

# A Task Allocation Problem Using Genetic Algorithm Method under A Multi-fighter and Multi-bomb Situation

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## 1. Introduction

Introduction [1]

## 2. One-strike and One-bomb situation

### 2.1. The utility function using Gaussian distributions

Suppose that two fighters are going to conduct an strike mission. Two types of bombs would be used in this mission. Denote the fighters by  $\mathbf{F} = \{f_1, f_2\}$ . Denote the bombs by  $\mathbf{B} = \{b_1, b_2\}$ . Each bomb has the ability to damage the target, as denoted by  $\mathbf{D}_\mathbf{B} = \{d_{b1}, d_{b2}\}$ . In this case, the fighter  $f_1$  will carry the bomb  $b_1$ , and the fighter  $f_2$  will carry the bomb  $b_1$  and  $b_2$ . Denote the asset by  $\mathbf{A} = \{a_1, a_2, a_3\}$ . The assets are listed below.

$$\begin{aligned} a_1 &= (f_1, b_1) \\ a_2 &= (f_2, b_1) \\ a_3 &= (f_2, b_2) \end{aligned} \quad (1)$$

Thus, The damage ability of the asset  $\mathbf{A}$  is denoted by  $\mathbf{D}_\mathbf{A} = \{d_{a1}, d_{a2}, d_{a3}\}$ .

Suppose that two targets are going to be bombed by the fighters  $\mathbf{F}$ . Denote the targets by  $\mathbf{T} = \{t_1, t_2\}$ . The target has two properties, the damage point and the value. If the damage that the target received from the bombs were larger than the damage point of this target, the target would be destroyed, and the value would be gained by the attacker, which represents the side that commands the fighters. Denote the damage point by  $\mathbf{DP} = \{dp_{t1}, dp_{t2}\}$ . Denote the values by  $\mathbf{V} = \{v_{t1}, v_{t2}\}$ . The properties of the targets are listed below.

$$\begin{aligned} t_1 &= (dp_{t1}, v_{t1}) \\ t_2 &= (dp_{t2}, v_{t2}) \end{aligned} \quad (2)$$

Denote the strike mission by  $\mathbf{M} = \{m_{a1}, m_{a2}, m_{a3}\}$ . In this scenario, the mission would be listed below.

$$\begin{aligned} m_{a1} &= [m_{a1,t1}, m_{a1,t2}]^T \\ m_{a2} &= [m_{a2,t1}, m_{a2,t2}]^T \\ m_{a3} &= [m_{a3,t1}, m_{a3,t2}]^T \end{aligned} \quad (3)$$

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In which,  $m_{a,t} \in \{0,1\}; a \in \mathbf{A}, t \in \mathbf{T}$ .

In this chapter, we propose a situation that the bomb carried by each fighter could only strike one target. Thus, the constraint is listed below.

$$\begin{aligned} (m_{a_1,t_1} + m_{a_1,t_2}) &\in \{0,1\} \\ (m_{a_2,t_1} + m_{a_2,t_2}) &\in \{0,1\} \\ (m_{a_3,t_1} + m_{a_3,t_2}) &\in \{0,1\} \end{aligned} \quad (4)$$

Rewrite the strike mission into matrix form, as listed below.

$$\mathbf{M} = [m_{a1}, m_{a2}, m_{a3}] = \begin{bmatrix} m_{a_1,t_1} & m_{a_2,t_1} & m_{a_3,t_1} \\ m_{a_1,t_2} & m_{a_2,t_2} & m_{a_3,t_2} \end{bmatrix} \quad (5)$$

In order to represent the relation between the mission and the damage, we propose a damage matrix  $\mathbf{D}$ , as shown below.

$$\mathbf{D} = \mathbf{M}\mathbf{d} \quad (6)$$

In which,  $\mathbf{d}$  represents the damage of the asset.

$$\mathbf{d} = [d_{a1}, d_{a2}, d_{a3}]^T = [d_{b1}, d_{b1}, d_{b2}]^T \quad (7)$$

Thus, the damage matrix  $\mathbf{D}$  is listed below.

$$\mathbf{D} = \begin{bmatrix} D_{t1} \\ D_{t2} \end{bmatrix} = \begin{bmatrix} m_{a_1,t_1} & m_{a_2,t_1} & m_{a_3,t_1} \\ m_{a_1,t_2} & m_{a_2,t_2} & m_{a_3,t_2} \end{bmatrix} \begin{bmatrix} d_{a1} \\ d_{a2} \\ d_{a3} \end{bmatrix} \quad (8)$$

In which,  $D_{t1}$  and  $D_{t2}$  represent the damage received by the target  $t_1$  and  $t_2$ , respectively. They are listed below.

$$D_t = \sum_{a \in \mathbf{A}} m_{a,t} d_a; t \in \mathbf{T} \quad (9)$$

In order to allocate the assets, which are bombs, we proposed an optimization problem, as shown below.

$$\begin{aligned} &\max_{\mathbf{M}} u(\mathbf{M}) \\ &s.t. m_{a,t} \in \{0,1\}; a \in \mathbf{A}, t \in \mathbf{T} \\ &0 \leq \sum_{t \in \mathbf{T}} m_{a,t} \leq 1; a \in \mathbf{A} \end{aligned} \quad (10)$$

In which,  $u$  represents the objective function of the optimization problem. In this objective function, we introduce the Gaussian function. The objective function  $u$  is listed below.

$$u(\mathbf{M}) = p_{t1} + p_{t2} \quad (11)$$

In which,  $p_{t1}$  and  $p_{t2}$  represent the profit of striking target  $t_1$  and  $t_2$ , respectively. They are listed below.

$$\begin{aligned} p_t &= v_t \text{Gauss}(x = D_t, \mu = dp_t, \sigma = \sigma_t) \\ &= \frac{v_t}{\sqrt{2\pi}\sigma_t} e^{-\frac{(D_t - dp_t)^2}{2\sigma_t^2}} \\ &= \frac{v_t}{\sqrt{2\pi}\sigma_t} \exp\left(-\frac{(D_t - dp_t)^2}{2\sigma_t^2}\right); (t \in \mathbf{T}) \end{aligned} \quad (12)$$

Thus, the objective function  $u(\mathbf{M})$  is listed below.

$$\begin{aligned} u(\mathbf{M}) &= \frac{v_{t1}}{\sqrt{2\pi}\sigma_{t1}} \exp\left(-\frac{(\sum_{a \in \mathbf{A}} m_{a,t1} d_a - dp_{t1})^2}{2\sigma_{t1}^2}\right) + \frac{v_{t2}}{\sqrt{2\pi}\sigma_{t2}} \exp\left(-\frac{(\sum_{a \in \mathbf{A}} m_{a,t2} d_a - dp_{t2})^2}{2\sigma_{t2}^2}\right) \\ &= \sum_{t \in \mathbf{T}} \frac{v_t}{\sqrt{2\pi}\sigma_t} \exp\left(-\frac{(\sum_{a \in \mathbf{A}} m_{a,t} d_a - dp_t)^2}{2\sigma_t^2}\right) \end{aligned} \quad (13)$$

Divide the constraints into two parts. The first part represents that any type of the bombs has a minimum number and a maximum number. The number of the bombs that will be used should lie in this range. They are listed below.

$$\begin{aligned} 0 &\leq (m_{a_1,t_1} + m_{a_1,t_2}) \leq 1 \\ 0 &\leq (m_{a_2,t_1} + m_{a_2,t_2}) \leq 1 \\ 0 &\leq (m_{a_3,t_1} + m_{a_3,t_2}) \leq 1 \end{aligned} \quad (14)$$

Rewrite the first part of the constraints into another form.

$$\begin{aligned} m_{a_1,t_1} + m_{a_1,t_2} - 1 &\leq 0 \\ -m_{a_1,t_1} - m_{a_1,t_2} &\leq 0 \\ m_{a_2,t_1} + m_{a_2,t_2} - 1 &\leq 0 \\ -m_{a_2,t_1} - m_{a_2,t_2} &\leq 0 \\ m_{a_3,t_1} + m_{a_3,t_2} - 1 &\leq 0 \\ -m_{a_3,t_1} - m_{a_3,t_2} &\leq 0 \end{aligned} \quad (15)$$

The second part represents the constraint of each asset. They are listed below.

$$\begin{aligned} 0 &\leq m_{a_1,t_1} \leq 1 \\ 0 &\leq m_{a_2,t_1} \leq 1 \\ 0 &\leq m_{a_3,t_1} \leq 1 \\ 0 &\leq m_{a_1,t_2} \leq 1 \\ 0 &\leq m_{a_2,t_2} \leq 1 \\ 0 &\leq m_{a_3,t_2} \leq 1 \end{aligned} \quad (16)$$

## 2.2. The utility function using Gaussian distributions

Repeat that we proposed an optimization problem, as shown below.

$$\begin{aligned} \max_{\mathbf{M}} u(\mathbf{M}) \\ \text{s.t. } m_{a,t} &\in \{0, 1\}; a \in \mathbf{A}, t \in \mathbf{T} \\ 0 &\leq \sum_{t \in \mathbf{T}} m_{a,t} \leq 1; a \in \mathbf{A} \end{aligned} \quad (17)$$

In this chapter, we use the Gaussian distribution and a linear function. The objective function  $u$  is listed below.

$$u(\mathbf{M}) = p_{t1} + p_{t2} \quad (18)$$

In which,  $p_{t1}$  and  $p_{t2}$  represent the profit of striking target  $t_1$  and  $t_2$ , respectively. They are listed below.

$$p_t = \begin{cases} v_t \text{Gauss}(x = D_t, \mu = dp_t, \sigma = \sigma_t), & x \leq dp_t \\ v_t \text{Gauss}(x = dp_t, \mu = dp_t, \sigma = \sigma_t), & x > dp_t \end{cases} \quad (19)$$

### 3. One-strike and One-bomb situation

In this chapter, we propose a situation that the number of the bombs may larger than 1. Thus, more than one bomb carried by each fighter could be allocated to one target.. Due to the situation that the size of each bomb carried by the fighter  $f_1$  or  $f_2$  is fixed, the maximum bombs that a fighter would use is fixed and is equal to the size of the bomb.

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## Abbreviations

The following abbreviations are used in this manuscript:

MDPI	Multidisciplinary Digital Publishing Institute
DOAJ	Directory of open access journals
TLA	Three letter acronym
LD	Linear dichroism

## References

1. Al-Hadeethi, Y.; Sayyed, M. Analysis of borosilicate glasses doped with heavy metal oxides for gamma radiation shielding application using Geant4 simulation code. *Ceramics International* **2019**, *45*, 24858 – 24864.

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