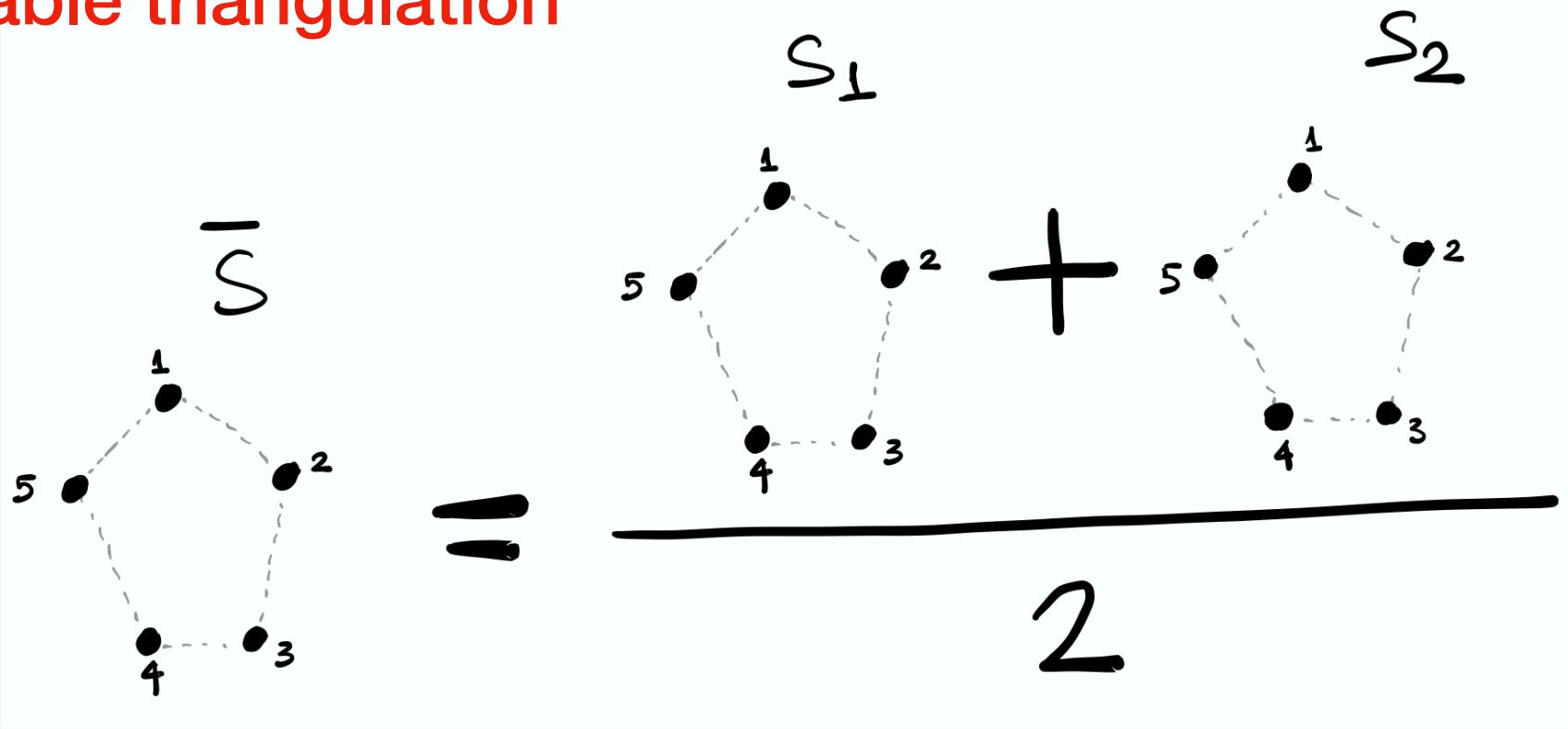
- Triangle order of in edges set varies. Total number of triangles may also vary.
- Inconsistent order means triangles cover different parts of image.
- Broken triangle-to-triangle correspondence: can't estimate consistent affine transformations.

# Inconsistent triangulations: one triangulation to rule them all



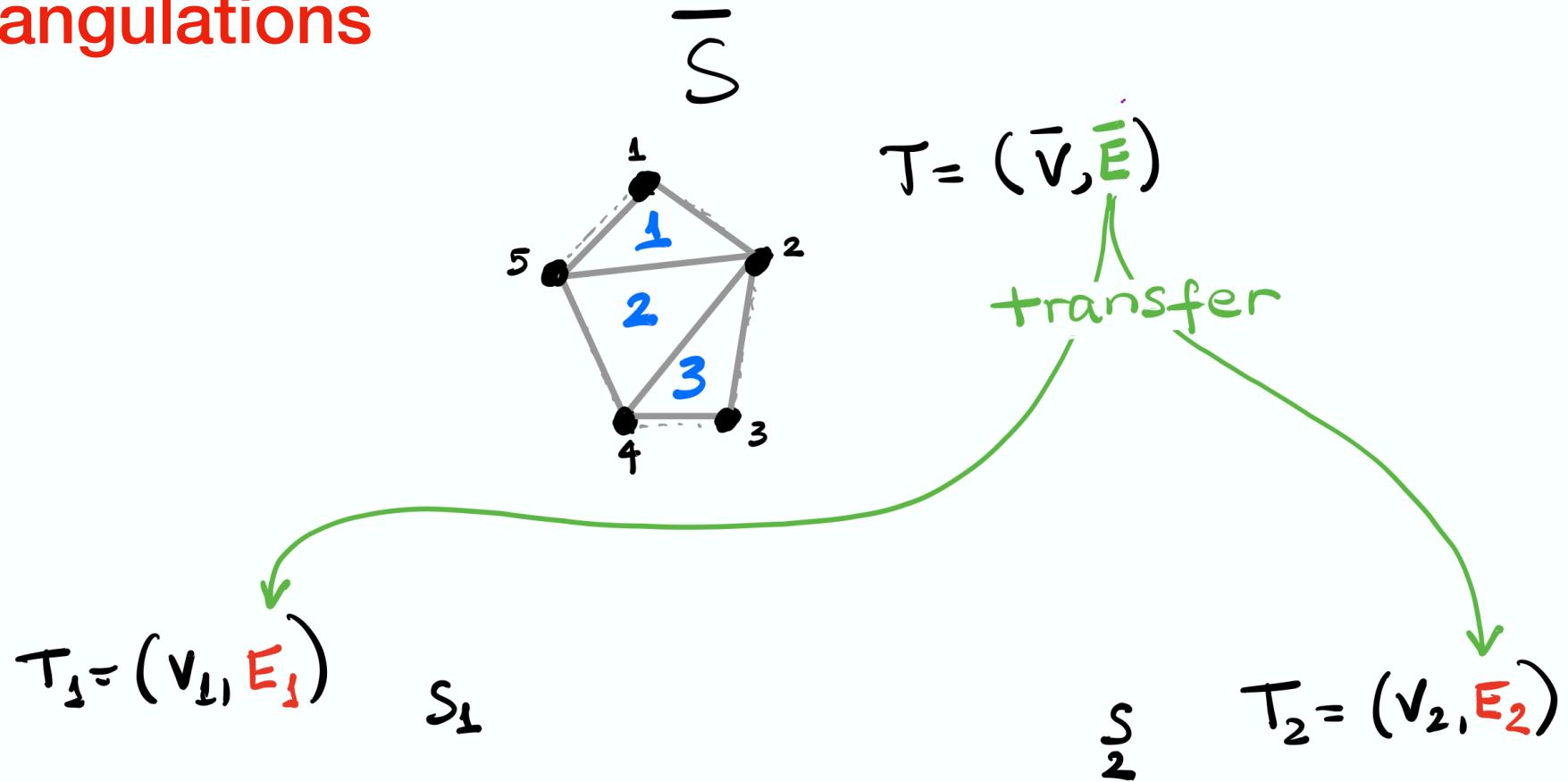
- Create a **single triangulation** to represent the connections for all triangulations.

# Inconsistent triangulations: use the mean as the stable triangulation



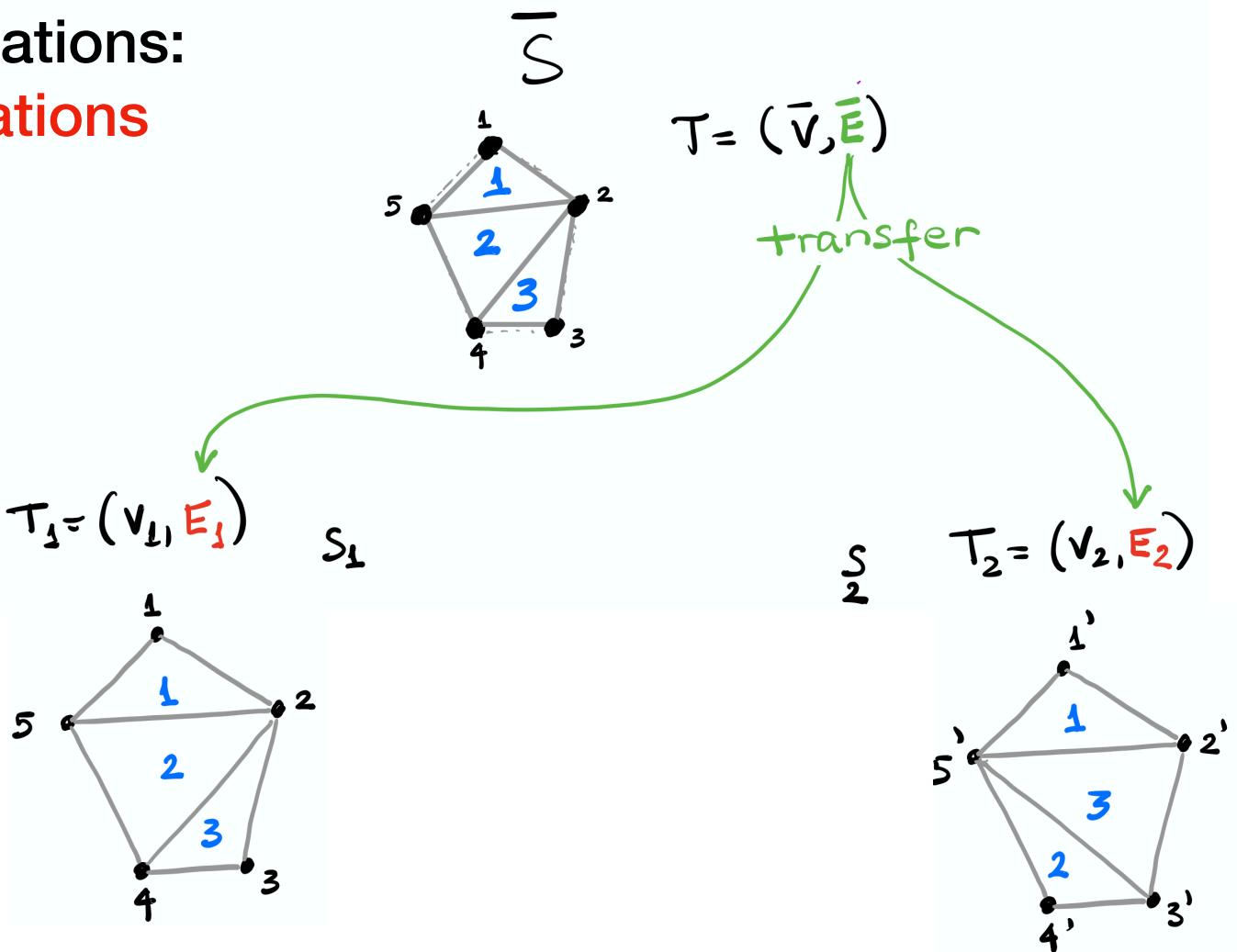
- **Use the mean triangulation:** The triangulation of the mean shape is the one most similar (statistically) to all shapes.

# Inconsistent triangulations: transferring triangulations



- Transfer the edges. Keep the vertices

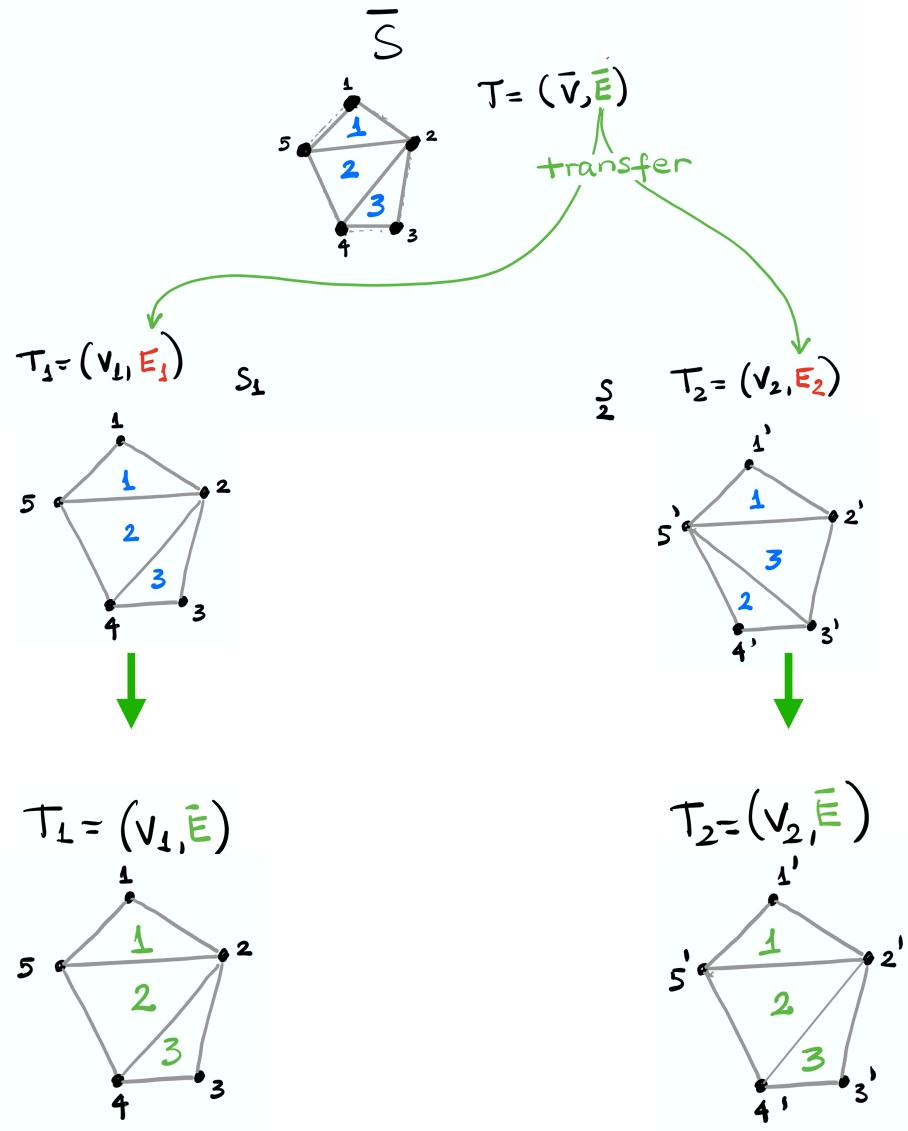
## Inconsistent triangulations: transferring triangulations



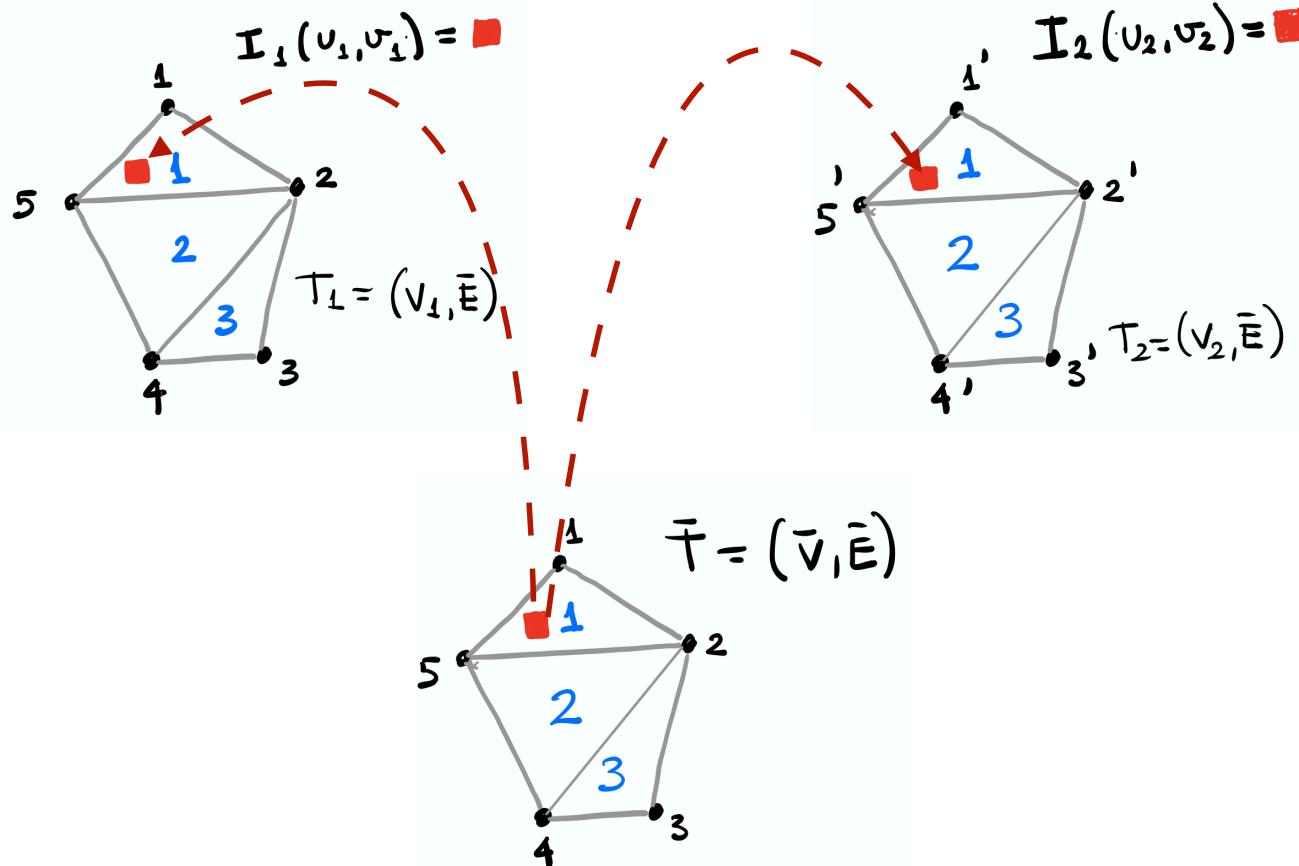
- Transfer the edges. Keep the vertices

# Inconsistent triangulations: transferring triangulations

- Transfer the edges. Keep the vertices
- Once all triangulations are consistent, we can calculate the required affine transformations between pairs of corresponding triangles



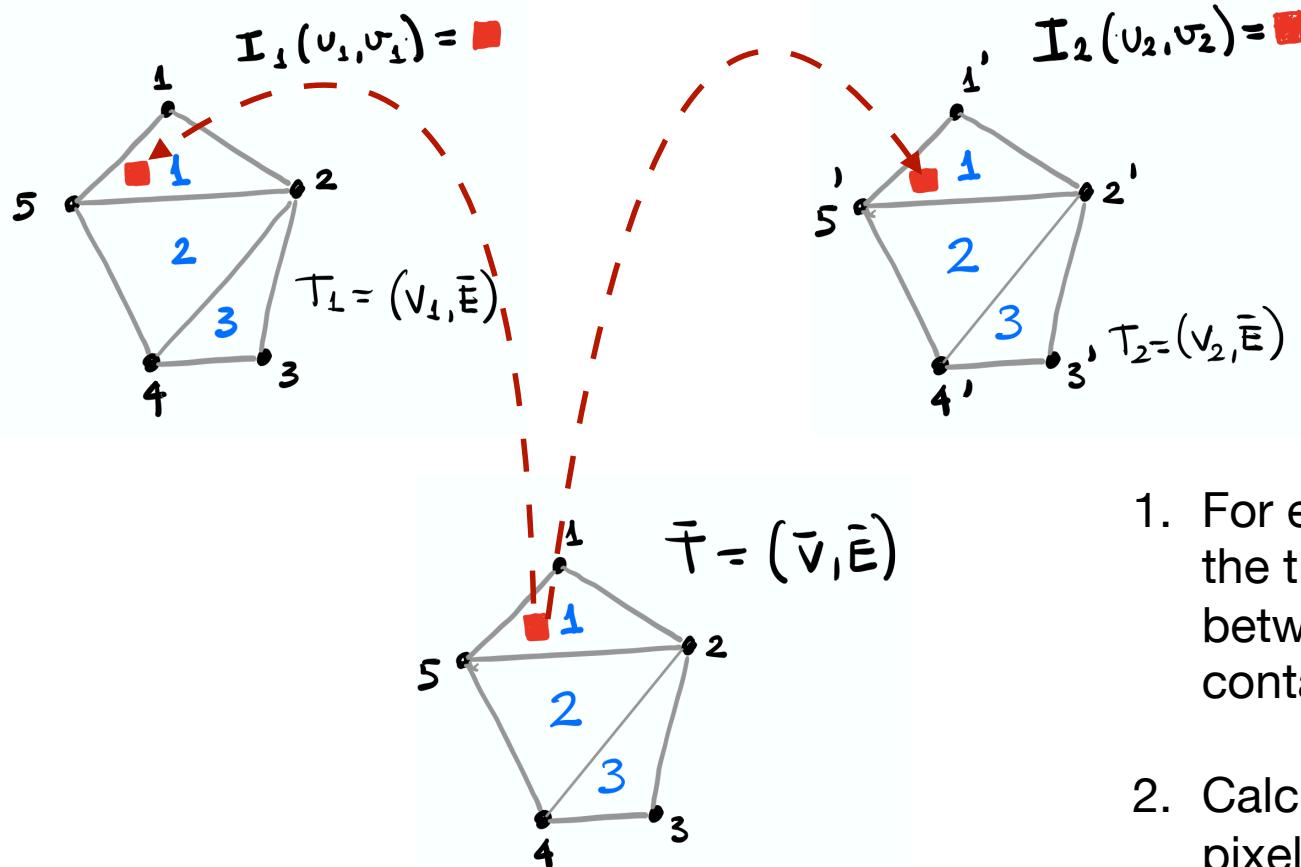
# Morphing: example with two triangulations



$$\bar{I}(x, y) = (1 - \alpha) I_1(u, v) + \alpha I_2(u, v)$$

- Source triangulations and images
- Destination triangulation and image

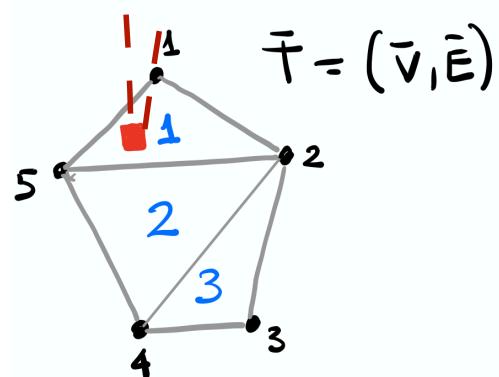
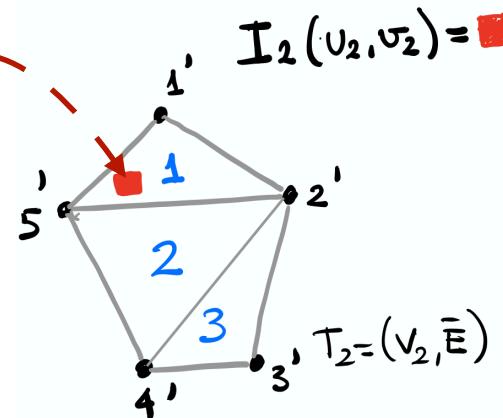
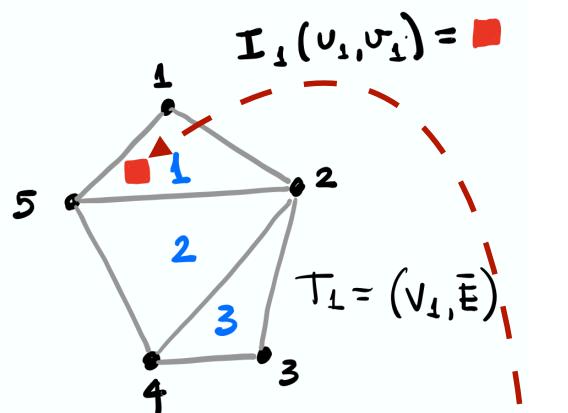
# Morphing: example with two triangulations



$$\bar{I}(x, y) = (1 - \alpha) I_1(u, v) + \alpha I_2(u, v)$$

1. For each pixel  $(x, y)$  of dst image, find the transformation (i.e., affine) between the corresponding triangles containing that pixel.
2. Calculate the color of the destination pixel at  $(x, y)$  as a blend of its corresponding pixels  $(u, v)$

# Morphing: example with two triangulations



$$\bar{I}(x, y) = (1 - \alpha) I_1(u, v) + \alpha I_2(u, v)$$

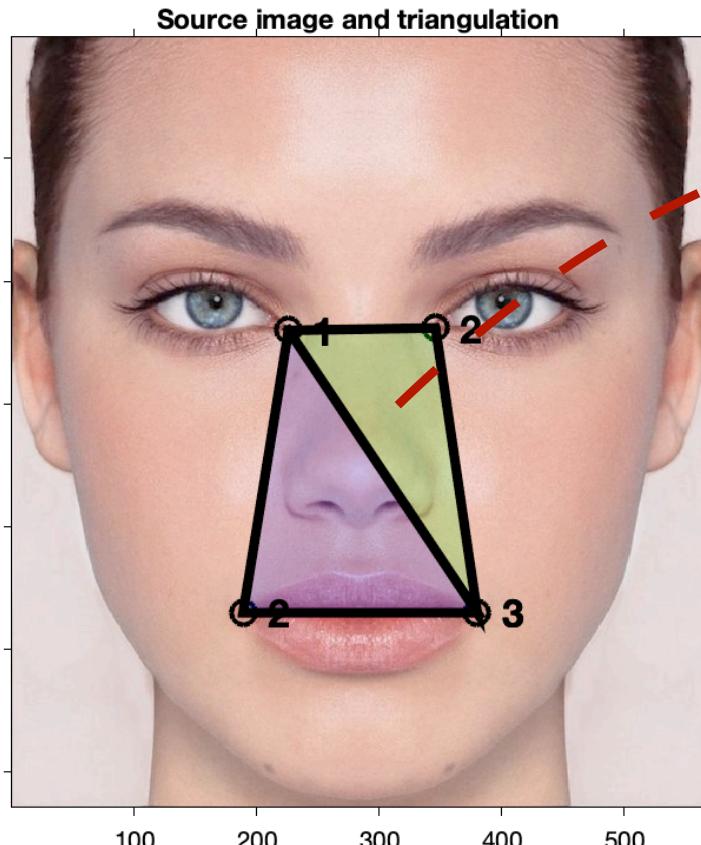
It might be helpful to pre-calculate all affine transformations and store them into a matrix or an indexed data structure, e.g.:

**A(s,t,3,3)** where s varies from 1 to number of shapes, and t varies from 1 to number of triangles.

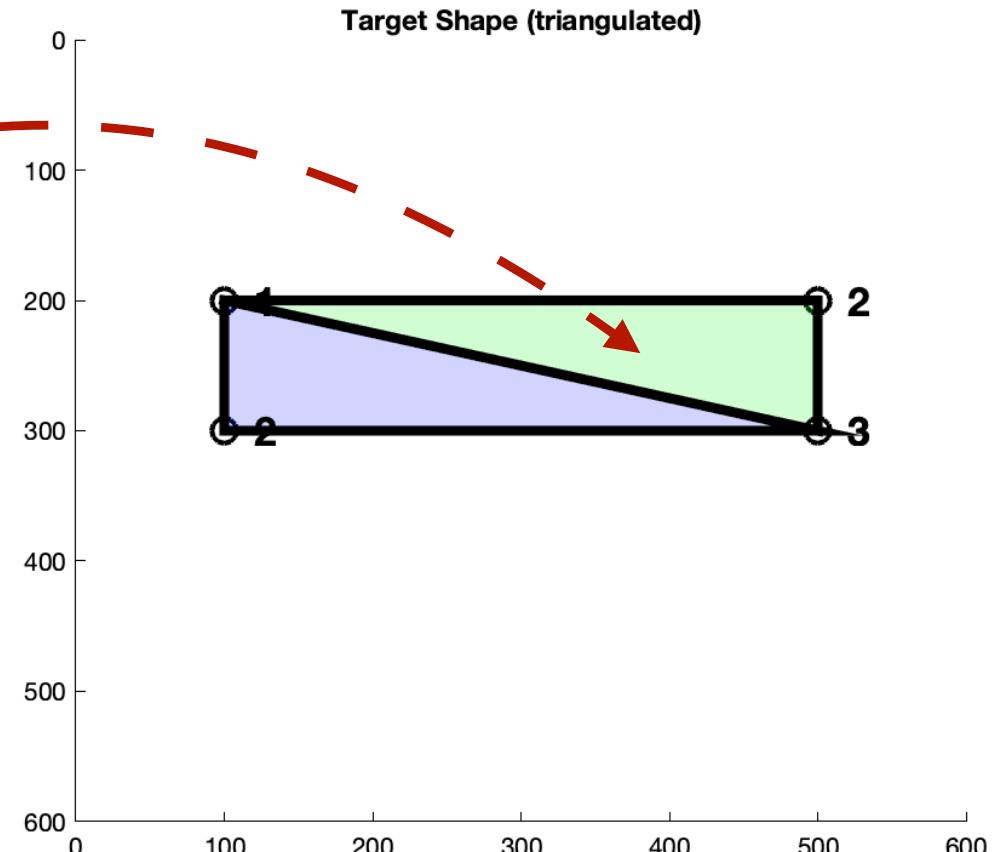
**T(s,t).A** where A is a 3x3 matrix, s is the shape index and t is the triangle index.

# Example

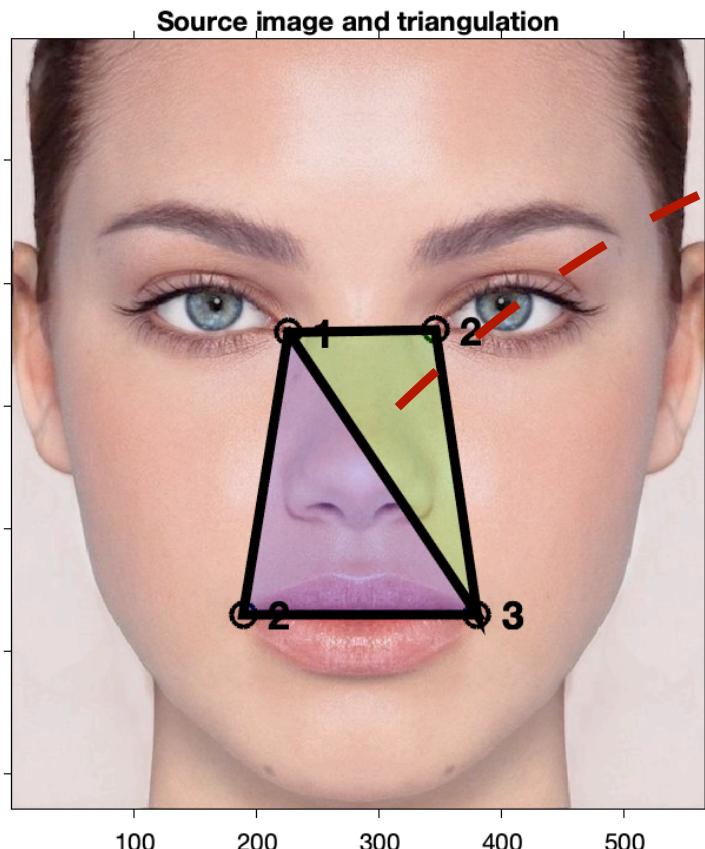
# 1. Calculate the affine transformation, A, between corresponding triangles



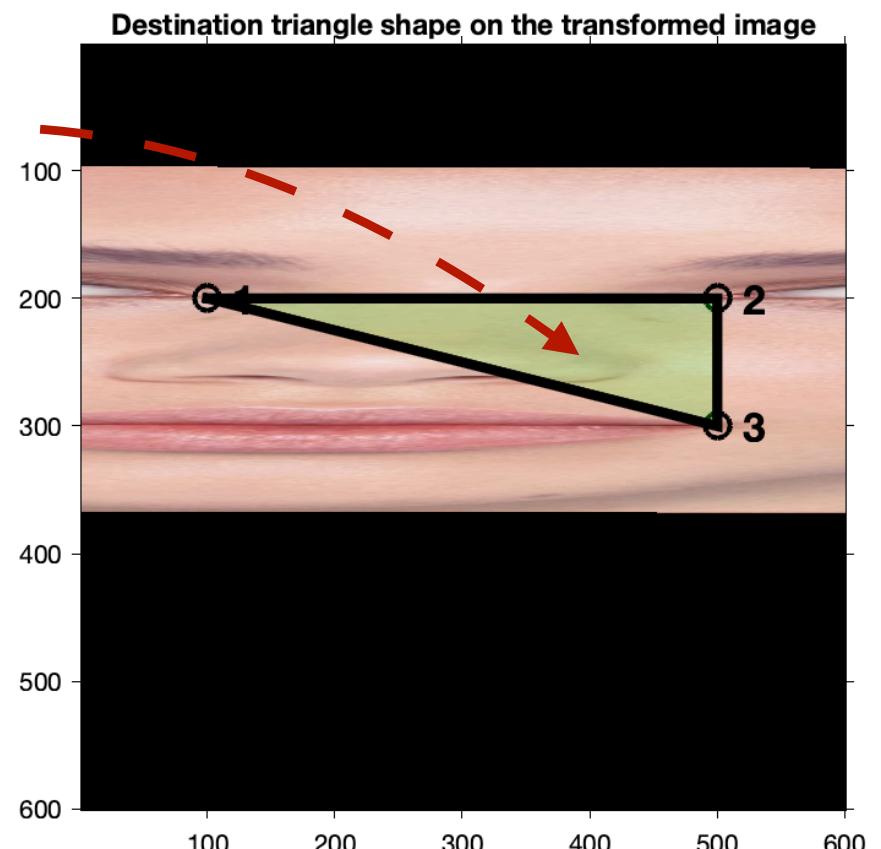
$A_1$



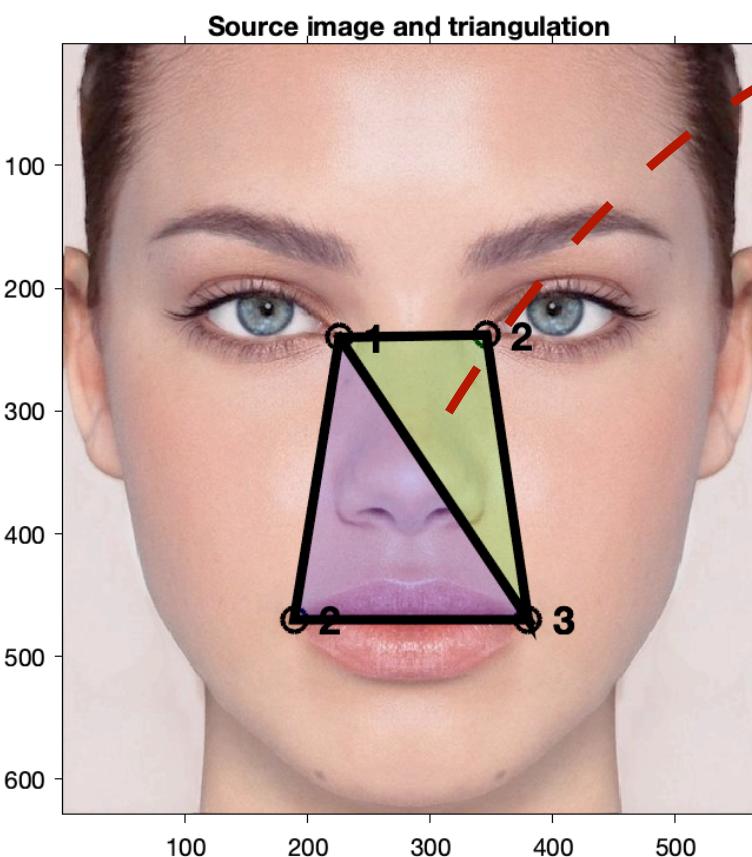
## 2. Warp the whole image using transformation A



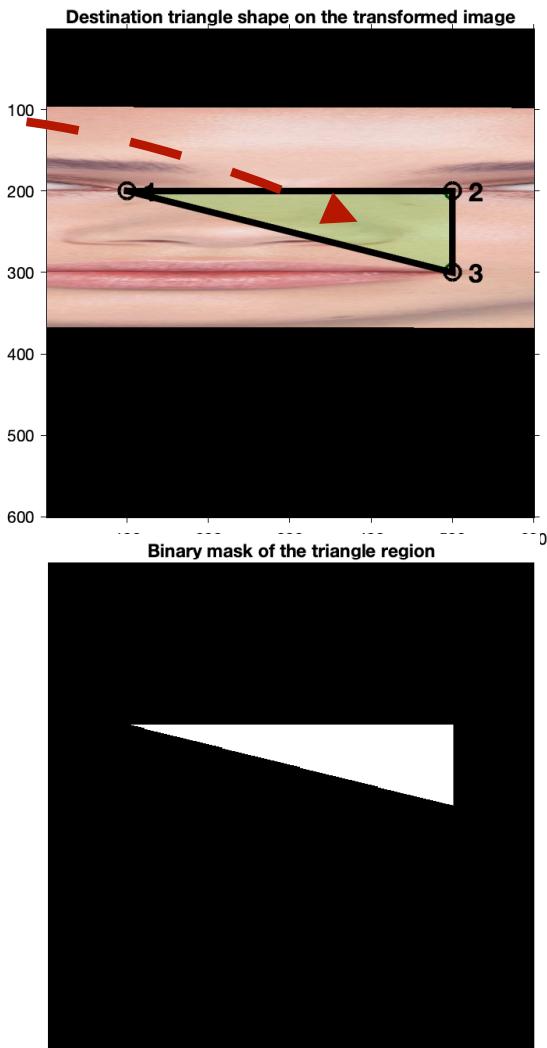
$A_1$



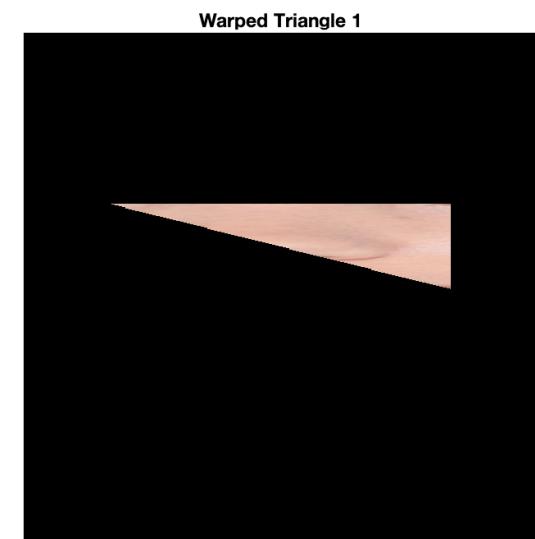
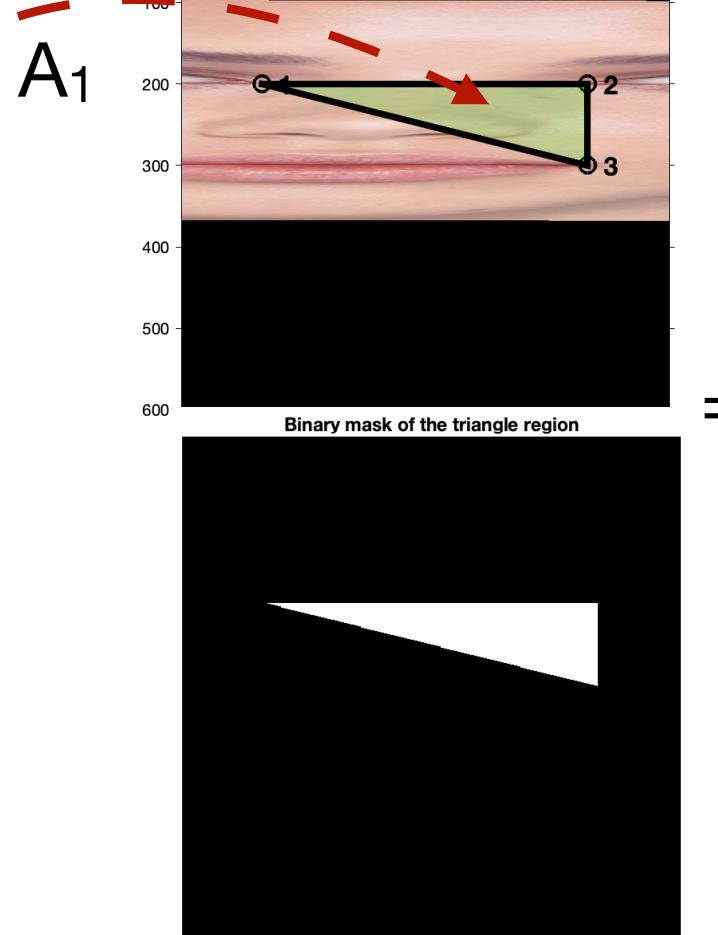
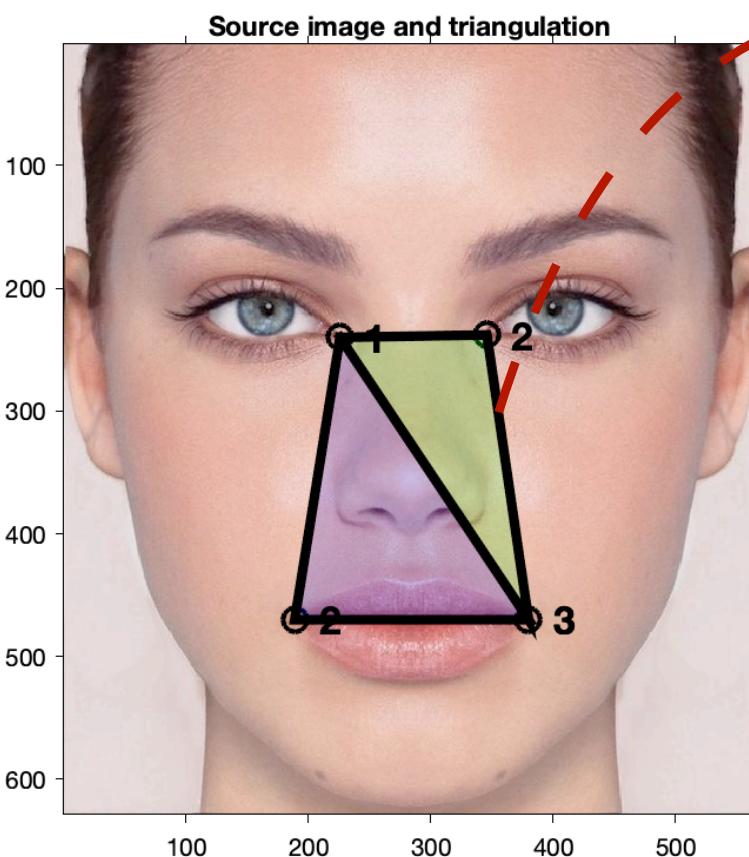
### 3. Create a binary mask for the image region enclosed by the destination triangle



$A_1$



## 4. Multiply the mask by the warped image to get the warped triangular region



## 5. Repeat the process for each corresponding triangle pair incrementally building the final image

